

Notebook - Competitive Programming

Anões do TLE

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1 Data structures

1.1 Union Find Disjoint Set (UFDS)

Uncomment the lines to recover which element belong to each set.

```
Time: \approx O(1) for everything.
class UFDS {
 public:
  vi ps, size;
  // vector < unordered_set < int >> sts;
  UFDS(int N) : size(N + 1, 1), ps(N + 1), sts(N) {
   iota(ps.begin(), ps.end(), 0);
    // for (int i = 0; i < N; i++) sts[i].insert(i);</pre>
  int find_set(int x) { return x == ps[x] ? x : (ps[x] = find_set(ps[x])); }
  bool same_set(int x, int y) { return find_set(x) == find_set(y); }
  void union_set(int x, int y) {
    if (same_set(x, y)) return;
    int px = find_set(x);
    int py = find_set(y);
    if (size[px] < size[py]) swap(px, py);</pre>
    ps[py] = px;
    size[px] += size[py];
    // sts[px].merge(sts[py]);
};
```

2 Dynamic programming

2.1 Kadane

```
int kadane(const vi& xs) {
  vi s(xs.size());
  s[0] = xs[0];
  for (size_t i = 1; i < xs.size(); ++i) s[i] = max(xs[i], s[i - 1] + xs[i]);
  return *max_element(all(s));
}</pre>
```

2.2 Longest Increasing Subsequence (LIS)

```
Time: O(N \cdot \log N).

int lis(vi const& a) {

  int n = a.size();

  const int INF = 1e9;

  vi d(n + 1, INF);

  d[0] = -INF;
```

```
for (int i = 0; i < n; i++) {
   int l = upper_bound(d.begin(), d.end(), a[i]) - d.begin();
   if (d[l - 1] < a[i] && a[i] < d[l]) d[l] = a[i];
}

int ans = 0;
for (int l = 0; l <= n; l++) {
   if (d[l] < INF) ans = l;
}

return ans;
}</pre>
```

3 Geometry

3.1 Convex Hull

Given a set of points find the smallest convex polygon that contains all the given points. Time: $O(N \cdot \log N)$

By default it removes the collinear points, set the boolean to true if you don't want that

```
struct pt {
 double x, y;
int orientation(pt a, pt b, pt c) {
 double v = a.x * (b.y - c.y) + b.x * (c.y - a.y) + c.x * (a.y - b.y);
 if (v < 0) return -1; // clockwise
 if (v > 0) return +1; // counter-clockwise
  return 0:
bool cw(pt a, pt b, pt c, bool include_collinear) {
 int o = orientation(a, b, c);
 return o < 0 || (include_collinear && o == 0);</pre>
bool collinear(pt a, pt b, pt c) { return orientation(a, b, c) == 0; }
void convex_hull(vector<pt>& a, bool include_collinear = false) {
  pt p0 = *min_element(a.begin(), a.end(), [](pt a, pt b) {
    return make_pair(a.y, a.x) < make_pair(b.y, b.x);</pre>
  });
  sort(a.begin(), a.end(), [&p0](const pt& a, const pt& b) {
    int o = orientation(p0, a, b);
    if (0 == 0)
      return (p0.x - a.x) * (p0.x - a.x) + (p0.y - a.y) * (p0.y - a.y) <
             (p0.x - b.x) * (p0.x - b.x) + (p0.y - b.y) * (p0.y - b.y);
    return o < 0:
  }):
  if (include_collinear) {
   int i = (int)a.size() - 1;
    while (i \ge 0 \&\& collinear(p0, a[i], a.back())) i--;
    reverse(a.begin() + i + 1, a.end());
  vector <pt> st;
```

```
for (int i = 0; i < (int)a.size(); i++) {
   while (st.size() > 1 &&
        !cw(st[st.size() - 2], st.back(), a[i], include_collinear))
        st.pop_back();
   st.push_back(a[i]);
}
a = st;
```

