

ECE4560 - Solution #5

Problem 1. [10 pts] Consider the setup depicted in Figure 1. The configurations associated to the different frames are

$$g_{\mathcal{A}}^{\mathcal{O}} = \left(\left\{ \begin{array}{c} 9 \\ 4 \end{array} \right\}, R(\pi/2) \right), \quad g_{\mathcal{B}}^{\mathcal{O}} = \left(\left\{ \begin{array}{c} 3 \\ 6 \end{array} \right\}, R(\pi/3) \right), \quad g_{\mathcal{C}}^{\mathcal{O}} = \left(\left\{ \begin{array}{c} 4 \\ 0 \end{array} \right\}, R(\pi/12) \right).$$

- (a) Suppose that from frame \mathcal{A} the 2D vector v_1 is $v_1^{\mathcal{A}} = (1, 1)^T$. Then what is the same vector written in \mathcal{O} 's frame? in \mathcal{B} 's frame?
- (b) Now, let frame \mathcal{C} see the vector $v_2^{\mathcal{C}} = (\frac{\sqrt{3}}{2}, -\frac{1}{2})^T$. What are the coordinates of the same vector in \mathcal{O} 's frame? in \mathcal{B} 's frame?

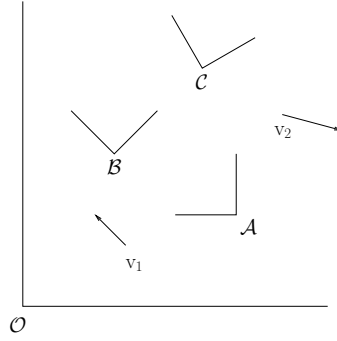


Figure 1: Problem #1 vector setup.

Solution 1. This will be worked out in homogeneous coordinates. The solution is equally valid in homogeneous or in vector form.

- (a) For the first part, the vector just needs to be transformed to the \mathcal{O} frame,

$$v_1^{\mathcal{O}} = g_{\mathcal{A}}^{\mathcal{O}} v_1^{\mathcal{A}} = \left[\begin{array}{c|c} R(\pi/2) & \left\{ \begin{array}{c} 9 \\ 4 \end{array} \right\} \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} 1 \\ 1 \\ 0 \end{array} \right\} = \left\{ \begin{array}{c} R(\pi/2) \left\{ \begin{array}{c} 1 \\ 1 \end{array} \right\} \\ \hline 0 \end{array} \right\} = \left\{ \begin{array}{c} -1 \\ 1 \\ 0 \end{array} \right\}.$$

For \mathcal{B} 's frame we'll need the transformation from \mathcal{A} to \mathcal{B} ,

$$\begin{aligned} g_{\mathcal{A}}^{\mathcal{B}} &= (g_{\mathcal{B}}^{\mathcal{O}})^{-1} g_{\mathcal{A}}^{\mathcal{O}} = \left[\begin{array}{c|c} R(\pi/3) & \left\{ \begin{array}{c} 3 \\ 6 \end{array} \right\} \\ \hline 0 & 1 \end{array} \right]^{-1} \left[\begin{array}{c|c} R(\pi/2) & \left\{ \begin{array}{c} 9 \\ 4 \end{array} \right\} \\ \hline 0 & 1 \end{array} \right] \\ &= \left[\begin{array}{c|c} R(-\pi/3) & -R(-\pi/3) \left\{ \begin{array}{c} 3 \\ 6 \end{array} \right\} \\ \hline 0 & 1 \end{array} \right] \left[\begin{array}{c|c} R(\pi/2) & \left\{ \begin{array}{c} 9 \\ 4 \end{array} \right\} \\ \hline 0 & 1 \end{array} \right] \\ &= \left[\begin{array}{c|c} R(-\pi/3 + \pi/2) & R(-\pi/3) \left\{ \begin{array}{c} 9-3 \\ 4-6 \end{array} \right\} \\ \hline 0 & 1 \end{array} \right] \\ &= \left[\begin{array}{c|c} R(\pi/6) & \left\{ \begin{array}{c} 3-\sqrt{3} \\ -1-3\sqrt{3} \end{array} \right\} \\ \hline 0 & 1 \end{array} \right] = \left[\begin{array}{cc|c} 0.866 & -0.500 & 1.268 \\ 0.500 & 0.866 & -6.196 \\ \hline 0 & 0 & 1 \end{array} \right] \end{aligned}$$

