

# MVS & Neural Radiance Fields



Video from the original ECCV'20 paper

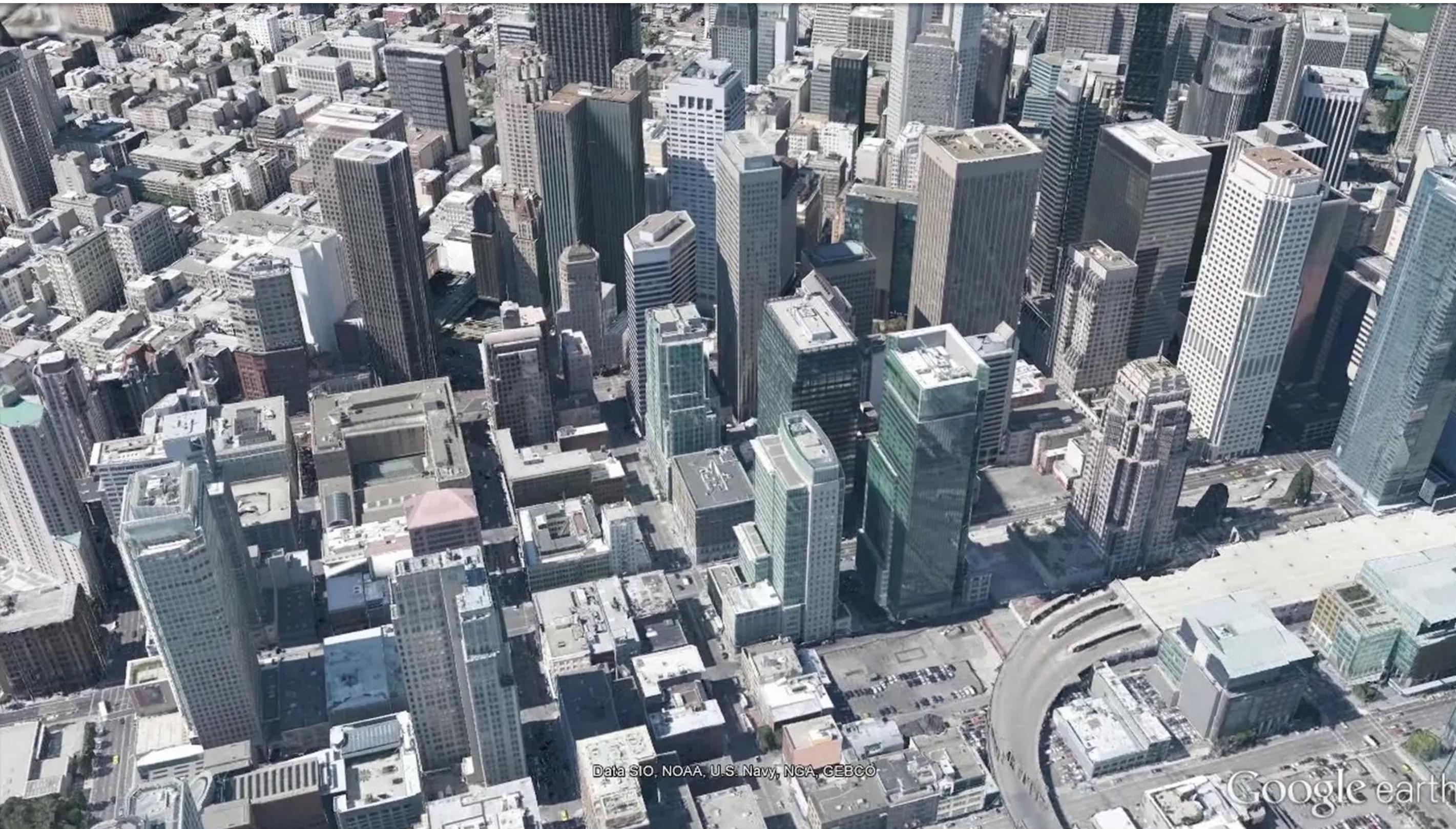
CS180/280A: Intro to Computer Vision and Computational  
Photography  
Angjoo Kanazawa and Alexei Efros  
UC Berkeley Fall 2023

# Logistics

- Project 4 due tonight! Good luck!

# Multi-View Stereo

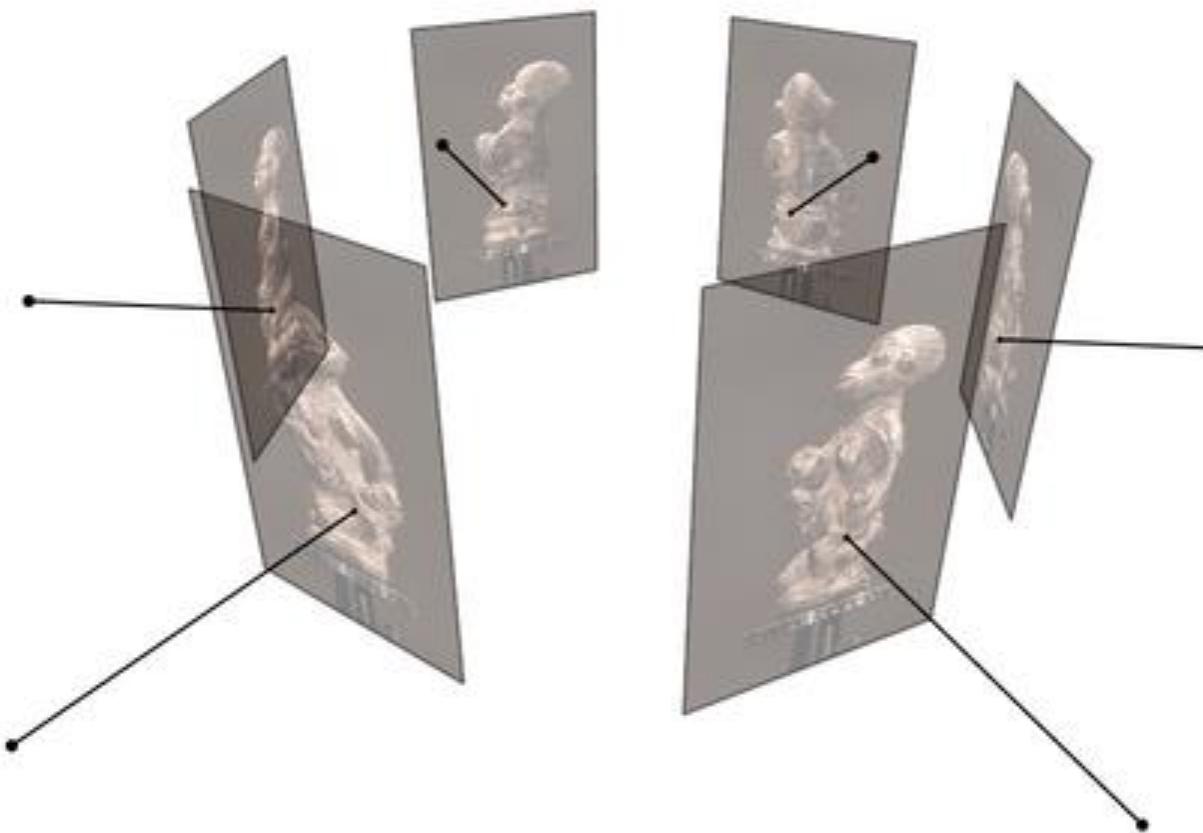
# What if we want solid models?



Slide credit: Noah Snavely

# Multi-view Stereo (Lots of calibrated images)

- Input: calibrated images from several viewpoints (known camera: intrinsics and extrinsics)
- Output: 3D Model



Figures by Carlos Hernandez

Slide credit: Noah Snavely

In general, conducted in a controlled environment with multi-camera setup that are all calibrated

# Whistle in the Form of Female Figure 600 AD - 900 AD



≡ Details

Los Angeles County Museum of Art



Los Angeles County Museum of Art



Sculpture



Mexico

Share

Compare

Saved 0

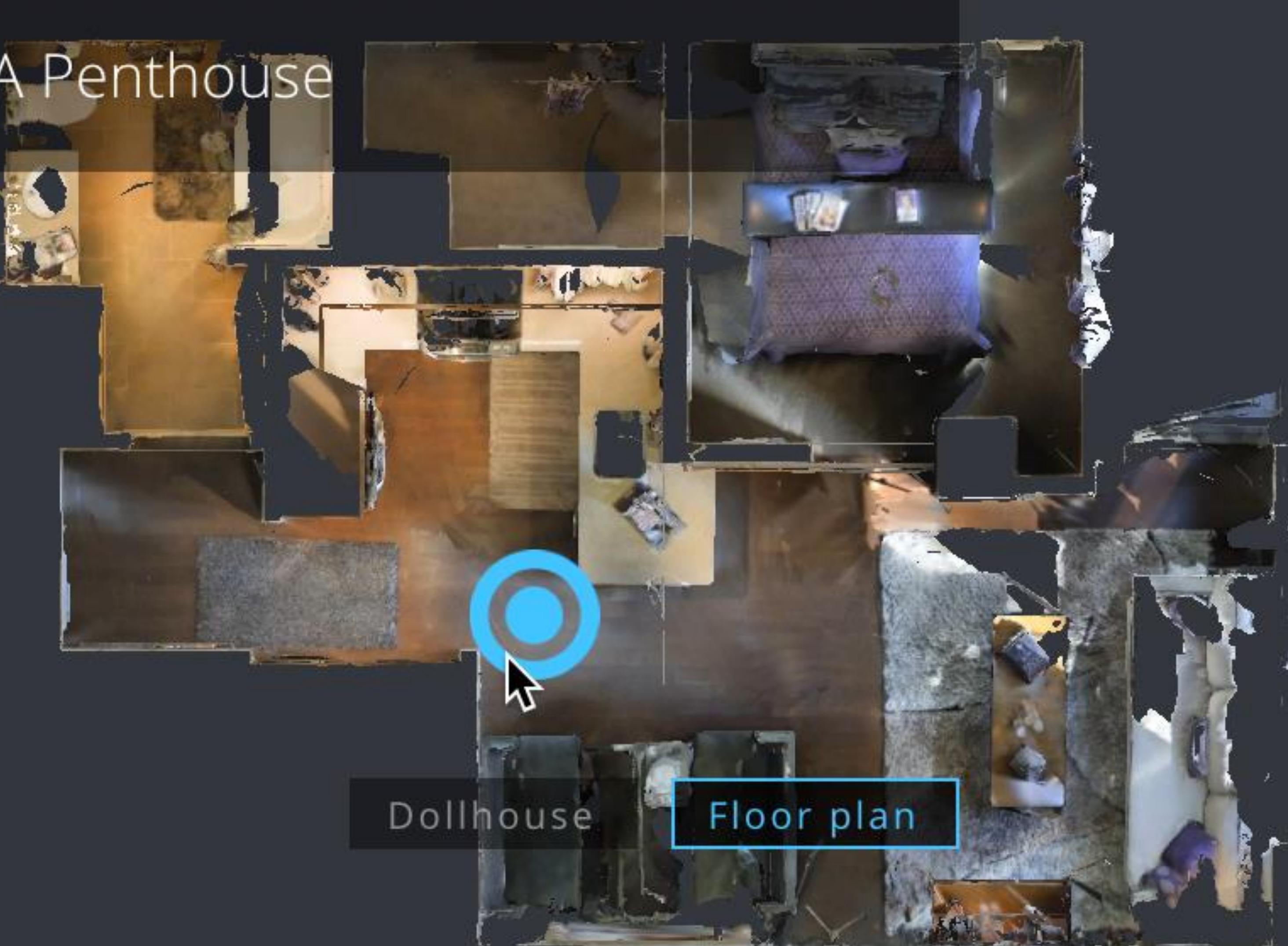
Discover

Google

Slide credit: Noah Snavely



< 1BR, 1BA Penthouse Terms ?

