

## The NUXMV Symbolic Model Checker<sup>\*</sup>

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**Abstract.** This paper describes the NUXMV symbolic model checker for finite- and infinite-state synchronous transition systems. NUXMV is the evolution of the NUSMV open source model checker. It builds on and extends NUSMV along two main directions. For finite-state systems it complements the basic verification techniques of NUSMV with state-of-the-art verification algorithms. For infinite-state systems, it extends the NUSMV language with new data types, namely Integers and Reals, and it provides advanced SMT-based model checking techniques. Besides extended functionalities, NUXMV has been optimized in terms of performance to be competitive with the state of the art. NUXMV has been used in several industrial projects as verification back-end, and it is the basis for several extensions to cope with requirements analysis, contract based design, model checking of hybrid systems, safety assessment, and software model checking.

### 1 Introduction

NUSMV [1] is a symbolic model checker for finite state fair transition systems. It has been developed jointly by Carnegie Mellon University, the University of Trento and Fondazione Bruno Kessler (FBK) since 1999. It is distributed as open source under the LGPL license, and it integrates some of the most successful BDD and SAT based symbolic model checking algorithms up to 2011 (the year of its last official release).

Since its first release in 1999, the public available version of NUSMV has been complemented and extended, internally at FBK, with multiple functionalities. This was done in order to facilitate its deployment in several operational settings, and to take into account the needs resulting from industrial and research projects. In particular, we integrated functionalities for requirements engineering, safety assessment, contract based design, and techniques for the analysis of hybrid systems; we also interfaced NUXMV with SMT engines. The whole set of new functionalities were developed as a single code-base, referred in several papers as NuSMT and NuSMV3. To better maintain such features, and to facilitate the deployment, we started a re-engineering process where we separated all of them in several different tools. In this view, NUSMV is the code-base that provides basic functionalities and common data structures to all the other tools (e.g. symbol table, handling of expressions, interface with the CUDD [2] BDD package, interface with the SAT solvers (e.g. MINISAT [3]). NUSMV also provides all the basic model checking algorithms for the pure Boolean case.

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In this paper we describe NUXMV, a new symbolic model checker for finite- and infinite-state synchronous fair transition systems. NUXMV is the evolution of NUSMV, as such it builds on NUSMV and extends it along two main directions. For finite-state systems, it complements NUSMV basic verification techniques with a family of new state-of-the-art verification algorithms. For infinite-state systems, it extends the NUSMV language with new data types, namely Integers and Reals, and it provides advanced SMT-based model checking techniques. NUXMV participated in the 2013 hardware model checking competition (HWMCC'13) positioning among the first four in the single and multiple tracks. NUXMV also compares well with other model checkers for infinite-state systems. Finally, NUXMV has been successfully used in several application domains and in industrial settings. It is currently the core verification engine for many other tools (also industrial ones). The tool is distributed in binary code, free to be used for academic research and for non-commercial uses. The latest version of NUXMV can be downloaded from <https://nuxmv.fbk.eu>.

## 2 Functionalities

NUXMV inherits, and thus provides to the user, all the functionalities of NUSMV [1]. In this section we describe all the new features distinguishing them in those for the analysis of finite-state domains, those for the analysis of infinite-state domains, and other generic features.

### 2.1 Analysis of finite-state domains

NUXMV complements the NUSMV language with the AIGER [4] format. AIGER is the language adopted in the hardware model checking competition. Once the AIGER file is read, the internal data structures of NUXMV are populated, and it is possible to verify the properties (if any) with any of the available verification algorithms, or specify new properties interactively “playing” with the design.

NUXMV implements a vast portfolio of algorithms for invariant checking. We currently provide an implementation for the McMillan interpolation-based approach [5] and for the interpolation sequence approach [6]. Interpolation based algorithms are complemented with k-induction algorithms [7] and a family of algorithms based on IC3 [8,9,10]. The IC3 algorithm using abstraction refinement [10] comes in two variant depending on the approach to refinement: the original one based on IC3, and a new variant based on BMC. All these techniques, benefit from the use of temporal decomposition [11] and from techniques to discover equivalences to simplify the problem. We remark that, to implement the interpolation based algorithms we extended MINISAT [3] to build a resolution proof.