which then leads to

$$v_1^{\mathcal{B}} = g_{\mathcal{A}}^{\mathcal{B}} v_1^{\mathcal{A}} = \left[\begin{array}{c|c} R(\pi/6) & \begin{Bmatrix} 3 - \sqrt{3} \\ -1 - 3\sqrt{3} \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \begin{Bmatrix} 1 \\ 1 \\ 0 \end{Bmatrix} = \begin{Bmatrix} \frac{\sqrt{3}}{2} - \frac{1}{2} \\ \frac{\sqrt{3}}{2} + \frac{1}{2} \\ 0 \end{Bmatrix} = \begin{Bmatrix} 0.366 \\ 1.366 \\ 0 \end{Bmatrix}$$

The above (naive) product works because the last element of a homogeneous vector is zero. That doesn't mean it will work for other types of products. For the $SE(2)$ case, there is a better, more generic form that will apply to two different vector classes. Can you figure that out?

(b) The same mechanics are going on here, but we'll do the transformation to \mathcal{B} first,

$$v_2^{\mathcal{B}} = g_{\mathcal{C}}^{\mathcal{B}} v_1^{\mathcal{C}} = \left[\begin{array}{c|c} R(\pi/12) & \begin{Bmatrix} 4 \\ 0 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \begin{Bmatrix} \sqrt{3}/2 \\ -1/2 \\ 0 \end{Bmatrix} = \begin{Bmatrix} R(\pi/12) \begin{Bmatrix} \sqrt{3}/2 \\ -1/2 \end{Bmatrix} \\ 0 \end{Bmatrix} = \begin{Bmatrix} 0.966 \\ -0.259 \\ 0 \end{Bmatrix}$$

Then the last vector computation builds off of this prior one,

$$\begin{aligned} v_2^{\mathcal{O}} &= g_{\mathcal{B}}^{\mathcal{O}} v_2^{\mathcal{B}} = \left[\begin{array}{c|c} R(\pi/3) & \begin{Bmatrix} 3 \\ 6 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \begin{Bmatrix} R(-\pi/12) \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} \\ 0 \end{Bmatrix} \\ &= \begin{Bmatrix} R(\pi/3) R(-\pi/12) \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} \\ 0 \end{Bmatrix} = \begin{Bmatrix} R(\pi/4) \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} \\ 0 \end{Bmatrix} = \begin{Bmatrix} \sqrt{2}/2 \\ \sqrt{2}/2 \\ 0 \end{Bmatrix} = \begin{Bmatrix} 0.707 \\ 0.707 \\ 0 \end{Bmatrix} \end{aligned}$$

where I took advantage of the fact that

$$\begin{Bmatrix} 0.966 \\ -0.259 \end{Bmatrix} = R(\pi/12) \begin{Bmatrix} \sqrt{3}/2 \\ -1/2 \end{Bmatrix} = R(\pi/12) R(-\pi/6) \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} = R(-\pi/12) \begin{Bmatrix} 1 \\ 0 \end{Bmatrix}$$

from the $v_2^{\mathcal{B}}$ calculation.

Problem 2. [10 pts] Suppose that we have the following frames

$$g_{\mathcal{A}}^{\mathcal{O}} = \left(\begin{Bmatrix} 5 \\ 2 \end{Bmatrix}, R(\pi/3) \right), \quad g_{\mathcal{B}}^{\mathcal{O}} = \left(\begin{Bmatrix} 2 \\ 7 \end{Bmatrix}, R(\pi/2) \right), \quad \text{and} \quad g_{\mathcal{C}}^{\mathcal{B}} = \left(\begin{Bmatrix} 0 \\ 3 \end{Bmatrix}, R(-\pi/6) \right).$$

We have seen how these frames function with regards to Euclidean 2-vectors. Now it is time to better understand special Euclidean 2-vectors, e.g., vectors associated to planar rigid body motion. You observe motions associated to $SE(2)$ as per Figure 2. Notice that in Figure 2 the vectors also have this semi-circle arrow by them, this is to denote the rotational component that is now a part of vectors in $SE(2)$.