3.2 Point To Segment

```
typedef pair <double, double > pdb;
double pt2segment(pdb A, pdb B, pdb E) {
 pdb AB = {B.fst - A.fst, B.snd - A.snd};
 pdb BE = {E.fst - B.fst, E.snd - B.snd}:
 pdb AE = {E.fst - A.fst, E.snd - A.snd};
 double AB_BE = AB.fst * BE.fst + AB.snd * BE.snd;
 double AB_AE = AB.fst * AE.fst + AB.snd * AE.snd;
 double ans;
 if (AB BE > 0) {
   double v = E.snd - B.snd:
   double x = E.fst - B.fst;
   ans = hypot(x, y);
 } else if (AB_AE < 0) {</pre>
   double y = E.snd - A.snd;
   double x = E.fst - A.fst:
   ans = hypot(x, y);
 } else {
   auto [x1, y1] = AB;
   auto [x2, y2] = AE;
   double mod = hypot(x1, y1);
   ans = abs(x1 * y2 - y1 * x2) / mod;
 return ans;
```

4 Graphs

4.1 Articulation Points

```
int dfs_num[MAX], dfs_low[MAX];
vi adj[MAX];

int dfs_articulation_points(int u, int p, int& next, set<int>& points) {
  int children = 0;
  dfs_low[u] = dfs_num[u] = next++;

  for (auto v : adj[u])
    if (not dfs_num[v]) {
        ++children;
```

```
dfs_articulation_points(v, u, next, points);
      if (dfs_low[v] >= dfs_num[u]) points.insert(u);
      dfs_low[u] = min(dfs_low[u], dfs_low[v]);
    } else if (v != p)
      dfs_low[u] = min(dfs_low[u], dfs_num[v]);
  return children:
set < int > articulation_points(int N) {
  memset(dfs_num, 0, (N + 1) * sizeof(int));
  memset(dfs_low, 0, (N + 1) * sizeof(int));
  set < int > points;
  for (int u = 1, next = 1; u \le N; ++u)
   if (not dfs_num[u]) {
      auto children = dfs_articulation_points(u, u, next, points);
      if (children == 1) points.erase(u);
  return points;
4.2 Bellman Ford
Time: O(V \cdot E). Returns the shortest path from s to all other nodes.
using edge = tuple<int, int, int>;
pair < vi. vi > bellman ford(int s. int N. const vector < edge > & edges) {
  vi dist(N + 1, oo), pred(N + 1, oo);
  dist[s] = 0;
  pred[s] = s;
  for (int i = 1; i <= N - 1; i++)</pre>
   for (auto [u, v, w] : edges)
      if (dist[u] < oo and dist[v] > dist[u] + w) {
        dist[v] = dist[u] + w;
        pred[v] = u;
  return {dist, pred};
4.3 BFS 0/1
Time: O(V+E).
vii adj[MAX];
vi bfs 01(int s. int N) {
 vi dist(N + 1, oo);
  dist[s] = 0:
```

```
deque < int > q;
  q.emplace_back(s);
  while (not q.empty()) {
    auto u = q.front();
    q.pop_front();
    for (auto [v. w] : adi[u])
      if (dist[v] > dist[u] + w) {
        dist[v] = dist[u] + w;
        w == 0 ? q.emplace_front(v) : q.emplace_back(v);
  }
  return dist;
4.4 Bridges
int dfs_num[MAX], dfs_low[MAX];
vi adj[MAX];
void dfs_bridge(int u, int p, int& next, vii& bridges) {
  dfs low[u] = dfs num[u] = next++:
  for (auto v : adj[u])
    if (not dfs_num[v]) {
      dfs_bridge(v, u, next, bridges);
      if (dfs_low[v] > dfs_num[u]) bridges.emplace_back(u, v);
      dfs low[u] = min(dfs low[u], dfs low[v]):
    } else if (v != p)
      dfs_low[u] = min(dfs_low[u], dfs_num[v]);
}
vii bridges(int N) {
  memset(dfs num, 0, (N + 1) * sizeof(int));
  memset(dfs_low, 0, (N + 1) * sizeof(int));
  vii bridges;
  for (int u = 1, next = 1; u \le N; ++u)
    if (not dfs_num[u]) dfs_bridge(u, u, next, bridges);
  return bridges;
     Negative Cycle Bellman Ford
Time: O(V \cdot E). Detects whether there is a negative cycle in the graph using Bellman Ford.
using edge = tuple<int, int, int>;
bool has_negative_cycle(int s, int N, const vector<edge>& edges) {
  vi dist(N + 1, oo):
```

```
for (int i = 1; i <= N - 1; i++)</pre>
    for (auto [u. v. w] : edges)
      if (dist[u] < oo and dist[v] > dist[u] + w) dist[v] = dist[u] + w;
  for (auto [u, v, w] : edges)
    if (dist[u] < oo and dist[v] > dist[u] + w) return true;
  return false:
4.6 Negative Cycle Floyd Warshall
Time: O(n^3). Detects whether there is a negative cycle in the graph using Floyd Warshall.
int dist[MAX][MAX];
vii adj[MAX];
bool has_negative_cycle(int N) {
  for (int u = 1; u <= N; ++u)
    for (int v = 1; v <= N; ++v) dist[u][v] = u == v ? 0 : oo;
  for (int u = 1; u <= N; ++u)</pre>
    for (auto [v, w] : adj[u]) dist[u][v] = w;
  for (int k = 1; k \le N; ++k)
    for (int u = 1; u <= N; ++u)
      for (int v = 1; v <= N; ++v)</pre>
        if (dist[u][k] < oo and dist[k][v] < oo)</pre>
          dist[u][v] = min(dist[u][v], dist[u][k] + dist[k][v]);
  for (int i = 1: i <= N: ++i)
    if (dist[i][i] < 0) return true;</pre>
  return false;
4.7 Dijkstra
pair < vl, vl > Graph::dijkstra(ll src) {
  vl pd(this->N, LLONG_MAX), ds(this->N, LLONG_MAX);
  pd[src] = src:
  ds[src] = 0;
  set <pll> st;
  st.emplace(0, src);
  while (!st.empty()) {
    11 u = st.begin()->snd;
    11 wu = st.begin()->fst;
    st.erase(st.begin());
    if (wu != ds[u]) continue:
    for (auto& [v, w] : adj[u]) {
      if (ds[v] > ds[u] + w) {
```