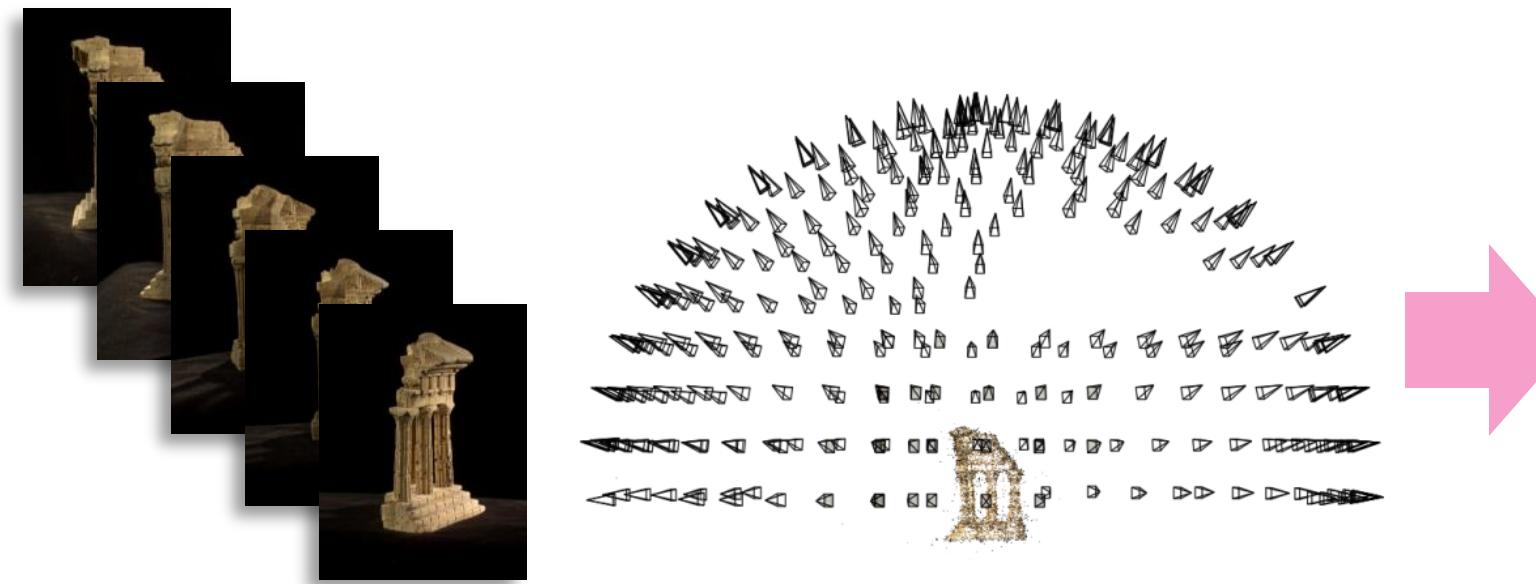


# Multi-view Stereo

**Problem formulation: given several images of the same object or scene, compute a representation of its 3D shape**



**Binocular Stereo**



**Multi-view stereo**

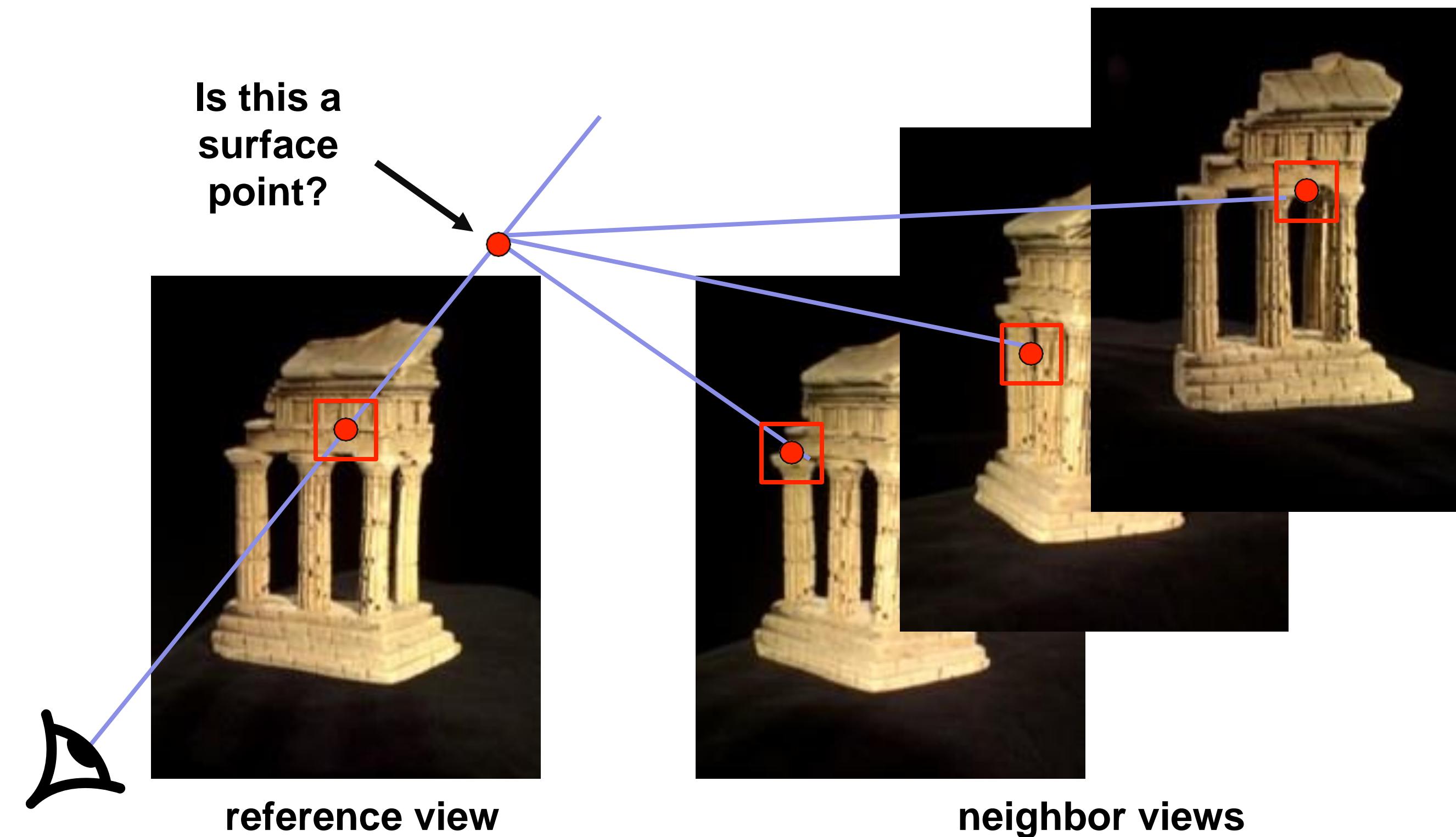
Slide credit: Noah Snavely

# Examples: Panoptic studio



<http://domedb.perception.cs.cmu.edu/>

# Multi-view stereo: Basic idea



Source: Y.  
Furukawa

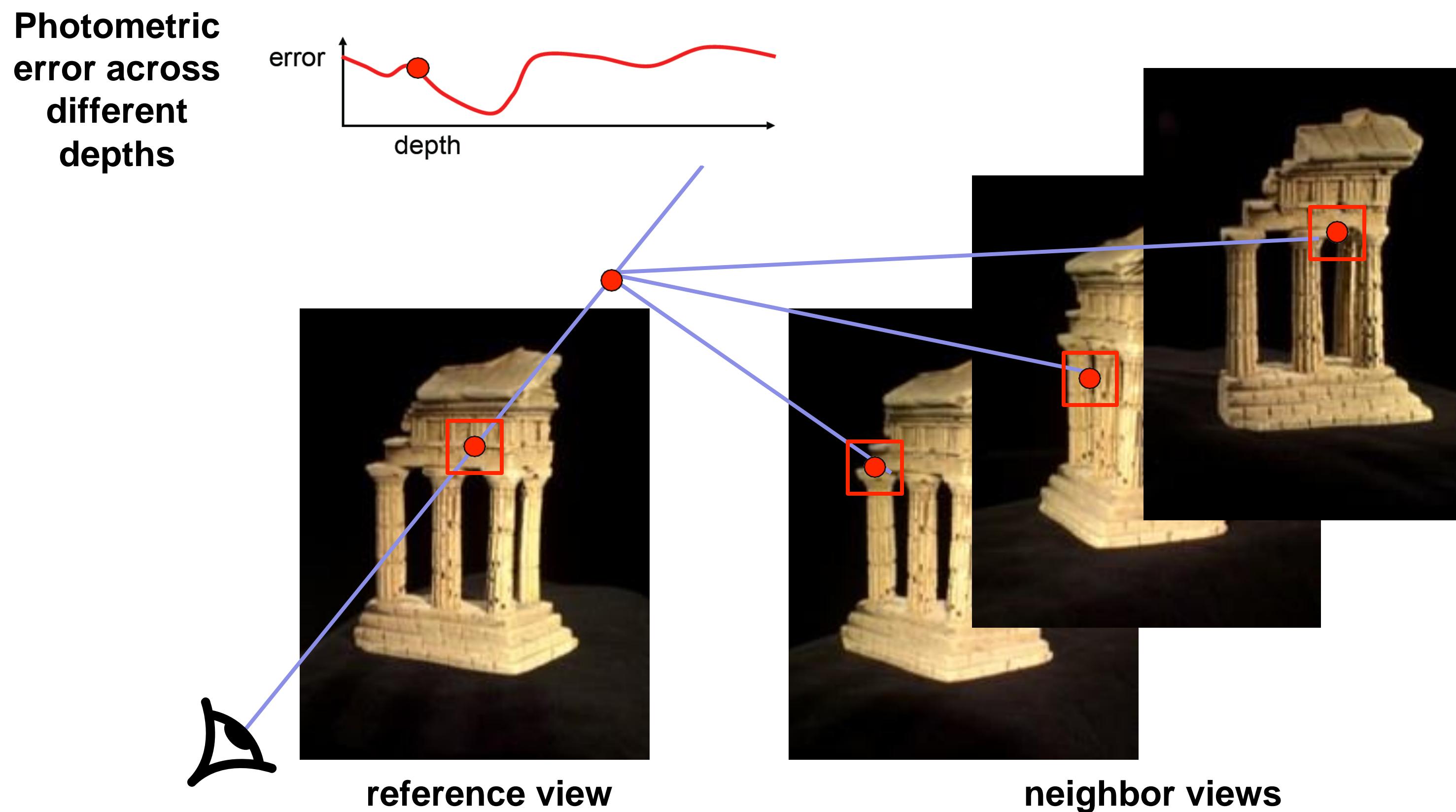
# Multi-view stereo: Basic idea

**Evaluate the likelihood of geometry at a particular depth for a particular reference patch:**



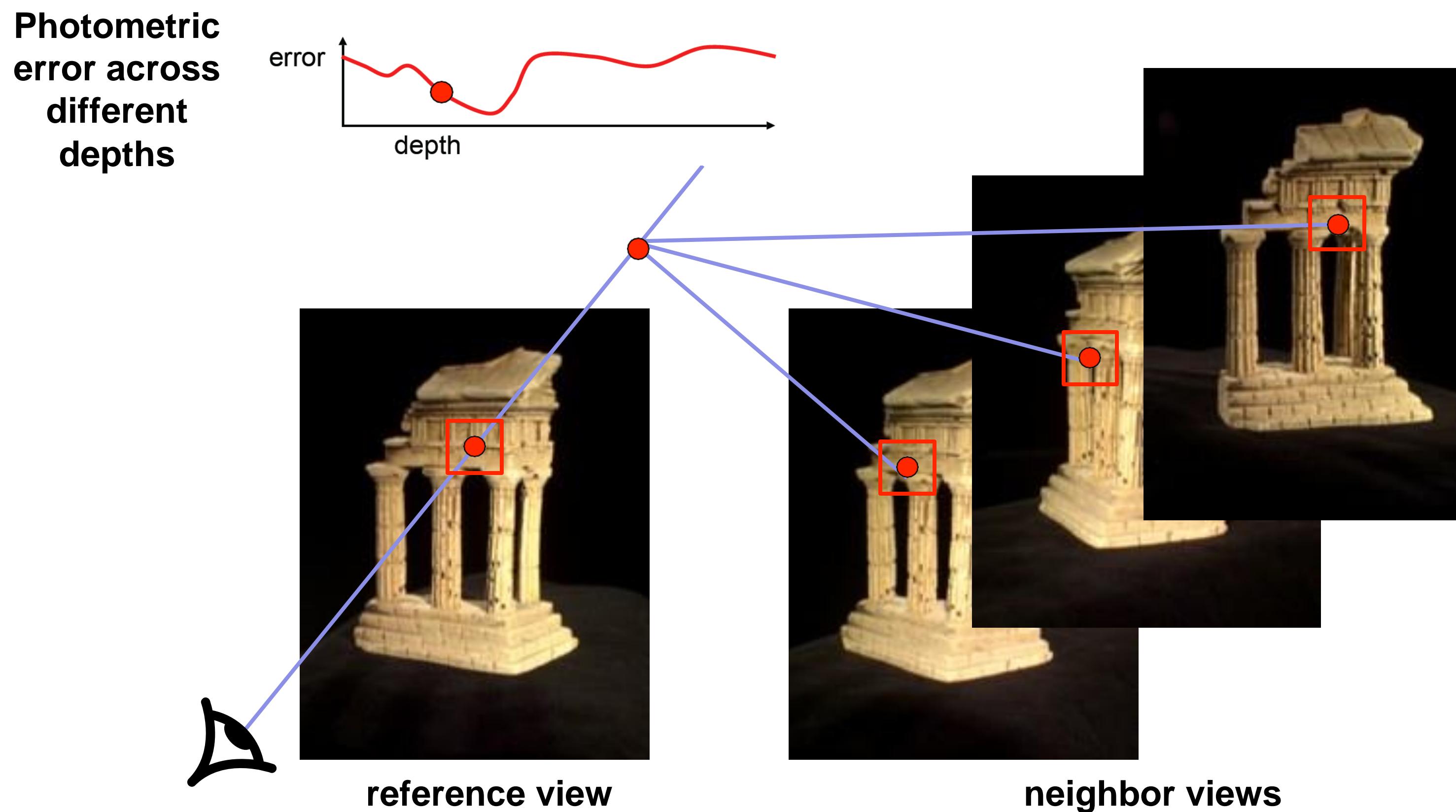
Source: Y.  
Furukawa

# Multi-view stereo: Basic idea



Source: Y.  
Furukawa

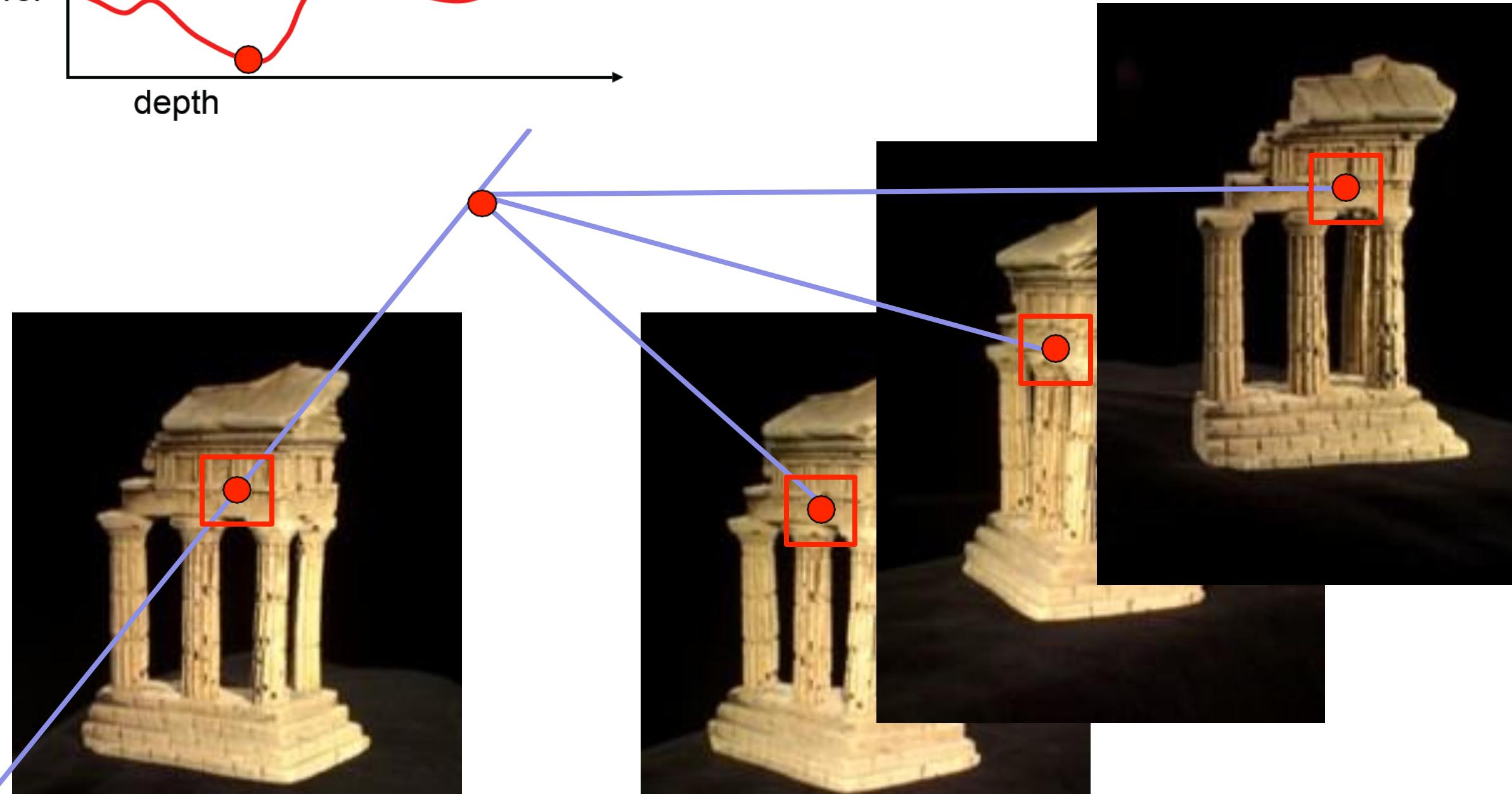
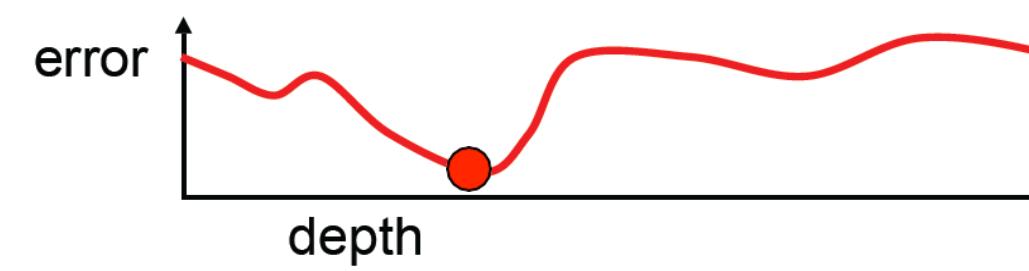
# Multi-view stereo: Basic idea



Source: Y.  
Furukawa

# Multi-view stereo: Basic idea

Photometric  
error across  
different  
depths



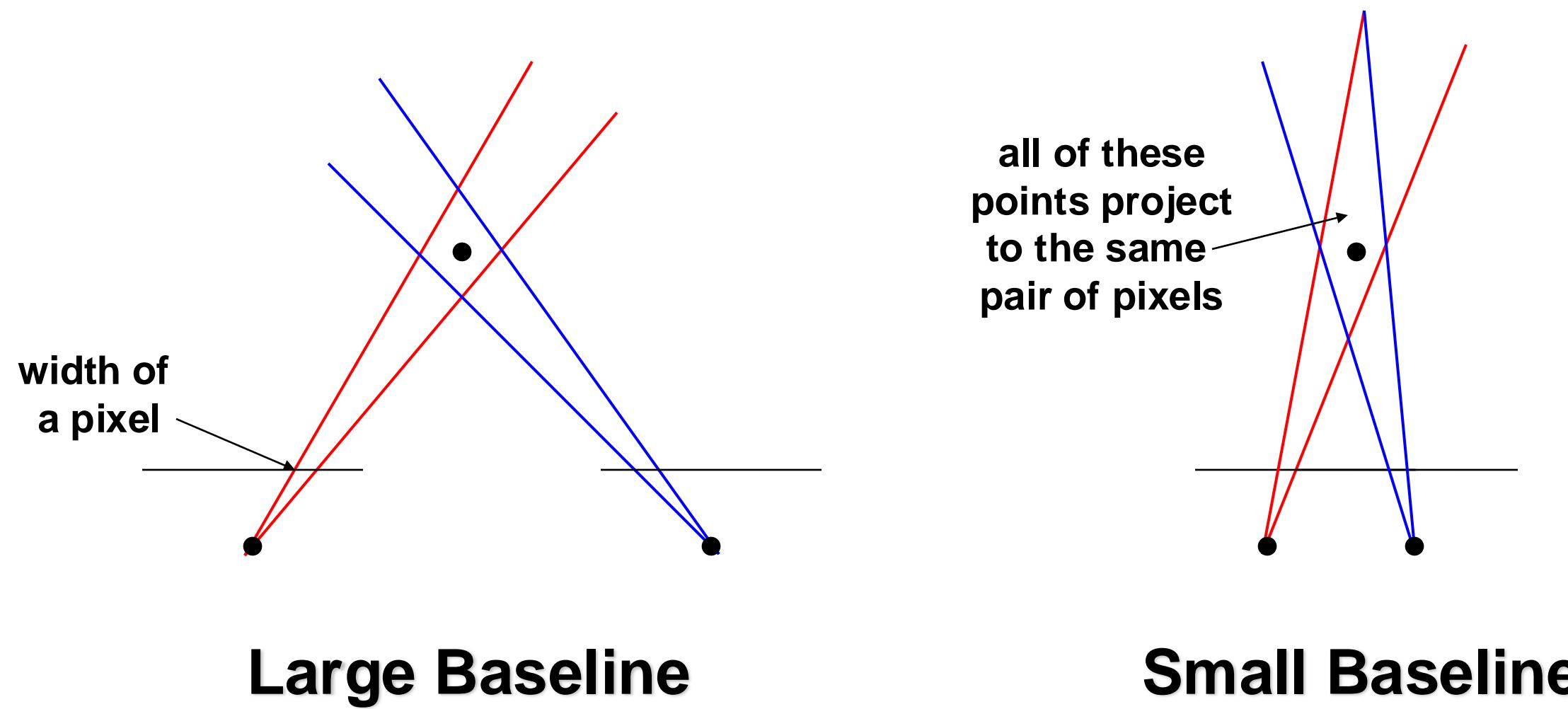
In this manner, solve for a depth map over the whole reference view

Furukawa

# Multi-view stereo: advantages over 2 view

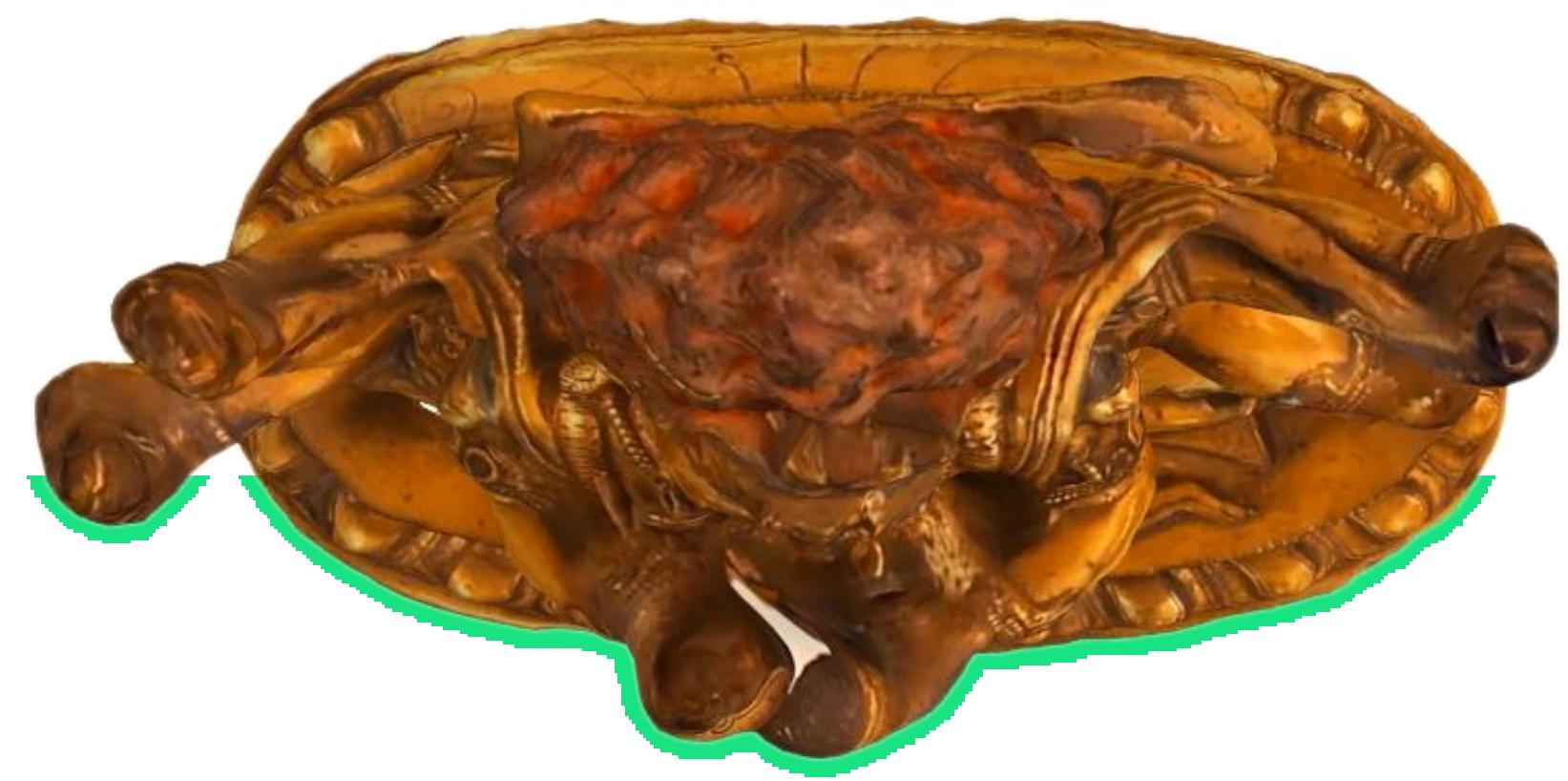
- Can match windows using more than 1 other image, giving a **stronger match signal**
- If you have lots of potential images, can **choose the best subset** of images to match per reference image
- Can reconstruct a depth map for each reference frame, and merge into a **complete 3D model**