(a) If frame \mathcal{A} sees the vector $\xi_1^{\mathcal{A}} = (2, 5, -\pi/12)^T$, then what is this same vector with respect to frames \mathcal{B} and \mathcal{O} ?

(b) If frame \mathcal{C} sees the vector $\xi_2^{\mathcal{C}} = (1, -4, \pi/15)^T$, then what is the same vector with respect to frames \mathcal{B} and \mathcal{O} ?

Solution 2. The solution to this problem requires for us to be wary about the product operation. The product operation for vectors of $SE(2)$, e.g., elements of $\mathfrak{se}(2)$, is different than for standard vectors. To highlight the specialness of the product, we will use the \star to denote the product and write it as in lecture,

$$g \star \xi = \left[\begin{array}{c|c} R(\theta) & 0 \\ \hline 0 & 1 \end{array} \right] \cdot \begin{Bmatrix} v \\ \omega \end{Bmatrix}.$$

Note that in this case, we are working with the vector notation for $SE(2)$ and its associated vector space $\mathfrak{se}(2)$. With that in mind, let's work out the solutions.

(a) For $\xi_1^A = (2, 5, -\pi/12)^T$,

$$\xi_1^B = g_A^B \star \xi_1^A = \left[\begin{array}{c|c} R(-\pi/6) & 0 \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} 2 \\ 5 \\ -\pi/12 \end{array} \right\} = \left\{ \begin{array}{c} \sqrt{3} + \frac{5}{2} \\ -1 + \frac{5\sqrt{3}}{2} \\ -\pi/12 \end{array} \right\} = \left\{ \begin{array}{c} 4.2321 \\ 3.3301 \\ -0.2618 \end{array} \right\}$$

and

$$\xi_1^O = g_A^O \star \xi_1^A = \left[\begin{array}{c|c} R(\pi/3) & 0 \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} 2 \\ 5 \\ -\pi/12 \end{array} \right\} = \left\{ \begin{array}{c} 1 - \frac{5\sqrt{3}}{2} \\ \sqrt{3} + \frac{5}{2} \\ \pi/10 \end{array} \right\} = \left\{ \begin{array}{c} -3.3301 \\ 4.2321 \\ -0.2618 \end{array} \right\}$$

(b) Likewise, for $\xi_2^C = (1, -4, \pi/15)^T$,

$$\xi_2^B = g_C^B \star \xi_2^C = \left[\begin{array}{c|c} R(-\pi/6) & 0 \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} 1 \\ -4 \\ \pi/15 \end{array} \right\} = \left\{ \begin{array}{c} \frac{\sqrt{3}}{2} - 2 \\ -\frac{1}{2} - 2\sqrt{3} \\ \pi/15 \end{array} \right\} = \left\{ \begin{array}{c} -1.1340 \\ -3.9641 \\ 0.2094 \end{array} \right\}$$

and

$$\begin{aligned} \xi_2^O &= g_C^O \star \xi_2^C = g_B^O \star (g_C^B \star \xi_2^C) \\ &= \left[\begin{array}{c|c} R(\pi/2) & 0 \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} \frac{\sqrt{3}}{2} - 2 \\ -\frac{1}{2} - 2\sqrt{3} \\ \pi/15 \end{array} \right\} = \left\{ \begin{array}{c} \frac{1}{2} + 2\sqrt{3} \\ \frac{\sqrt{3}}{2} - 2 \\ \pi/15 \end{array} \right\} = \left\{ \begin{array}{c} 3.9641 \\ -1.1340 \\ 0.2094 \end{array} \right\} \end{aligned}$$

Problem 3 [10 pts] Continuing with the setup from the previous Problem, let's suppose that frame \mathcal{B} and frame \mathcal{C} were actually attached to the same rigid body and that you watched the body move from its original configuration to some new configuration (\mathcal{B}' and \mathcal{C}'). As the rigid body was moving, you measured that the body velocity of the frame \mathcal{B} was $\xi_B^b = (2, -3, \pi/9)^T$. What is the body velocity associated to the frame \mathcal{C} , i.e., what is ξ_C^b ? The setup is depicted in Figure 3.