dist[s] = 0;

```
ds[v] = ds[u] + w;
        pd[v] = u:
        st.emplace(ds[v], v);
  }
  return {ds, pd};
     Floyd Warshall
vii adj[MAX];
pair < vector < vi > , vector < vi >> floyd_warshall(int N) {
  vector < vi > dist(N + 1, vi(N + 1, oo)):
  vector < vi > pred(N + 1, vi(N + 1, oo));
  for (int u = 1; u <= N; ++u) {</pre>
    dist[u][u] = 0;
    pred[u][u] = u;
  for (int u = 1; u <= N; ++u)</pre>
   for (auto [v, w] : adj[u]) {
      dist[u][v] = w:
      pred[u][v] = u;
  for (int k = 1; k \le N; ++k) {
    for (int u = 1; u <= N; ++u) {</pre>
      for (int v = 1: v \le N: ++v) {
        if (dist[u][k] < oo and dist[k][v] < oo and</pre>
            dist[u][v] > dist[u][k] + dist[k][v]) {
          dist[u][v] = dist[u][k] + dist[k][v];
          pred[u][v] = pred[k][v];
    }
  return {dist, pred};
     Graph
class Graph {
 private:
 11 N;
  bool undirected:
  vector < vll > adi:
 public:
  Graph(ll N, bool is_undirected = true) {
    this ->N = N;
    adi.resize(N):
    undirected = is_undirected;
```

```
void add(ll u, ll v, ll w) {
   adj[u].emplace_back(v, w);
   if (undirected) adj[v].emplace_back(u, w);
};
4.10 Retrieve Path 2d
v1l Graph::retrieve_path_2d(11 src, 11 trg, const vector<vl>& pred) {
  vll p;
  do {
   p.emplace_back(pred[src][trg], trg);
    trg = pred[src][trg];
 } while (trg != src);
 reverse(all(p));
 return p;
4.11 Retrieve Path
vll Graph::retrieve_path(ll src, ll trg, const vl& pred) {
  vll p;
  do {
   p.emplace_back(pred[trg], trg);
   trg = pred[trg];
 } while (trg != src);
  reverse(all(p));
  return p;
    Math
5.1 Binomial
ll binom(ll n, ll k) {
 if (k > n) return 0;
 vll dp(k + 1, 0);
  dp[0] = 1;
  for (ll i = 1; i <= n; i++)</pre>
   for (11 j = k; j > 0; j--) dp[j] = dp[j] + dp[j - 1];
  return dp[k];
5.2 Count Divisors
ll count_divisors(ll num) {
 11 count = 1;
  for (int i = 2; (11)i * i <= num; i++) {
   if (num % i == 0) {
      int e = 0;
      do {
```

```
e++;
        num /= i:
      } while (num % i == 0);
      count *= e + 1:
 if (num > 1) {
    count *= 2;
 return count:
     Factorization With Sieve
map<11, 11> factorization_with_sieve(11 n, const vl& primes) {
 map<11, 11> fact;
 for (ll d : primes) {
    if (d * d > n) break:
   11 k = 0;
    while (n \% d == 0) {
     k++;
     n /= d;
    if (k) fact[d] = k;
 if (n > 1) fact[n] = 1;
 return fact;
5.4 Factorization
map<ll, 1l> factorization(ll n) {
 map < 11 . 11 > ans:
 for (11 i = 2; i * i <= n; i++) {</pre>
   11 count = 0;
    for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count;
 if (n > 1) ans[n]++;
 return ans;
     Fast Exp Iterative
long long fast_exp_it(long long a, int n) {
 long long res = 1, base = a;
 while (n) {
    if (n & 1) res *= base;
    base *= base;
    n >>= 1:
```

```
return res;
