

**University of Brasília**  
**Electrical Engineering Department**



**Topics in Biomedical Engineering**  
**Task 6**

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September 16, 2022

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# 1 Subject f2o02 - Elderly Subject

The elderly subject (**f2o02**) is the same analyzed in the Task 5. The processes of filtering (Notch Filter - 60 Hz in the ECG signal of this subject and Low-Pass Filter in the RRI signal), R peaks detection, SBP/DBP peaks detection, interpolation, resampling (Berger Algorithm) and spectral windowing (Hanning Window) were done according to the previous task.

The Low-Pass Filter applying in the RRI signal is important because it works as an anti-aliasing filter and must be applied before calculate the spectral analysis.

## 1.1 Signal Preprocessing

The steps of preprocessing were the same adopted in the Task 5. The time interval was restricted in five minutes (300 seconds), and, in this subject, the interval between 2100 and 2400 seconds (minute 35 and minute 40) has little noise and generates a good observation around electrocardiogram and blood pressure signals. Thus, the **interval 2100 to 2400** seconds was the observed interval.

## 1.2 Transfer Function ( $H(j\omega)$ - SBP $\rightarrow$ RRI)

In sequence, with the spectral analysis (PSD - Power Spectral Density) done on the CRSIDLab in the previous task, was determined the transfer function of this system. The system was defined considering SBP (Systolic Blood Pressure) as the input and the RRI (RR Interval) as the output.

The MATLAB's code to define the transfer function of the subject **f2o02** was:

```
1 %% Subject f2o02 - Elderly
2 clc; clear all; close all;
3 warning('off');
4
5 % obs.: only 60 Hz filter
6 %% TASK 6
7
8 load t5_f2o02.mat; % load of patient file - CRSIDLab
9 open('patient');
10
```

```

11 tempo = patient.sig.ecg.rri.aligned.time;
12 rri_detrend = detrend(patient.sig.ecg.rri.aligned.data)
    ; % retira trend linear do rri
13 sbp_detrend = detrend(patient.sig.bp.sbp.aligned.data);
    % retira trend linear do sbp
14
15 % Janelamento (detrend) antes de se calcular a FFT:
16 N = length(rri_detrend);
17 u = sbp_detrend.*hanning(length(sbp_detrend)); % esta
    será a entrada X(s)
18 y = rri_detrend.*hanning(length(rri_detrend)); % esta
    será a saída Y(s)
19 fs = 4; % em Hz; frequencia de reamostragem
20
21 T = N/fs; % Tempo de observação, = N*dt, onde dt = 1/fs
    = 1/4 s
22 U = fft(u);
23 U = U(2:((N/2)+1)); % Usar apenas metade do vetor. U(1)
    representa o valor médio
24 Suu = 1/N*real(conj(U).*U); % PSD é real por definição(
    a parte imaginária deve ser muito pequena)
25
26 Y = fft(y); % FFT = Fast Fourier Transform
27 Y = Y(2:((N/2)+1));
28
29 Syy=1/N*real(conj(Y).*Y); % Densidade espectral de
    potencia (PSD) de y
30 Suy=1/N*conj(U).*Y; % Densidade espectral de potência
    cruzada (CPSD) de u e y
31 f=(1:(N/2)).'/T; % Vetor de frequências
32 Hsbp=Suy./Suu; % Estimativa para função de resposta em
    frequência (FRF)
33 Csbp=abs(Suy).^2./(Suu.*Syy); % Estimativa para a coerê
    ncia
34
35 % Plotando a função resposta em frequência (FRF) e a
    coerência
36 % (seguindo o modelo implementado em "Lec3_SmoothSuu.m"
    :
37 figure(1)
38 subplot(311)