Solution 3. Here we are not looking at disembodied vectors, but vectors that are attached to a particular point of a rigid body. The rigid body itself is undergoing a motion and we want to figure out the equivalent motion of a frame (\mathcal{C}) located elsewhere on the body than the default frame (\mathcal{B}) we've defined for the body.

The solution to this is obtained by applying the adjoint operation.

$$\xi_C^b = \xi_C^C = \text{Ad}_{g_B^C} \xi_B^b = \text{Ad}_{g_B^C} \xi_B^B = g_B^C \xi_B^B (g_B^C)^{-1}.$$

But, we don't have g_B^C . We do, however, have g_C^B , so we can use that instead (and invert it):

$$\xi_C^C = \text{Ad}_{(g_C^B)^{-1}} \xi_B^B = (g_C^B)^{-1} \xi_B^B g_C^B.$$

We can solve for this in vector form or in homogeneous form. Either way, we get the same answer. The homogeneous

matrix form of the solution goes first, since that is the most direct in terms of applying the product operations,

$$\begin{aligned}
\hat{\xi}_C^C &= \left[\begin{array}{c|c} R(\pi/6) & -R(\pi/6) \begin{Bmatrix} 0 \\ 3 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \hat{\xi}_B^B \left[\begin{array}{c|c} R(-\pi/6) & \begin{Bmatrix} 0 \\ 3 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \\
&= \left[\begin{array}{c|c} R(\pi/6) & -R(\pi/6) \begin{Bmatrix} 0 \\ 3 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \left[\begin{array}{c|c} (\pi/9)^\wedge & \begin{Bmatrix} 2 \\ -3 \end{Bmatrix} \\ \hline 0 & 0 \end{array} \right] \left[\begin{array}{c|c} R(-\pi/6) & \begin{Bmatrix} 0 \\ 3 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \\
&= \left[\begin{array}{c|c} R(\pi/6) (\pi/9)^\wedge R(-\pi/6) & R(\pi/6) \left(\begin{Bmatrix} 2 \\ -3 \end{Bmatrix} + (\pi/9)^\wedge \begin{Bmatrix} 0 \\ 3 \end{Bmatrix} \right) \\ \hline 0 & 1 \end{array} \right] \\
&= \left[\begin{array}{c|c} (\pi/9)^\wedge & R(\pi/6) \begin{Bmatrix} 2 - \frac{\pi}{3} \\ -3 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \\
&= \left[\begin{array}{c|c} (\pi/9)^\wedge & \begin{Bmatrix} \sqrt{3} - \pi\sqrt{3}/6 + 3/2 \\ 1 - \pi/6 - 3\sqrt{3}/2 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \\
&= \left[\begin{array}{c|c} (0.3491)^\wedge & \begin{Bmatrix} 2.3252 \\ -2.1217 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right]
\end{aligned}$$

Then, in vector form where we use the \star notation to highlight the fact that it is a special product,

$$\begin{aligned}
\xi_C^C &= \left(\text{Ad}_{(g_C^B)^{-1}} \right) \star \xi_B^B \\
&= \left[\begin{array}{c|c} R(\pi/6) & -\mathbb{J}R(\pi/6) \begin{Bmatrix} 0 \\ 3 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} 2 \\ -3 \\ \pi/9 \end{array} \right\} = \left[\begin{array}{c|c} R(\pi/6) & \begin{Bmatrix} -3\sqrt{3}/2 \\ -3/2 \end{Bmatrix} \\ \hline 0 & 1 \end{array} \right] \left\{ \begin{array}{c} 2 \\ -3 \\ \pi/9 \end{array} \right\} \\
&= \left\{ \begin{array}{c} \sqrt{3} + 3/2 - \pi\sqrt{3}/6 \\ 1 - 3\sqrt{3}/2 - \pi/6 \\ \pi/9 \end{array} \right\} = \left\{ \begin{array}{c} 2.3252 \\ -2.1217 \\ 0.3491 \end{array} \right\}
\end{aligned}$$

Both forms agree as expected, except that one is hatted (in homogeneous form) and the other isn't hatted (in vector form).

Problem 4. [15 pts] The main part of this exercise is to make sure that we are all comfortable with the mathematical notation thus far.

(a) Given that $\xi \in \mathfrak{se}(2)$ and in particular, $\xi = (4, 6, \pi/12)^T$, what is $\hat{\xi}$?

