

Computer Architecture  
Machine Representation of Programs: Data

Cain Susko

Queen's University  
School of Computing

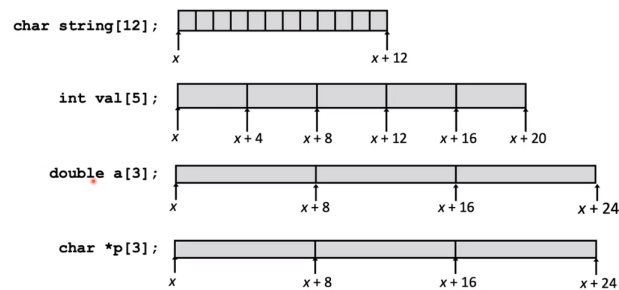
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## Arrays

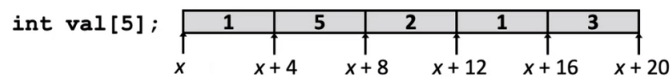
Arrays are a way of storing data of the same type:

$$T \ A[L].$$

This is an array  $A$  of data Type  $T$  and length  $L$ . Additional Examples are:



Arrays can be accessed using pointers like so:

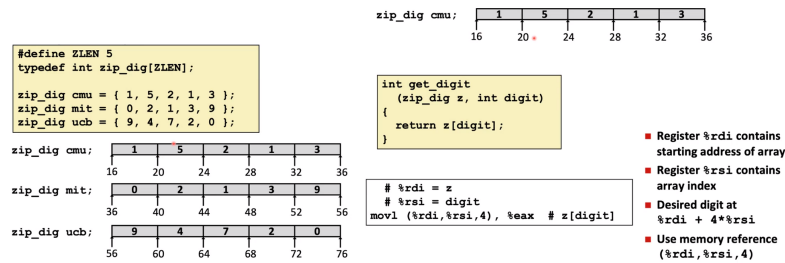


■ Reference	Type	Value
<code>val[4]</code>	<code>int</code>	3
<code>val</code>	<code>int *</code>	<code>*x</code>
<code>val+1</code>	<code>int *</code>	<code>x+4</code>
<code>&amp;val[2]</code>	<code>int *</code>	<code>x+8</code>
<code>val[5]</code>	<code>int</code>	??
<code>*(val+1)</code>	<code>int</code>	5
<code>val + i</code>	<code>int *</code>	<code>x+4i</code>

Note: `val` is equal to the pointer at the start of the array.

## 1D Arrays

A comprehensive example of an array is the following:



Consider the example of a n Array in a loop: Note: this is just one of many

```

void zincr(zip_dig z) {
    size_t i;
    for (i = 0; i < ZLEN; i++)
        z[i]++;
}

```

```

# %rdi = z
movl $0, %eax      # i = 0
jmp .L3            # goto middle
.L4:               # loop:
addl $1, (%rdi,%rax,4) # z[i]++
addq $1, %rax       # i++
.L3:               # middle
cmpq $4, %rax       # i:4
jbe .L4            # if <=, goto loop
rep; ret

```

forms of loops we covered in a previous lesson. Additionally, note that the `ret` instruction is used but there is no value returned (acceptable usage).

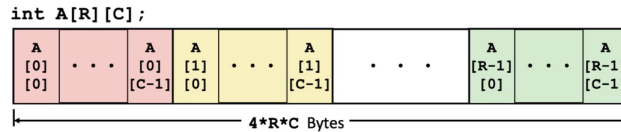
## Multi-Dimensional Arrays

the declaration of a multi-dimensional or nested array is:

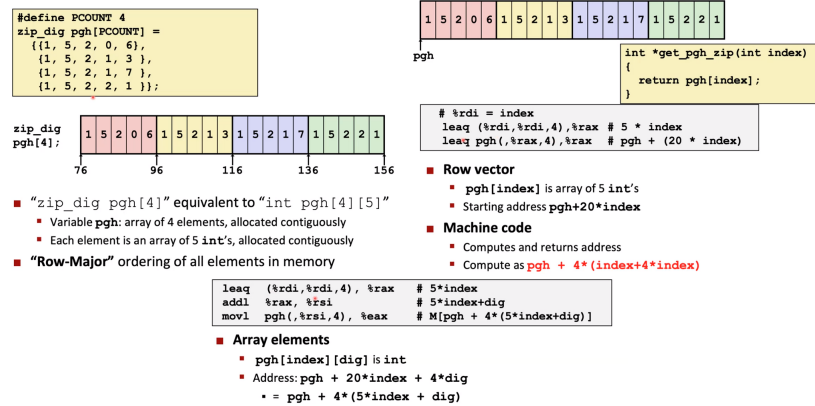
$T \ A[R][C].$

where  $A$  is an array of objects with type  $T$  as well as  $R$  rows and  $C$  columns. The size of the array can be found by doing  $R \times C \times k - \text{bytes}$ .