```

```

39 loglog(f,abs(Hsbp), 'b', 'linewidth', 1.3); grid;
40 xlabel('Frequency');
41 ylabel('|H(w)|');
42 title('Module of Frequency Response');
43
44 subplot(312)
45 semilogx(f,angle(Hsbp)*180/pi, 'b', 'linewidth', 1.3);
    grid;
46 xlabel('Frequency');
47 ylabel('<H(w)');
48 title('Phase of Frequency Response');
49
50 subplot(313)
51 semilogx(f,Csbp, 'b', 'linewidth', 1.3); grid;
52 xlabel('Frequency');
53 ylabel('C(w)');
54 title('Coherence'); hold on;
55 saveas(gcf, 't6_old_fig1.png');
56 % Veja que o fato da coerência dar sempre 1 é um "
    % problema" da FFT sem média alguma.
57 % Fazendo pelo método de Welch:
58
59 %% * MÉTODO DE WELCH *
60 % Resumo: Divide o sinal em vários trechos. Esses
    % trechos são organizados de forma a
61 % ficarem com determinada percentagem de seu
    % comprimento sobreposta ao trecho
62 % anterior. Assim, o método calcula o espectro
    % aplicando a transformada de Fourier
63 % nesses trechos menores do sinal.
64 % Aqui, utiliza-se 50% de sobreposição e 8 trechos do
    % sinal.
65
66 [SuuW, fw1] = cpsd(u,u,[],[],[],4);
67 [SyyW, fw2] = cpsd(y,y,[],[],[],4);
68 [SuyW, fw3] = cpsd(u,y,[],[],[],4);
69
70 %%% Função de transferência
71 HWsbp=SuyW./SuuW;
72 CWsbp=abs(SuyW).^2./(SuuW.*SyyW);

```

```

73
74 % Plotando o resultado (como em "Lec3_SmoothSuu.m"):
75 figure(2)
76 subplot(311)
77 loglog(fw1,abs(HWsbp), 'r', 'linewidth', 1.3); grid;
78 xlabel('Frequency');
79 ylabel('|H(w)|');
80 title('Module of the Frequency Response - Welch Method'
      );
81
82 subplot(312)
83 semilogx(fw1,angle(HWsbp)*180/pi, 'r', 'linewidth',
      1.3); grid;
84 xlabel('Frequency');
85 ylabel('<H(w)');
86 title('Phase of the Frequency Responde - Welch Method')
      ;
87
88 subplot(313)
89 semilogx(fw1,CWsbp,'r', 'linewidth', 1.3); grid %
      COMPARE COM AS FIGURAS DO FFT
90 xlabel('Frequency');
91 ylabel('C(w)');
92 title('Coherence - Welch Method');
93 saveas(gcf, 't6_old_fig2.png');
94 %% Cálculo das áreas de BF (baixa frequencia) e AF (
      alta frequencia) da FT:
95 % (continuação)
96
97 %close all; clear all; clc;
98
99 HWsbp_lf = zeros(size(HWsbp));
100 HWsbp_hf = zeros(size(HWsbp));
101 for i = 1:length(HWsbp)
102     if (fw1(i)>= 0.04) && (fw1(i) <= 0.15)
103         HWsbp_lf(i) = abs(HWsbp(i));
104     else
105         HWsbp_lf(i) = 0;
106     end
107
108     if (fw1(i)> 0.15) && (fw1(i) <= 0.4)