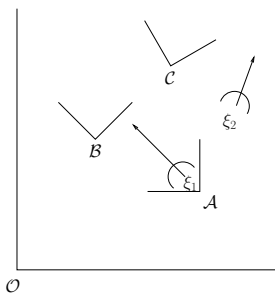


Figure 2: Vectors setup.

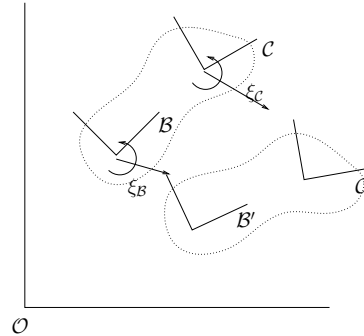


Figure 3: Rigid body vectors setup.

(b) Given

$$\hat{\xi} = \begin{bmatrix} 0 & -\frac{\pi}{8} & 7 \\ \frac{\pi}{8} & 0 & -3 \\ 0 & 0 & 0 \end{bmatrix},$$

what is $\xi \in \mathfrak{se}(2)$?

(c) Given that $\xi \in \mathfrak{se}(3)$ and in particular, $\xi = (1, -9, 3, 1, -0.8, -0.5)^T$, what is $\hat{\xi}$?

(d) Given that

$$\hat{\xi} = \begin{bmatrix} 0 & -0.9 & -0.1 & 3 \\ 0.9 & 0 & -0.2 & -2 \\ 0.1 & 0.2 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix},$$

what is $\xi \in \mathfrak{se}(3)$?

Solution 4.

(a) The solution is

$$\hat{\xi} = \left[\begin{array}{cc|c} 0 & -\frac{\pi}{12} & 4 \\ \frac{\pi}{12} & 0 & 6 \\ \hline & & 0 \end{array} \right] = \left[\begin{array}{cc|c} 0 & -0.2618 & 4 \\ 0.2618 & 0 & 6 \\ \hline & & 0 \end{array} \right]$$

(b) The unhat operation gives

$$\xi = (\hat{\xi})^\vee = \left\{ \begin{array}{c} 7 \\ -3 \\ -\frac{\pi}{8} \end{array} \right\} = \left\{ \begin{array}{c} 7 \\ -3 \\ 0.3927 \end{array} \right\}.$$

(c) The hat operation gives

$$\hat{\xi} = \left[\begin{array}{ccc|c} 0 & 0.5 & -0.8 & 1 \\ -0.5 & 0 & -1 & -9 \\ 0.8 & 1 & 0 & 3 \\ \hline & & & 0 \end{array} \right]$$

(d) The unhat operation gives

$$\xi = (3, -2, 1, 0.2, -0.1, 0.9)^T$$

Problem 5. (10 pts) The differential equations represented by:

$$\dot{g} = g * \xi?$$

for some constant $\xi = (\xi_1, \xi_2, \xi_3)$ is given more explicitly by

$$\left\{ \begin{array}{c} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{array} \right\} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix} \left\{ \begin{array}{c} \xi_1 \\ \xi_2 \\ \xi_3 \end{array} \right\}. \quad (1)$$

Integrating this for some time τ and some initial condition g_i should mimic the effect of moving along a trajectory with a constant body velocity (starting from g_i). Let's see what that would look like.

Integrate the differential equation (1) for the case that $\xi = (1, -1, \frac{1}{4})$, $g_i = g(0) = (0, 0.5, \pi/6)$ and final time is $\tau = \pi$. Now do the same for the case that the body velocity is now $\xi = (1, -1, 0)$. Does the output make sense? What is the big difference between the two velocities?

To perform the integration in Matlab, use the function **ode45** or an equivalent (you should have some familiarity with that by now). In Mathematica, you can use the **NDSolve** function. In both programs, you can access the help and online help to figure out how the integrators work if you still have questions. Plot the planar trajectory of the system with a few snapshots of the $SE(2)$ configuration overlaid on top of the trajectory (use the **hold** command). The snapshots help you visualize the orientation.

If you do it in Matlab, then you should have a script m-file to command Matlab to do the integration and process the output, plus a function m-file to specify the differential equation.

