



MAC420/5744: Introdução à Computação Gráfica

Marcel P. Jackowski
mjack@ime.usp.br

Aula #20: Princípios de animação

What is animation ?

- **Modeling geometry** = specifying shape
 - Use of meshes, hierarchies, curved surfaces, etc
- **Animation** = specifying shape as a function of time
 - Modeling done once per frame?
 - Needs to be smooth, concerted movement

Keyframes in hand-drawn animation

- End goal: a drawing per frame, with nice smooth motion
- “**Straight ahead**” is drawing frames in order (using a lightbox to see the previous frame or frames)
 - Hard to get a character to land
 - at a particular pose
 - at a particular time
- Instead, use **key frames**
 - draw important poses first, then fill in the in-betweens



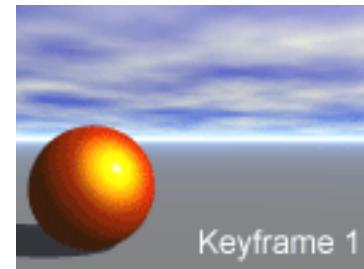
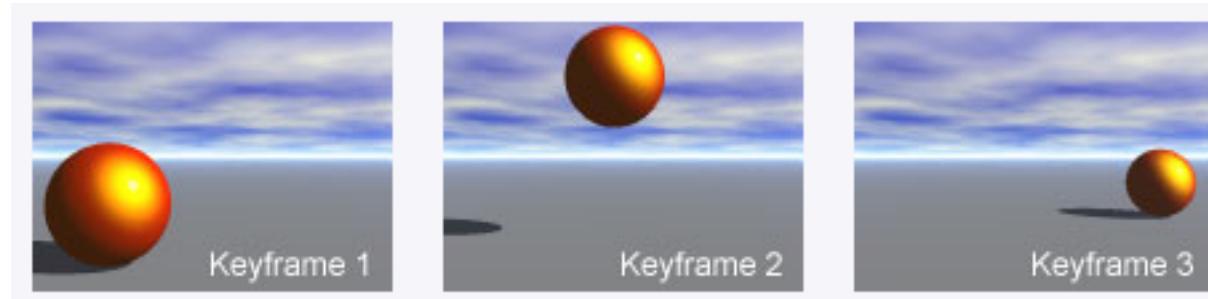
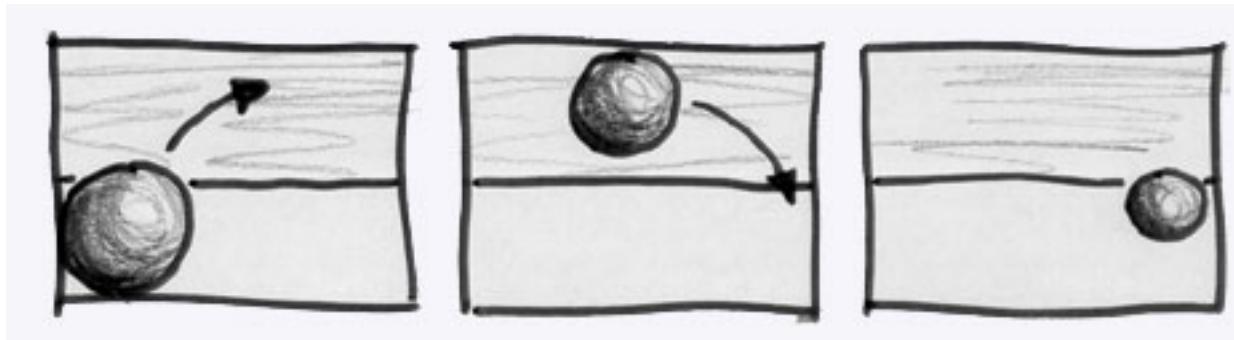
Keyframes in computer animation

- Just as with hand-drawn animation, adjusting the model from scratch for every frame would be tedious and difficult
- Same solution: animator establishes the keyframes, software fills in the in-betweens
- Two key ideas of computer animation:
 - Create **high-level controls** for adjusting geometry
 - **Interpolate these controls** over time between keyframes

The most basic animation control

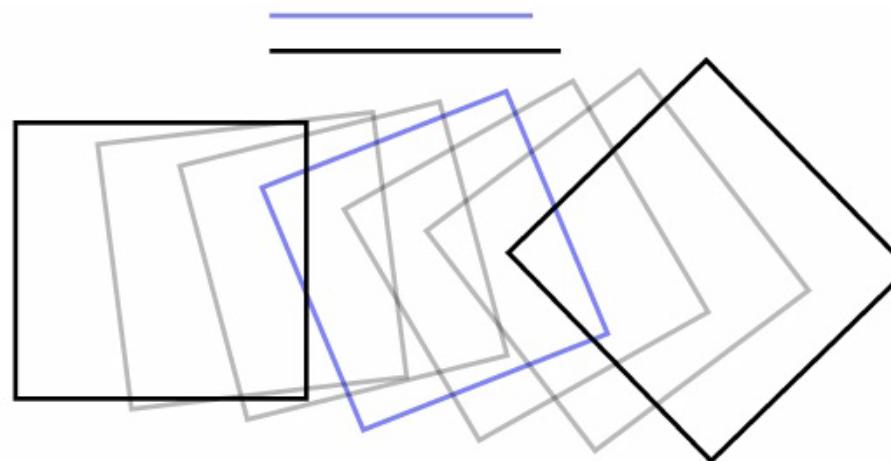
- Affine transformations position things in modeling
- Time-varying affine transformations move things around in animation
- A hierarchy of time-varying transformations is the **main workhorse** of animation
 - Basic framework within which all the more sophisticated techniques are built

Keyframe animation



Interpolating transformations

- Move a set of points by applying an affine transformation
- How to animate the transformation over time?
 - Interpolate the matrix entries from keyframe to keyframe?
 - This is fine for translations but bad for rotations



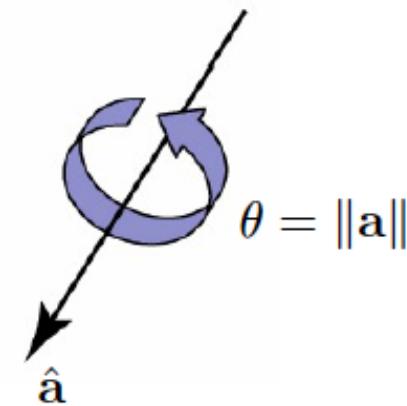
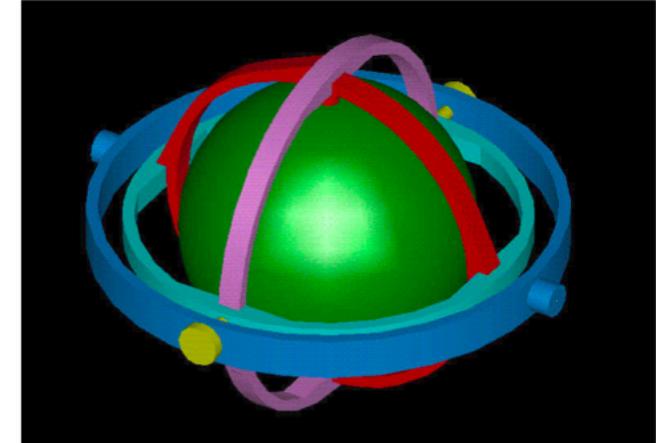
Parameterizing rotations

- Euler Angles
 - Rotate around x, then y, then z
 - Nice and simple

$$f(\alpha, \beta, \gamma) = R_z(\gamma)R_y(\beta)R_x(\alpha)$$

- Axis/Angle
 - Specify **axis** to rotate around, then
 - Specify **Angle** by which to rotate

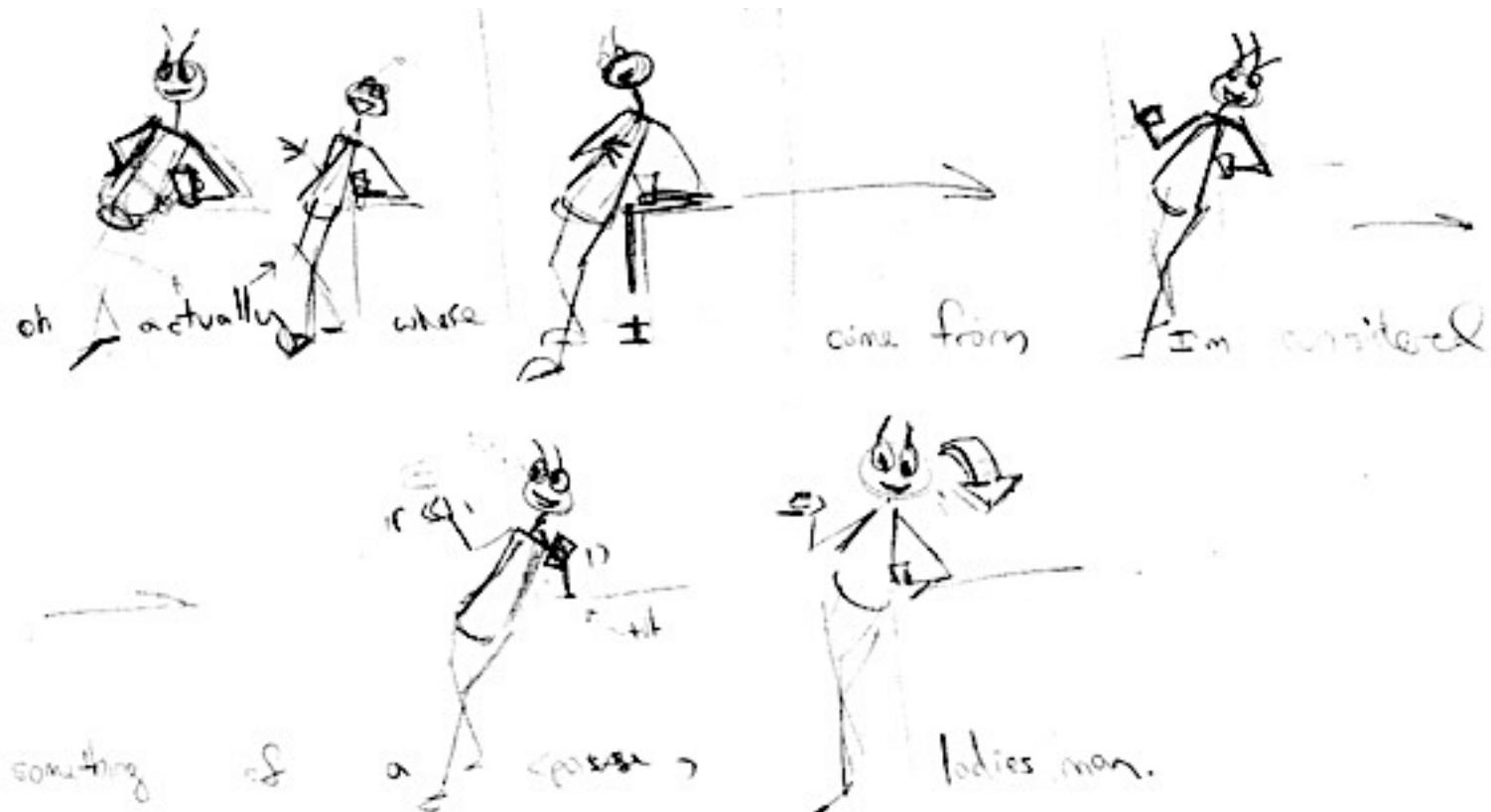
$$f(\mathbf{a}) = R_{\hat{\mathbf{a}}}(\|\mathbf{a}\|)$$