# Choosing the baseline

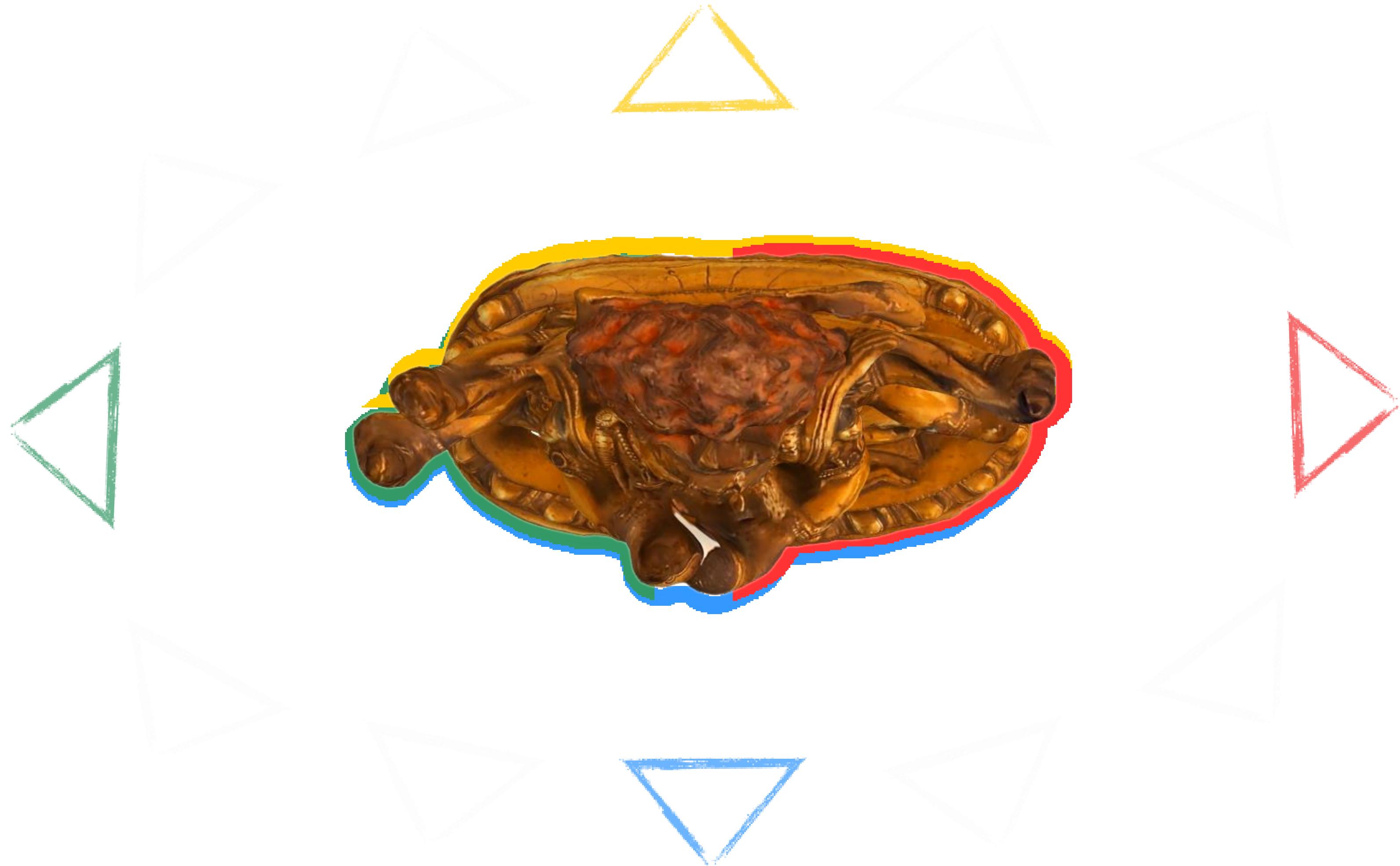


- What's the optimal baseline?
  - Too small: large depth error
  - Too large: difficult search problem

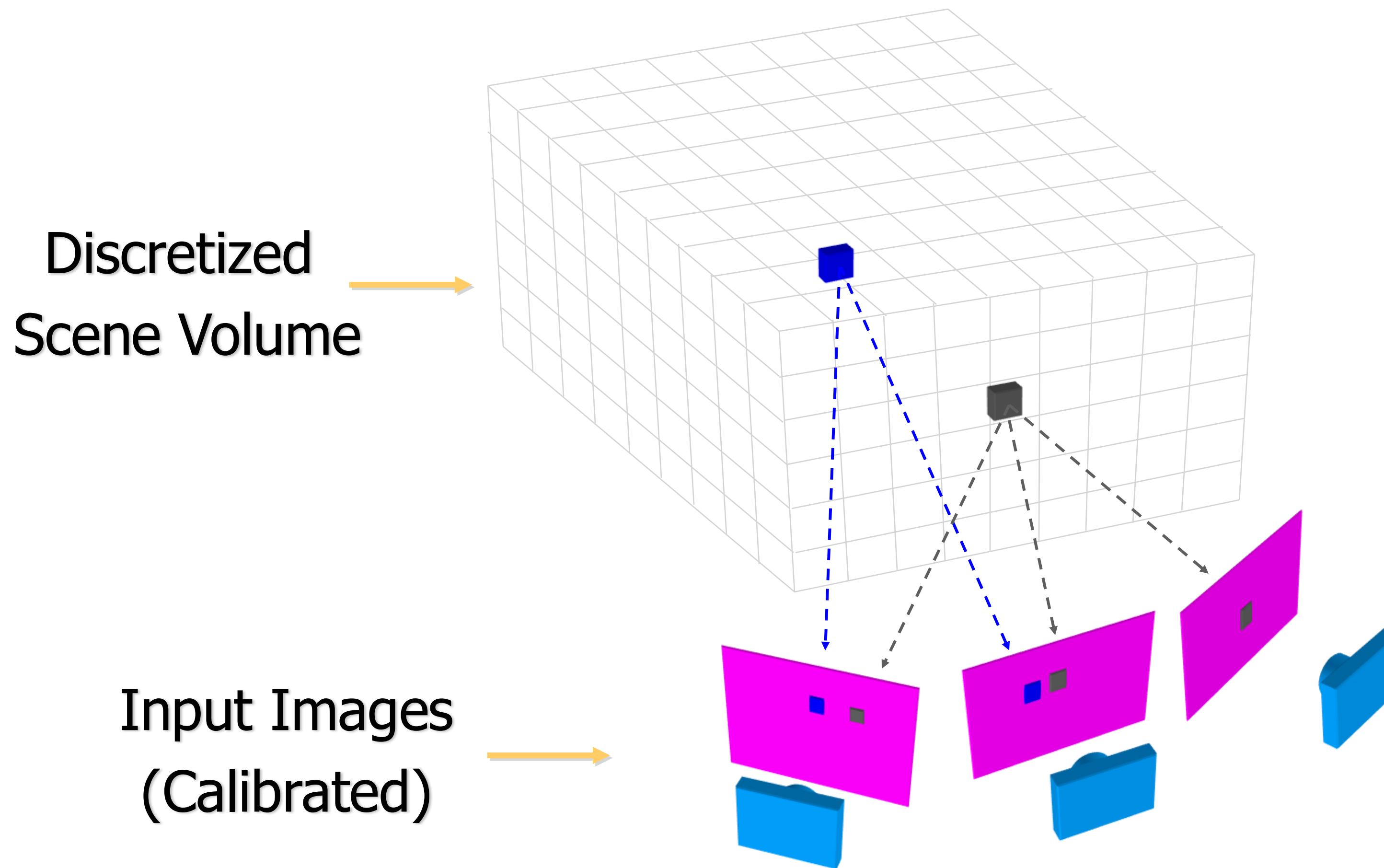
Slide credit: Noah Snavely





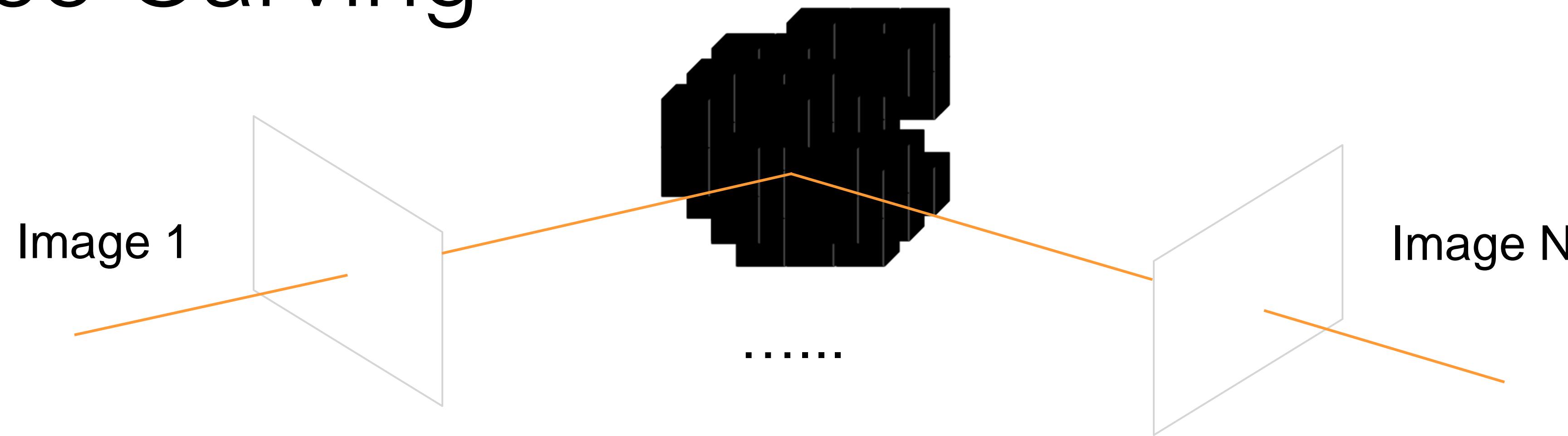


# Volumetric stereo



**Goal:** Assign RGB values to voxels in  $V$   
***photo-consistent*** with images

# Space Carving



- **Space Carving Algorithm**

- Initialize to a volume  $V$  containing the true scene
- Choose a voxel on the outside of the volume
- Project to visible input images
- Carve if not photo-consistent
- Repeat until convergence