```

```

109         HWsbp_hf(i) = abs(HWsbp(i));
110     else
111         HWsbp_hf(i) = 0;
112     end
113 end
114
115 area_H_LF = trapz(HWsbp_lf);
116 area_H_HF = trapz(HWsbp_hf);
117
118 %% Cálculo das áreas de BF (baixa frequencia) e AF (
    alta frequencia) da FT:
119 % Considerando apenas os pontos com coerência acima de
    0,5: parte onde a entrada
120 % e a saída possuem uma relação linear
    independentemente do tipo de sys
121 % (onde faz sentido calcular a função de transferência
    (tf))
122
123 HWsbp_lf_c = zeros(size(HWsbp));
124 HWsbp_hf_c = zeros(size(HWsbp));
125 for i = 1:length(HWsbp)
126     if (fw1(i) >= 0.04) && (fw1(i) <= 0.15) && (CWsbp(i)
        > 0.5)
127         HWsbp_lf(i) = abs(HWsbp(i));
128     else
129         HWsbp_lf(i) = 0;
130     end
131     if (fw1(i) > 0.15) && (fw1(i) <= 0.4) && (CWsbp(i) >
        0.5)
132         HWsbp_hf(i) = abs(HWsbp(i));
133     else
134         HWsbp_hf(i) = 0;
135     end
136 end
137
138 area_H_LF_c = trapz(HWsbp_lf);
139 area_H_HF_c = trapz(HWsbp_hf);
140
141 sprintf('Elderly Subject - f2o02: \n HLF_c = %d \n
    HLF_c = %d', area_H_LF_c, area_H_HF_c) % print areas

```

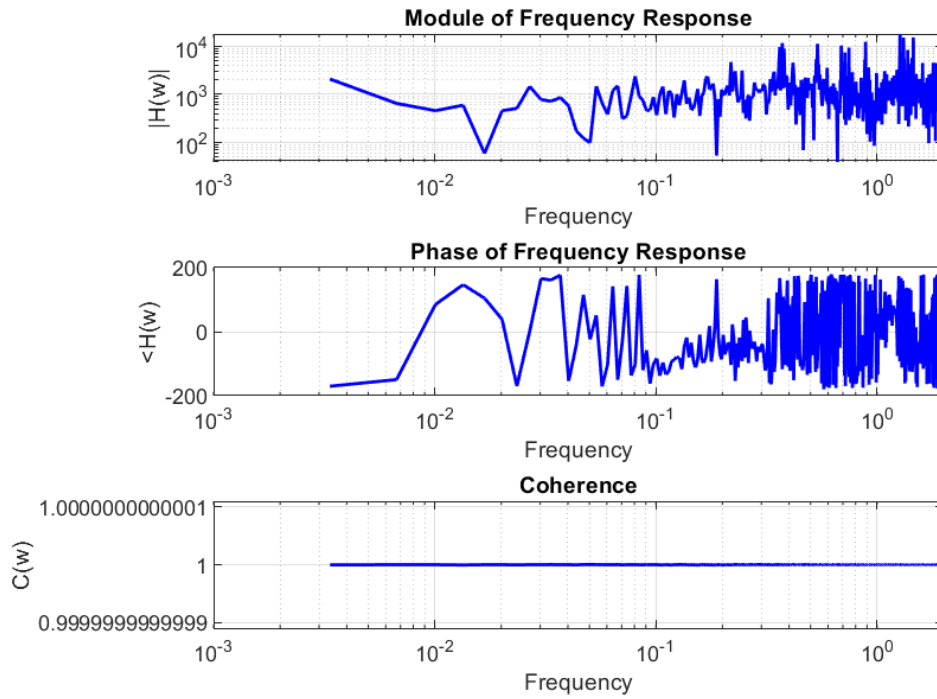


Figure 1

It is possible to visualize in the Figure 1 that the non-application of a spectral average model, the Welch method in this case, generates a unitary value of coherence.

In the Figure 2, the Welch method was applied in the input and output before calculating the transfer function. Visually, it provided significant values of coherence to be analyzed.