Approaches to animation

- Straight ahead
 - Draw/animate one frame at a time
 - Can lead to spontaneity, but is hard to get exactly what you want
- Pose-to-pose, top-down process
 - Plan shots using storyboards
 - Plan key poses first
 - Finally fill in the in-between frames

Pose-to-pose animation planning



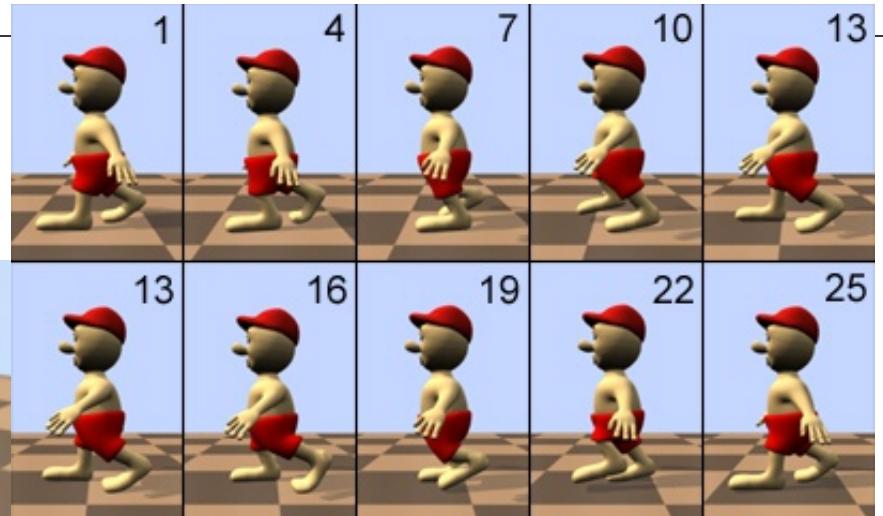
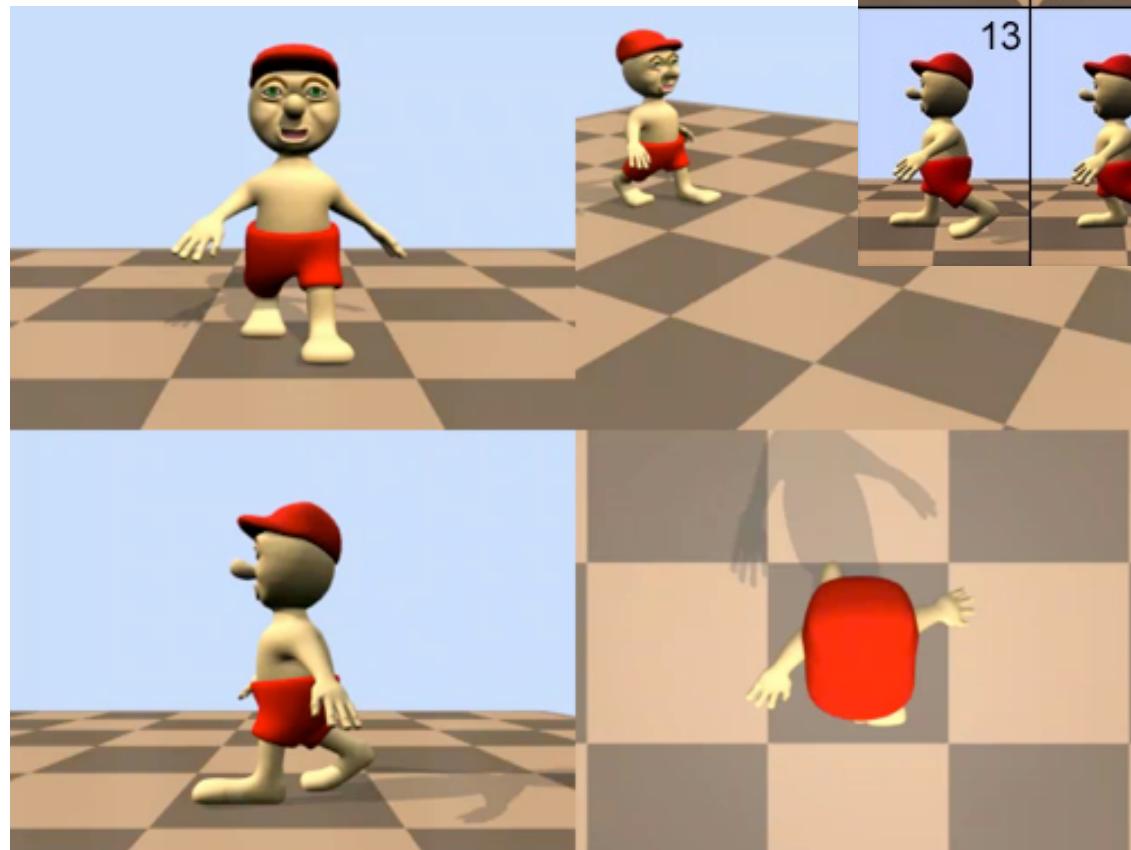
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- First work out poses that are key to the story
- Next fill in animation in between

Keyframe animation

- Keyframing is the technique used for pose-to-pose animation
 - Head animator draws key poses—just enough to indicate what the motion is supposed to be
 - Assistants do “in-betweening” and draw the rest of the frames
 - Interpolation is the principal operation

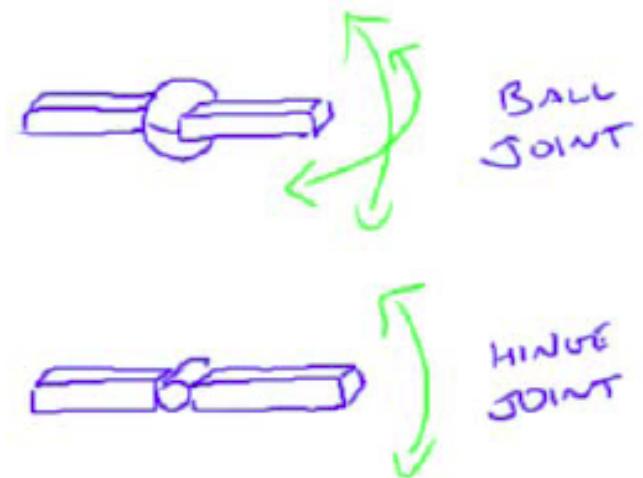
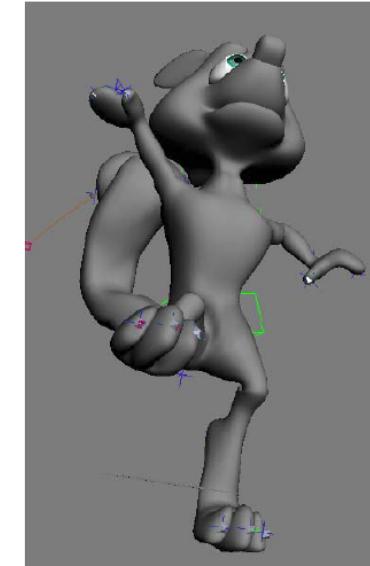
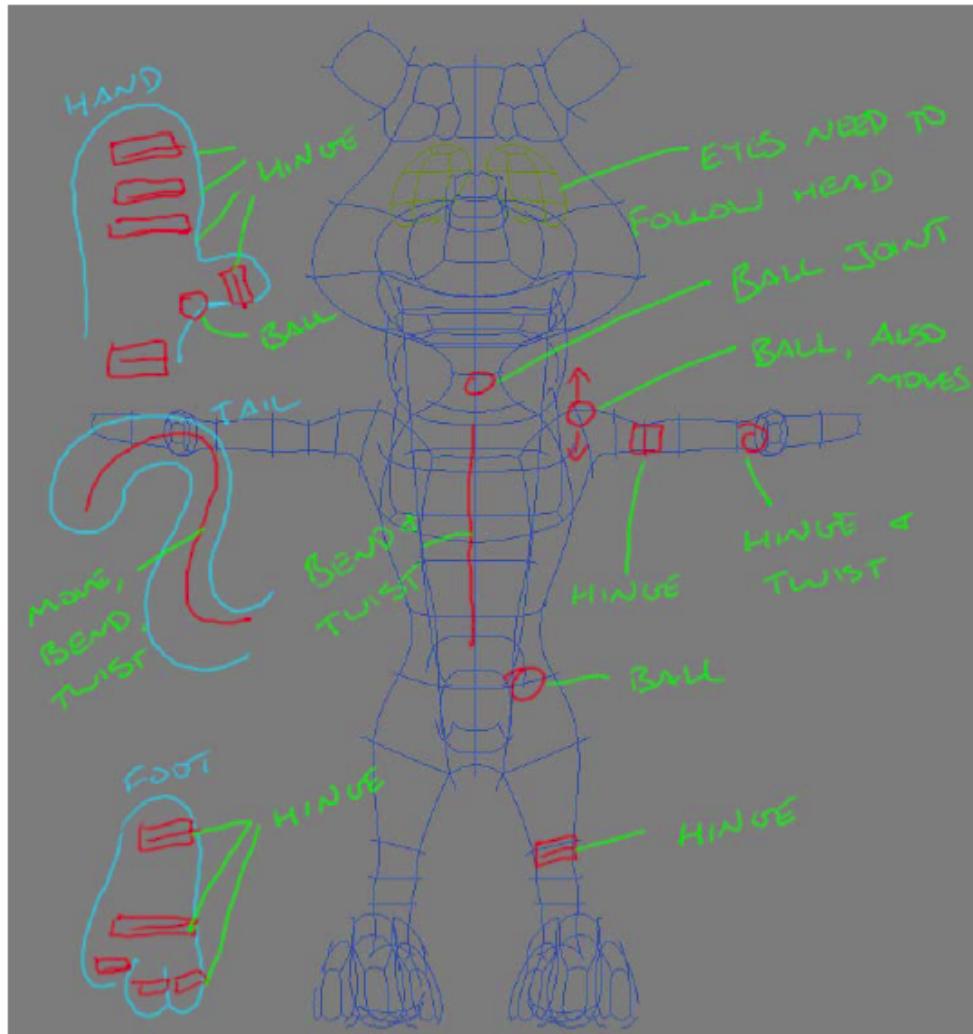
Walk cycle