# Space Carving Results



**Input Image (1 of 45)**



**Reconstruction**



**Reconstruction**



**Reconstruction**

Source: S. Seitz

# Space Carving Results



**Input Image  
(1 of 100)**



**Reconstruction**

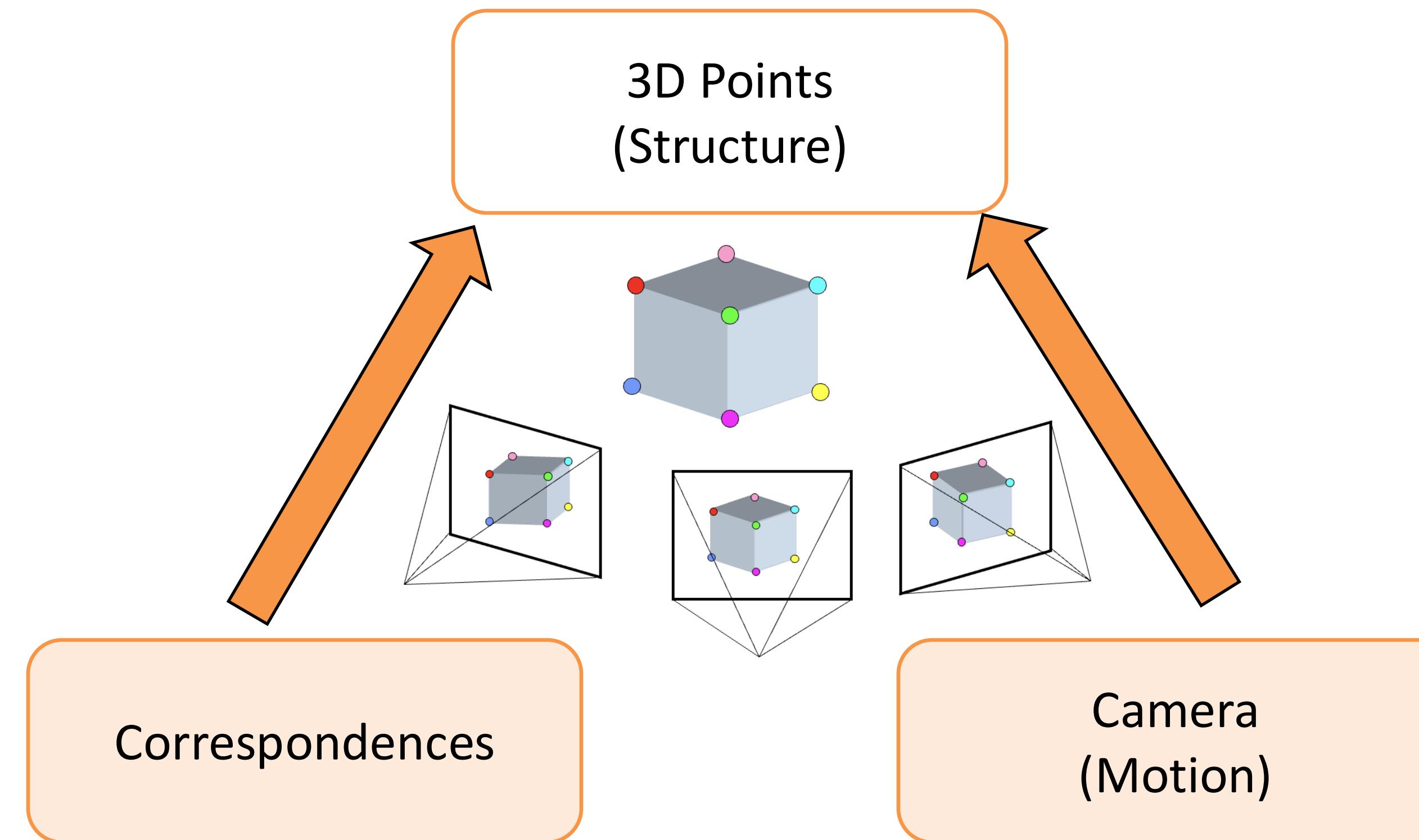
Source: S. Seitz

# Tool for you: COLMAP

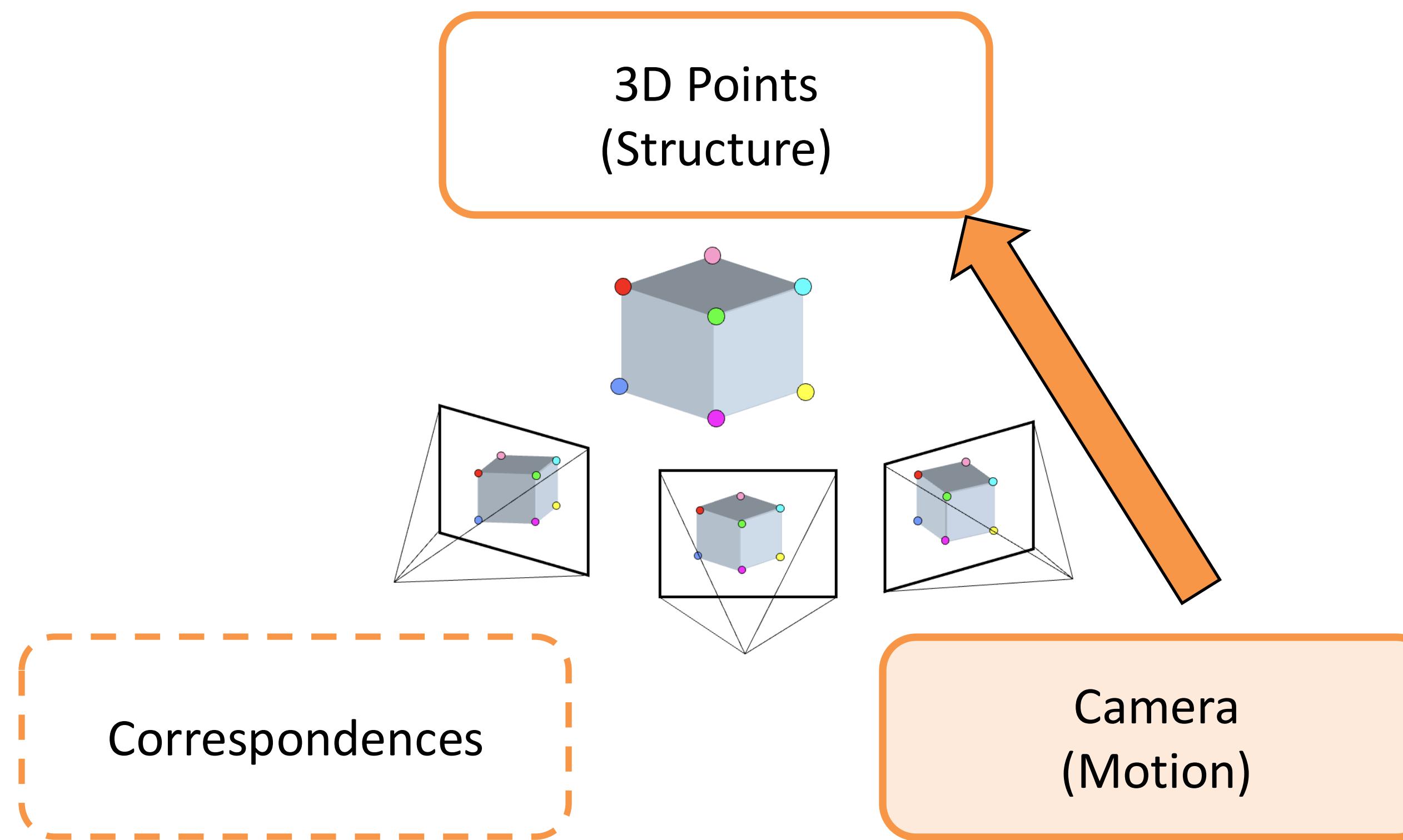
<https://github.com/colmap/colmap>

A general SfM + MVS pipeline

# Multi-View Stereo



# Volumetric “Neural” Rendering



**Does not use explicit correspondences,  
relies on reconstruction loss (Analysis-by-Synthesis)**

# Neural Radiance Fields



Video from the original ECCV'20 paper

# Capturing Reality



Earliest cave painting (45,500 years old) in Sulawesi, Indonesia

# Capturing Reality



Monet's Cathedral series: study of light 1893-1894

# Capturing Reality



First self-portrait Cornelius 1839



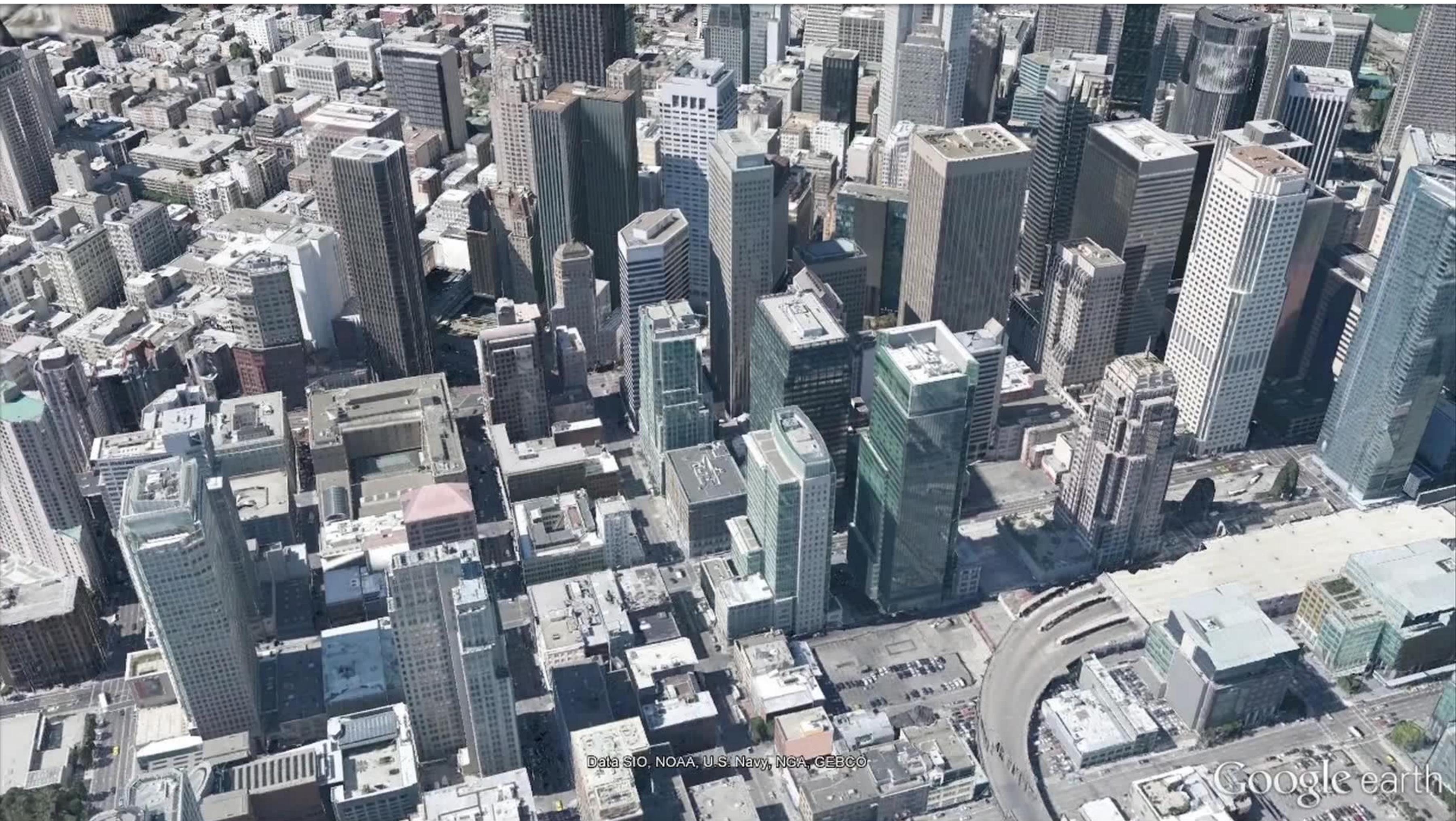
First Movie - Muybridge 1878

# Capturing Reality – in 3D



Building Rome in a Day, Agarwal et al. ICCV 2009

# Capturing Reality – in 3D (MVS – last lecture)



Google Earth 2016~

# What is next?

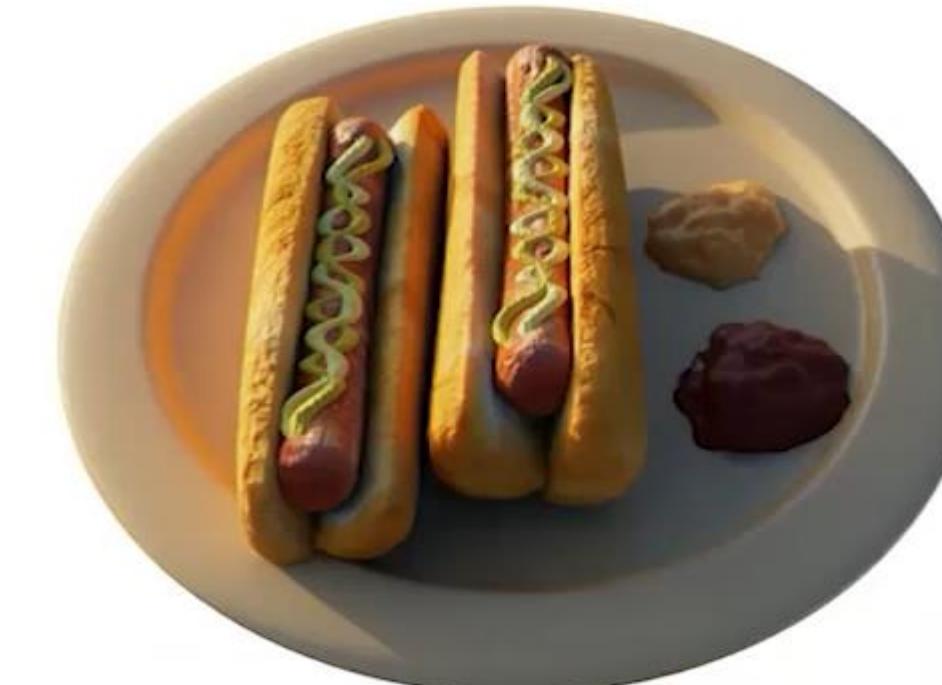
# 2020: Neural Radiance Field (NeRF)



Mildenhall\*, Srinivasan\*, Tancik\*, Barron, Ramamoorthi, Ng, ECCV 2020

# It has been three years

- Original NeRF paper: 4200+ citations in 3 years



# Handling Appearance Changes



# Real-time Rendering



Video from PlenOctrees [Yu et al. CVPR 2021]

# Real-time Inference

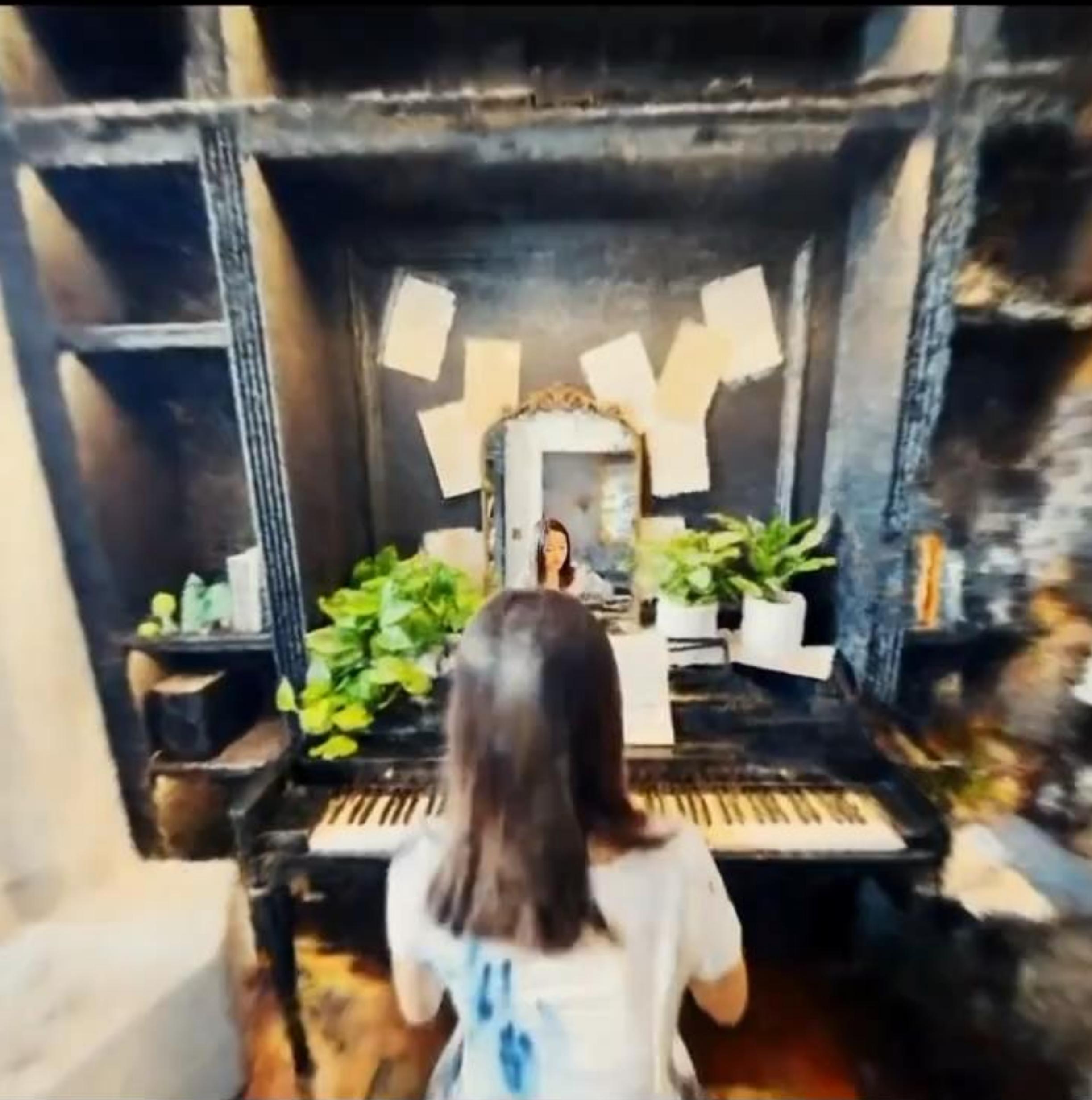
## INSTANT NEURAL GRAPHICS PRIMITIVES WITH A MULTIRESOLUTION HASH ENCODING

Thomas Müller Alex Evans Christoph Schied Alexander Keller

<https://nvlabs.github.io/instant-ngp>



NVIDIA®



@karenxcheng, with  
InstantNGP [Müller et  
al., SIGGRAPH 2022]

[GETTING STARTED](#)[GITHUB](#)[DOCUMENTATION](#)

nerfstudio

VIEWPORT RENDER VIEW



▶ RESUME TRAINING

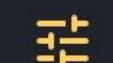
[Show Scene](#)[Show Images](#)

Refresh Page

Resolution: 640x1024px

Time Allocation: 100% spent on viewer

Server Connected | Render Connected



CONTROLS



RENDER



SCENE

[LOAD PATH](#)[EXPORT PATH](#)

Height

1080

Width

1920

FOV

50

Seconds

4

FPS

24

[ADD CAMERA](#)

Smoothness

0.00



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CAMERA 0



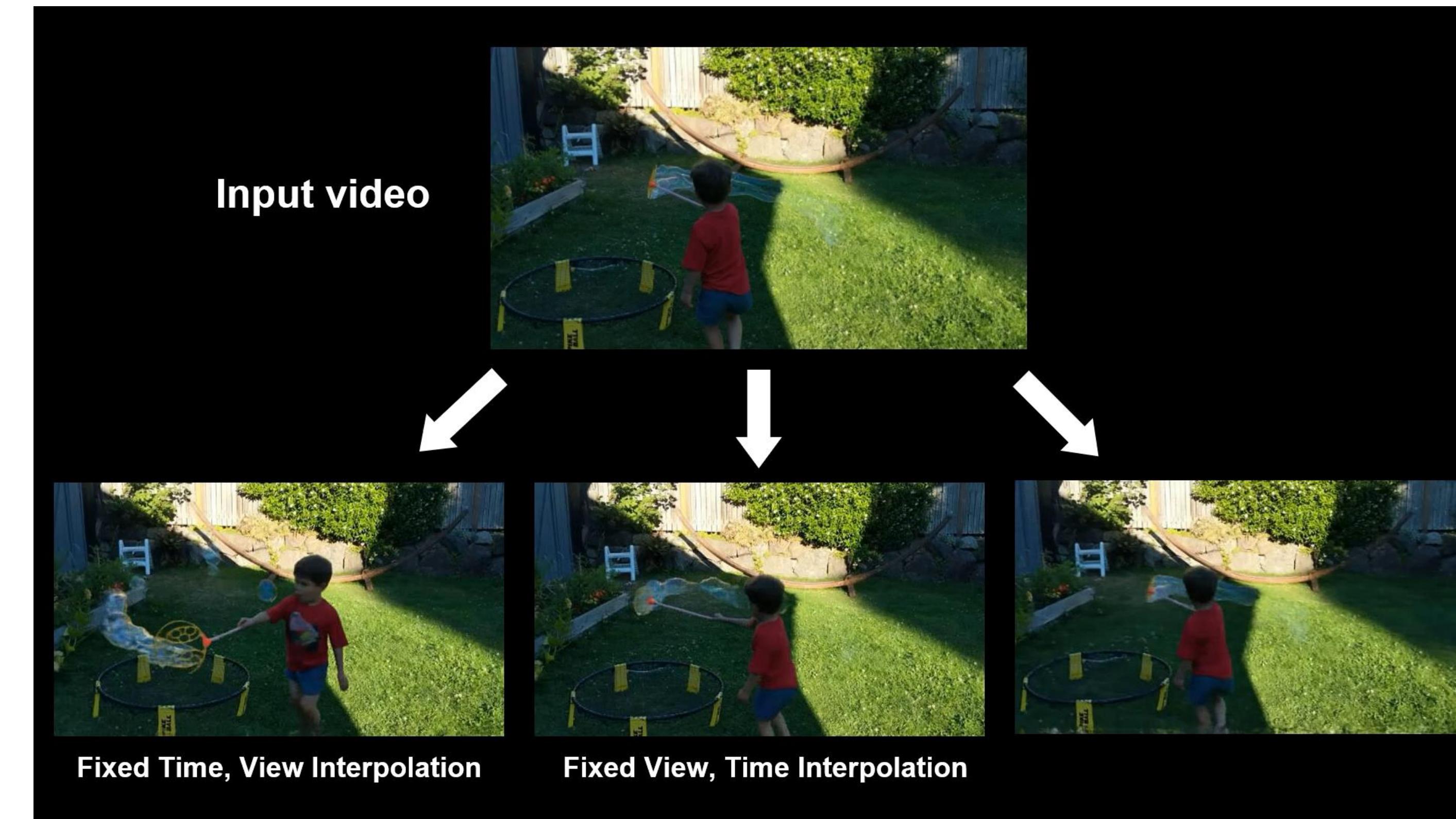
# Dynamic NeRFs



[Xian et al., CVPR 2021]