Still related to the verification of invariants, we also improved the BDD based invariant checking algorithms by allowing the user to specify hints in the spirit of guided reachability [12]. The hints are specified using a restricted fragment of the PSL SERE [13]. The hints can also be used to compute the full set of the reachable states.

For LTL SAT based model checking, we complemented the BMC based algorithms of NUSMV [14,15] with k-liveness [16] integrated within an IC3 framework. K-liveness is based on counting and bounding the number of times a fairness constraint can become

true. This is used in conjunction with the construction of a monitor for LTL properties, for which we use the LTL2SMV [17] as provided by NuSMV.

## 2.2 Analysis of infinite-state domains

In order to allow the user to specify infinite-state systems, we extended the language of NUSMV with two new data types, namely Reals and unbounded Integers. This, for instance, enables to specify domains with infinite data types (like e.g. the example in Fig. 1).

To analyze such kind of designs, we integrated in NUXMV several new verification algorithms based on Satisfiability Modulo Theory (SMT) [18] and on abstraction, or combination of abstraction with other techniques.

We lifted Simple Bounded Model Checking (SBMC) [15] from the pure Boolean case to the SMT case. The encoding is the same as that of SBMC, but instead of using a SAT solver we use an SMT solver. The SBMC SMT based approach for LTL verification is complemented with k-liveness combined with IC3 extended to the infinite-state case [19]. This approach relies on recent results on applying an IC3-based approach to the verification of infinite-state systems [20]. We remark that, although these approaches are in general incomplete, if a lazo-shaped counterexample exists, it is guaranteed to be eventually found. Moreover, for certain designs, they are able to conclude that the property hold.

As far as invariant checking is concerned, we lifted the pure Boolean approaches like BMC, k-induction, interpolation, and IC3 to the infinite-state systems case. Intuitively, we use an SMT solver in place of the SAT solver. Similarly to the finite case, we provide an SMT based implementation for the McMillan approach [5], the interpolation sequence approach [6], k-induction [7] and for algorithms based on IC3 [20,21].

NUXMV also implements several approaches based on abstraction refinement [22]. We provide new algorithms combining abstraction with BMC and k-induction [23]. The algorithms do not rely on quantifier elimination techniques to compute the abstraction, but encode the model checking problem over the abstract state space into SMT problems. The advantage, is that they avoid the possible bottleneck of abstraction computation. The very same approach has been recently lifted and tightly integrated within the IC3 framework [21], with very good results. All these techniques complement the “classical” counterexample guided (predicate) abstraction refinement (CEGAR) [22], also implemented in NUXMV. The CEGAR approach requires the computation of a quantifier-free formula that is equivalent to the abstract transition relation w.r.t. a given set of predicates. This, in turn, requires the solving of an AllSAT problem [24]. For this step, NUXMV implements different techniques: a combination of BDD and SMT [25,26], where BDDs are used as compact Boolean model enumerators within an AllSMT approach; a technique that exploits the structure of the system under verification, to partition the abstraction problem into the combination of several smaller abstraction problems [27]. For the refinement step to discard the spurious counterex-

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1 MODULE main
2 IVAR
3   d : Real;
4 VAR
5   state : {s0, s1};
6   res : Real;
7 ASSIGN
8   init(state) := s0;
9   next(state) := case
10    state = s0 & res >= 0.10 : s1;
11    state = s1 & res >= 0.20 : s0;
12    TRUE : state;
13  esac;
14  next(t) := case
15    state = s0 & res < 0.10 : res + d;
16    state = s1 & res < 0.20 : res + d;
17    TRUE : 0.0;
18  esac;
19 INIT
20   res >= 0.0
21 TRANS
22   (state = s0 -> (d >= 0 & d <= 0.01)) &
23   (state = s1 -> (d >= 0 & d <= 0.02))
24 INVARSPEC res <= 0.3;

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Fig. 1. Example of the NUXMV language.

ample, NUXMV implements three approaches based on the analysis of the unsatisfiable core, on the analysis of the interpolants, and on the weakest preconditions.