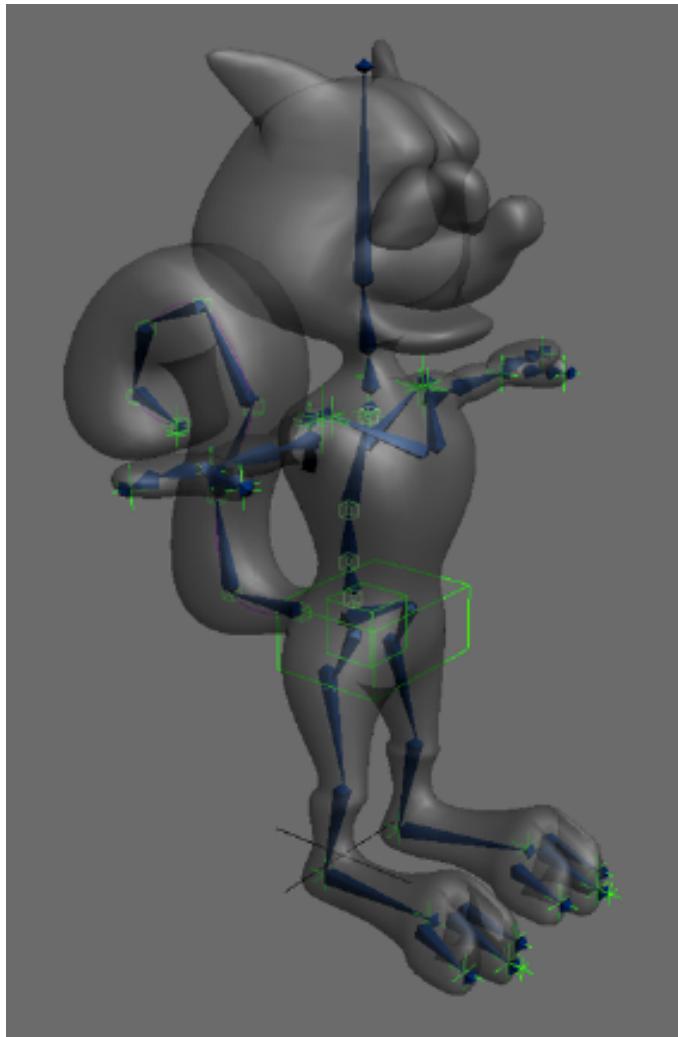
Controlling geometry conveniently

- Could animate by moving every control point at every keyframe
 - This would be labor intensive
 - It would also be hard to get smooth, consistent motion
- Better way: animate using smaller set of meaningful degrees of freedom (DOFs)
 - Modeling DOFs are inappropriate for animation
 - E.g. “*move one inch of left forearm*”
- Animation DOFs need to be higher level
 - E.g. “*bend the elbow*”

Characters with DOFs



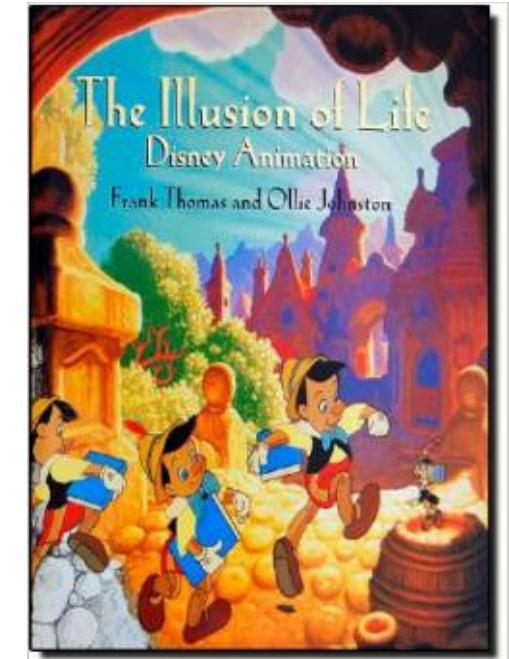
Rigged character



- Surface is deformed by a set of bones
- Bones are in turn controlled by a smaller set of controls
- The controls are useful, intuitive DOFs for an animator to use

The artistic process of animation

- What are animators trying to do?
 - Important to understand what tools they need
- Basic principles are universal across media
 - 2D hand-drawn animation
 - 2D and computer animation
 - 3D computer animation
- Widely cited set of principles laid out by Frank Thomas and Ollie Johnston in “The Illusion of Life” (1981)
 - 12 animation principles



I. Timing

- Speed of an action is crucial to the impression it makes



60 fps



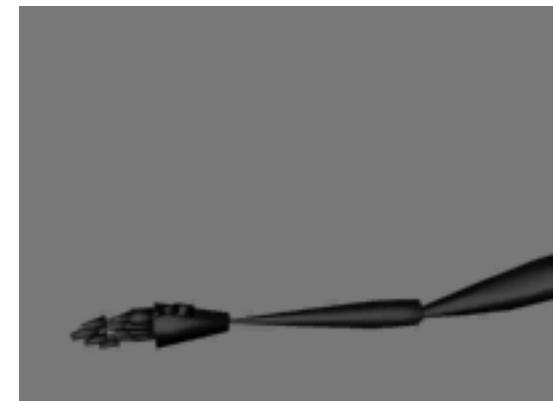
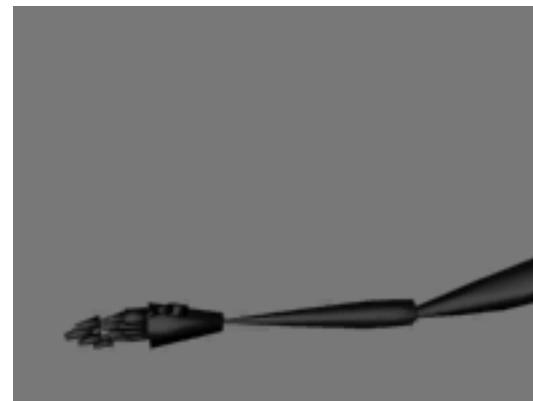
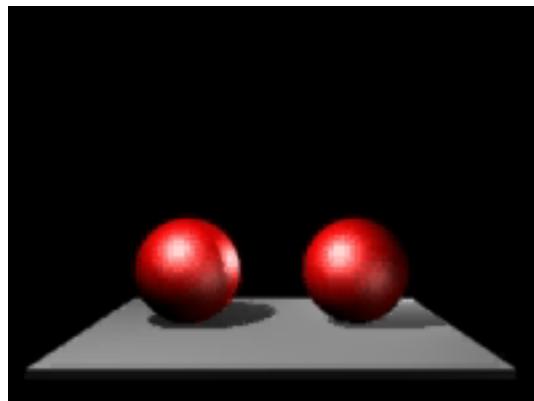
30 fps



5 fps

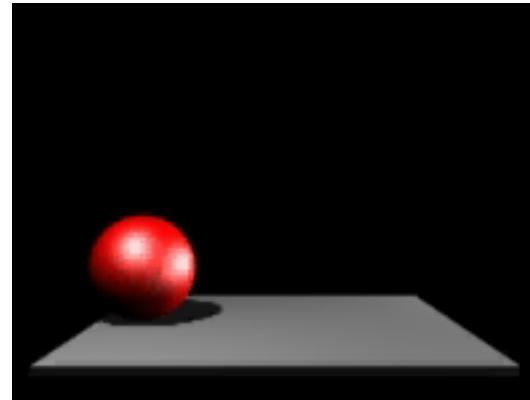
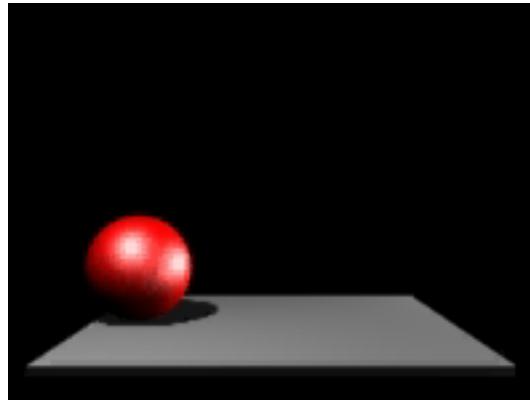
2. Ease in/out (or slow in/out)

- Real objects do not start and stop suddenly
 - Animation parameters shouldn't either
 - A little goes a long way (just a few frames acceleration or deceleration for “snappy” motions)



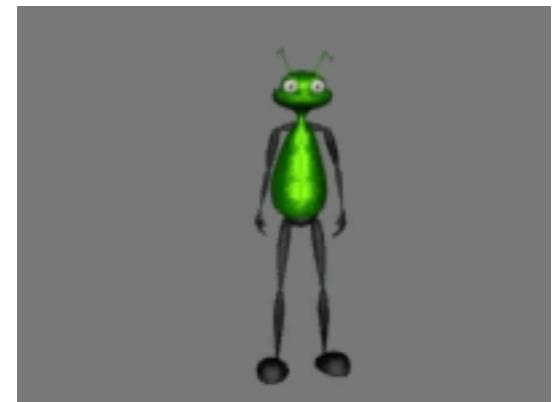
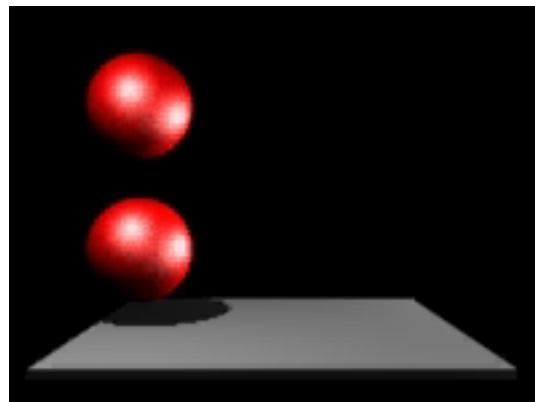
3. Moving in arcs