Solution 4. To do this in Matlab requires one to setup a function to pass to **ode45** for doing the integration. That function is as follows:

```
function gdot = se2ode(t, g)

xi = [1; -1; 1/4];

th = g(3);
gdot = [ cos(th) , -sin(th) , 0 ; sin(th), cos(th), 0; 0, 0, 1 ]*xi;

end
```

It gets invoked through **ode45** in the following manner:

```
[t, gsol] = ode45(@se2ode, [0, pi], gi);
```

The solution is given by `gsol(end,:)`, the last element in the solution trajectory. In the first case, the final configuration is $g(\tau) = (4.2925, 1.0651, 5\pi/12)$, or $g(\tau) = (4.2925, 1.0651, 1.3090)$. For the second body velocity vector, the final configuration is $g(\tau) = (4.2915, -0.6499, 0.5236)^T$ or $g(\tau) = (4.2915, -0.6499, \pi/6)^T$. A plot of the solution trajectories versus time is given in Figure 4, as well as a parametric plot of the translation overlaid with a few snapshots of the actual $SE(2)$ frame. When the body does not undergo any rotational component, then the trajectory is straight. When the body does experience an angular velocity, then the trajectory is curved. This makes sense, imagine if you were to walk forward and also turn a bit. What kind of trajectory would you describe? If you walked long enough, you should be where?

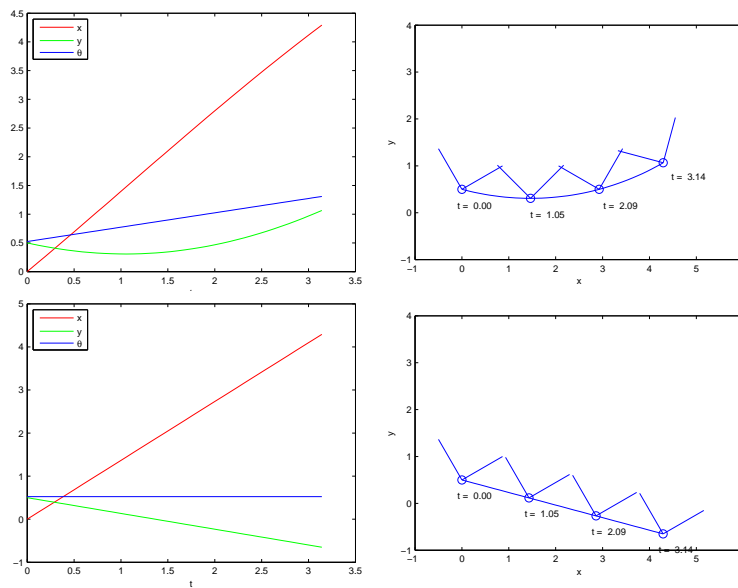


Figure 4: Solution trajectory plots for Problem 1.

In Mathematica it is similar, going along the lines of

```
DiffEq = {x'[t] == xi1 Cos[theta[t]] - xi2 Sin[theta[t]],
          y'[t] == xi1 Sin[theta[t]] + xi2 Cos[theta[t]],
          theta'[t] == xi3, x[0] == 0, y[0] == 1/2, theta[0] == pi/6};
gsol = NDSolve[DiffEq, {x, y, theta}, {t, 0, pi}];
```

Notice that the `DiffEq` variable has both the differential equation and the initial condition.

Problem 6. [Manipulator Option] (30 pts) This problem deals with calibration of the SCARA-type planar manipulator to be used in the lab portion of the class. Calibration usually requires measuring the link lengths associated to your manipulator, the servo command limits for each of the joints, and the angular limits of the manipulator. The limits imposed may actually be less than the full range of motion of the servo motors.

Since the link lengths have already been established based on the actual design, what is needed is to mapping between joint coordinate units and servo command units.

- a. Determine what are the proper servo command limits for your particular manipulator. The manipulator code for interfacing should be uploaded to the course wiki as will a page describing in more detail what this problem is about. Please be careful, since they can break.
- b. The second phase is to associate angles to the servo commands. Using the straight-out reference configuration as the zero configuration for the joint-angles, determine the angular limits associated to the joints with respect to that reference configuration as best as you can. You WILL need a protractor.