### 2.3 Miscellaneous functionalities

NUXMV provides novel functionalities that aim at facilitating the modeling and the understanding of complex designs. For instance, it allows for the generation of an explicit state representation (subject to the projection over a set of user specified predicates) in XMI format of the design under verification. The generated XMI can be visualized in any UML based viewer supporting the import from XMI.

LTL and invariant properties have been extended to allow for the use of input signals and next values of state variables. This does not add any expressive power to the language, but facilitates the writing of properties from the user's point of view. Internally, each state formula containing a reference to an input or next signal is replaced with a corresponding monitor allowing for the reuse of off-the-shelf verification engines.

NUXMV also provides several model transformation techniques aiming to reduce the state space of the design. It uses static analysis techniques to extract possible values for variables, and then re-encode the design using such information (e.g. using a word at 32 bit to store 2 values can be re-encoded with just one Boolean variable). These techniques are complemented with others aiming at simplifying the model through constants and free inputs propagation [28].

Finally, in NUXMV we removed the NUSMV limitation that restricted the support to bit vectors with less than 64 bits only.

## 3 Architecture

NUXMV extends the NUSMV [1] architecture as described here after. NUXMV shares with NUSMV all the basic functionalities, e.g. the symbol table, the flattening of the design, the Boolean encoding of scalar variables, the representation of the finite-state machines at the different abstraction levels (e.g., scalar, BDD). Moreover, it inherits from NUSMV all the basic model checking algorithms for finite domains both using BDDs (using the CUDD [2]) and SAT (e.g. MINISAT [3]). To implement the new functionalities, we added new Boolean reasoning engines. We extended MINISAT with the construction of the resolution proof. On top of this, we built an interface to extract interpolants. In this respect, we extended the standard API in NUSMV to also provide API for extracting and manipulating interpolants. This also enables for the use of different SAT engines in a transparent way.

For IC3 based algorithms, NUXMV provides two modes: execution as a library, or call of an external executable (this was also done to participate to the hardware model checking competition). The use of an external executable also opens to experiment with other engines, and to reuse the results within NUXMV, provided the I/O interface is respected. The model checking problem is dumped into AIGER format, and for violated properties the resulting AIGER trace is converted back into a NUXMV trace.

To reason over infinite-state systems, we created an interface towards SMT engines. We instantiated this interface on the MATHSAT5 [29] SMT solver (although in principle other SMT solvers could be plugged in). The interface enables for a wide range

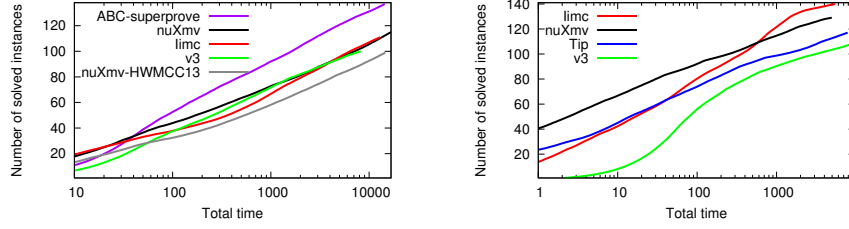


Fig. 2. Results for finite domains on the HWMCC13 samples.

of queries: satisfiability checking and AllSMT queries; extraction of unsatisfiable cores and of interpolants; and, quantifier elimination. This interface is the basis on top of which the majority of the SMT based algorithms are built. For IC3 based algorithms, a more tight integration with the SMT solver is required, therefore we implemented them directly on top of MATHSAT5. We then interfaced this new engine with NUXMV.

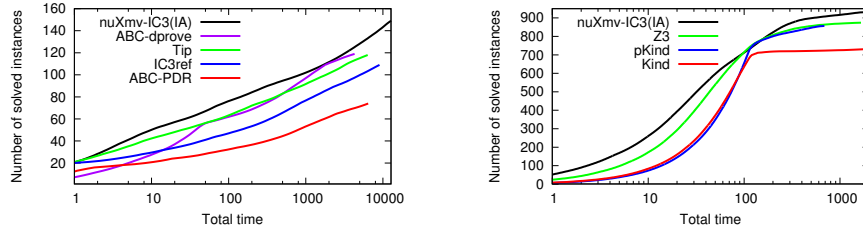
NUXMV has been developed in C and in C++. It compiles and executes on the most widely used Operating Systems (OSs) and architectures; namely, Linux, MS Windows, and MacOS X. Porting to other OSs is also possible (although not tested yet).