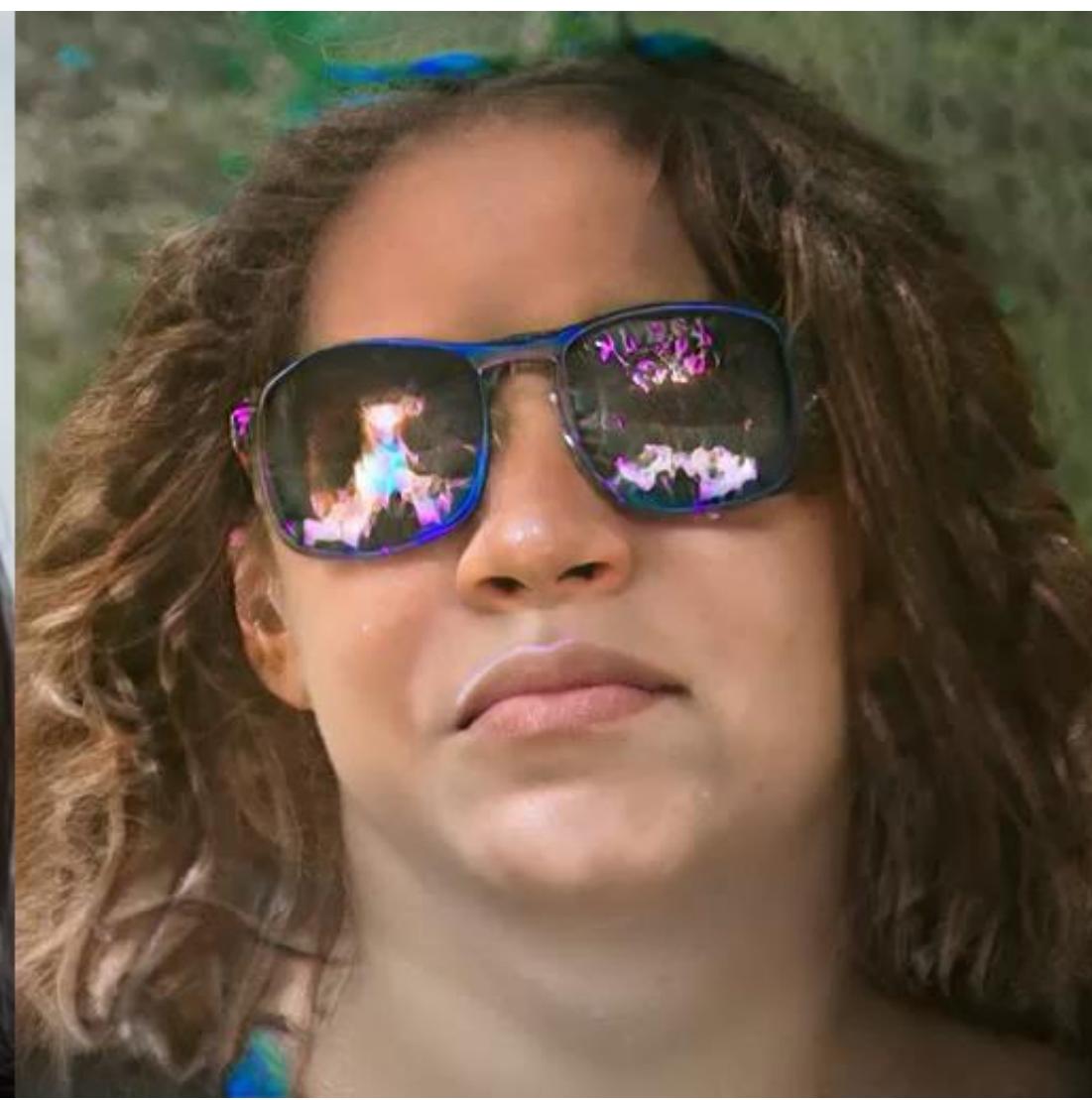


HyperNeRF [Park et al., SigAsia 2021]  
Nerfies [Park et al., ICCV 2021]



NSFF [Li et al., CVPR 2021]

# Generative 3D Faces



EG3D: Efficient Geometry-aware 3D Generative Adversarial Networks, Chan et al. CVPR 2022



# City-Scale NeRFs

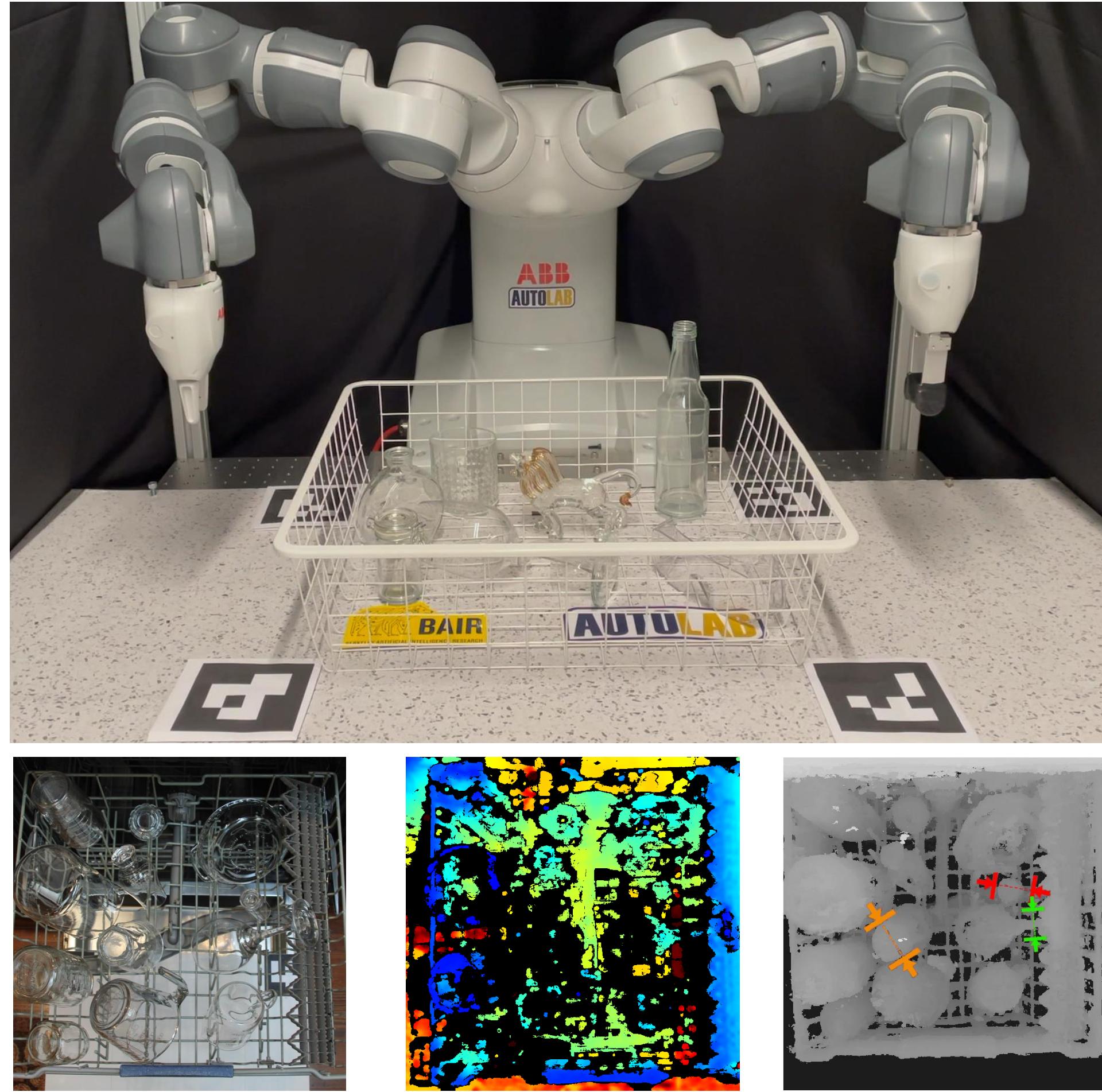


BlockNeRF  
[Tancik et al.  
CVPR 2022]

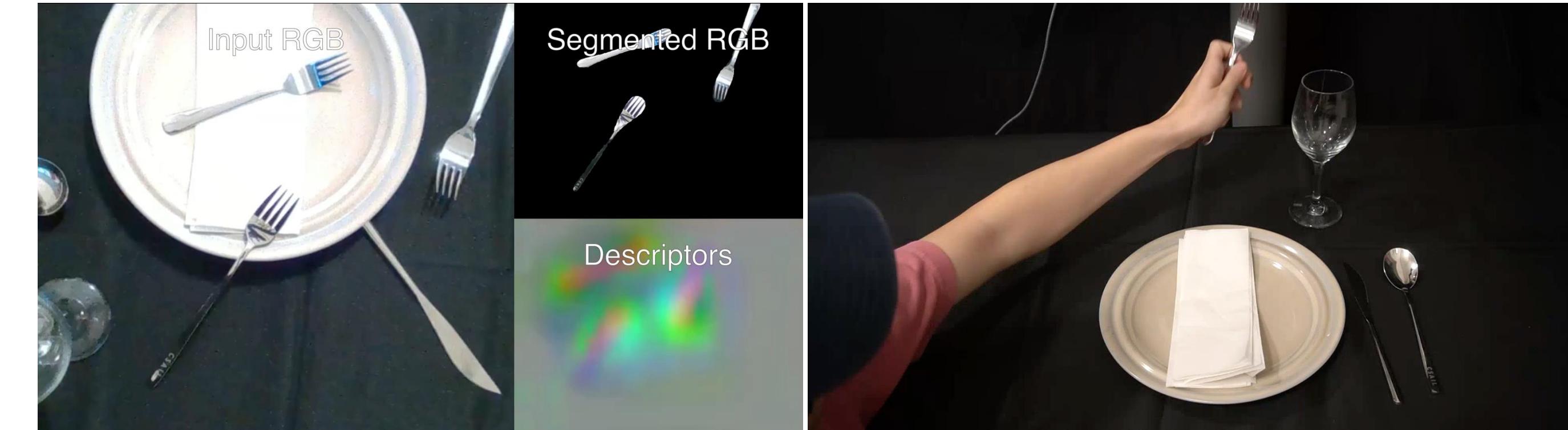


RawNeRF  
[Mildenhall et al.  
CVPR 2022]

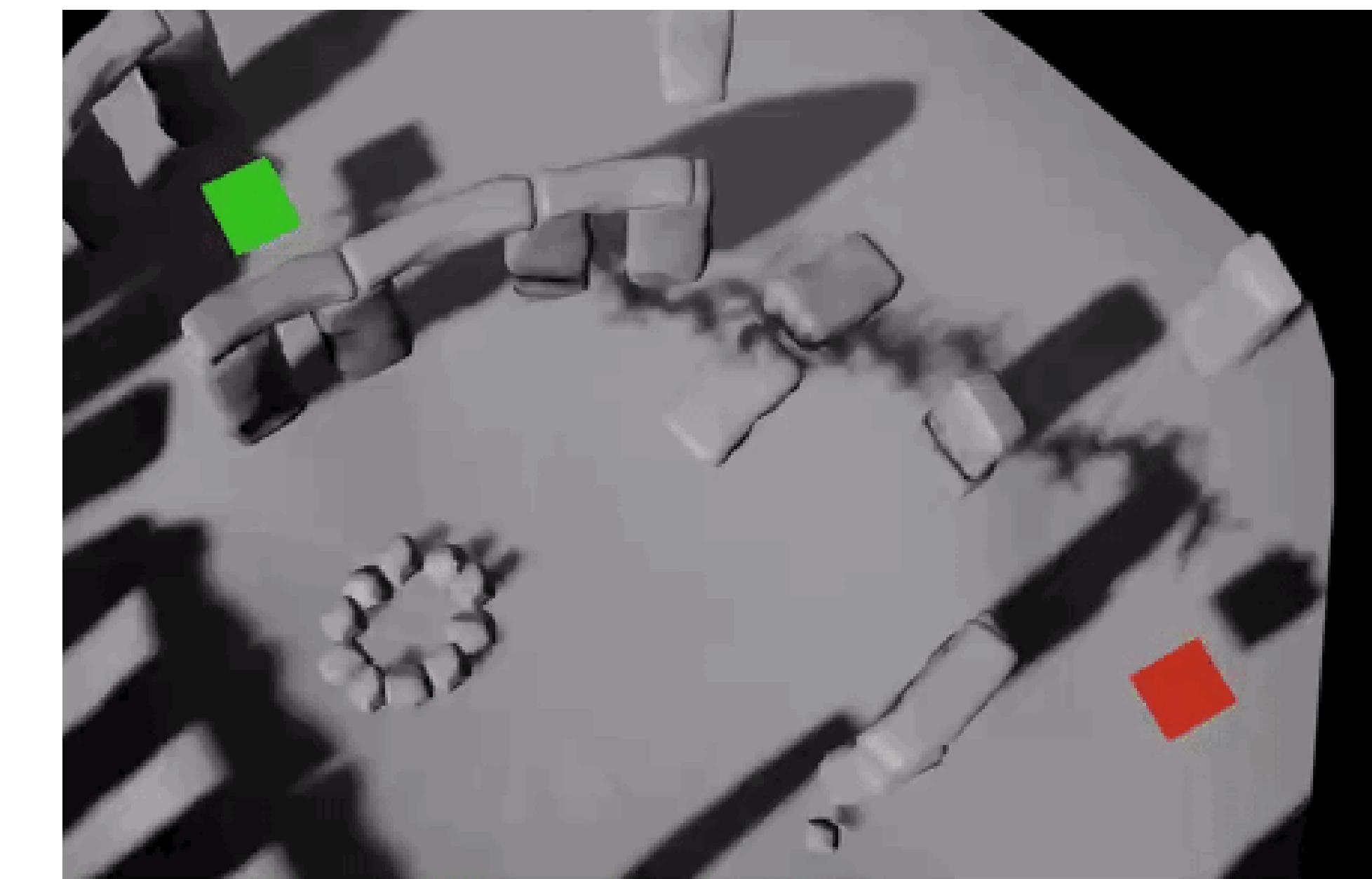
# Robotics



Dex-NeRF: Using a Neural Radiance field to Grasp Transparent Objects, [Ichnowski and Avigal et al. CoRL 2021]



NeRF-Supervision: Learning Dense Object Descriptors from Neural Radiance Fields, [Yen-Chen et al. ICRA 2022]



Vision-Only Robot Navigation in a Neural Radiance World [Adamkiewicz and Chen et al. ICRA 2022]

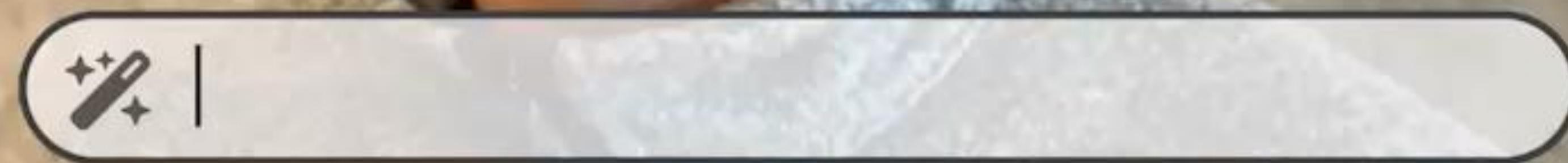
# Generating 3D scenes with diffusion models



# Querying with Language



# Editing with Instructions



# Goals of the next few lectures

- Visit the fundamentals in Neural Volumetric Rendering by abstracting away recent developments
- Provide first principles + background for you to go and read these papers & play around with the tools
- New Project 5!! Implement these concepts yourself



 nerfstudio

Capture of UC Berkeley redwoods with

# Birds Eye View & Background

# Birds Eye View

- What is NeRF?
- How is it different or similar to existing approaches?
- What is its historical context?

# Problem Statement

**Input:**

A set of calibrated Images



**Output:**

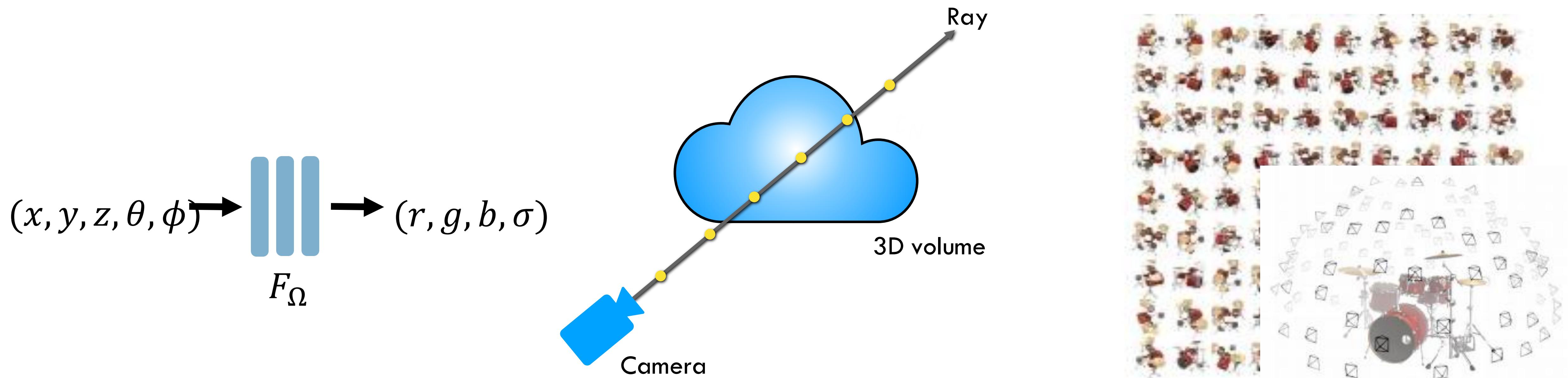
A 3D scene representation that  
renders novel views