- Real objects also don't move in straight lines
 - Generally curves are more graceful and realistic



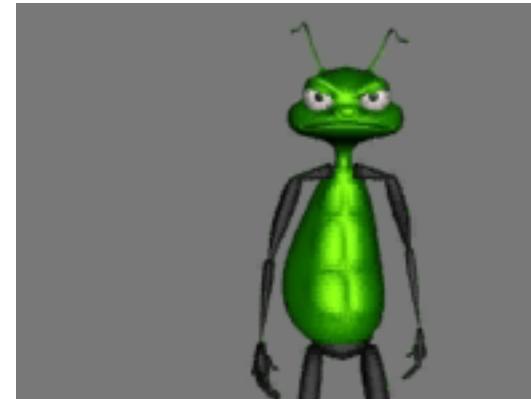
4. Anticipation

- Most actions are preceded by some kind of “wind-up”



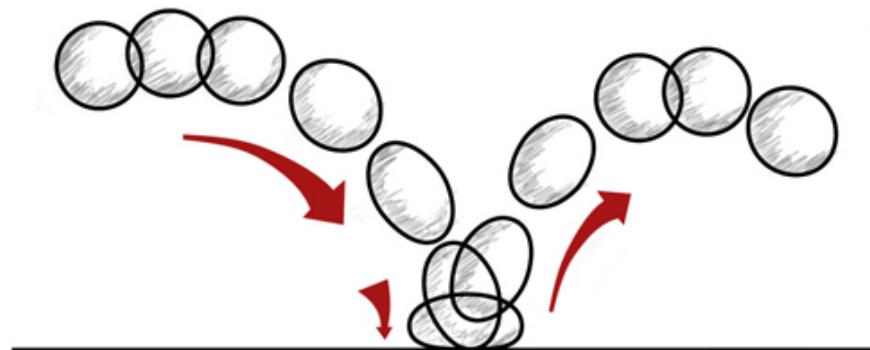
5. Exaggeration

- Animation is not always about modeling reality
- Exaggeration is very often used for emphasis



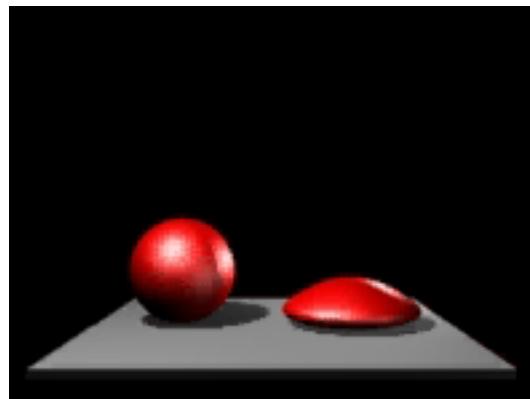
6. Squash and stretch

- Objects do not remain perfectly rigid as they move
- Adding stretch with motion and squash with impact:
 - Models deformation of soft objects
 - Indicates motion by simulating exaggerated “motion blur”



6. Squash and stretch (ii)

- Objects do not remain perfectly rigid as they move
- Adding stretch with motion and squash with impact:
 - Models deformation of soft objects
 - Indicates motion by simulating exaggerated “motion blur”

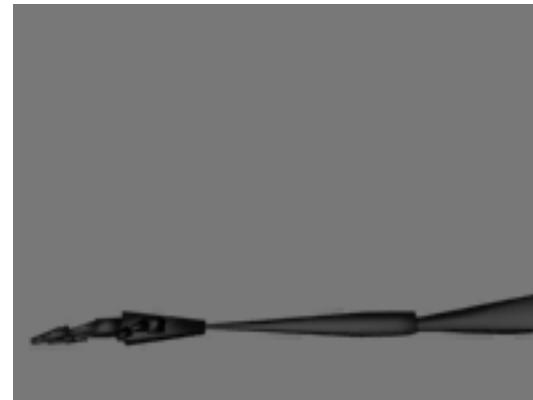
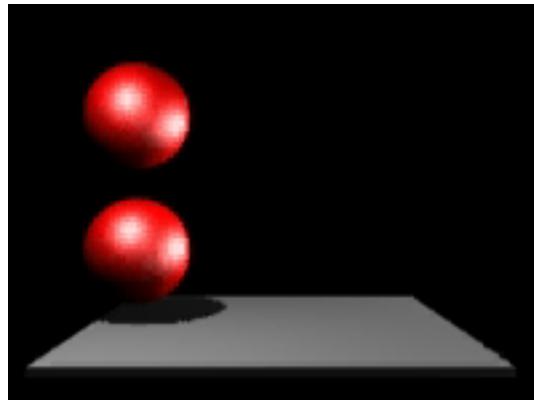


7. Secondary action

- Secondary action creates interest and realism in animation
- It should be staged such that it can be noticed but still *not overpower the main action*
- A good example of this is a character at a table acting and delivering their main acting
 - A side piece of acting business might be the character thumbing their fingers on the table
 - This isn't the main action say, perhaps it occurs as the other hand is more largely gesturing and your focus is on the face.

8. Follow through and overlapping action

- Follow through is the same as anticipation, only at the end of an action
- Overlapping action is an action that occurs because of another action

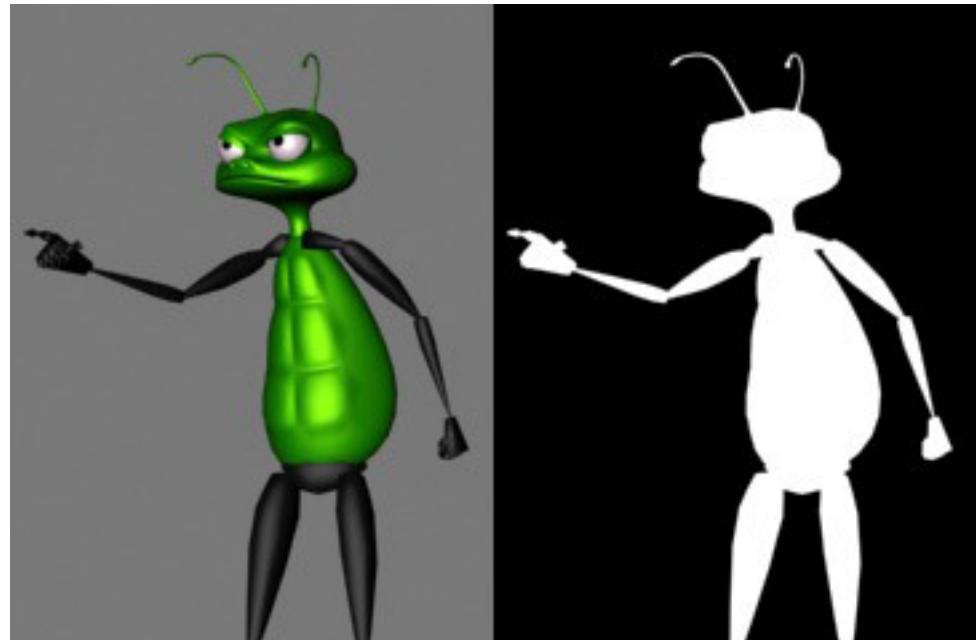
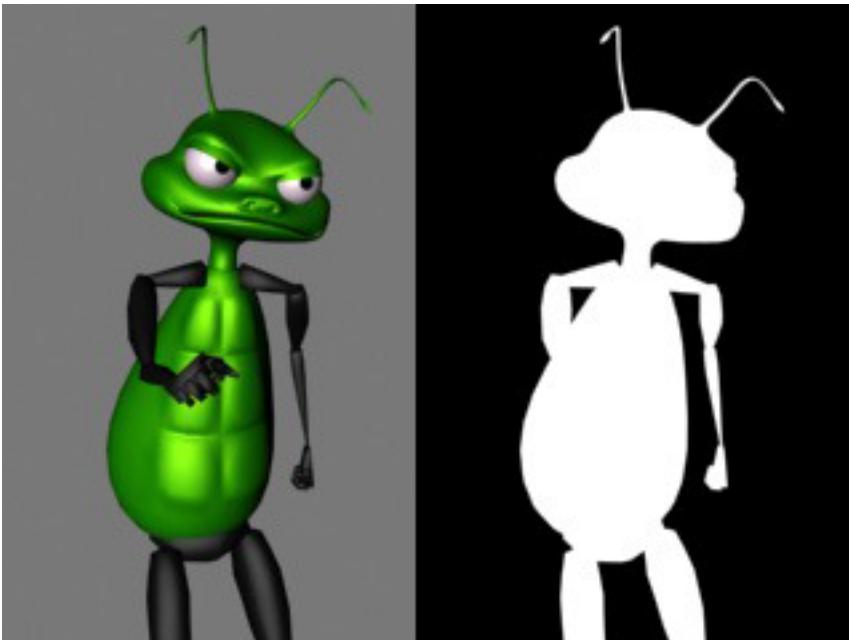


9. Animation strategy

- **Straight ahead:** draws or sets up objects one frame at a time in order
 - This approach tends to yield a more creative and fresh look but can be difficult to time correctly and tweak
- **Pose to pose:** excellent for tweaking timing and planning out the animation ahead of time
 - This is very useful when specific timing or action must occur at specific points
 - You always know exactly what will happen

10. Staging

- Want to produce clear, good-looking 2D images
 - Need good camera angles, set design, and character positions



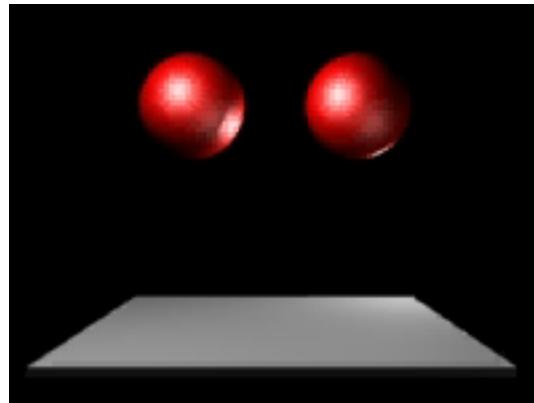
III. Appeal

- Appeal means anything that a person likes to see
 - Quality of charm, design, simplicity, communication or magnetism
 - Appeal can be gained by correctly utilizing other principles such as exaggeration in design, avoiding symmetry, using overlapping action, and others.
- It's important to note that appeal doesn't necessarily mean good vs. evil
 - For example, in Disney's animated classic "Peter Pan", Captain Hook is an evil character, but most people would agree that his character and design has appeal

