### **DASHMM Basic User Guide**

The Dynamic Adaptive System for Hierarchical Multipole Moments (DASHMM) is a C++ library providing a general framework for computations using multipole methods. In addition to the flexibility to handle user-specified methods and expansion, DASHMM includes built-in methods and expansions, including the Barnes-Hut (BH) and Fast Multipole Method (FMM), and two expansions implementing the Laplace Kernel used in electrostatics and Newtonian gravitation. Although only the Laplace kernel is currently implemented in DASHMM, in future versions more kernels will be added.

This document covers the basic use of the DASHMM library. More functionality is exposed through the advanced interface to DASHMM, including the ability to define and register methods and expansions with the library. For instructions on the advanced interface, please see the DASHMM Advanced User Guide. Instructions for installing and building applications using the library can be found in the DASHMM Installation Guide. Finally, the latest information, resources and tutorials can be found at the DASHMM webpage: <a href="https://www.crest.iu.edu/projects/dashmm/">https://www.crest.iu.edu/projects/dashmm/</a>

In the following, snippets of code, or the names of code constructs will be set in a fixed width font. For example, main ().

Unless otherwise indicated, every construct presented in this guide is a member of the dashmm namespace.

#### Introduction to DASHMM

DASHMM is a library built using C++ templates parameterized by four types: a source data type, a target data type, an expansion type and a method type. The source and target data types are used to specify the information that the user presents to DASHMM. These give positions for both the sources and targets, as well as providing the charge for the sources, and a location in which to store the results of the evaluation in the targets. The expansion conceptually encompasses the kernel being used (e.g. Laplace) and the details about how that kernel is expanded into multipole moments (e.g. using spherical harmonics). The method encompasses both how the various expansions are generated and how those expansions are used.

DASHMM is built using the advanced runtime system, HPX-5, but the basic interface to DASHMM does not require any knowledge of how to use HPX-5. Instead, the basic interface handles the distribution of the parallel work. The model of use for the basic interface to DASHMM is to take a serial code and make some calls to the DASHMM library. In so doing, the program will make use of parallel resources. In this mode of operation, when execution is outside a DASHMM library call, the runtime can be considered to be not operating. Data saved in the global address space provided by HPX-5 persists between calls, but the runtime is not executing any operations.

To present data to DASHMM, the user will make use of the Array object. Array objects live in the global address space provided by HPX-5. The user will need to allocate an Array, and put or get memory from that array.

The evaluation of a particular multipole method is accomplished through an Evaluator object. These objects have two responsibilities: they register a number of required actions with the HPX-5 runtime, and they perform multipole method evaluations. Evaluators take input from Array objects, and place the results into an Array object.

# **Types Defined by DASHMM**

DASHMM provides a few types that used throughout the system. The following are those needed in the basic interface.

Return codes from DASHMM library calls are all of the ReturnCode (non-scoped) enumeration type. The possible values are kSuccess, kRuntimeError, kIncompatible, kAllocationError, kInitError, kFiniError, and kDomainError. See below for cases in which these values might be returned.

DASHMM aliases std::complex<double> as dcomplex\_t, which is used in a number of places in the basic interface.

Finally, there is a Point class that encapsulates the notion of a three-dimensional location. Points are used to specify the locations of sources and targets. A full description of Point can be found in /path/to/dashmm/include/dashmm/point.h, but the most important methods will be covered here. Points are constructed from three doubles giving the position of the point. The coordinates of the point can be accessed by name (the x(), y() and z() methods) or by index (e.g. somepoint [1] for the y coordinate).

# **Initializing DASHMM**

To use DASHMM, one must initialize and finalize the library. These tasks are accomplished with two library functions.

ReturnCode init(int \*argc, char \*\*\*argv)

To start the runtime system, a user must call init and provide the address of the command line arguments used to launch the program. The runtime has some settings that can be controlled from the command prompt, and so these must be handed to the runtime. For a list of command line arguments that the runtime accepts, please see the DASHMM Advanced User Guide, or the HPX-5 documentation. After init, any runtime related command line argument will have been removed from argv, and argc will be updated accordingly.

Only a single call to init is allowed in any program that makes use of DASHMM. The majority of the use of DASHMM must occur *after* the call to init. For important exceptions, see Evaluators and Mapping Actions onto Arrays below.

On successful initialization of the runtime and of DASHMM, kSuccess is returned. Otherwise kInitError is returned indicating some problem.

ReturnCode finalize()

Before finishing a program, the user must call finalize to shut down the runtime. Once finalize returns, the user's program is free to continue performing any other work required, but all DASHMM and runtime resources will have been destroyed. So any data that is to be read from DASHMM's internal state must occur before this call.

