

Assignment 3 Problem 4

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Consider the following integral:

$\int_0^{\pi/2} \frac{\sin^n(x)}{\sin^n(x) + \cos^n(x)} dx$ where n is any positive integer.

(a) *Use Wolfram Alpha or another computer algebra system to evaluate the above integral (for a general n). Write down the result.*

Standard computational time exceeded.

(b) *Using a computer algebra system, evaluate the above integral for $n = 1, 4, 7$.*

For $n = 1$:

$$\int_0^{\pi/2} \frac{\sin(x)}{\sin(x) + \cos(x)} dx = \frac{\pi}{4}$$

For $n = 4$:

$$\int_0^{\pi/2} \frac{\sin^4(x)}{\sin^4(x) + \cos^4(x)} dx = \frac{\pi}{4}$$

For $n = 7$:

$$\int_0^{\pi/2} \frac{\sin^7(x)}{\sin^7(x) + \cos^7(x)} dx = \frac{\pi}{4}$$

(c) *Evaluate the integral by hand as follows.*

(i) Rewrite the integral using the substitution $u = \frac{\pi}{2} - x$.