5.6 Fast Exp
long long fast_exp(long long a, int n) {
  if (n == 1) return a:
  auto x = fast_exp(a, n / 2);
  return x * x * (n % 2 ? a : 1);
5.7 GCD
The Euclidean algorithm allows to find the greatest common divisor of two numbers a and b in
O(\log \cdot \min(a, b)).
11 gcd(l1 a, l1 b) { return b ? gcd(b, a % b) : a; }
    Integer Mod
5.8
const ll INF = 1e18;
const 11 mod = 998244353:
template <11 MOD = mod>
struct Modular {
  ll value;
  static const 11 MOD_value = MOD;
  Modular(11 v = 0) {
    value = v % MOD;
    if (value < 0) value += MOD;</pre>
  Modular(ll a, ll b) : value(0) {
    *this += a;
    *this /= b:
  Modular& operator+=(Modular const& b) {
    value += b.value;
    if (value >= MOD) value -= MOD:
    return *this;
  Modular& operator -= (Modular const& b) {
    value -= b.value;
    if (value < 0) value += MOD:</pre>
    return *this:
  Modular& operator*=(Modular const& b) {
    value = (11)value * b.value % MOD;
    return *this;
  friend Modular mexp(Modular a, ll e) {
```

```
Modular res = 1;
    while (e) {
      if (e & 1) res *= a;
      a *= a:
      e >>= 1;
    return res;
  friend Modular inverse (Modular a) { return mexp(a, MOD - 2); }
  Modular& operator/=(Modular const& b) { return *this *= inverse(b); }
  friend Modular operator+(Modular a, Modular const b) { return a += b; }
  Modular operator++(int) { return this->value = (this->value + 1) % MOD; }
  Modular operator++() { return this->value = (this->value + 1) % MOD; }
  friend Modular operator - (Modular a, Modular const b) { return a -= b; }
  friend Modular operator - (Modular const a) { return 0 - a; }
  Modular operator -- (int) {
    return this->value = (this->value - 1 + MOD) % MOD:
  }
  Modular operator -- () { return this -> value = (this -> value - 1 + MOD) % MOD; }
  friend Modular operator*(Modular a, Modular const b) { return a *= b; }
  friend Modular operator/(Modular a. Modular const b) { return a /= b: }
  friend std::ostream& operator <<(std::ostream& os, Modular const& a) {</pre>
    return os << a.value:
  friend bool operator == (Modular const& a, Modular const& b) {
    return a.value == b.value:
  friend bool operator!=(Modular const& a, Modular const& b) {
    return a.value != b.value:
 }
};
     Is prime
O(\sqrt{N})
bool isprime(ll n) {
  if (n < 2) return false;
  if (n == 2) return true;
  if (n % 2 == 0) return false;
  for (11 i = 3; i * i < n; i += 2)
    if (n % i == 0) return false:
  return true:
5.10 LCM
Calculating the least common multiple (commonly denoted LCM) can be reduced to calculating the GCD
with the following simple formula: lcm(a, b) = (a \cdot b)/gcd(a, b)
Thus, LCM can be calculated using the Euclidean algorithm with the same time complexity:
11 lcm(ll a, ll b) { return a / gcd(a, b) * b; }
```