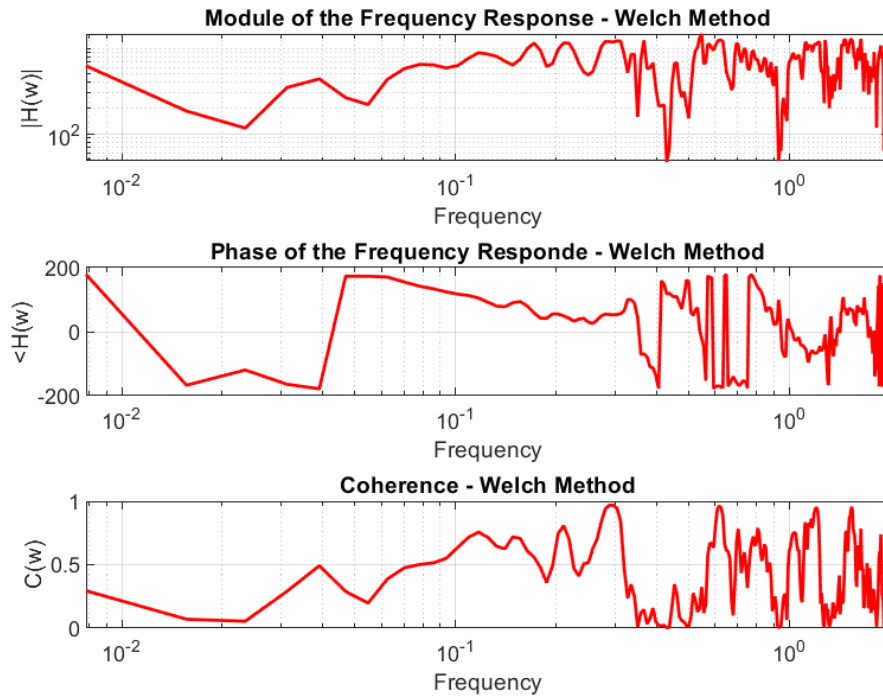


Figure 2

This code also calculates the absolute area in the low frequencies (0.04 to 0.15 Hz) and in the high frequencies (0.15 to 0.4 Hz). These calculated absolute areas, considering coherence bigger than 0.5, were:

```
'Elderly Subject - f2o02:
  HLF_c = 7.200607e+03
  HLF_c = 1.562884e+04'
```

Figure 3

The choice to calculate the absolute area of the signal spectrum only in snippets with coherence bigger than 0.5 was done in order to get more reasonable results. The coherence measure how linear the relationship between

input and output is, and the transfer function is a relation between the ratio of the output and the input of a linear system. Therefore, this value of coherence (bigger than 0.5) is an acceptable marker in the biomedical signal analysis literature. It is stated on Saul, J. P., Berger et al. Transfer function analysis of the circulation: unique insights into cardiovascular regulation. American Journal of Physiology-Heart and Circulatory Physiology. 1991: "The coherence spectra are near or above 0.5 throughout at most indicating that the magnitude and phase estimates are relatively reliable at those frequencies."

## 2 Subject **f2y02** - Young Subject

The young subject (**f2o02**) is also the same analyzed in the Task 5. The processes of filtering (No filters in the ECG signal of this subject and Low-Pass Filter in the RRI signal), R peaks detection, SBP/DBP peaks detection, interpolation, resampling (Berger Algorithm) and spectral windowing (Hanning Window) were done according to the previous task.

The Low-Pass Filter applying in the RRI signal is important because it works as an anti-aliasing filter and must be applied before calculate the spectral analysis.

### 2.1 Signal Preprocessing

In the same way of the elderly subject, the steps of preprocessing were the same adopted in the Task 5. The time interval was restricted in five minutes (300 seconds), and, in this subject, the interval between 2100 and 2400 seconds (minute 35 and minute 40) has also little noise and provides a good observation around electrocardiogram and blood pressure signals. Thus, the **interval 2100 to 2400** seconds was the observed interval.

### 2.2 Transfer Function ( $H(j\omega)$ - SBP $\rightarrow$ RRI)

In this subject, was also determined the transfer function of this system. The system was also defined considering SBP (Systolic Blood Pressure) as the input and the RRI (RR Interval) as the output.

