

FIR Filters

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Introduction

FIR filters are frequency-selective filters utilized in a variety of digital signal processing applications in which linear-phase integrity is important. Because FIR filters are computationally expensive compared to IIR filters, designing efficient filtering algorithms can be critical in applications with limited memory storage or a low tolerance for latency. However, FIR filters are inherently stable systems and do not induce phase distortion into filtered signals. Therefore, FIR filters are often used in data, audio, and image processing when data integrity is critical. This project investigates FIR filters commonly used in audio effect manipulation, image restoration, and image edge detection.

Methods

The following FIR filtering techniques were implemented in this research:

Echo:

A linear-phase shift that generates a signal delay with a relative magnitude to the original signal. This phenomenon produces echoes and reverberations in audio signals, as well as “ghosts” in images.

Cascading Systems:

The output of the first system is the input to the second system, and the overall output of the cascade system is taken to be the output of the second system.

$$x[n] \rightarrow \text{FIR FILTER-1} \rightarrow w[n] \rightarrow \text{FIR FILTER-2} \rightarrow y[n]$$
$$w[n] = x[n] - q[n-1] (\text{FIR Filter 1})$$

$$y[n] = \sum_{l=0}^M r^l w[n-l] (\text{FIR Filter 2})$$

FIR Filter 1: utilized to create echoes on signals and data sets (audio, and image data).

FIR Filter 2: utilized to (approximately) undo the effect of FIR-Filter 1. This type of application is called *Deconvolution*.

Deconvolution:

A signal processing technique used to rectify an undesired convolution. This is useful in image restoration.

First-Difference Filter: $y(n) = x(n) - x(n-1)$

A filter designed for detecting significant fluctuations in a signal. This concept is known as edge detection and can be used in many image processing applications including bar code scanning.

Analysis

A simplistic approach to FIR filtering has been achieved in this research to exhibit idealistic filters and their responses. However, in the physical world, additional variables must be considered when designing adaptive, robust filtering systems.

The merit of a deconvolution filter depends greatly on the selected coefficients. In this research, the original convoluted signal was known, which guided the selection of the restorative filtering design. When the original signal is unknown, a more complicated process known as “blind” deconvolution is required.

Bar code scanners are subject to environmental conditions such as contoured or rotated barcodes, variable ambient lighting, and bar code damage. A multi-phase processing system may be required.

Audio Effect

Process



An Echo Filter: $y_1[n] = x_1[n] - r x_1[n - P]$

Experiment:

An echo was added to an audio recording that was sampled at $f_s = 8000$ Hz. The time delay and strength of the echo are 0.2 sec and 90% respectively.

$$f_s = 8000 \text{ Hz}$$
$$\text{delay} = 0.2 \text{ s}$$
$$r = 0.9 \text{ (90\% of the original)}$$

$$T_s = \frac{1}{f_s} \Rightarrow P = \frac{\text{delay}}{T_s} = 1600$$

Application

Click here to listen to Original Audio:

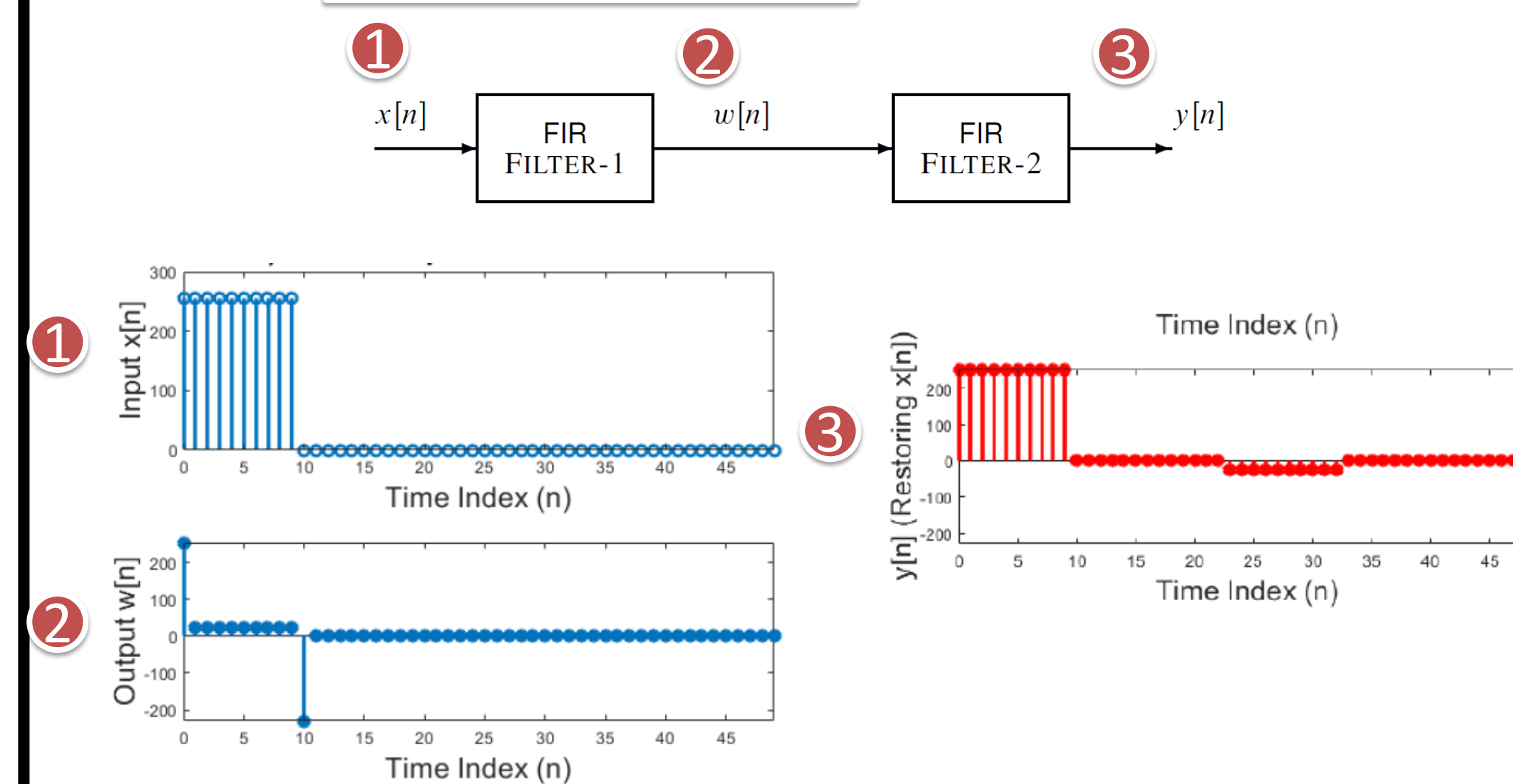


Click here to listen to Audio with Echo:



Image Restoration

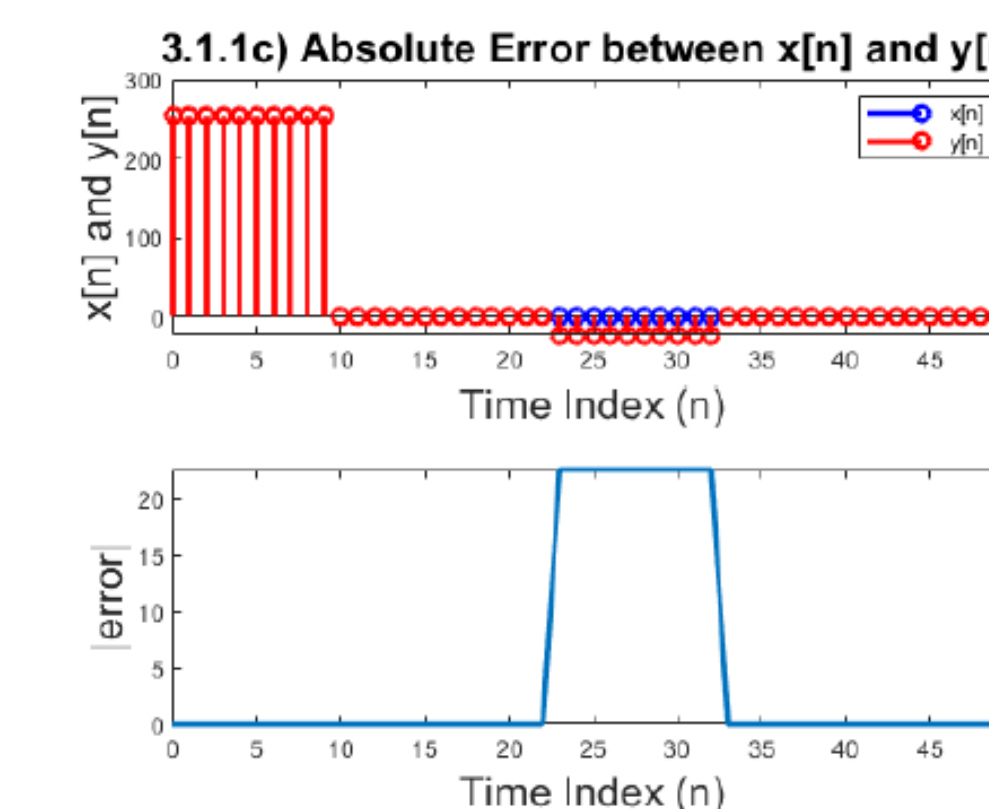
Process



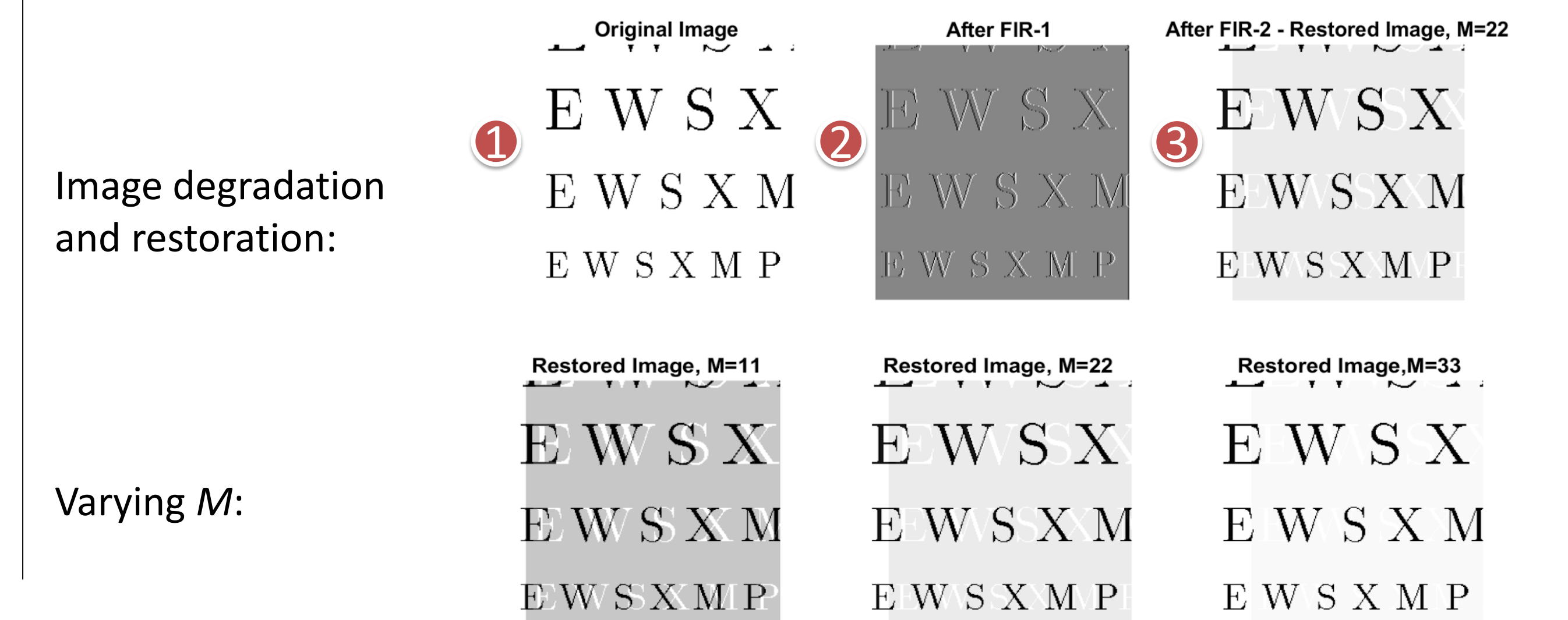
Filter Coefficients:

FIR Filter 1: $q=0.9$

FIR Filter 2: $r=0.9, M=22$

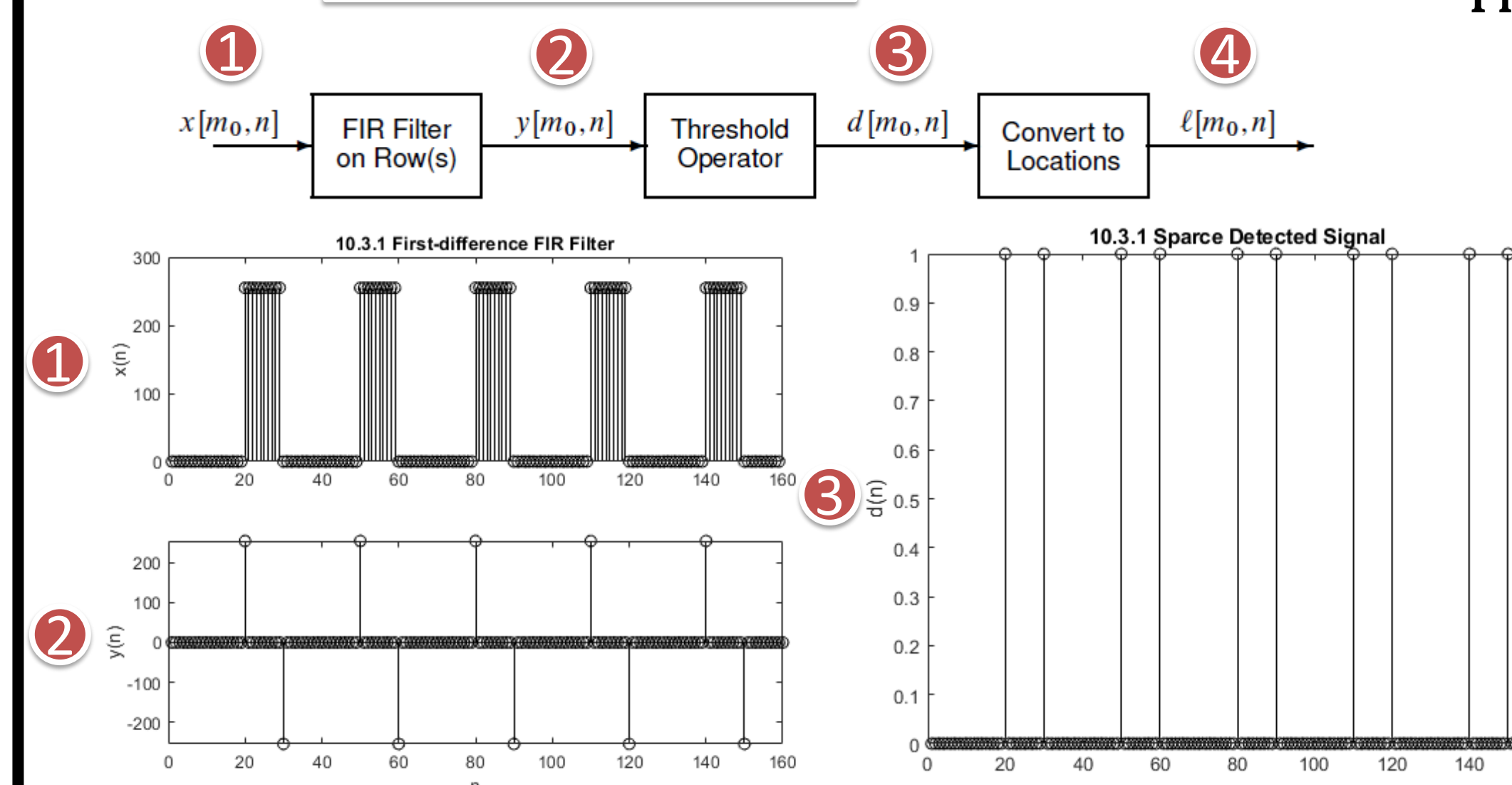


Application



Edge Detection

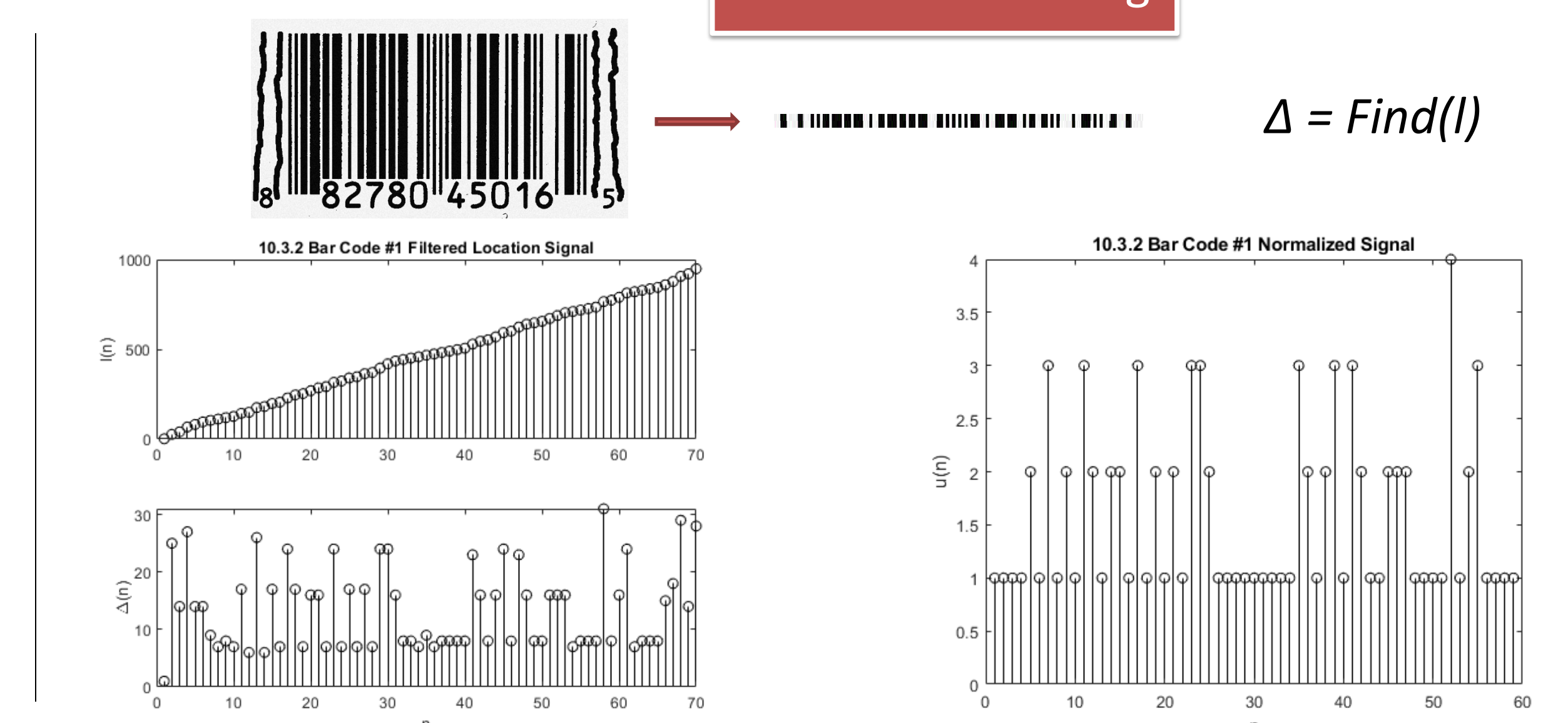
Process



Filter Coefficients: $h(n) = \{1, -1\}$

$$l = \text{Find}(d)$$

Bar Code Decoding



References

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3. Smith, Steven W. “The Scientist and Engineer’s Guide to Digital Signal Processing”. San Diego, Calif: California Technical Pub, 1997. Print.