5.11 Euler phi $\varphi(n)$

Computes the number of positive integers less than n that are coprimes with n, in $O(\sqrt{N})$.

```
11 phi(11 n) {
  if (n == 1) return 1:
  auto fs = factorization(n):
  auto res = n;
  for (auto [p, k] : fs) {
    res /= p;
    res *= (p - 1):
  return res;
}
5.12 Sieve
vl sieve(ll N) {
  bitset < MAX + 1> sieve;
  v1 ps{2, 3}:
  sieve.set();
  for (11 i = 5, step = 2; i \le N; i += step, step = 6 - step) {
    if (sieve[i]) {
      ps.push_back(i);
      for (ll j = i * i; j <= N; j += 2 * i) sieve[j] = false;</pre>
  }
  return ps;
5.13 Sum Divisors
ll sum divisors(ll num) {
 11 result = 1;
  for (int i = 2; (11)i * i <= num; i++) {
    if (num % i == 0) {
      int e = 0:
      do {
        e++;
        num /= i:
      } while (num % i == 0);
      11 \text{ sum} = 0, \text{ pow} = 1;
      do {
        sum += pow;
        pow *= i;
      } while (e-- > 0):
      result *= sum:
  if (num > 1) {
    result *= (1 + num);
  return result;
```

}

5.14 Sum of difference

```
Function to calculate sum of absolute difference of all pairs in array: \frac{1}{2}\sum_{i=1}^{N}\sum_{j=1}^{N}|A_i-A_j|
```

```
11 sum_of_diference(vl& arr, ll n) {
    sort(all(arr));

    ll sum = 0;
    for (ll i = 0; i < n; i++) {
        sum += i * arr[i] - (n - 1 - i) * arr[i];
    }

    return sum;
}</pre>
```

6 Problems

6.1 Kth Digit String (CSES)

```
Time: O(\log_{10} K).
Space: O(1).
ll kth_digit_string(ll k) {
  if (k < 10) return k;</pre>
  11 c = 180, i = 2, u = 10, r = 0, ans = -1, m;
  for (k -= 9; k > c; i++, u *= 10) {
    k -= c;
   c /= i:
    c *= 10 * (i + 1);
  if ((m = k % i))
    r++;
  else
    m = i;
  11 \text{ tmp} = (k / i) + r + u - 1;
  for (m = i + 1 - m; m--; tmp /= 10) ans = tmp % 10;
  return ans;
```

7 Strings

7.1 Manacher

Given string s with length n. Find all the pairs (i,j) such that substring s[i...j] is a palindrome. String t is a palindrome when $t = t_{rev}$ (t_{rev} is a reversed string for t). Time: O(N)

```
vi manacher(string s) {
   string t;
   for (auto c : s) t += string("#") + c;
   t = t + '#';
```

```
int n = t.size();
t = "$" + t + "^";

vi p(n + 2);
int l = 1, r = 1;
for (int i = 1; i <= n; i++) {
   p[i] = max(0, min(r - i, p[1 + (r - i)]));
   while (t[i - p[i]] == t[i + p[i]]) p[i]++;
   if (i + p[i] > r) {
      l = i - p[i], r = i + p[i];
   }
   p[i]--;
}

return vi(begin(p) + 1, end(p) - 1);
```