The MATLAB's code to define the transfer function of the subject **f2y02** was:

```

1 %% Subject f2y02 - Young
2 clc; clear all; close all;
3 warning('off');
4
5 % obs.: not necessary to apply filters
6 %% TASK 6
7
8 load t5_f2y02.mat; % load of patient file - CRSIDLab
9 open('patient');
10
11 tempo = patient.sig.ecg.rri.aligned.time;
12 rri_detrend = detrend(patient.sig.ecg.rri.aligned.data)
    ; % retira trend linear do rri
13 sbp_detrend = detrend(patient.sig.bp.sbp.aligned.data);
    % retira trend linear do sbp
14
15 % Janelamento (detrend) antes de se calcular a FFT:
16 N = length(rri_detrend);
17 u = sbp_detrend.*hanning(length(sbp_detrend)); % esta
    será a entrada X(s)
18 y = rri_detrend.*hanning(length(rri_detrend)); % esta
    será a saída Y(s)
19 fs = 4; % em Hz; frequencia de reamostragem
20
21 T = N/fs; % Tempo de observação, = N*dt, onde dt = 1/fs
    = 1/4 s
22 U = fft(u);
23 U = U(2:((N/2)+1)); % Usar apenas metade do vetor. U(1)
    representa o valor médio
24 Suu = 1/N*real(conj(U).*U); % PSD é real por definição(
    a parte imaginária deve ser muito pequena)
25
26 Y = fft(y); % FFT = Fast Fourier Transform
27 Y = Y(2:((N/2)+1));
28
29 Syy=1/N*real(conj(Y).*Y); % Densidade espectral de
    potencia (PSD) de y
30 Suy=1/N*conj(U).*Y; % Densidade espectral de potência
    cruzada (CPSD) de u e y
31 f=(1:(N/2)).'/T; % Vetor de frequências

```

```

32 Hsbp=Suy ./ Suu; % Estimativa para função de resposta em
    frequência (FRF)
33 Csbp=abs(Suy).^2./(Suu.*Syy); % Estimativa para a coerê
    ncia
34
35 % Plotando a função resposta em frequência (FRF) e a
    coerência
36 % (segundo o modelo implementado em "Lec3_SmoothSuu.m"
    :
37 figure(1)
38 subplot(311)
39 loglog(f,abs(Hsbp),'b','linewidth',1.3); grid;
40 xlabel('Frequency');
41 ylabel('|H(w)|');
42 title('Module of Frequency Response');
43
44 subplot(312)
45 semilogx(f,angle(Hsbp)*180/pi,'b','linewidth',1.3);
    grid;
46 xlabel('Frequency');
47 ylabel('<H(w)');
48 title('Phase of Frequency Response');
49
50 subplot(313)
51 semilogx(f,Csbp,'b','linewidth',1.3); grid;
52 xlabel('Frequency');
53 ylabel('C(w)');
54 title('Coherence'); hold on
55 saveas(gcf,'t6_young_fig1.png');
56 % Veja que o fato da coerência dar sempre 1 é um "
    problema" do método de coerência sem média alguma.
57 % Fazendo pelo método de Welch:
58
59 %% * MÉTODO DE WELCH *
60 % Resumo: Divide o sinal em vários trechos. Esses
    trechos são organizados de forma a
61 % ficarem com determinada percentagem de seu
    comprimento sobreposta ao trecho
62 % anterior. Assim, o método calcula o espectro
    aplicando a transformada de Fourier