12. Personality

- Refers to the correct application of the other principles
 - Personality determines the success of an animation
- The animated creature really becomes alive and enters the true character of the role
- One character would not perform an action the same way in two different emotional states
- No two characters would act the same. It is also important to make the personality of a character distinct, but at the same time be familiar to the audience
- Personality has a lot to do with what is going on in the mind of the character, as well as the traits and mannerisms of the character

Principles in practice: weight



Controlling shape for animation

- Start with modeling DOFs (control points)
- Deformations control those DOFs at a higher level
 - E.g. Move first joint of second finger on left hand
- Animation controls control those DOFs at a higher level
 - E.g. open/close left hand
- Both cases can be handled by the same kinds of deformers

Interpolating transformations

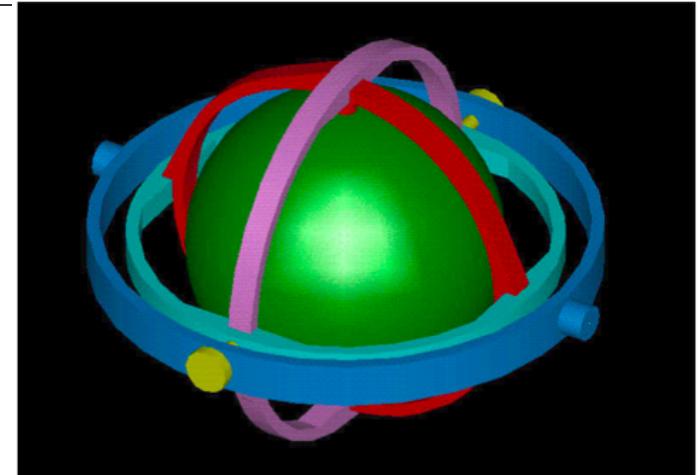
- Linear interpolation of matrices is not effective
- One approach: always keep transformations in a canonical form (e.g. translate-rotate-scale)
 - Then the pieces can be interpolated separately
 - Rotations stay rotations, scales stay scales, all is good
- But you might be faced with just a matrix
 - What then?

Decomposing transformations

- A product $M = TRS$ is not hard to take apart
 - Translation sits in the top right
 - RS still has three orthogonal columns
 - Scale factors are the lengths of the columns
- But that doesn't cover everything
 - Count DOFs: $3 + 3 + 3 < 12$
- If we allow S to be a scale along arbitrary axes then it will work, where
 - T is a translation
 - R is a rotation
 - S is a symmetric matrix (positive definite if no reflection)

Parameterizing rotations

- Euler angles
 - Rotate around x, then y, then z
 - Problem: gimbal lock
 - If two axes coincide, you lose one DOF
- Unit quaternions
 - A 4D representation (like 3D unit vectors for 2D sphere)
 - Good choice for interpolating rotations
- These are first examples of motion control
 - Matrix = deformation
 - Angles/quaternion = animation controls



Unit vectors

- When we want to represent directions we use unit vectors: points that are literally on the unit sphere in \mathbb{R}^3
 - Now no points are special
 - Every point has a unique representation
 - Equal sized changes in coordinates are equal sized changes in direction
- Down side: one too many coordinates
 - Have to maintain normalization

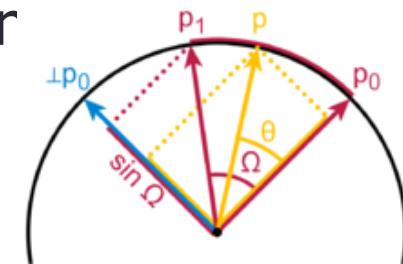
Interpolating directions

- Interpolating in the space of 3D vectors is well behaved
 - Simple computation: interpolate linearly and normalize
- This is what we do all the time, e.g. with normals for fragment shading

$$\hat{\mathbf{v}}(t) = \text{normalize}((1-t)\mathbf{v}_0 + t\mathbf{v}_1)$$

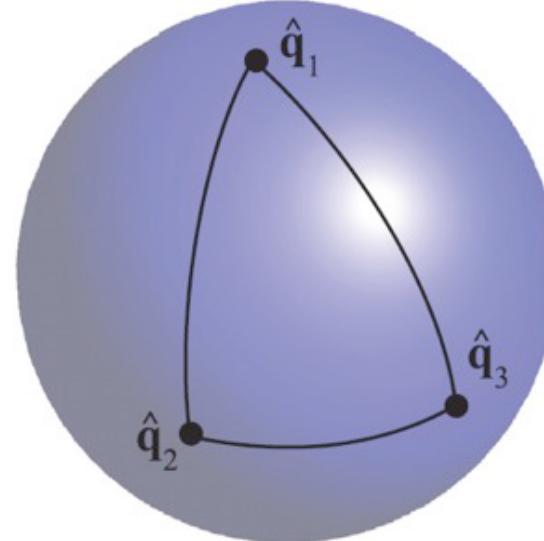
- For constant speed: spherical linear ir

$$P_s(t) = \frac{\sin[(1-t)\Omega]}{\sin(\Omega)} P + \frac{\sin[t\Omega]}{\sin(\Omega)} P'$$



Spherical linear interpolation

- Intuitive interpolation between different orientations
 - Nicely represented through quaternions
 - Useful for animation
 - Given two quaternions, interpolate between them
- Shortest path between two points on sphere



Quaternion interpolation

- Spherical linear interpolation naturally works in any dimension
- Traverses a great arc on the sphere of unit quaternions
 - Uniform angular rotation velocity about a fixed axis

$$\psi = \cos^{-1}(q_0 \cdot q_1)$$

$$q(t) = \frac{q_0 \sin(1-t)\psi + q_1 \sin t\psi}{\sin \psi}$$

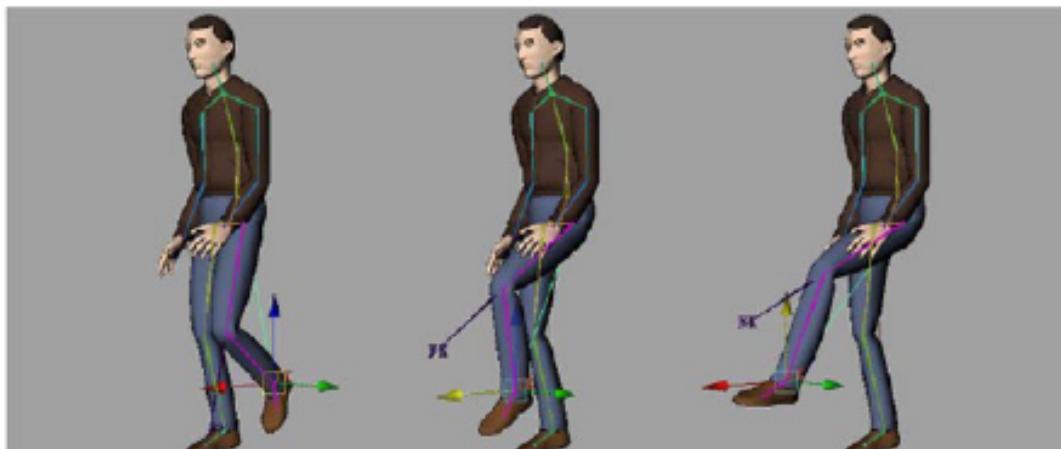
Hierarchies and articulated figures

- In mechanics, the relationship between DOFs and 3D pose is *kinematics*
- Robotics as source of mathematical methods
 - robots are transformation hierarchies
 - forward kinematics
 - inverse kinematics