8 Trees

8.1 LCA Binary Lifting (CP Algo)

The algorithm described will need $O(N \cdot \log N)$ for preprocessing the tree, and then $O(\log N)$ for each LCA query.

```
ll n, 1;
vector < 11 > adj [MAX];
ll timer:
vector<ll> tin, tout;
vector < vector < ll >> up;
void dfs(ll v, ll p) {
 tin[v] = ++timer:
  for (ll i = 1; i <= 1; ++i) up[v][i] = up[up[v][i - 1]][i - 1];
  for (ll u : adj[v]) {
   if (u != p) dfs(u, v);
  tout[v] = ++timer;
bool is_ancestor(ll u, ll v) { return tin[u] <= tin[v] && tout[u] >= tout[v];
11 1ca(11 u, 11 v) {
  if (is_ancestor(u, v)) return u;
  if (is_ancestor(v, u)) return v;
  for (11 i = 1: i >= 0: --i) {
    if (!is_ancestor(up[u][i], v)) u = up[u][i];
  return up[u][0];
void preprocess(ll root) {
  tin.resize(n):
```

```
tout.resize(n);
timer = 0;
l = ceil(log2(n));
up.assign(n, vector<ll>(l + 1));
dfs(root, root);
}
```

8.2 LCA SegTree (CP Algo)

The algorithm can answer each query in $O(\log N)$ with preprocessing in O(N) time.

```
struct LCA {
 vector <11> height, euler, first, segtree;
 vector < bool > visited;
 11 n;
 LCA(vector < vector < 11 >> & adj, 11 root = 0) {
    n = adj.size();
    height.resize(n):
   first.resize(n):
    euler.reserve(n * 2):
    visited.assign(n, false);
    dfs(adj, root);
    11 m = euler.size():
    segtree.resize(m * 4);
   build(1, 0, m - 1);
  void dfs(vector<vector<ll>>& adi. ll node. ll h = 0) {
    visited[node] = true;
    height[node] = h;
    first[node] = euler.size();
    euler.push_back(node);
    for (auto to : adi[node]) {
     if (!visited[to]) {
        dfs(adj, to, h + 1);
        euler.push_back(node);
   }
  void build(ll node, ll b, ll e) {
   if (b == e) {
      segtree[node] = euler[b];
   } else {
      11 \text{ mid} = (b + e) / 2;
      build(node << 1. b. mid):
      build(node << 1 | 1, mid + 1, e);
     11 1 = segtree[node << 1], r = segtree[node << 1 | 1];</pre>
      segtree[node] = (height[1] < height[r]) ? 1 : r;</pre>
   }
 }
 11 query(11 node, 11 b, 11 e, 11 L, 11 R) {
    if (b > R || e < L) return -1;
    if (b >= L && e <= R) return segtree[node]:
   11 \text{ mid} = (b + e) >> 1;
```

```
ll left = query(node << 1, b, mid, L, R);
ll right = query(node << 1 | 1, mid + 1, e, L, R);
if (left == -1) return right;
if (right == -1) return left;
return height[left] < height[right] ? left : right;
}

ll lca(ll u, ll v) {
  ll left = first[u], right = first[v];
  if (left > right) swap(left, right);
  return query(1, 0, euler.size() - 1, left, right);
}
};
```