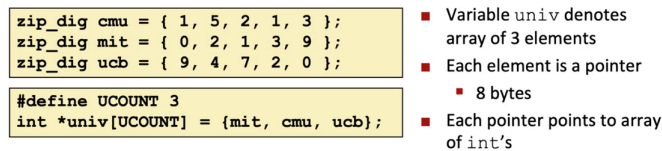
The arrangement in memory or a 2D array is row majored, meaning they're stored row by row, linearly in memory:



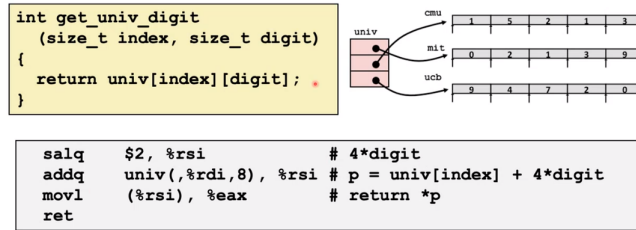
Consider the following nested array example:



We can also make arrays of different structures, for example, the **Multi-Level Array**:



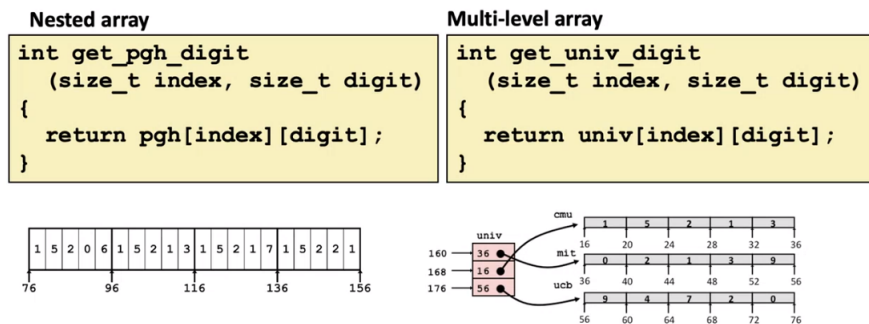
To access the elements in this type of array one could use the following procedure:



#### ■ Computation

- Element access `Mem[Mem[univ+8*index]+4*digit]`
- Must do two memory reads
  - First get pointer to row array
  - Then access element within array

Note: because this data is not contiguous, the accessing of data may be less efficient. This can be more clearly seen in the following display:



Accesses looks similar in C, but address computations very different:

`Mem[pgh+20*index+4*digit]`    `Mem[Mem[univ+8*index]+4*digit]`

## Code in C

The representation of an  $N \times N$  matrix in C must have fixed dimensions. Indexing the array can be done either with explicit indexing:

```
#define IDX(n, i, j) ((i)*(n)+(j))
/* Get element a[i][j] */
int vec_ele(size_t n, int *a,
            size_t i, size_t j)
{
    return a[IDX(n,i,j)];
}
```

Or by using implicit indexing (Now Supported by gcc!):

```
/* Get element a[i][j] */
int var_ele(size_t n, int a[n][n],
            size_t i, size_t j) {
    return a[i][j];
}
```

The machine code for this type of access is the following:

### ■ Array elements

- Address  $A + i * (C * K) + j * K$
- $C = n, K = 4$
- Must perform integer multiplication

```
/* Get element a[i][j] */
int var_ele(size_t n, int a[n][n], size_t i, size_t j)
{
    return a[i][j];
}
```

```
# n in %rdi, a in %rsi, i in %rdx, j in %rcx
imulq    %rdx, %rdi      # n*i
leaq     (%rsi,%rdi,4), %rax # a + 4*n*i
movl     (%rax,%rcx,4), %eax # a + 4*n*i + 4*j
ret
```