To provide a more intuitive presentation of the algorithmic principles of the DCBAN model proposed in this thesis, the training and inference processes of DCBAN are presented in pseudocode form, as shown in Algorithm 1. This pseudocode illustrates the complete process, from fMRI data preprocessing and feature extraction to the training of semantic and text prediction models, and finally, to the dynamic confidence adaptive fusion diffusion generation. Through this process, it is clear that the core of DCBAN relies on the organic collaboration of three key modules: Deep Nested Singular Value Decomposition (DeepSVD), Bayesian Adaptive Feature Ridge Regression (BAFRR), and Dynamic Confidence Adaptive Fusion Diffusion (DCAF).

### Algorithm 1: DCBAN

Input: Visual image  $I_{\it RGB}$   $\sim$  raw fMRI data obtained while viewing  $I_{\it RGB}$   $\sim$  prompt associated with  $I_{\it RGB}$ 

Hyperparameters: DeepSVD/BAFRR/DCAF internal hyperparameters (see Table 2. Hyperparameter Settings and instructions)

Output: Reconstructed visual image

### Preprocessing of raw fMRI data

1: X ← GLM\_denoise\_and\_beta\_average(fMRI raw data)

Construct Training Labels:

- 2: Semantic features  $Y_Z$  are extracted by VAE from  $I_{RGB}$ .
- 3: Text features  $Y_C$  are extracted by CLIP from the prompt.

Prediction models for semantic and text features are trained.

Dimension Alignment:
$$Y_{PCA} \leftarrow PCA (Y, \underline{X.shape}[1])$$
DeepSVD Fine-grained Feature Extraction:
$$\lambda, V \leftarrow \underline{DeepSVD}(X, Y_{PCA})$$
Obtain BAFRR Coefficient Solution:
$$\delta_{best} \leftarrow \underline{ARSO}(X, Y_{PCA})$$
7: 
$$\beta \leftarrow \underline{Train BAFRR}(X, Y, \lambda, V,)$$

end for

// After the loop,  $\beta_Z$  and  $\beta_C$  are obtained.

Predict Visual Image Semantic Features:

Predict Visual Image Text Features:

Dynamic Confidence Adaptive Diffusion to Reconstruct Visual Image:

10: Reconstructed Visual mage← DCAF(Z, C)

Return Reconstructed Visual Image

To provide a more intuitive explanation of the detailed processes involved in the three main modules of DCBAN—DeepSVD, BAFRR, and DCAF—the corresponding pseudocode has been included, as shown in Algorithm 2-4.

### Algorithm 2: DeepSVD

Input: fMRI feature X  $_{\circ}$  dimension-reduced visual image features  $Y_{PCJ}$   $_{\circ}$ 

**Hyperparameters:** DeepSVD internal hyperparameters (see Table 2. Hyperparameter Settings and instructions)

Output: Highly correlated singular values \( \), singular value vectors V

```
1: Repeat until early stopping:
          T_0 = \mathbf{X}
2:
3:
           for i in {1..56} do
               \begin{array}{l} T_{i} \leftarrow 3 \times 3 \text{Conv} \left( T_{i-1}; \Phi_{-i} \right) \\ f_{i}, \ \ g_{i} \leftarrow \text{SVD}(T_{i}) \end{array}
4:
5:
                Compute low-rank constraint loss (see Equation (1))
               \mathcal{L}_{rank} \leftarrow \mathcal{L}_{rank} f_i g_i
6:
                Compute Mean Squared Error (MSE) (see Equation (3))
                \mathcal{L}_{MSE} \leftarrow \mathcal{L}_{MSE} (T_i Y_{PCA})
7:
                Global joint loss (see Equation (4))
                \mathcal{L}_{total} \leftarrow \mathcal{L}_{total} (\mathcal{L}_{rank}, \mathcal{L}_{MSE})
8:
                Update network parameters (see Equation (5))
                AdamUpdate(Hyperparameters)
9:
10:
           end for
11: until early_stop
12: X<sub>lowrank</sub> ← Fully Connected Layer(T<sub>56</sub>)
       Output of Highly Correlated Singular Values (see Equation (6)):
13: \lambda \leftarrow Calculation\_of\_strongly\_correlated\_singular\_values(\mathbf{X}_{lowrank})
       Output of Highly Correlated Singular Vectors (see Equation (7)):
14: V ← Calculation_of)singular_vectors (X<sub>lowrank</sub>)
```

```
Algorithm 3: BAFRR
```

```
Input: fMRI feature X \times visual image feature Y \times highly correlated singular value \lambda, singular value vector V
```