```

```

63 % nesses trechos menores do sinal.
64 % Aqui, utiliza-se 50% de sobreposição e 8 trechos do
    sinal.
65
66 [SuuW, fw1] = cpsd(u, u, [], [], [], 4);
67 [SyyW, fw2] = cpsd(y, y, [], [], [], 4);
68 [SuyW, fw3] = cpsd(u, y, [], [], [], 4);
69
70 %%% Função de transferência
71 HWsbp=SuyW./SuuW;
72 CWsbp=abs(SuyW).^2./(SuuW.*SyyW);
73
74 % Plotando o resultado (como em "Lec3_SmoothSuu.m"):
75 figure(2)
76 subplot(311)
77 loglog(fw1, abs(HWsbp), 'r', 'linewidth', 1.3); grid;
78 xlabel('Frequency');
79 ylabel('|H(w)|');
80 title('Module of the Frequency Response - Welch Method'
    );
81
82 subplot(312)
83 semilogx(fw1, angle(HWsbp)*180/pi, 'r', 'linewidth',
    1.3); grid;
84 xlabel('Frequency');
85 ylabel('<H(w)');
86 title('Phase of the Frequency Responde - Welch Method')
    ;
87
88 subplot(313)
89 semilogx(fw1, CWsbp, 'r', 'linewidth', 1.3); grid %
    COMPARE COM AS FIGURAS DO FFT
90 xlabel('Frequency');
91 ylabel('C(w)');
92 title('Coherence - Welch Method');
93 saveas(gcf, 't6_young_fig2.png');
94
95 %%% Cálculo das áreas de BF (baixa frequencia) e AF (
    alta frequencia) da FT:
96 % (continuação)
97

```

```

98 %close all; clear all; clc;
99
100 HWsbp_lf = zeros (size (HWsbp));
101 HWsbp_hf = zeros (size (HWsbp));
102 for i = 1:length (HWsbp)
103     if (fw1(i) >= 0.04) && (fw1(i) <= 0.15)
104         HWsbp_lf(i) = abs(HWsbp(i));
105     else
106         HWsbp_lf(i) = 0;
107     end
108
109     if (fw1(i) > 0.15) && (fw1(i) <= 0.4)
110         HWsbp_hf(i) = abs(HWsbp(i));
111     else
112         HWsbp_hf(i) = 0;
113     end
114 end
115
116 area_H_LF = trapz (HWsbp_lf);
117 area_H_HF = trapz (HWsbp_hf);
118
119 %% Cálculo das áreas de BF (baixa frequencia) e AF (
120     alta frequencia) da FT:
121 % (continuação)
122 % Considerando apenas os pontos com coerência acima de
123     0,5: parte onde a entrada
124     % e a saída possuem uma relação linear
125     independentemente do tipo de sys
126     % (onde faz sentido calcular a função de transferência
127     (tf))
128
129 HWsbp_lf_c = zeros (size (HWsbp));
130 HWsbp_hf_c = zeros (size (HWsbp));
131 for i = 1:length (HWsbp)
132     if (fw1(i) >= 0.04) && (fw1(i) <= 0.15) && (CWsbp(i)
133         > 0.5)
134         HWsbp_lf(i) = abs(HWsbp(i));
135     else
136         HWsbp_lf(i) = 0;
137     end
138     if (fw1(i) > 0.15) && (fw1(i) <= 0.4) && (CWsbp(i) >

```

```

134         0.5)
135         HWsbp_hf(i) = abs(HWsbp(i));
136     else
137         HWsbp_hf(i) = 0;
138     end
139 end
140 area_H_LF_c = trapz(HWsbp_lf);
141 area_H_HF_c = trapz(HWsbp_hf);
142
143 sprintf('Young Subject - f2y02: \n HLF_c = %d \n HLF_c
= %d', area_H_LF_c, area_H_HF_c) % print areas