8.3 LCA Sparse Table

The algorithm described will need O(N) for preprocessing, and then O(1) for each LCA query. 0 indexed!

```
typedef vector < vl> vl2d;
#define all(a) a.begin(), a.end()
#define len(x) (int)x.size()
template <typename T>
struct SparseTable {
 vector <T> v:
 11 n:
  static const 11 b = 30;
  vl mask, t:
  11 op(11 x, 11 y) { return v[x] < v[y] ? x : y; }</pre>
  11 msb(ll x) { return __builtin_clz(1) - __builtin_clz(x); }
  SparseTable(const vector<T>& v ) : v(v ), n(v.size()), mask(n), t(n) {
   for (ll i = 0, at = 0; i < n; \max[i++] = at |= 1) {
      at = (at << 1) & ((1 << b) - 1);
      while (at and op(i, i - msb(at & -at)) == i) at ^= at & -at:
   for (11 i = 0; i < n / b; i++)</pre>
     t[i] = b * i + b - 1 - msb(mask[b * i + b - 1]):
   for (ll j = 1; (1 << j) <= n / b; j++)
     for (ll i = 0; i + (1 << j) <= n / b; i++)
       t[n / b * i + i] =
          op(t[n / b * (j - 1) + i], t[n / b * (j - 1) + i + (1 << (j - 1))]);
  ll small(ll r, ll sz = b) { return r - msb(mask[r] & ((1 << sz) - 1)); }
  T querv(ll 1, ll r) {
   if (r - l + 1 <= b) return small(r, r - l + 1);</pre>
   ll ans = op(small(1 + b - 1), small(r));
   11 x = 1 / b + 1, y = r / b - 1;
   if (x <= y) {
     11 j = msb(y - x + 1);
      ans = op(ans, op(t[n / b * j + x], t[n / b * j + y - (1 << j) + 1]));
   return ans;
 }
};
```

```
struct LCA {
  SparseTable < 11 > st;
 11 n;
 vl v, pos, dep;
 LCA(const v12d& g, ll root) : n(len(g)), pos(n) {
    dfs(root, 0, -1, g);
    st = SparseTable < 11 > (vector < 11 > (all (dep)));
 void dfs(ll i, ll d, ll p, const vl2d& g) {
    v.emplace_back(len(dep)) = i, pos[i] = len(dep), dep.emplace_back(d);
    for (auto j : g[i])
      if (j != p) {
        dfs(j, d + 1, i, g);
        v.emplace_back(len(dep)) = i, dep.emplace_back(d);
 }
 11 lca(ll a, ll b) {
   11 1 = min(pos[a], pos[b]);
   11 r = max(pos[a], pos[b]);
    return v[st.query(1, r)];
 11 dist(ll a, ll b) {
    return dep[pos[a]] + dep[pos[b]] - 2 * dep[pos[lca(a, b)]];
};
```

8.4 Tree Isomorph

Checks whether two tree are isomorph. The function thash() returns the hash of the tree (using centroids as special vertices). Two trees are isomorph if their hash are the same.

```
map < vector < int > , int > mphash;
struct tree {
 int n;
 vector < vector < int >> g;
 vector < int > sz, cs;
 tree(int n_) : n(n_), g(n_), sz(n_) {}
 void dfs_centroid(int v, int p) {
    sz[v] = 1:
    bool cent = true;
   for (int u : g[v])
      if (u != p) {
        dfs_centroid(u, v), sz[v] += sz[u];
        if (sz[u] > n / 2) cent = false:
    if (cent and n - sz[v] <= n / 2) cs.push_back(v);</pre>
 int fhash(int v, int p) {
    vector < int > h;
    for (int u : g[v])
      if (u != p) h.push_back(fhash(u, v));
    sort(h.begin(), h.end());
```

```
if (!mphash.count(h)) mphash[h] = mphash.size();
    return mphash[h];
}

ll thash() {
    cs.clear();
    dfs_centroid(0, -1);
    if (cs.size() == 1) return fhash(cs[0], -1);
    ll h1 = fhash(cs[0], cs[1]), h2 = fhash(cs[1], cs[0]);
    return (min(h1, h2) << 30) + max(h1, h2);
}

void add(int a, int b) {
    g[a].emplace_back(b);
    g[b].emplace_back(a);
}
};</pre>
```

9 Settings and macros

9.1 macro.cpp

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
#define ordered_set tree<int, null_type, less<int>, rb_tree_tag,
    tree_order_statistics_node_update>
using namespace std;
typedef long long 11;
typedef pair<int, int> pii;
typedef pair<11, 11> pll;
typedef vector<int> vi;
typedef vector<1l> v1;
typedef vector<pii> vii;
typedef vector <pll> vll;
#define fst first
#define snd second
#define all(x) x.begin(), x.end()
#define vin(vt) for (auto &e : vt) cin >> e
#define LSOne(S) ((S) & -(S))
#define MSOne(S) (1ull << (63 - __builtin_clzll(S)))</pre>
#define fastio ios_base::sync_with_stdio(0); \
               cin.tie(0): \
               cout.tie(0)
const vii dir4 {{1.0}.{-1.0}.{0.1}.{0.-1}}:
auto solve() { }
int main() {
   fastio:
   11 t = 1:
```

```
//cin >> t;
while (t--) solve();
return 0;
}
9.2 short-macro.cpp
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
typedef pair<int, int> ii;
```

#define all(x) x.begin(), x.end()

```
#define vin(vt) for (auto &e : vt) cin >> e
auto solve() { }
int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);

    ll t = 1;
    //cin >> t;

    while (t--) solve();

    return 0;
}
```