

Week 7 \rightarrow C.A

Non-Parametric Estimation

\rightarrow Only use the data to come up with the model

Data Driven Modelling

for a pdf

To learn about a variable w/o making assumptions on it

for a model
 $g(x, y)$

Section 4

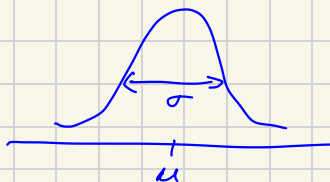
To learn about a pattern w/o making assumptions on it

"Parametric" vs "Non-Parametric"

"Parametric" means we assume a shape or structure to describe the data, up to a finite number of parameters

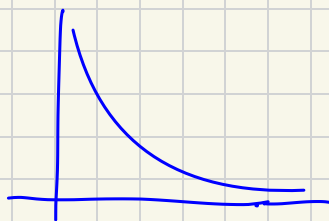
Ex1

$$x \sim N(\mu, \sigma^2)$$



Ex2

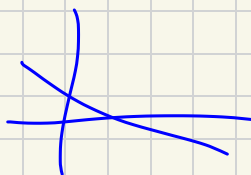
$$x \sim \text{Exp}(\mu)$$



Ex 3

Regression (= pattern)

$$Y = \beta_0 + \beta_1 X$$



N.B In MLE: $\hat{\beta} = \arg \max_{\beta} \sum_{i=1}^n \log f(r_i(\beta))$

Residuals $r_i(\beta) = y_i - \beta x_i$ (ex)
 $f(r) = N(0, \sigma^2) \rightarrow$ pdf of ϵ

KDE'S

Sample points \rightarrow kernels (x_i)

Scaling factor $\rightarrow h$ (bandwidth) (bw in R)

$$K\left(\frac{x - x_i}{h}\right)$$

$\rightarrow k$ is the template distⁿ
 \hookrightarrow (i.e.) normal, uniform etc