# Three Key Components

Objective: Synthesize  
all training views

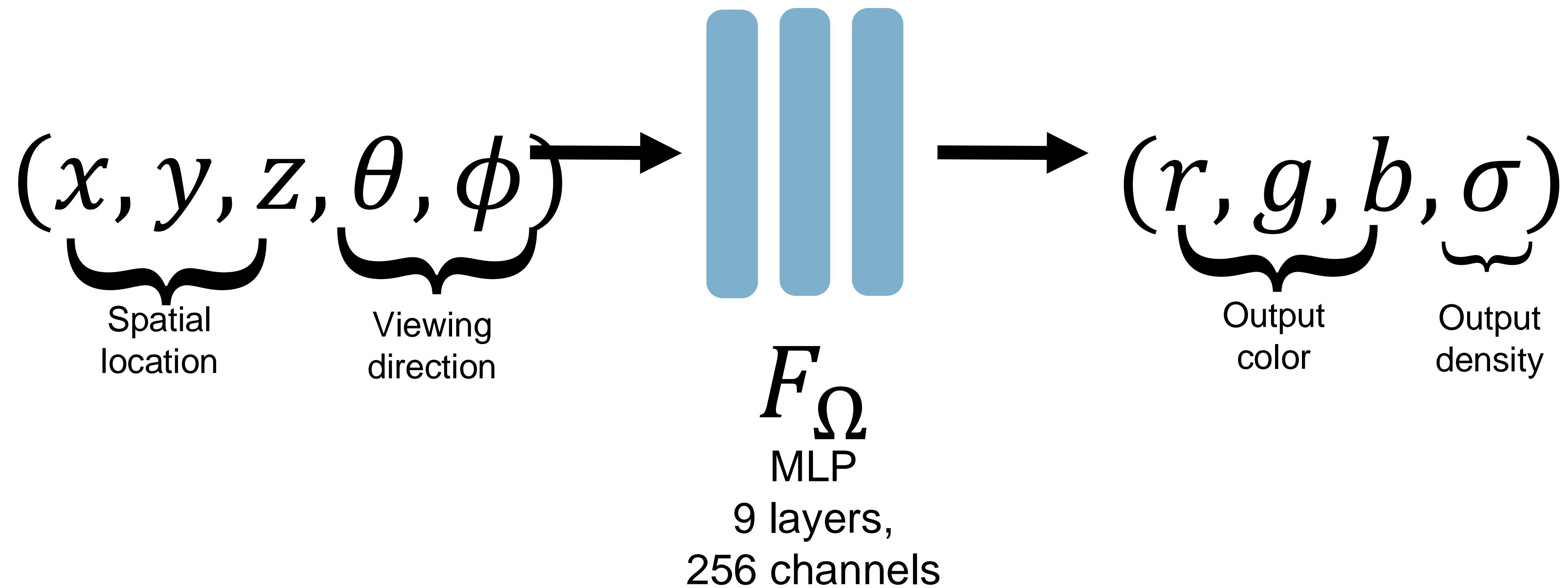


Neural Volumetric 3D  
Scene Representation

Differentiable Volumetric  
Rendering Function

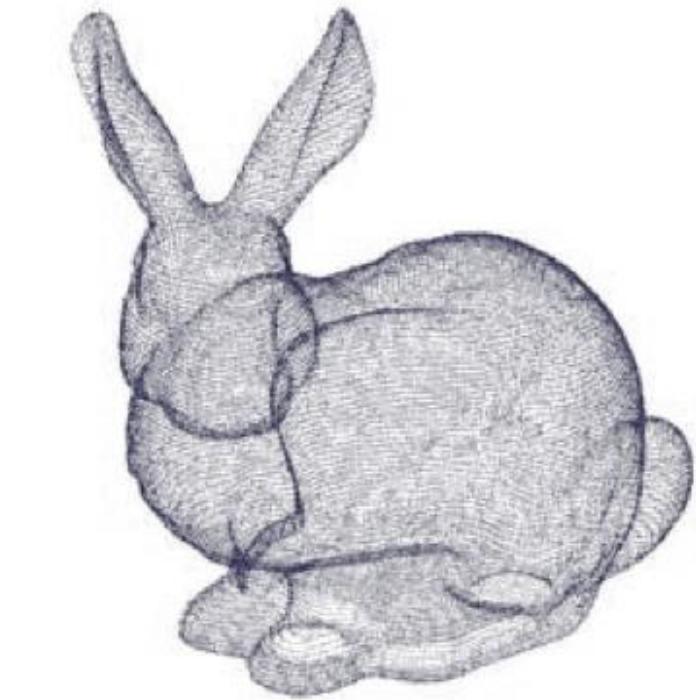
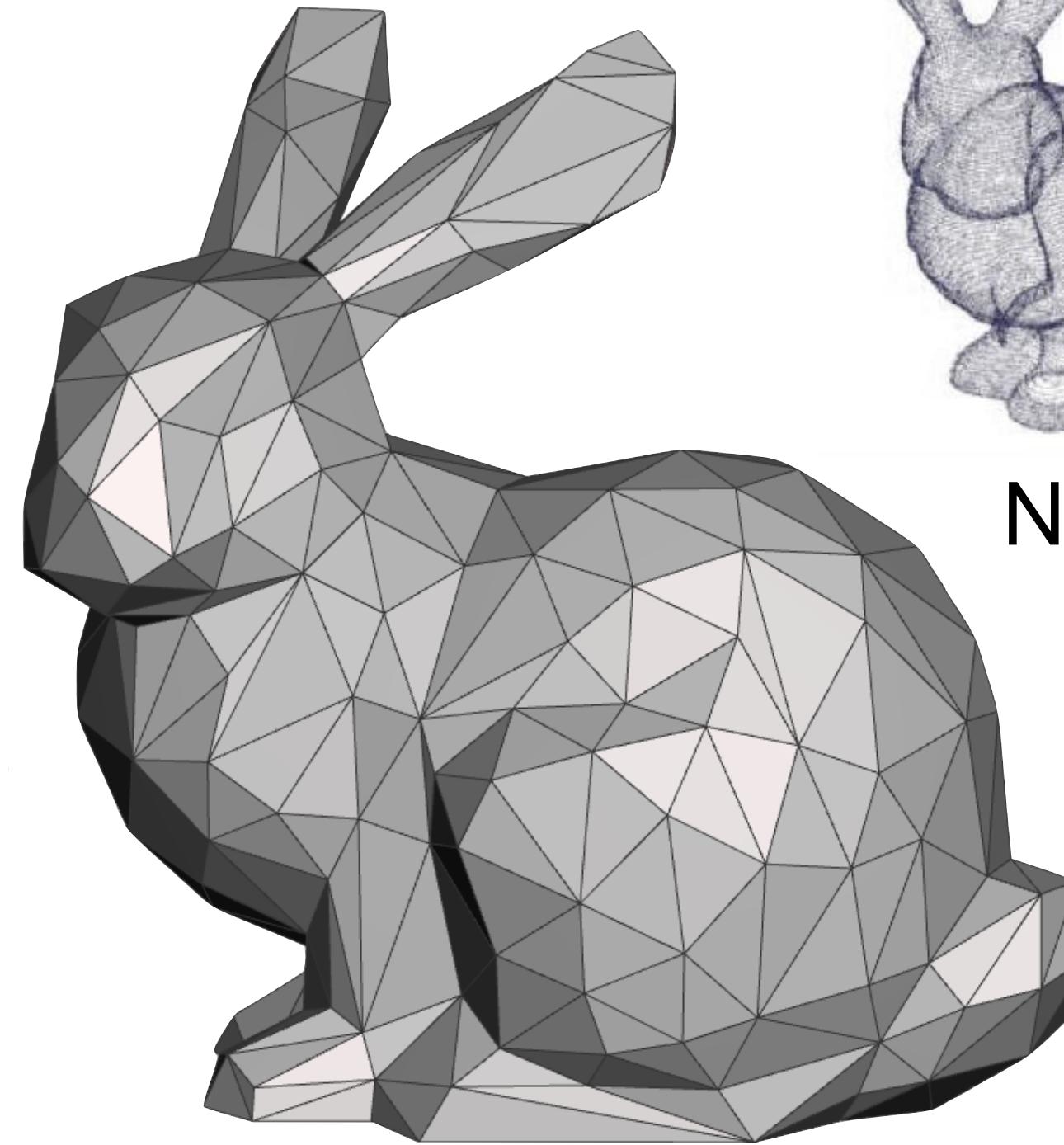
Optimization via  
Analysis-by-Synthesis

# Representing a 3D scene as a continuous 5D function



What kind of a 3D representation is this?

# It is not a Mesh



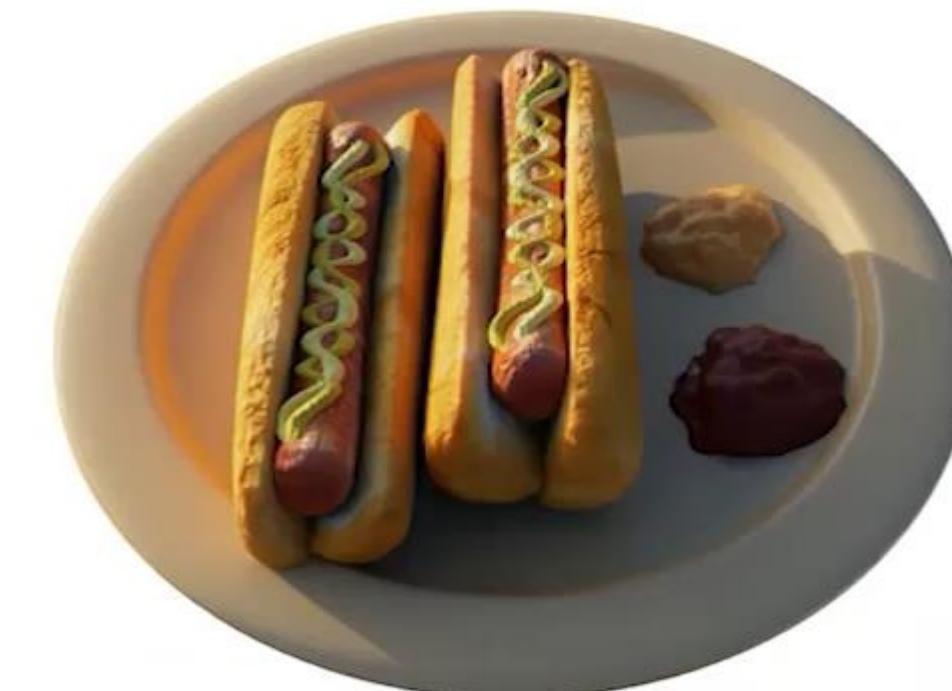
Not a point cloud  
either



## It is volumetric

It's *continuous* voxels made of shiny transparent cubes

# What is the problem that is being solved?



# Plenoptic Function

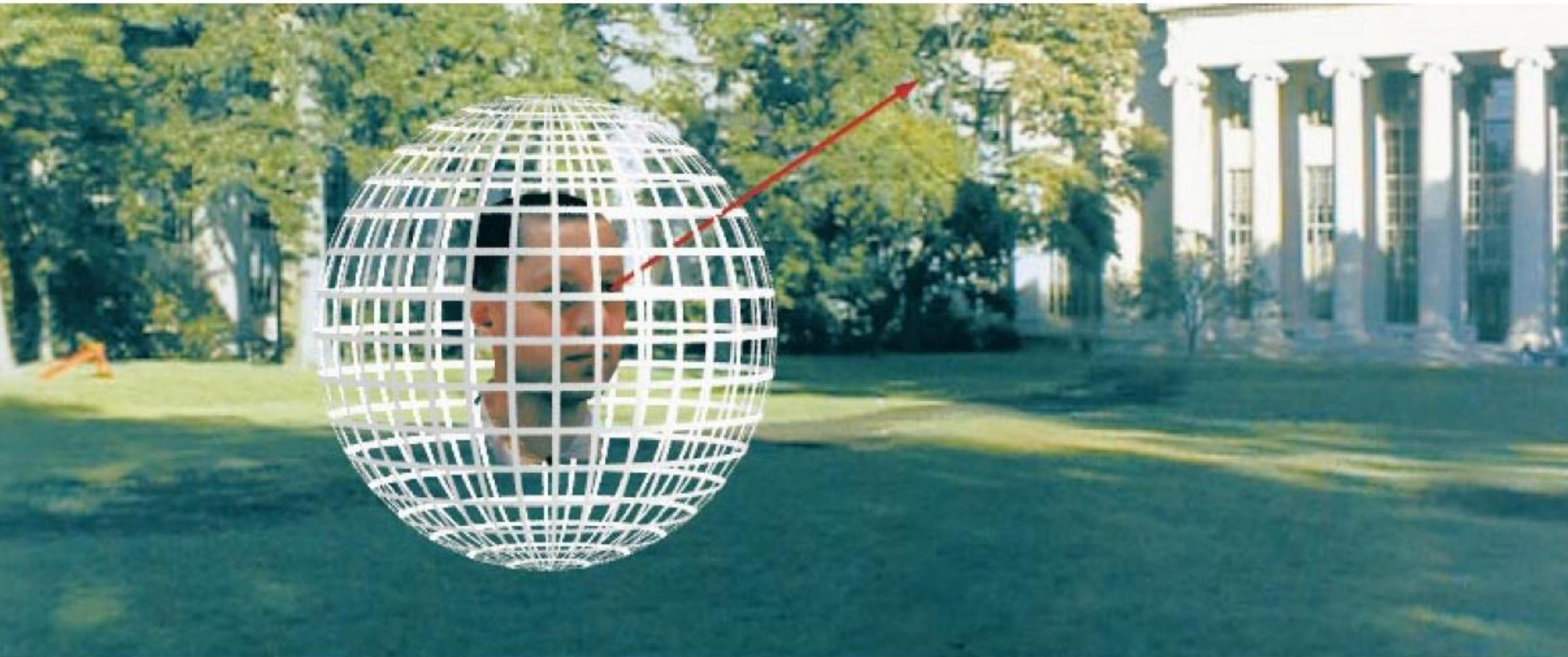
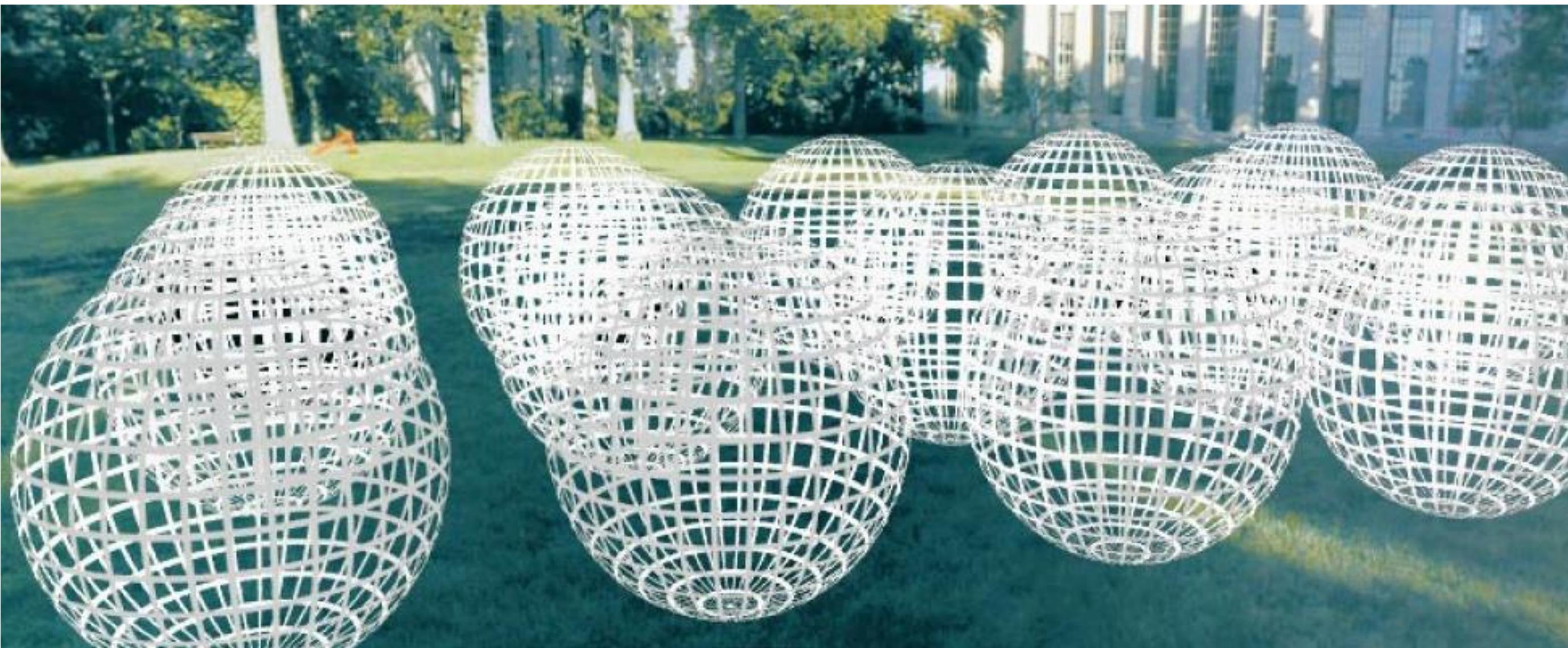


Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The Plenoptic Function (Adelson & Bergen '91)

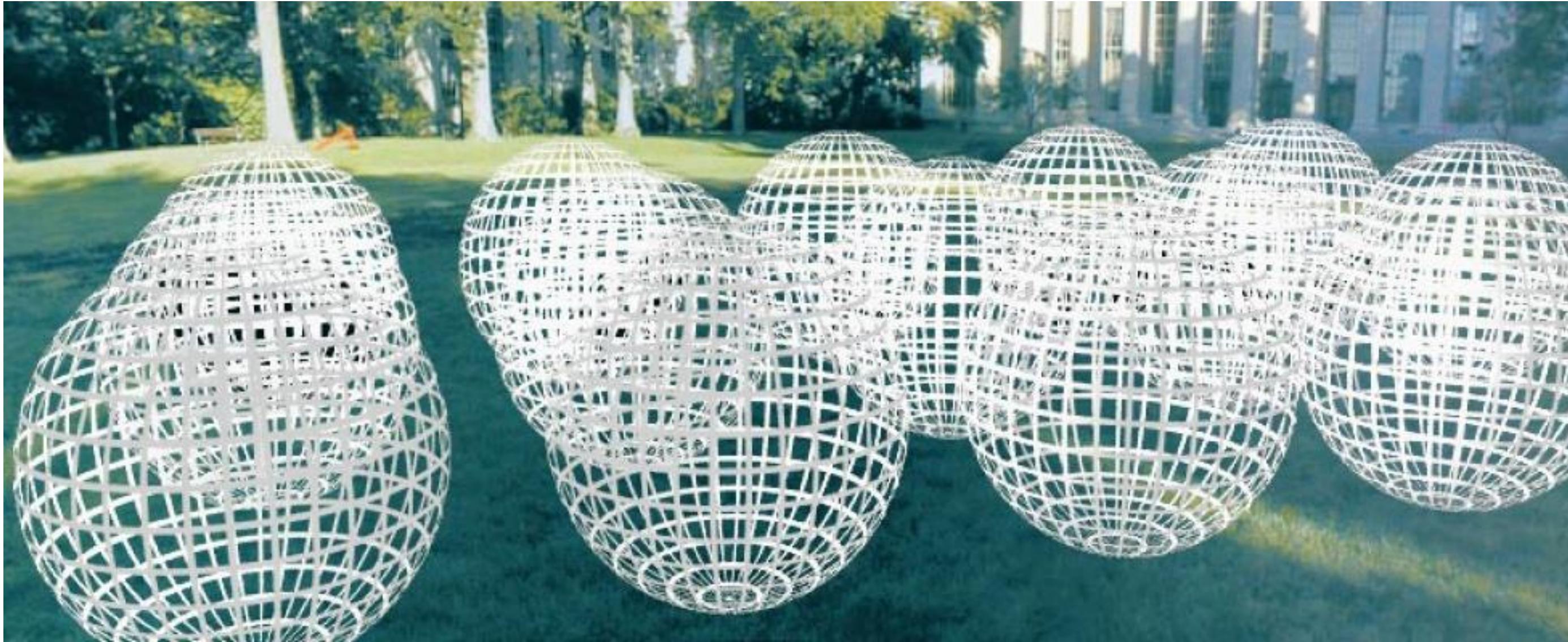
# A holographic movie



$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

- is intensity of light
  - Seen from ANY position and direction
  - Over time
  - As a function of wavelength

