

least squares

$$\arg \min_{B_0, B_1} \sum_{i=1}^n (Y_i - (B_0 + B_1 X_i))^2$$

MSE

$$E[(\hat{B} - B_{true})^2] \approx \frac{1}{M} \sum_{m=1}^M (\hat{B}_m - B_{true})^2$$

Bias

$$E(T(X)) - \theta_{true} \quad (\text{e.g.}) \quad \hat{\sigma}^2 - \sigma^2$$

→ Get using MC estimates

Std Error

$$\frac{\sigma}{\sqrt{n}}$$

var

$$\text{var}(\bar{x}) \approx \hat{\text{var}}(\bar{x}) = \frac{1}{M-1} \sum_{i=1}^M (\hat{B}_i - E[\hat{B}])^2$$

s^2 vs σ^2

$$s^2 = \frac{1}{n-1}, \quad \sigma^2 = \frac{1}{n}$$

Bias

$$\frac{1}{M} \sum_{i=1}^M T_i(x) - \theta_{true}$$

$$\hookrightarrow \hat{E}(T(x)) = \frac{1}{M} \sum_{i=1}^M T_m(x) \xrightarrow[M \rightarrow \infty]{LLN} E[T(x)]$$

Performance Indicators

$$1) \text{ Bias}(\hat{B}): \frac{1}{M} \sum_{m=1}^M \hat{B}_m - B_{true} = \bar{\hat{B}} - B_{true}$$

$$2) \text{ var}(\hat{B}): \frac{1}{M-1} \sum_{m=1}^M (\hat{B}_m - \bar{\hat{B}})^2 = \hat{SE}(\hat{B})^2$$

↪ MC est of B - average of your MC estimates of B

$$3) \text{ MSE}(\hat{B}): E[(\hat{B} - B_{true})^2] \approx \frac{1}{M} \sum_{m=1}^M (\hat{B}_m - B_{true})^2 = \hat{MSE}(\hat{B})$$

$$\hookrightarrow \text{RMSE} = \sqrt{\text{MSE}}$$

↓
MC estimate of B - actual B

Confidence
Intervals.

Quantile based : $[\{\hat{\theta}\}_{.025}, \{\hat{\theta}\}_{.975}]$
Naive