```

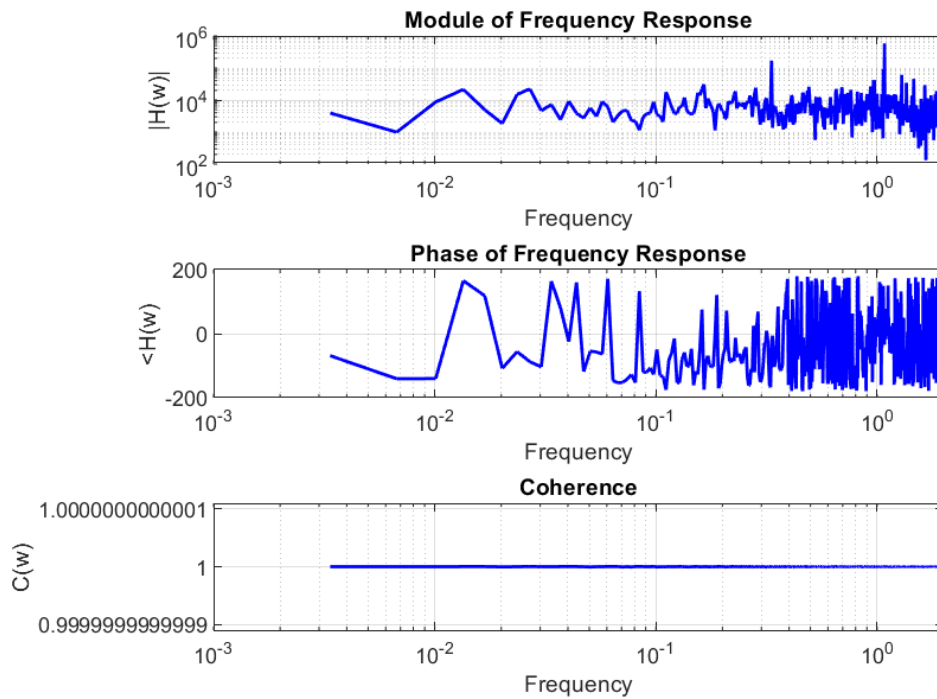


Figure 4

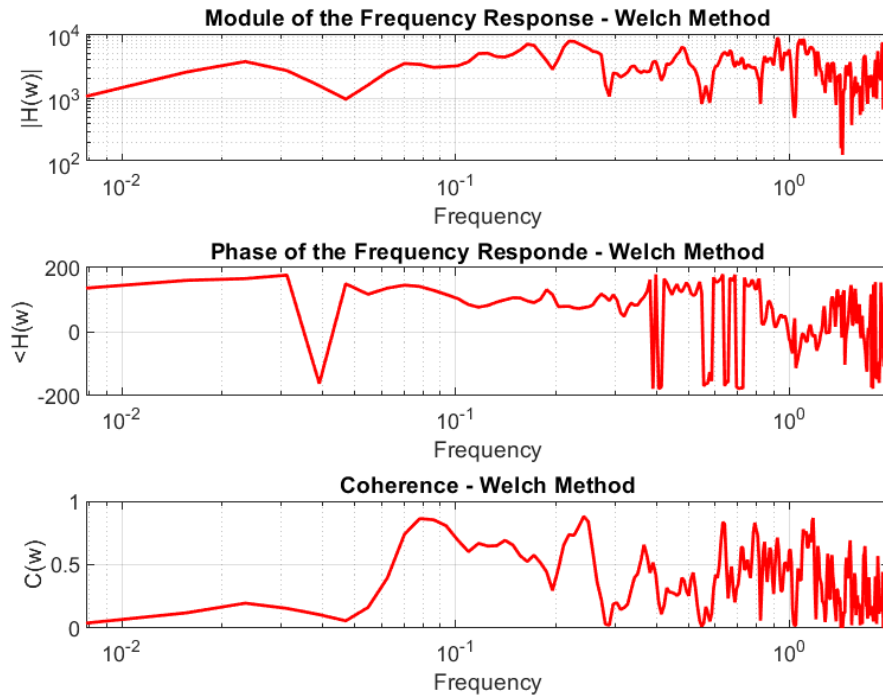


Figure 5

This code also calculates the absolute area in the low frequencies (0.04 to 0.15 Hz) and in the high frequencies (0.15 to 0.4 Hz). These calculated absolute areas, considering coherence bigger than 0.5, were:

```
'Young Subject - f2y02:
  HLF_c = 4.329858e+04
  HLF_c = 8.190362e+04'
```

Figure 6



## References

- [1] “PhysioBank ATM.” [https://archive.physionet.org/cgi-bin/atm/ATM?database=fantasia&tool=plot\\_waveforms](https://archive.physionet.org/cgi-bin/atm/ATM?database=fantasia&tool=plot_waveforms).