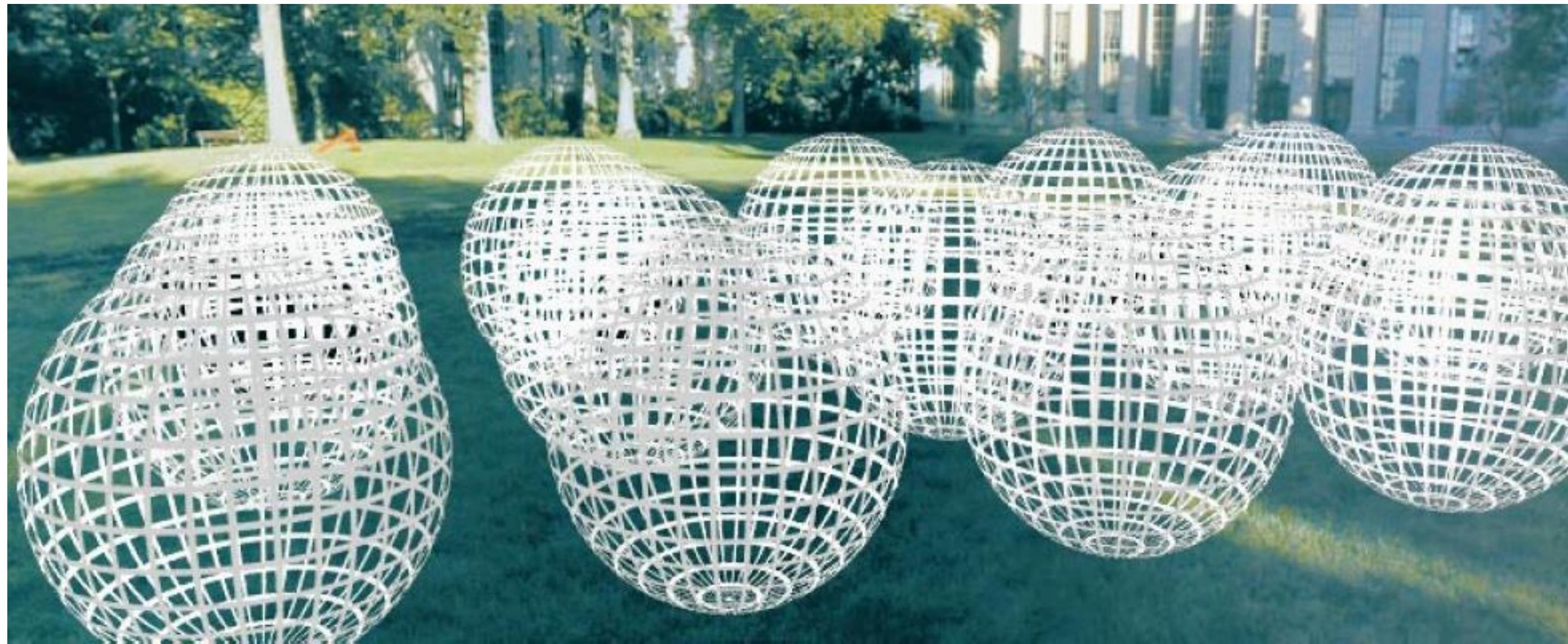
# The plenoptic function



$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

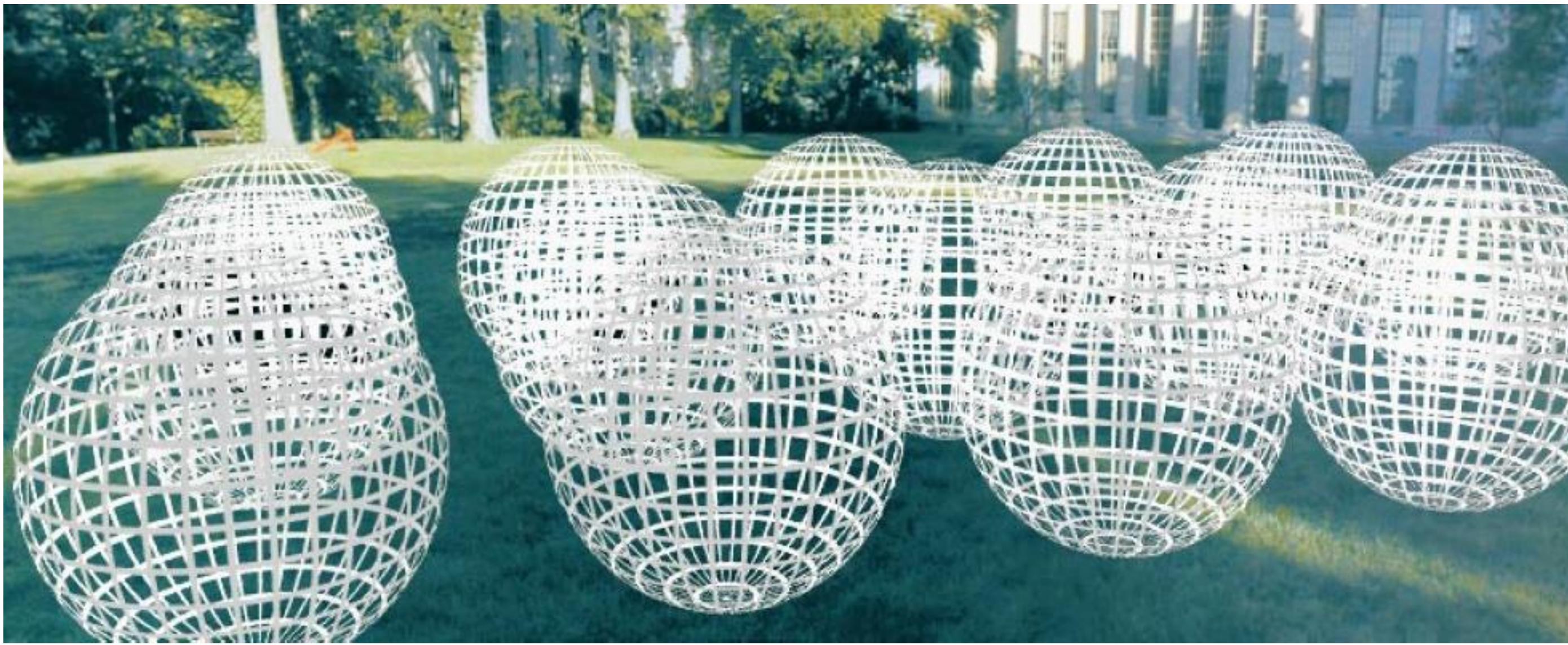
7D function, that can reconstruct every position & direction,  
at every moment, at every wavelength  
= it recreates the entirety of our visual reality!

# Goal: Plenoptic Function from a set of images



- Objective: Recreate the visual reality
- All about recovering photorealistic pixels, not about recording 3D point or surfaces
  - Image Based Rendering
  - aka **Novel View Synthesis**

# Goal: Plenoptic Function from a set of images

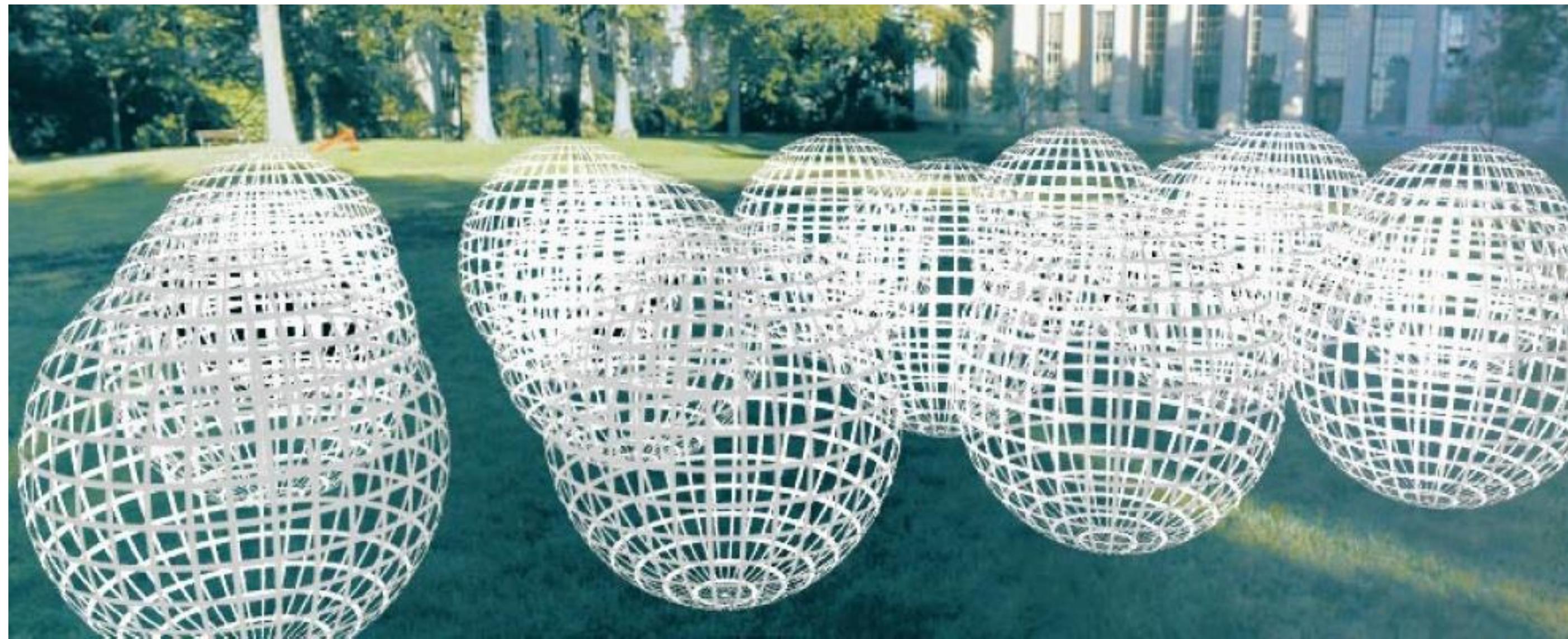


It is a conceptual device

Adelson & Bergen do not discuss how to solve this

# Plenoptic Function

7D function:  
2 – direction  
1 – wavelength  
1 – time  
3 – location



$$P(\theta, \phi, \cancel{\lambda}, \cancel{t}, V_x, V_y, V_z) \longrightarrow P(\theta, \phi, V_x, V_y, V_z)$$

Look familiar  
😊?

Let's simplify:

1. Remove the time
2. Remove the wavelength & let the function output RGB colors

# Lightfield / Lumigraph

- Previous approaches for modeling the Plenoptic Function
- Take a lot of pictures from many views
- Interpolate the rays to render a novel view



Stanford Gantry  
128 cameras



Lytro camera

# Lightfield / Lumigraph

- Previous approaches for modeling the Plenoptic Function
- Take a lot of pictures from many views
- Interpolate the rays to render a novel view



**Stanford Gantry**  
**128 cameras**



**Lytro camera**

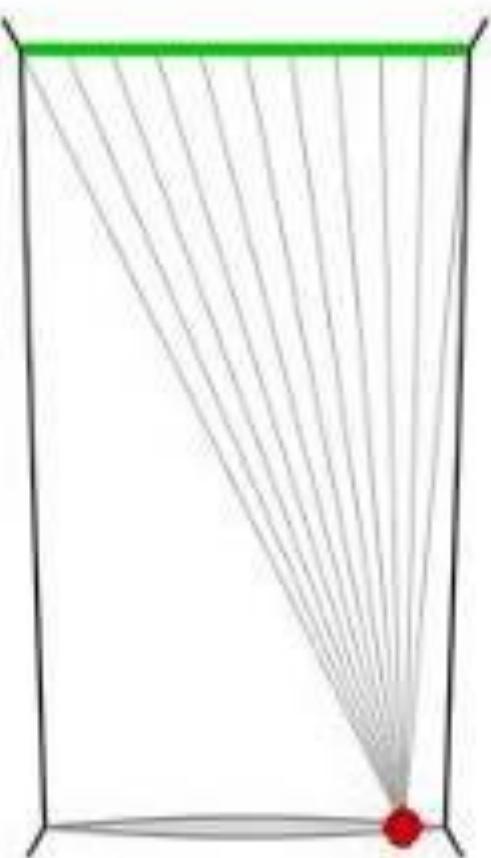
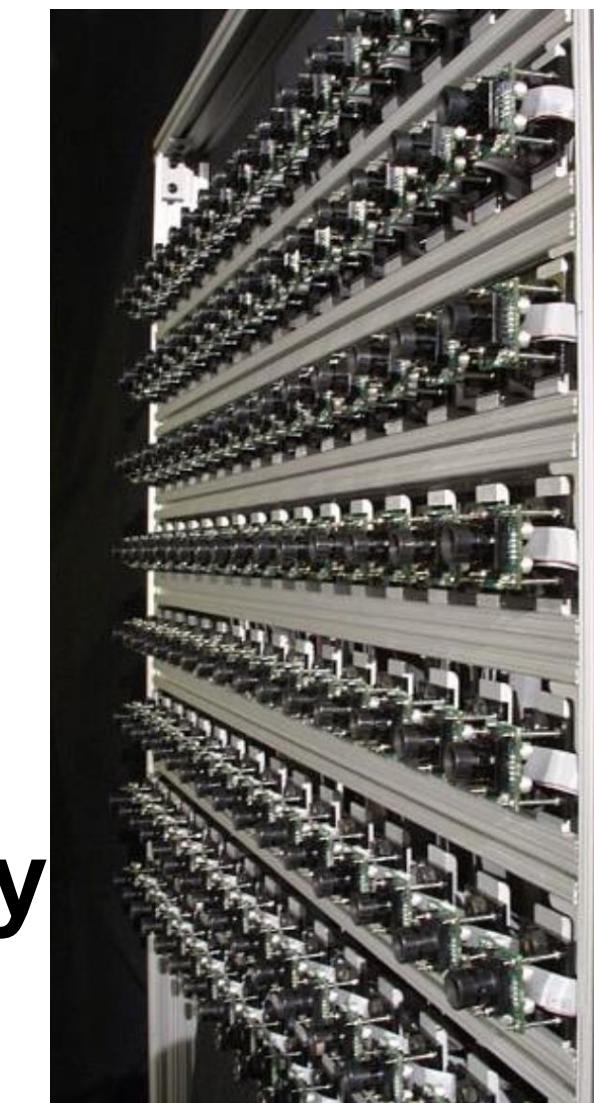
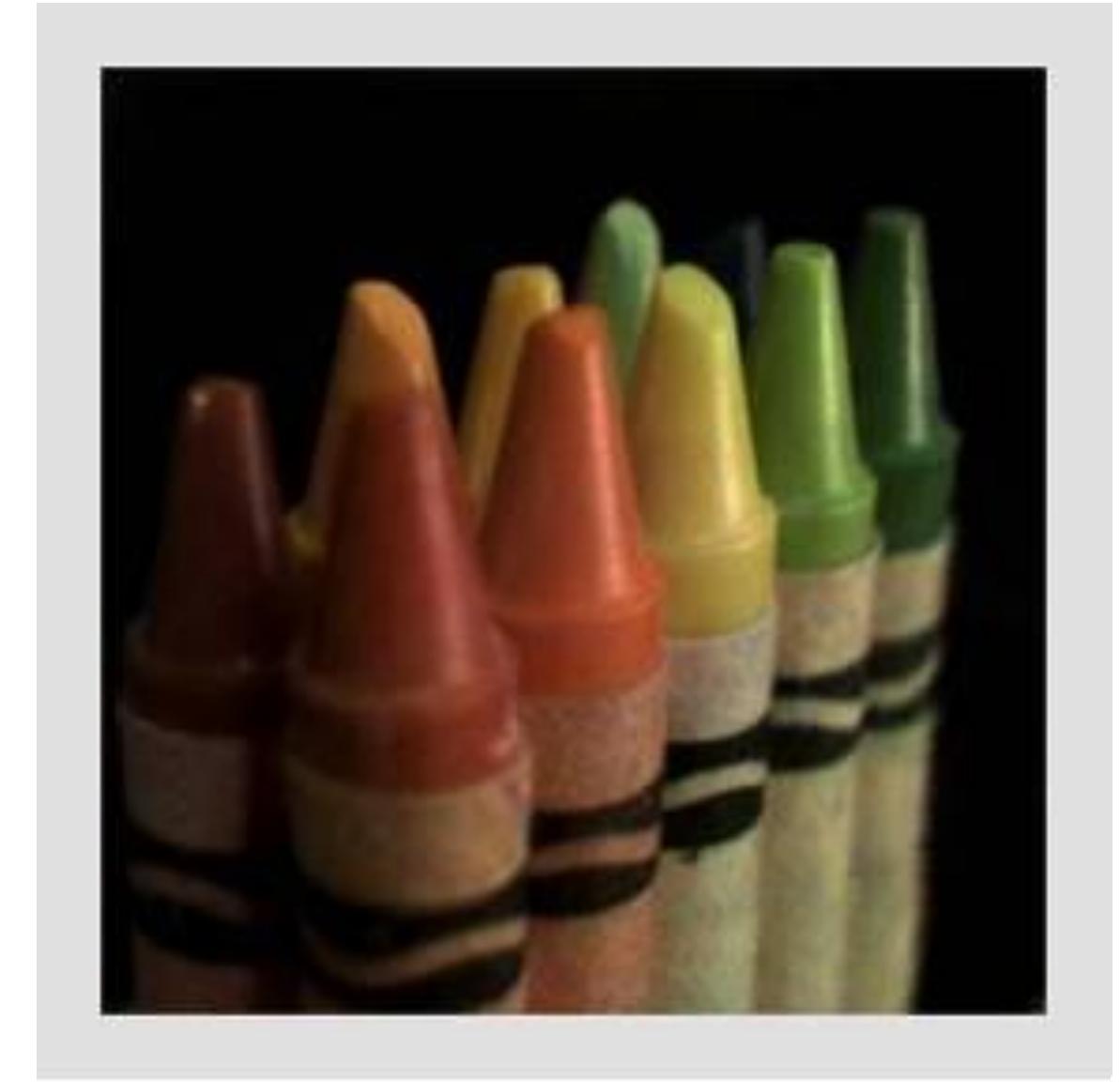


Figure from Marc Levoy

# Lightfield / Lumigraph

- Previous approaches for modeling the Plenoptic Function
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Stanford Gantry  
128 cameras