Hyperparameters: BAFRR internal hyperparameters (see Table 2. Hyperparameter Settings and instructions)

Output: Semantic feature Z v text feature C

```
Grid Definition (Equation 8):
```

1: 
$$\Lambda = \{\delta_i \mid \delta_i = \delta_{min} + i \cdot \Delta \delta, i = 0, 1, 2..., N\}$$

Use GP surrogate model + Expected Improvement (EI) as the acquisition function for L iterations

Store (a,mse)

- 2: Obs = []
- 3: for δ in Λ do:

```
Cross-validation evaluation

4: for i in \{1, ..., k\} do:

5: (X_{train}, Y_{train}, X_{val}, Y_{val}) = SplitKFold(X, Y, i, k)

6: \beta_{\delta_i} = BAFRR(Y_{train}, \lambda, \delta_i)

7: Y_{pred} = X_{val} @ \beta_{\delta_i}

8: mse = KFoldMSE(Y_val, Y_pred)

9: Obs.append((\delta_i, \alpha, mse))

10: end for
```

11: end for

#### Optimal Score Selection:

12:  $\delta_{\text{best}}$  = min(Obs, key=lambda item: item[2])

13: def BAFRR (Y, λ, V, δ ):

### Preprocess to singular value space

14:  $\tilde{Y} = V^T Y$ 

Unregularized solution (OLS) is solved in singular value space

15: 
$$\tilde{\beta}_{OLS} = S^{-2}(\lambda \odot \tilde{Y})$$
  
Generate search grid A

16: 
$$A = (\alpha_k \mid \alpha_k = 10^{\log_{10}(SM4LL\_BIAS \sigma_{min}^2) + k \cdot \Delta A}, k = 0,1,...,N)$$

Perform Bayesian optimization for L iterations to generate the adaptive grid

 $A_L$ 

17: For i in L do:

18: GP.fit(α<sub>i</sub>)

Select the next set of α\alphaα with the highest potential based on EI

19: 
$$EI(\alpha_i) = (m(\alpha_{i_{\text{test}}}) - m(\alpha_i)) \cdot \Phi(Z) + \sigma(\alpha_i) \cdot \phi(Z)$$

- 20:  $A_L$  =OptimizeGrid (A)
- 21: end for

Calculate the  $\begin{subarray}{c} A_{\it L} \end{subarray}$  of lpha values and corresponding  $\gamma$  values in P

22: 
$$P = \{(\alpha_1, \gamma_1), (\alpha_2, \gamma_2), ..., (\alpha_n, \gamma_n)\}$$

## Compute Ridge Regression target parameters

23:  $\alpha_{\delta}$  = Interpolate (P,  $\delta$ )

# Solve Ridge Regression

24: 
$$\tilde{\beta}_{RR} = [\lambda^2/(\lambda^2 + \alpha_{\delta})] \odot \hat{\beta}_{OLS}$$

25: 
$$\beta = V \tilde{\beta}_{RR}$$

27: end

28: 
$$\beta_Z = BAFRR(Y_Z, \lambda, V, \delta_{best})$$

29: 
$$\beta_C = BAFRR(Y_C, \lambda, V, \delta_{best})$$

30: 
$$Z = X_{\text{test}} \beta_Z$$

31: 
$$C = X_{test} \beta_C$$

### Return Z,C

### Algorithm 4: DCAF

Input: Decoded semantic features Z., decoded text features C., time step niter

**Hyperparameters:** Internal hyperparameters of DCAF (see Table 2. Hyperparameter Settings and instructions)

Output: Reconstructed visual image

### Feature Alignment

1: Align(C)

### Feature Flattening

2: 
$$Z_1 = Flatten(C)$$

### Form Bottleneck Structure

3: 
$$Z_2 = \text{Re}lu(MLP(Z_1))$$

### **Output Confidence Weights**

4: 
$$conf_weight = \sigma(Z_2)$$

## Dynamic Confidence Adaptive Fusion Diffusion for Visual Image Reconstruction

5: for n in range(niter) do:

6: 
$$time\_decay(n) = mco(0,1-n/niter)$$
  
7:  $\xi^{(n)} = conf\_weight \times time\_decay(n)$ 

Dynamically Couple to Generate Dynamic Text Features

8: 
$$C_{\text{dincomix}}^{(n)} = \xi^{(n)} \cdot C + (1 - \xi^{(n)}) \cdot u_C$$

Reconstruct Visual Image Using Diffusion Model

9: Reconstructed Visual Image  $\leftarrow$  diffusion\_model(Z,  $C_{dynanic}^{(n)}$ )

10: end

Return: Reconstructed Visual Image