

CS 6505 - Homework 7

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1. Run Ford Fulkerson to find the residual graph after maximizing flow.
2. BFS from s and mark all vertices reachable from s . Call this set L .
3. Reverse the direction of all edges and BFS from t and mark all these vertices. Call this set R .
4. Reverse the direction of all edges.
5. For each edge in G (the original graph), check whether it is an edge from an element of L to an element of R . If so, it is a critical edge.

The runtime of this algorithm is $O(nm + 2(n + m) + m(n + n))$ time, since Ford Fulkerson runs in $O(nm)$ time and BFS takes $O(n+m)$ time (twice). Then for each edge we check whether its first endpoint is in L and whether its second endpoint is in R .