All calls to DASHMM library routines must occur before the call to finalize. Only a single call to finalize is allowed in any program that makes use of DASHMM.

If finalize is successful, kSuccess will be returned. Otherwise, kFiniError will be returned.

# **Array Objects**

To provide data to DASHMM, one must make use of Array objects. An Array is a class that handles a chunk of associated global memory. Further, Array is a template class, with a parameter that can be any trivially copyable type. The relevant members of Array<T> are (see Mapping Actions onto Arrays below for another useful member of Array<T>):

Array<T>::Array()

Array objects possess a single constructor that takes one argument that has a default value. For the basic use of DASHMM, this default value is all that is needed. Interested users can consult the DASHMM Advanced User Guide for more information.

ReturnCode Array<T>::allocate(size\_t record\_count)

After an array object is created, allocate will allocate space in the global address space for  ${\tt record\_count}$  records whose size is  ${\tt sizeof}({\tt T})$ . The distribution of these records is chosen by DASHMM. Further, for Arrays used during an evaluation, the distribution and the ordering of the records are subject to change. This allows DASHMM to make changes that will benefit the scaling and performance of the evaluation. It is an error to call allocate more than once before a call to destroy.

This routine returns kSuccess on success, kRuntimeError if there is an error from the runtime, kAllocationError if the request fails because of a lack of available resources, and kDomainError if the Array already has some global memory allocated to it.

ReturnCode Array<T>::destroy()

This function instructs DASHMM to reclaim the resources used by an array object. It is an error to use put or get after the object has been deallocated. On success, this routine return kSuccess. If there is an error from the runtime, this routine returns kRuntimeError.

ReturnCode Array<T>::put(size\_t first, size\_t last, void \*in\_data)

Once an array is allocated, the records can be filled with a call to put. The provided in\_data is copied into the array's records in the range [first, last). It is the user's responsibility to assure that the buffer pointed to by in data contains sufficient data to fill the given number of records.

This routine returns kSuccess on successful put, kRuntimeError if there is an error with the runtime, or kDomainError if there are problems with the given range (e.g. last is beyond the end of the array).

```
ReturnCode Array<T>::get(size t first, size t last, void *out data)
```

Data may be retrieved from an array using a call to <code>get</code>. Similar to <code>put</code>, the data retrieved is from records in the range [first, last). The data is placed into <code>out\_data</code>. It is the user's responsibility to assure that <code>out\_data</code> has sufficient capacity for the retrieved data.

The routine returns kSuccess on success, kRuntimeError if there is a runtime error, or kDomainError if the range specified is incompatible with the underlying array.

## **Source and Target Data**

Evaluation of multipole methods require source and target data provided by an Array. DASHMM relies on C++ templates to allow for some flexibility for the user. Two important type parameters that appear in DASHMM evaluations are the Source and Target types. These types specific what data each source and target carries. Each expansion will place different requirements on the Source and Target types, but one requirement is universal: the types used for Sources and Targets must be trivially copyable.

For the built-in expansions provided with the current version of DASHMM, the requirements on Source types are identical. The source must provide a member of type Point called position, and a member of type double called charge. Additional data may be provided beyond that that the user might fine useful for their particular case. For example, the following would be a valid Source type:

The built-in expansions provided with the current version of DASHMM all place identical requirements on the Target type. The target must provide a member of type Point called position, and a member of type dcomplex\_t called phi for most cases. See the specific expansions below for details.

It is permissible to have both the Source and Target types be the same (for instance, if you are computing the self-interaction of a number of bodies) so long as all required fields are present. Note in particular, the position will serve as position for both the sources and targets in this case.

#### **Evaluators**

The central object in DASHMM is the Evaluator object. This object not only sets up the specific case for the chosen method and expansion, but also performs the evaluation. Evaluator objects are template classes that require four template arguments: the Source type, the Target type, the Expansion type and the Method type. Source and Target types have been discussed above. The built-in expansion and method types will be covered below.

An Evaluator object should only be created once for each combination of template arguments. When Evaluators are constructed, they handle registration of various actions (for more on actions, see the HPX-5 documentation) specific for the chosen types. This registration must happen only once, so it is an error to create multiple instances of a particular Evaluator. Fortunately, there is no hardship imposed by this restriction because Evaluators are stateless, and so having multiple instances does not benefit the user.