Kinematics



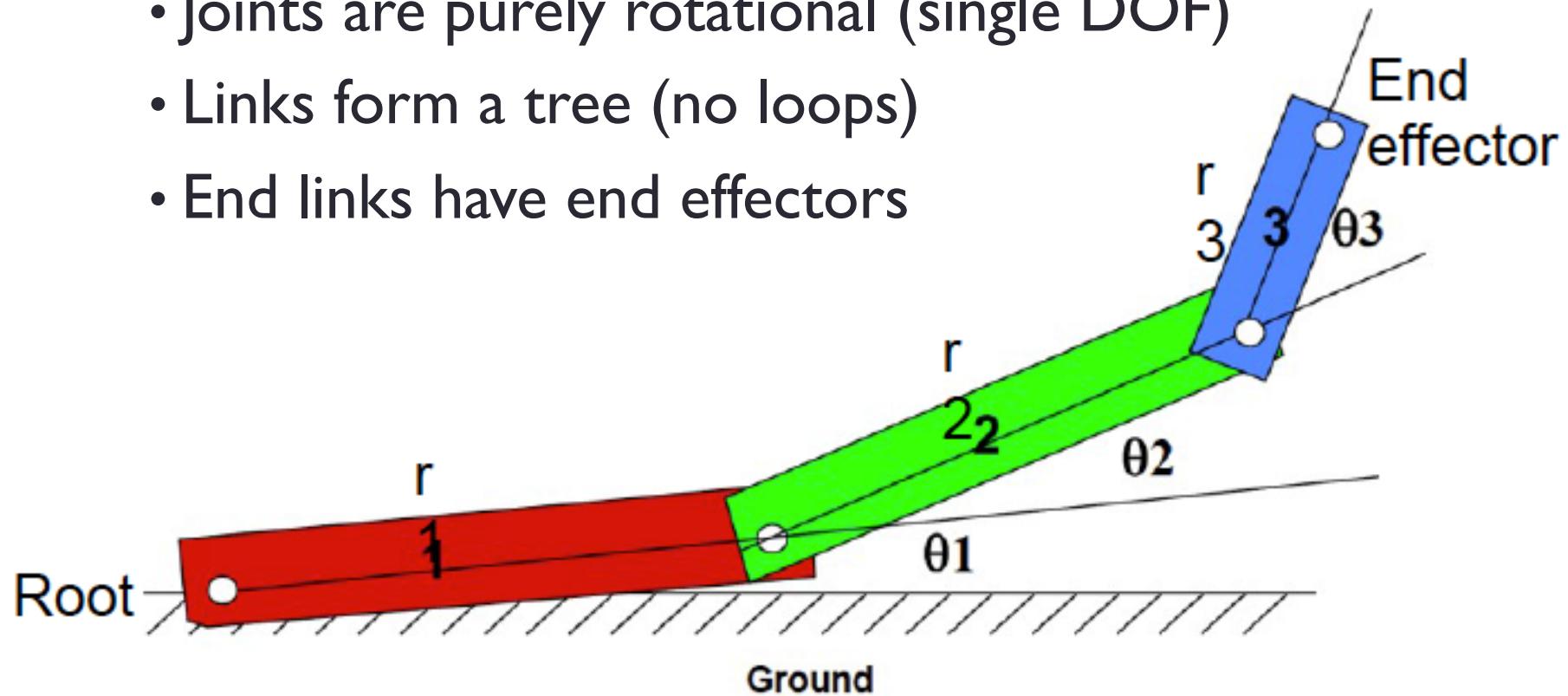
Forward Kinematics



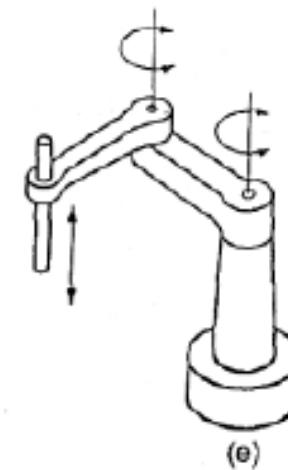
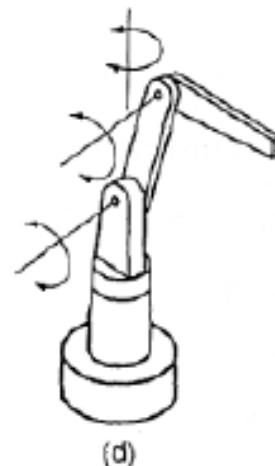
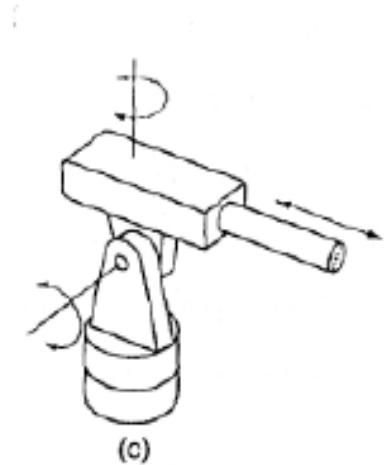
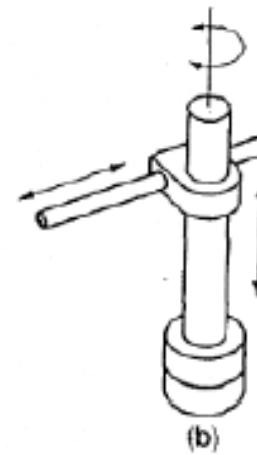
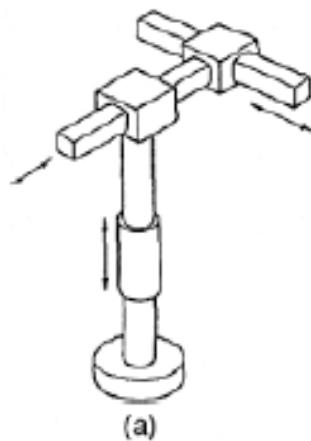
Inverse Kinematics

Rigid links and joint structure

- Links connected by joints
 - Joints are purely rotational (single DOF)
 - Links form a tree (no loops)
 - End links have end effectors



Articulation in robotics



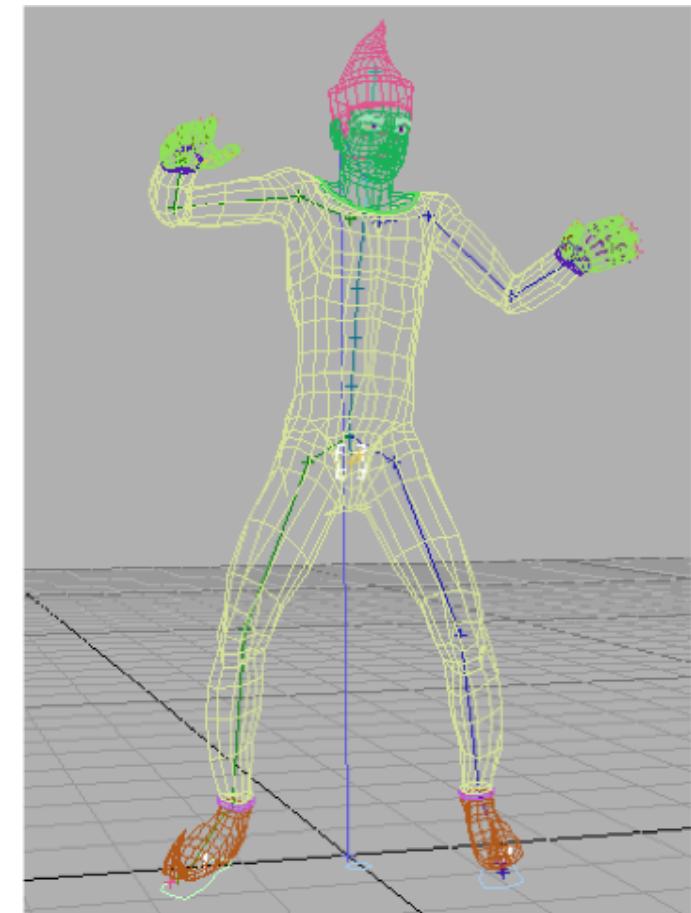
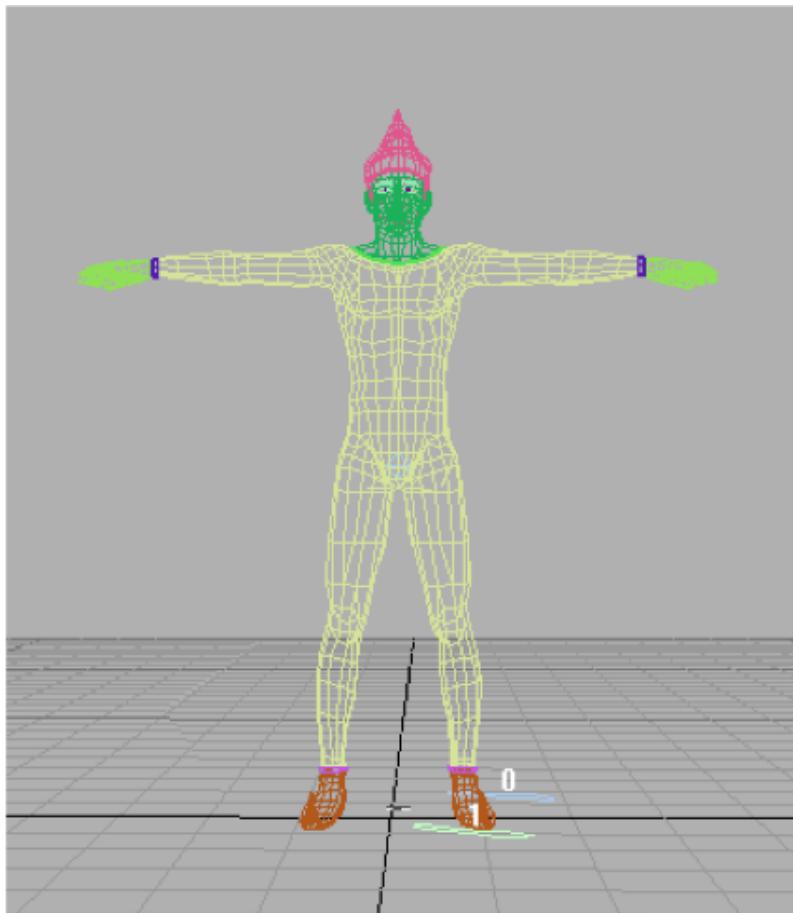
- a. rectangular or cartesian
- b. cylindrical or post-type
- c. spherical or polar
- d. joint-arm or articulated
- e. SCARA (selective compliance assembly robot arm)

Basic surface deformation methods

- Mesh skinning: deform a mesh based on an underlying skeleton
- Blend shapes: make a mesh by combining several meshes
- Both use simple linear algebra
 - Easy to implement—first thing to try
 - Fast to run—used in games
- The simplest tools in the offline animation toolbox

Mesh skinning

- A simple way to deform a surface to follow a skeleton



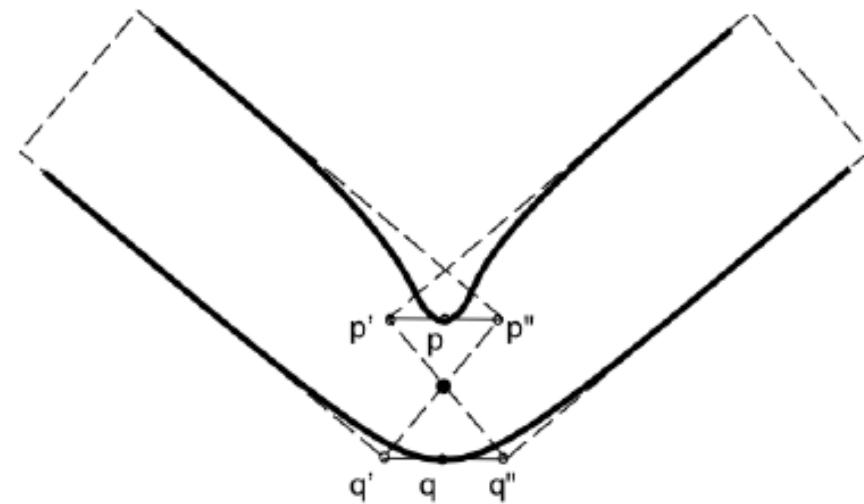
Mesh skinning math: setup

- Surface has control points p_i
 - Triangle vertices, spline control points, subdivide base vertices
- Each bone has a transformation matrix M_j
 - Normally a rigid motion
- Every point–bone pair has a weight w_{ij}
 - In practice only nonzero for small # of nearby bones
 - The weights are provided by the user

Mesh skinning math

- Deformed position of a point is a weighted sum
 - of the positions determined by each bone's transform alone
 - weighted by that vertex's weight for that bone

$$\mathbf{p}'_i = \sum_j w_{ij} M_j \mathbf{p}_i$$



[Lewis et al. SIGGRAPH 2000]

Mesh skinning

- Simple and fast to compute
 - Can even compute in the vertex stage of a graphics pipeline
- Used heavily in games
- One piece of the toolbox for offline animation
 - Many other deformers also available



Mesh skinning: classic problem

- Surface collapses on the inside of bends and in the presence of strong twists.