## 4 Performance evaluation

In order to see where NUXMV is positioned w.r.t. the state-of-the-art, we report in this section some results. In Fig. 2 we plot the comparison of NUXMV against the three best performers at the HWMCC13. The comparison is run on the same benchmarks used in the HWMCC13 in the single safety (left) and in the liveness (right) tracks. We compare two versions of NUXMV, the one that participated in the competition (NUXMV-HWMCC13) and the current one. The results show that, still ABC is the top performer, but the current version of NUXMV is able to solve more problems than the one submitted to the competition. Moreover, it solves more problems than *iimc* and *v3* that are performing better than NUXMV-HWMCC13. Concerning the liveness track, NUXMV did not participate in the competition. Here *iimc* is still the winner, but NUXMV performs better than *v3* and *tip* (positioned 2nd and 3rd resp. in the HWMCC13).

In Fig. 3 we report some results for the SMT cases. On the left we compare IC3 with implicit abstraction algorithm [21] as available in NUXMV against state-of-the-art engines on a set of bit-vector (BV) benchmarks (we took all the benchmarks used in [20], using BV as background theory instead of LRA, the instances of the *bitvector* set of the Software Verification Competition [30] and the instances from the test suite of InvGen [31]). For the other solvers, bit-blasting was performed. In Fig. 3 on the right, we compare NUXMV with other model checkers for Linear Integer Arithmetic (LIA). (The label *nuXmv-IC3(LIA)* corresponds to the label *IC3+IA(BV)* of [21]). We used benchmarks taken from Lustre programs as available from the web page of Kind [32]. These results show that in both cases NUXMV can solve more problems than the other state-of-the-art tools.

These results, clearly show that NUXMV is well positioned in the space of formal verification engines, both for the finite domain case, and for the infinite domain one.



**Fig. 3.** Results on SMT domains: BV and LIA (taken from [21]).

## 5 Applications

The NUXMV symbolic model checker has been used in a wide range of applications, both at academic and at industrial level.

As far as the industrial settings are concerned, we report that NUXMV is used at Rockwell-Collins as one of the available back-end verification engines [33]. NUXMV has been extended and is daily used by Ales s.r.l., also as a back-end verification engine, for their internal verification flow [34]. Moreover, Ansaldo STS integrated NUXMV within their development environment for the verification of railways interlocking software [35]. We also remark that NUXMV has been widely used in several industrial projects with the European Space Agency (ESA). For instance, it is the back-end of the COMPASS tool [36], developed within the COMPASS [37] and AUTOGEF [38] projects both funded by ESA. It has also been used in the EuRailCheck tool for the validation of a fragment of the ETCS requirements [39]. EuRailCheck was developed in response of an invitation to tender issued by the European Railway Agency.

NUXMV is also the back-end of several other tools. (We remark that, since the development of NUXMV started a long time ago, its functionalities were used already by other tools, often relying on intermediate, non-official versions of NUXMV itself.) It has been integrated in AutoFocus [40]. It is used in the KRATOS [41] software model checker, in RATSY [42] for temporal logic synthesis, and in OCRA [43] for contract based requirements analysis. Finally, it is the basis on top of which we built the safety assessment tool FSAP [44] and the HyCOMP [45] tool for the verification of hybrid systems.

## 6 Conclusions and Future Work

In this paper we presented NUXMV, a new symbolic model checker for finite- and infinite-state transition systems. We described its functionalities, and we reported some results that compare its performance with the state-of-the-art. The results show that it is well positioned w.r.t. the other possible competitors.

As future work, we would like to add support for arrays, their combination with bit vectors, and uninterpreted functions, and to interface with the BTOR format. We would like to exploit multi-core architectures to further speed-up the analyses. Finally, we would like to wrap the NUXMV functionalities in a scripting language to facilitate the experimentation of new algorithms and the customization w.r.t. user needs.

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