The single instance of a given Evaluator must be created before dashmm::init is called. Creation of Evaluators after init is an error.

```
Evaluator<Source, Target, Expansion, Method>::Evaluator()
```

Construction of an Evaluator instance is simple; there are no arguments to Evaluator's constructor. For example, if we wish to perform a multipole evaluation using FMM on a LaplaceSPH expansion for UserSource and UserTarget, then one creates an object as follows:

```
Evaluator<UserSource, UserTarget, LaplaceSPH, FMM> eval{};
```

Any Evaluator object will define a number of type aliases from their template arguments. In particular source\_t, target\_t, expansion\_t and method\_t are defined. The first two are of little utility, but the latter two are a savings given that both expansions and methods are themselves template classes (see the sections on built-in methods and expansion for more). expansion\_t and method\_t both contain the fully specified type. In the previous example, we would have expansion\_t being equivalent to LaplaceSPH<UserSource, UserTarget>, and method\_t being equivalent to FMM<UserSource, UserTarget, LaplaceSPH>.

The central call in the basic interface to DASHMM is evaluate. This routine performs the multipole method evaluation, computing the potential at the specified targets as a result of the specified sources. This will use the provided method, and the provided expansion of the potential in question. The built-in methods can be obtained from some methods covered below.

The source and target points are provided via DASHMM Array objects. DASHMM will likely sort both arrays, and so the user should not count on the ordering of the records after a call to evaluate. If the original ordering is important, the user will need to add an index to the Source and Target types. It is

permissible to have both sources and targets be the same array so long as the Source and Target types are identical.

During the evaluation, two hierarchical space-partitioning trees are constructed, one each for the sources and targets. The refinement\_limit specifies the refinement termination criterion. If a given tree node contains fewer sources or targets than the refinement\_limit, the partitioning halts.

The user must provide actual objects of expansion\_t and method\_t to evaluate. The particular Expansion or Method types might have parameters that specify fully their behavior (for instance, the number of digits of accuracy for the LaplaceSPH expansion, or the critical angle for the BH method; see below).

evaluate can be called multiple times from the same instance of an Evaluator. These evaluations do not have to share any arguments with other evaluations, so the user can use completely different data, the same data but different parameters for the passed in expansion, or every argument can be identical.

This routine returns kSuccess on successful evaluation, or kRuntimeError if there is some error in the runtime.

## **Built-in Expansions**

Expansions in DASHMM represent not only a particular kernel, but a particular way of expanding the given potential. Many expansion operations use either source or target data and so Expansions in DASHMM are also template classes, parameterized by the Source and Target types.

Currently, DASHMM provides one built-in kernel, the Laplace kernel. This potential represents the potential of a point charge in electrostatics, or a point mass in Newtonian gravitation. This kernel is exposed through three different expansions.

LaplaceCOM<Source, Target>::LaplaceCOM()

This expansion is an expansion about the center of mass of the represented sources. This expansion includes contributions up to the quadrupole term, but because it is an expansion about the center of mass, the dipole term is identically zero. This expansion is well suited to gravitation and the BH method, and should not be used for problems with both signs of charge. This expansion is not compatible with FMM; this expansion does not implement all of the required operations for use with FMM.

This expansion requires Source to have a member of type Point called position and a member of type double called charge. This expansion requires Target to have a member of type Point called position and a member of type dcomplex\_t called phi.

The LaplaceCOM type defines a number of other methods, but the only relevant method for basic use of DASHMM is the constructor. An object of this type must be passed into Evaluator::evaluate.

LaplaceCOMAcc<Source, Target>::LaplaceCOMAcc()

This is similar to the LaplaceCOM, except that this will compute the acceleration rather than the potential.

This expansion requires Source to have a member of type Point called position and a member of type double called charge. This expansion requires Target to have a member of type Point called position and a member of type double [3] called acceleration.

LaplaceSPH<Source, Target>::LaplaceSPH(int n digits)

This expansion is intended for use with the FMM This expansion implements all relevant operations, and provides a variable length expansion so that the user provided accuracy limit, given by  $n_{digits}$ , can be reached.

Before an object of this type can be constructed for a given  $n_{digits}$ , the user must call laplace\_sph\_precompute (int  $n_{digits}$ ). This routine performs some one-time initialization of coefficients used by LaplaceSPH, and needs to be called only once for each value of  $n_{digits}$ .

This expansion requires Source to have a member of type Point called position and a member of type double called charge. This expansion requires Target to have a member of type Point called position and a member of type dcomplex t called phi.

#### **Built-in Methods**

Methods in DASHMM need to know on which Expansion type they are being applied. And because Expansions need to know the Source and Target types, Methods in DASHMM are templates over the Source, Target and Expansion types.