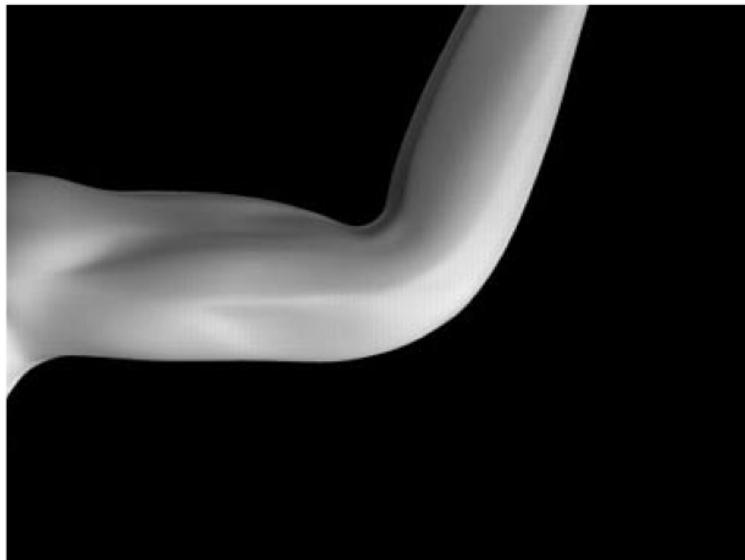


Figure 2: The ‘collapsing elbow’ in action, c.f. Figure 1.

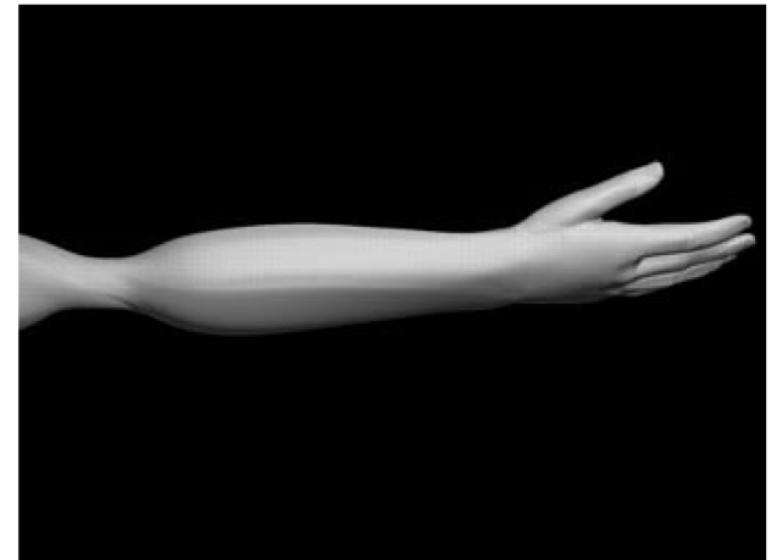
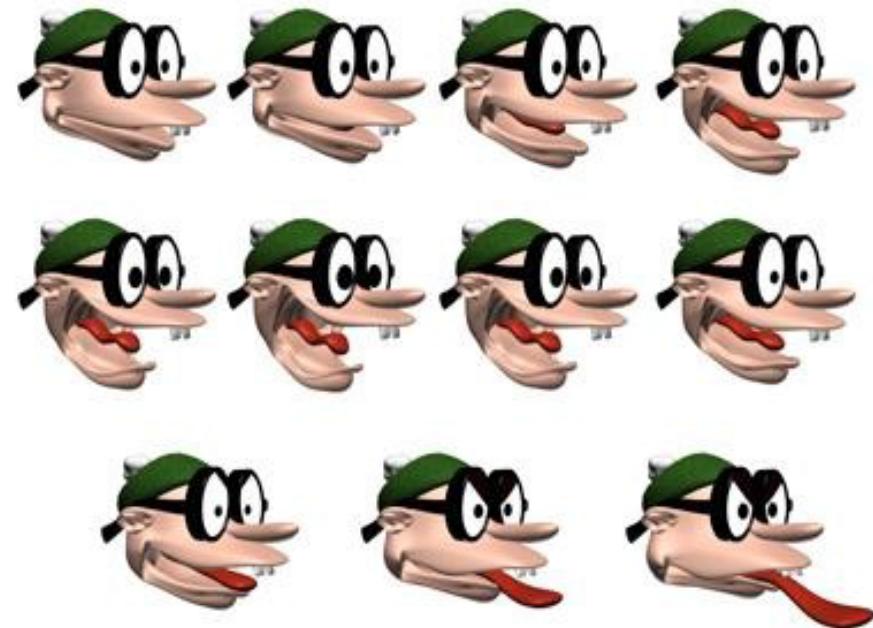
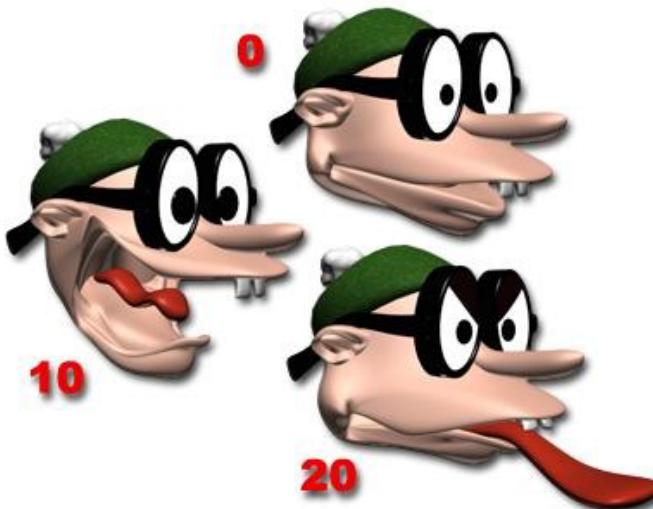


Figure 3: The forearm in the ‘twist’ pose, as in turning a door handle, computed by SSD. As the twist approaches 180° the arm collapses.

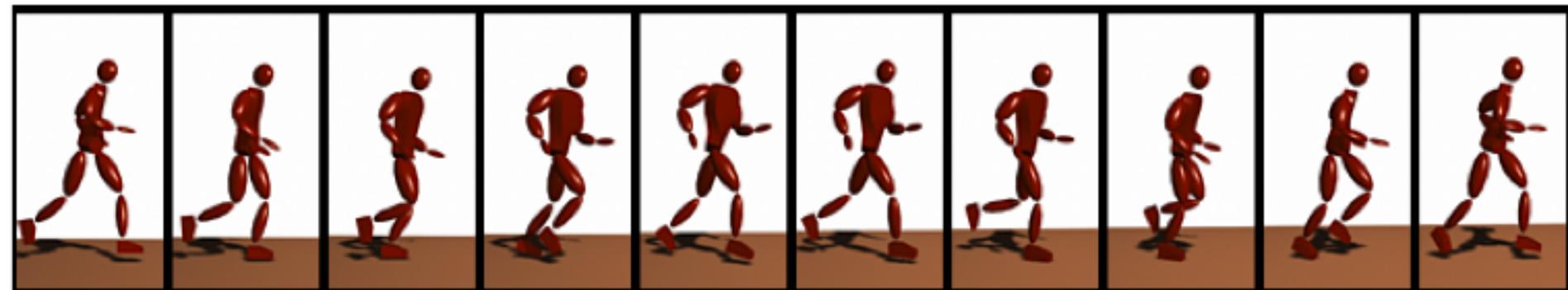
Blend shapes

- Another very simple surface control scheme
- Based on interpolating among several key poses
 - Aka. blend shapes or morph targets



Motion capture

- A method for creating complex motion quickly: measure it from the real world



Motion capture in movies

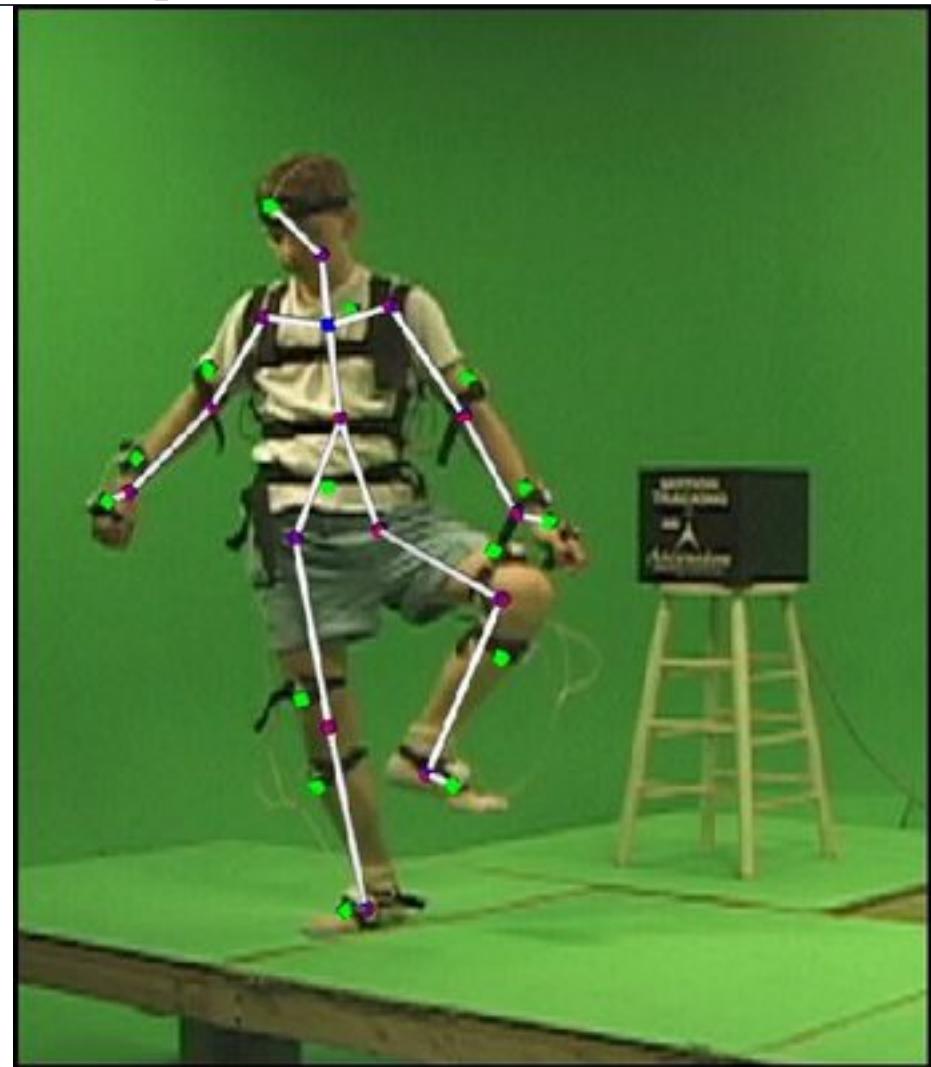


Motion capture in games



Magnetic motion capture

- Tethered
- Nearby metal objects cause distortions
- Low freq. (60Hz)