Although the robot may be able to go to bigger angles, try to round the joint-angle workspace to the nearest 30, 45, 90, or 180 degrees. For example, if you measure that it can go -37 degrees to 48 degrees, then make the joint angle limits $[-30, 45]$ in order to have nice clean limits. You'll need to figure out what servo commands correspond to those particular angle limits.

If you can hit the 90 degrees mark, then you might be able to use these little cardboard pieces on the shelf to identify that the right angle has been hit properly.

The course wiki is located at `pvela.gatech.edu/classes` and the proper link to follow is labelled *Manipulator Interface*. The manipulator is called **piktul** and you can find one on the shelving in the lab room. They are small white, RC servo manipulators. The manipulator circuit board should be plugged into the serial cable attached to the computers.

Solution 6. Hopefully you got the little arm calibrated properly. It will be important for future demos. The way I test proper calibration is to send the arm to different configurations that align linear parts of the robot with the x-axis or the y-axis. I then look at the robot from an angle such that the linear part of the robot is just next to one of the axis lines. If they are parallel, then the calibration is good. If not, then it is off.

An example configuration would be $\alpha = [1; 45; 45; -30; 0.5]$, which would align the second link with the x-axis. If it is not parallel, then the calibration is off. I also test that the final orientation of the gripper is 60° .

The important thing is to hit the "save" button and copy the `pikparms.mat` Matlab file somewhere you always have access to it. In the future, when using the `piktul`, you'd instantiate it via:

```
> arm = piktul( load('pikparms.mat') );
```

which would both load the saved calibration parameters and also instantiate the `piktul` robot with those parameters. It may decalibrate over time, but with a good initial calibration, it is quick to fix minor errors. The way to do this would be to invoke the calibration routine in a similar manner,

```
> piktul_calibrate( load('pikparms.mat') );
```

It will load your saved settings and you can fine tune from there.

Problem 6. [Turtlebot Option] (30 pts) Following the instructions at the wiki site for Turtlebot learning `pvela.gatech.edu/classes` to get the Turtlebot up and working. Demonstrate the following:

- a) The ability to teleoperate the Turtlebot using the provided laptop (or using your own if you prefer and you have some modern linux installation on it that can run ROS);
- b) The ability to remotely connect to the Turtlebot (from a workstation in the lab, or from your laptop).
- c) The ability to remotely teleoperate by remotely connecting to the Turtlebot.
- d) Answer the questions of the *First Run* page labeled "**3. Understanding**".

You should demo this during inquiry hours on Tuesday or on Thursday. If need be, you can try to negotiate a demo time outside of those hours with the TA.

Solution 6. Hopefully you connected. It can be tricky, but once you get it, you've got it for good. As noted in class, this thread does not have formal solutions, but rather the dialog that occurs during the demo should serve to guide you along.

Problem 6. [Biped Option] (30 pts) Following the instructions at the wiki site for biped learning pvela.gatech.edu/classes to get the motor interface understood and working for a single motor, as well as to start to model and visualize kinematically the biped robot. In particular, work out Module 0, bullet 1. Demo things working, answer any associated questions, and plot whatever is requested.

Solution 6. Hopefully you the Dynamixels running fine and the interface is not a problem. That, and your stick biped is lookin' good.

Problem 6. [Group Option] (30 pts). If you are working on a group project, then you will be assigned a group contact. The group contact will either be me or a graduate student. You should work out whatever baby steps this group contact assigns the group as opposed to the lab problem. Most likely the info/e-mail will go out on Friday. It is your responsibility to turn in the results to the group contact. There should be sufficient output for them to assess progress.

You are welcome to negotiate a different schedule for this option with the group contact. It could be Wednesday to Wednesday, Friday to Friday, etc. whatever works, so long as it roughly cleaves to the homework schedule. At the end no matter what option is selected, there should have been n deliverables for all teams.

Solution 6. The first project hopefully got you started on the road towards the final goal. Initially it's a baby step, maybe to get the hardware or software interface working, to get some basic display code working for your robot, or possibly even some forward kinematics. In doing so, you should be turning in some kind of document, picture, or video as demonstration that the initial steps were accomplished.

The expectation is that the group response should be similar in details as the solutions to the homeworks are, which means that not only should they communicate accomplishments, but they should also convey the overall procedure involved. Your submissions may not be like that now, but should approach this ideal in future iterations.