DASHMM currently provides three built-in methods for immediate use, the Barnes-Hut Method, the Fast Multipole Method, and a direct summation method. As with the built-in expansions, the built-in methods have other routines. But also, just like the built-in expansion, it is only the constructor that is needed in basic use of DASHMM.

BH<Source, Target, Expansion>::BH(double theta)

This instance of the BH method will use the provided theta as the critical angle for deciding if a given expansion is usable. This criterion matches exactly the criterion introduced by Barnes & Hut. When theta is 0, this method is effectively the same as Direct.

FMM<Source, Target, Expansion>::FMM()

Users of FMM will not need to specify the error tolerance with this function. Instead, the error tolerance is specified by the expansion; the more terms in the expansion, the lower the error. See LaplaceSPH above for details.

```
Direct<Source, Target, Expansion>::Direct()
```

This method performs the potential computation using the direct summation technique. This is intended as a means for comparing approximate potentials computed with another method with the 'exact' answer. As it is direct summation, this method will take a long time to finish for even modest source and target counts.

## **Mapping Actions onto Arrays**

DASHMM also allows the user to specify functions that are applied to each element of an Array. This is useful in cases where multiple evaluations occur with simple work occurring between each. The prototypical example of this is a time-stepping code that uses multipole methods to compute the acceleration of the particles which then have their positions updated. This mechanism is provided through the ArrayMapAction object.

There are two reasons to let DASHMM handle such a task: the memory stored in the Array object is in HPX-5's global address space, and DASHMM can parallelize the work. If DASHMM is not used for this, the user would need to copy the Array data out of the global address space with Array::get before operating on it. Then, the user would need to call Array::put to return the data to the global address space so the might perform another multipole moment evaluation.

The ArrayMapAction object is a template class with two template parameters. The first specifies the record type of the array to which this action will be applied. The second specified the type of the environment that will be passed to the action. The environment is any data that is needed by the action that is not stored in the array records. For the example of time-stepping, the environment would contain at least the time step.

Like the Evaluator object, the ArrayMapAction<T, E> should be declared before dashmm::init(); the runtime needs to have the action represented by the ArrayMapAction registered. The constructor for the ArrayMapAction takes a single argument, a pointer to the function implementing the action to be performed on the records of the array. Once the object is constructed, a member of Array<T> will apply the action. For an example that uses this facility, please see /path/to/dashmm/demo/stepping.

This will create an object that represents an action that can be applied to each record of an Array<T> object. The type E specifies the type of an environment that will be passed to the function fcn on each application to a record in the array.

The first argument to the provided function will be the base address of a subset of the records to which the action will be applied. The second argument to the provided function will give the number of records that this invocation of the function will treat. The third argument gives the total offset in the array to the first record treated by this function. Note that this does not mean that the indexing inside the function should begin with the third argument; instead, the indexing should begin with 0 and run up to but not including the first argument. The third argument is provided for convenience if it should be

important to know in a specific case what the absolute offset is in the array. The last argument to the function will be an environment provided by the user.

This will apply the given action to all the records in the array on which the map method is called. The provided environment will be used for each invocation of the function. This will return kSuccess.

## **DASHMM Example**

This section presents a short example of the use of DASHMM. Details of the functions called can be found above. In the following we assume that there are two functions that generate the source and target data using information from the command line, and one function to do something with the results. Also, to keep the example brief, return codes are not checked. Real applications should check the result of each DASHMM library call.

```
#include <dashmm/dashmm.h>
struct source {
 Point position;
 double charge;
struct target {
 Point position;
 Dcomplex t phi;
dashmm::Evaluator<source, target, LaplaceSPH, FMM> fmmeval{};
int main(int argc, char **argv) {
 dashmm::init(&argc, &argv);
 int n_sources{0};
 source *S = generate sources(argc, argv, &n sources);
 dashmm::Array<source> S handle{};
 s handle.allocate(n sources);
 s_handle.put(0, n_sources, S);
 int n targets{0};
 target *T = generate_targets(argc, argv, &n_targets);
 dashmm::Array<target> T handle{};
 T handle.allocate(n targets);
 T_handle.put(0, n_targets, T);
  laplace sph precompute(6);
 LaplaceSPH<source, target> expansion{6};
 FMM<source, target, LaplaceSPH> method{};
 int refinement limit{10};
  fmmeval.evaluate(S handle, T handle, refinement limit,
                  method, expansion);
 T_handle.get(0, n_targets, T);
 do something with results (T, n targets);
 S handle.destroy();
 T handle.destroy();
 delete [] S;
 delete [] T;
 dashmm::finalize();
 return 0;
}
```