Mechanical motion capture

- Measures joint angles directly
- Works in any environment
- Restricts motion

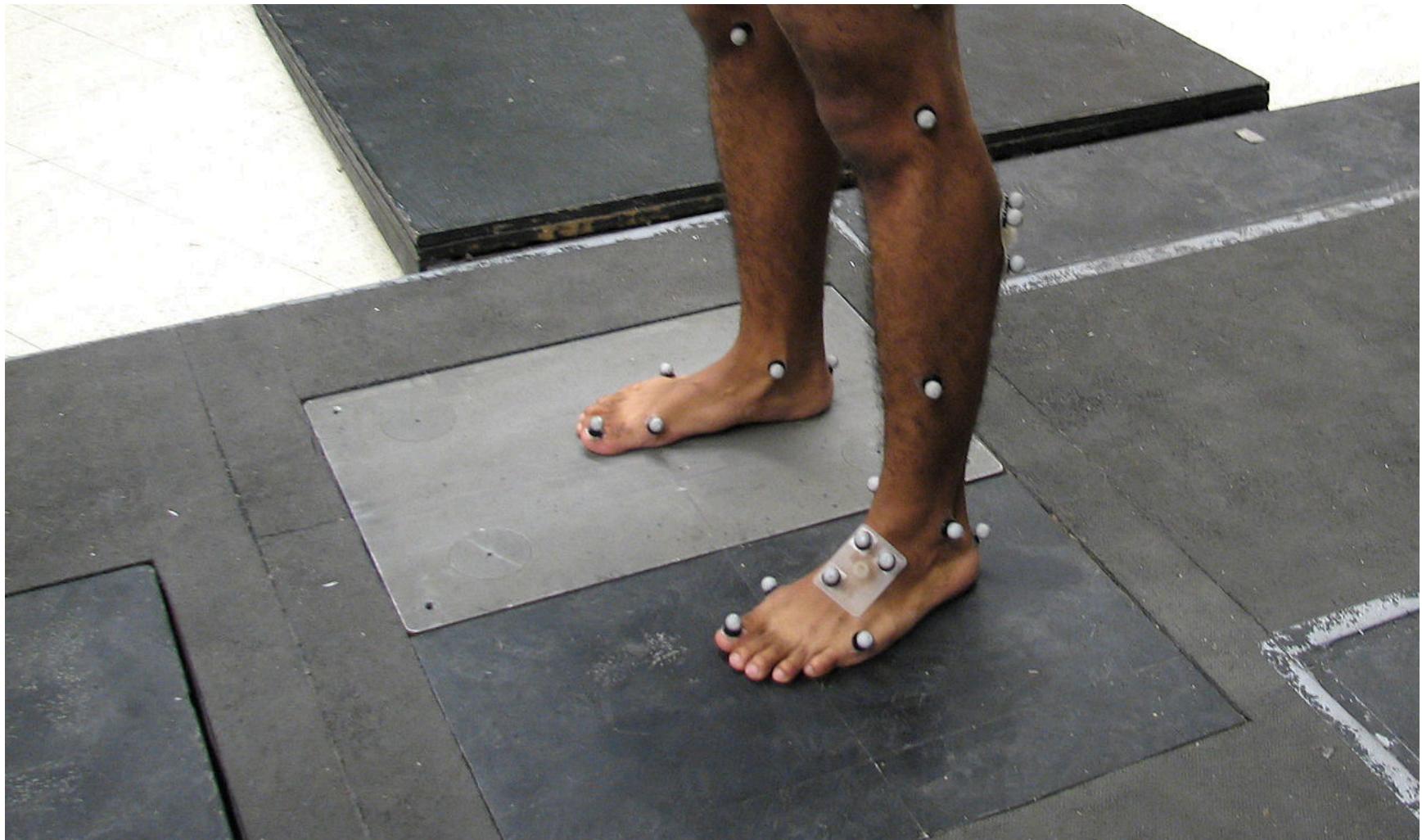


Optical motion capture

- Passive markers on subject, positions obtained by triangulation



Optical motion capture

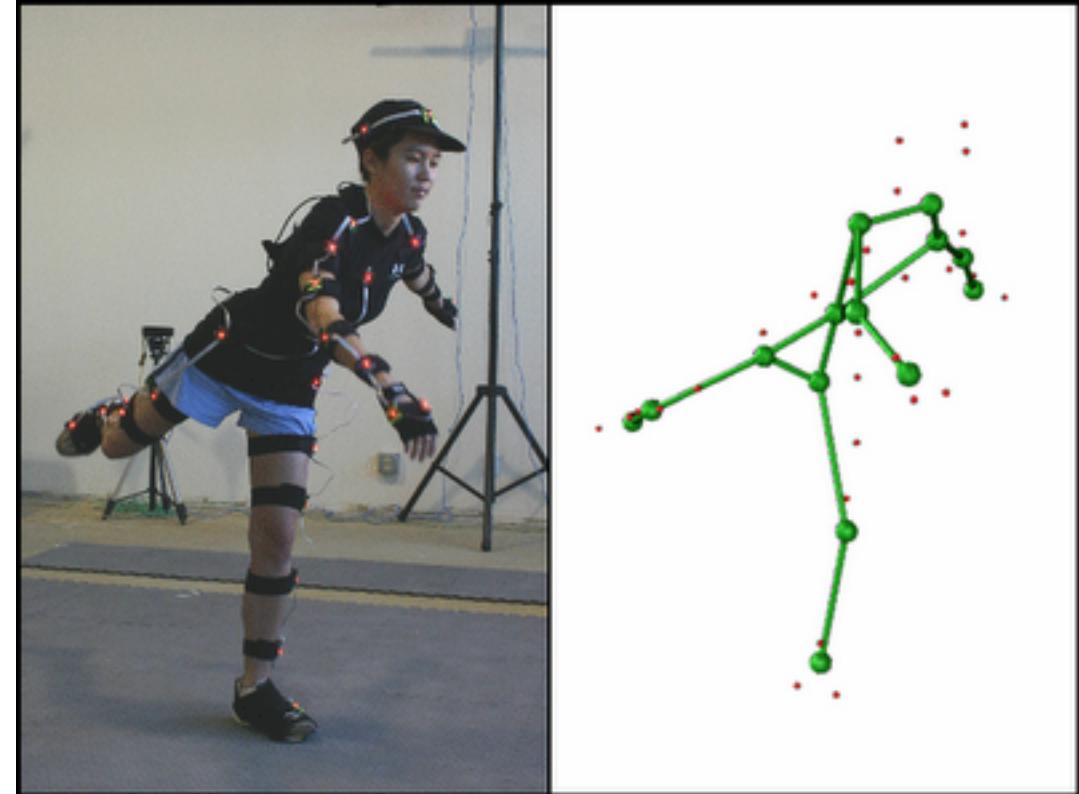


Optical motion capture



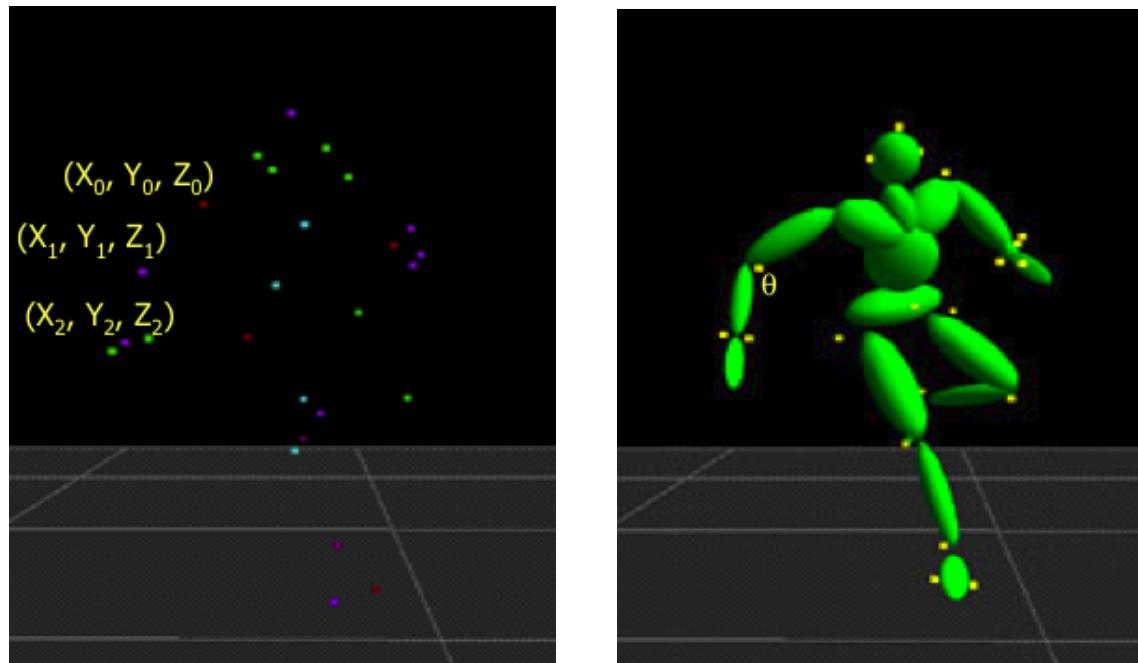
Optical motion capture

- 8 or more cameras
- Restricted volume
- High frequency (240Hz)
- Occlusions are troublesome



From marker data to usable motion

- Motion capture system gives inconvenient raw data
 - Optical is “least information” case: accurate position but:
 - Which marker is which?
 - Where are the markers are relative to the skeleton?



Motion capture data processing

- Marker identification: which marker is which
 - Start with standard rest pose
 - Track forward through time (but watch for markers dropping out due to occlusion!)
- Calibration: match skeleton, find offsets to markers
 - Use a short sequence that exercises all DOFs of the subject
 - A nonlinear minimization problem
- Computing joint angles: explain data using skeleton DOFs
 - A inverse kinematics problem per frame!

Motion capture in context

- Mocap data is very realistic
 - Timing matches performance exactly
 - Dimensions are exact
- But it is not enough for good character animation
 - Too few DOFs
 - Noise, errors from nonrigid marker mounting
 - Contains no exaggeration
 - Only applies to human-shaped characters
- Therefore *mocap* data is generally a starting point for skilled animators to create the final product

References

- Principles of animation
 - <https://vimeo.com/93206523>
- Real time Shape Deformation (SIGGRAPH 2014)
 - <http://skinning.org>