Lytro camera

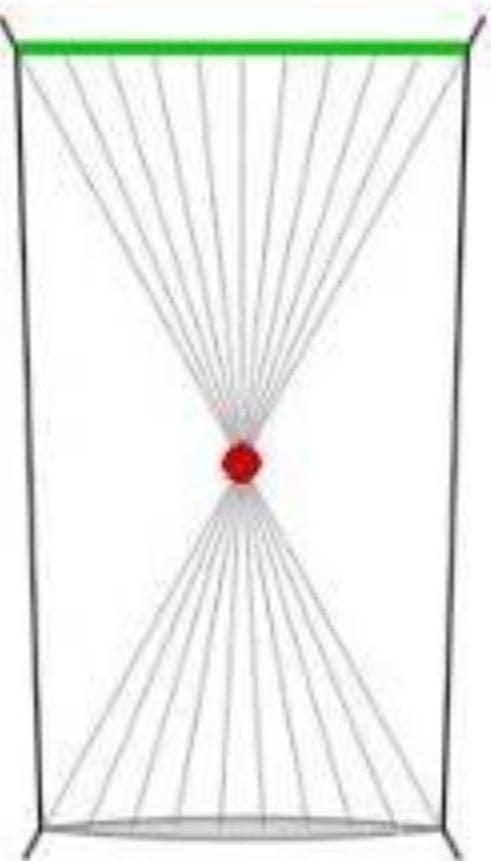
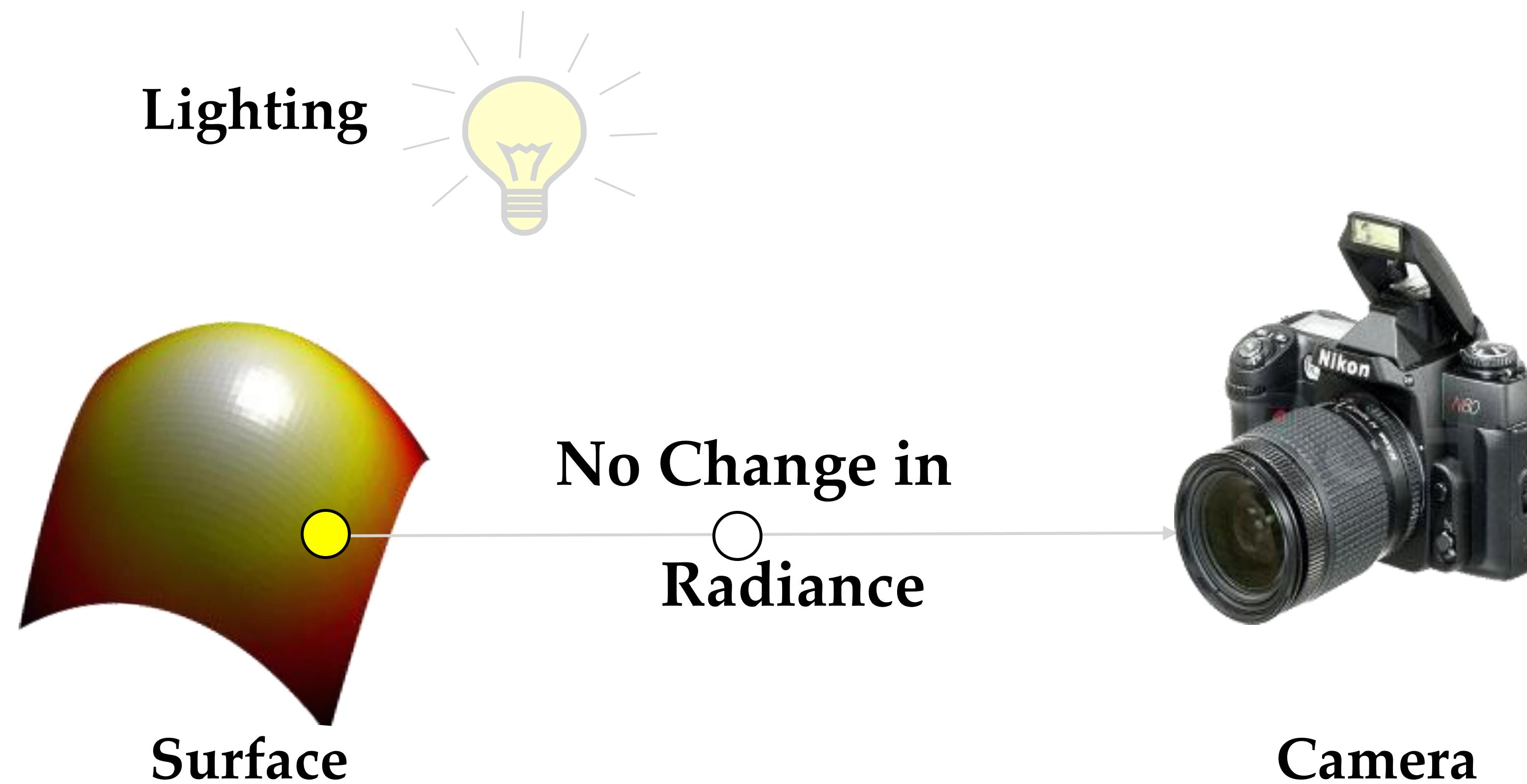


Figure from Marc Levoy

# Big Assumption: a ray does not change color



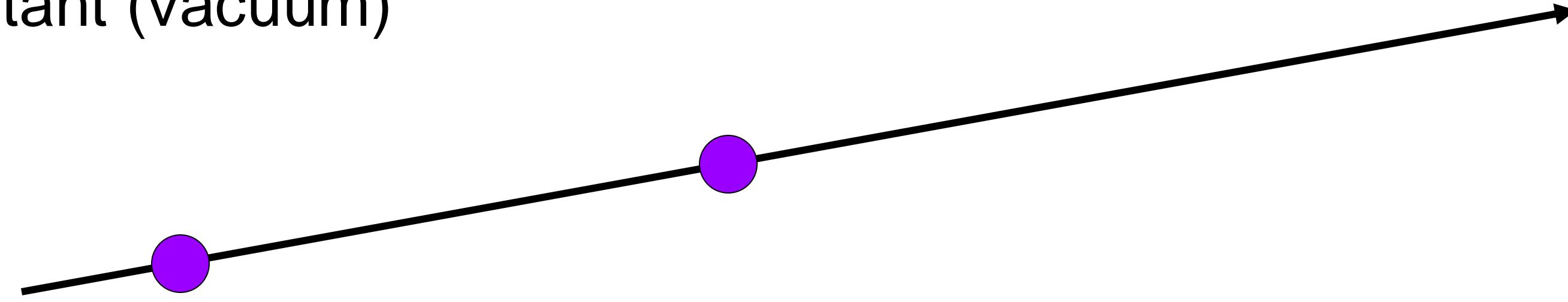
True if there is no occlusion or fog

# With this assumption: Ray Reuse

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## Infinite line

- Assume light is constant (vacuum)



## The 5D function

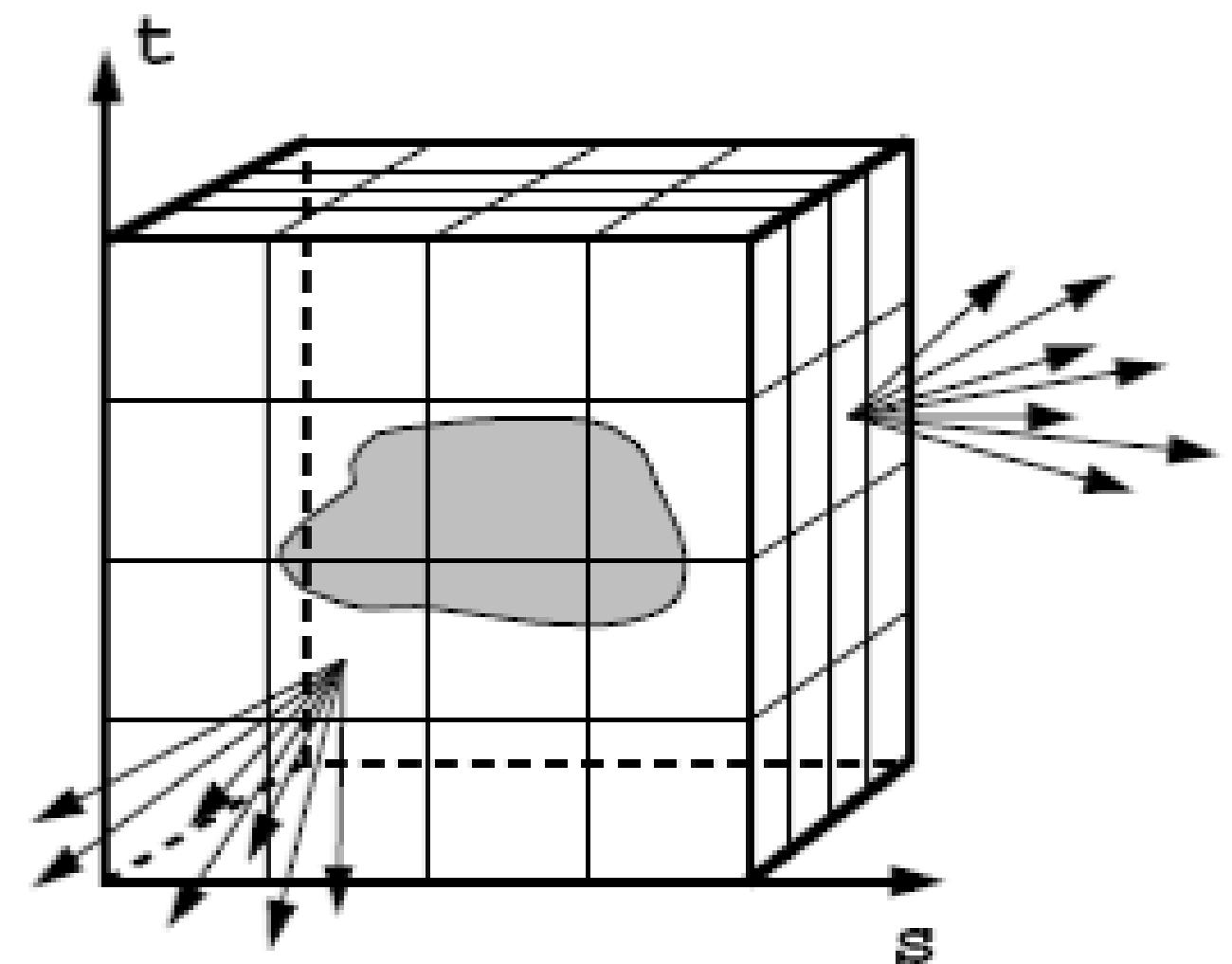
- 3D position
- 2D direction

## is now 4D

- 2D direction
- 2D position
- non-dispersive medium

# Ray Reuse Assumption

Because of this it only models the plenoptic surface:

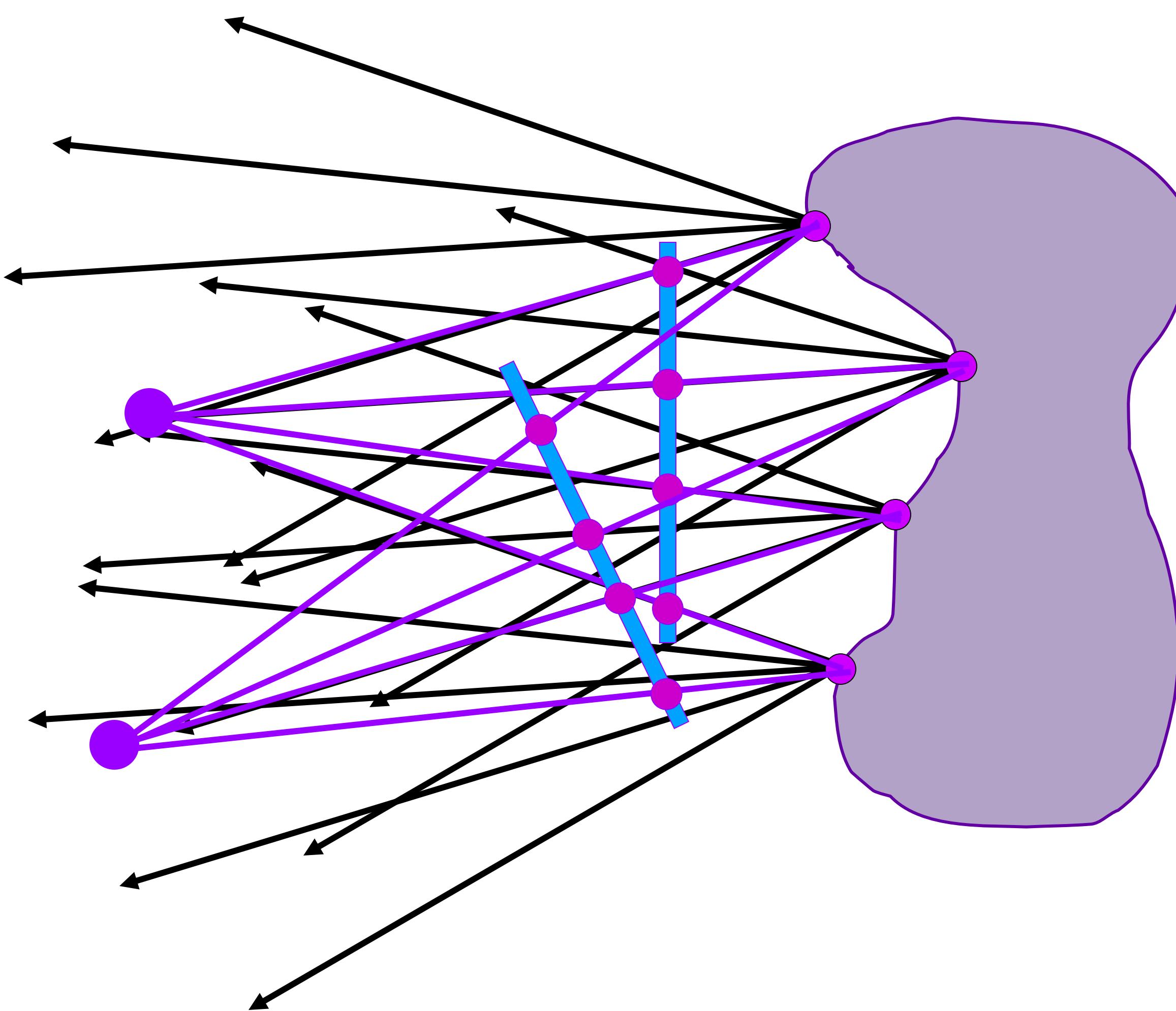


It's like



Figure 1: The surface of a cube holds all the radiance information due to the enclosed object.

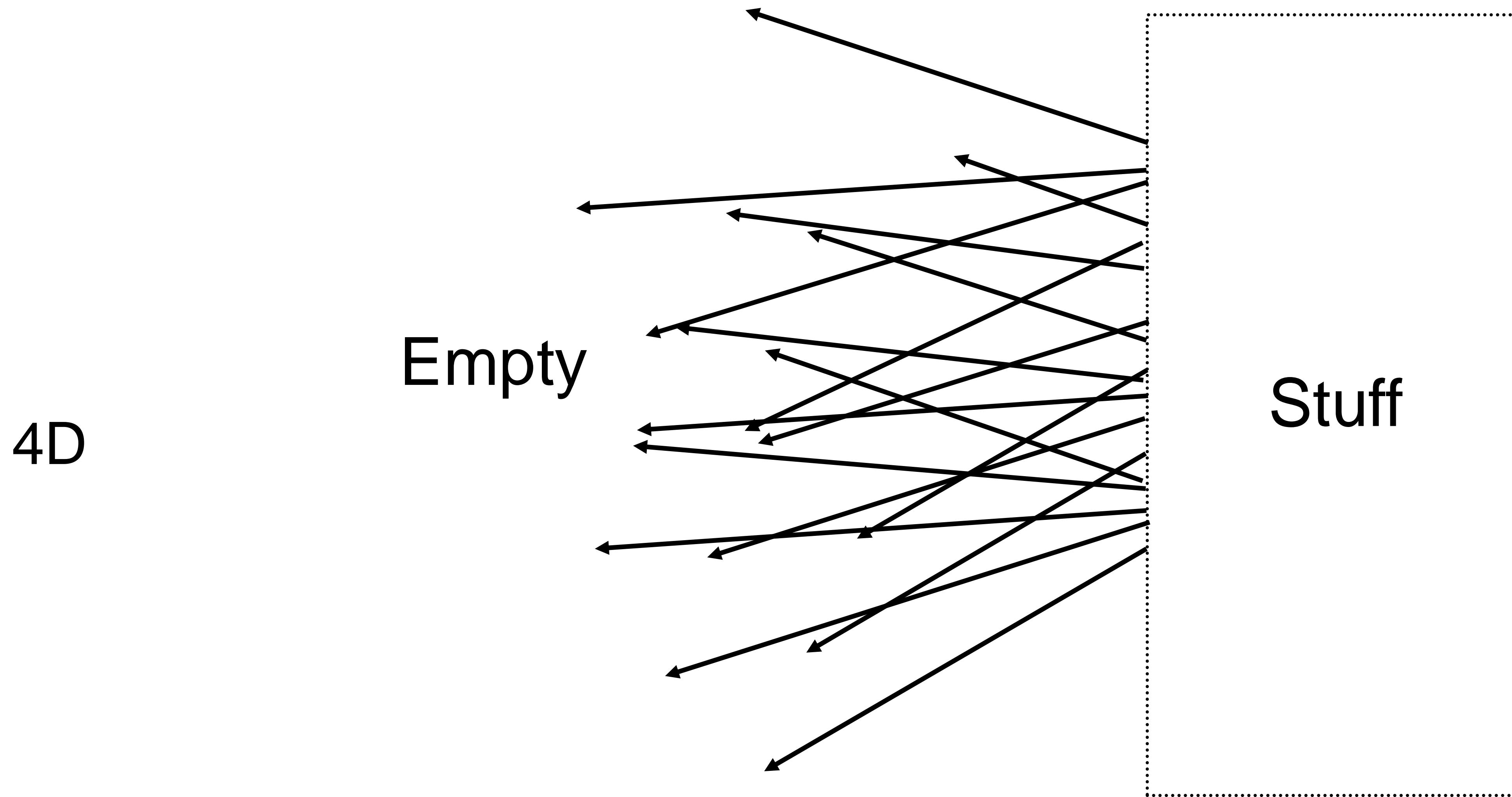
# Synthesizing novel views



# Lumigraph / Lightfield

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Outside convex space

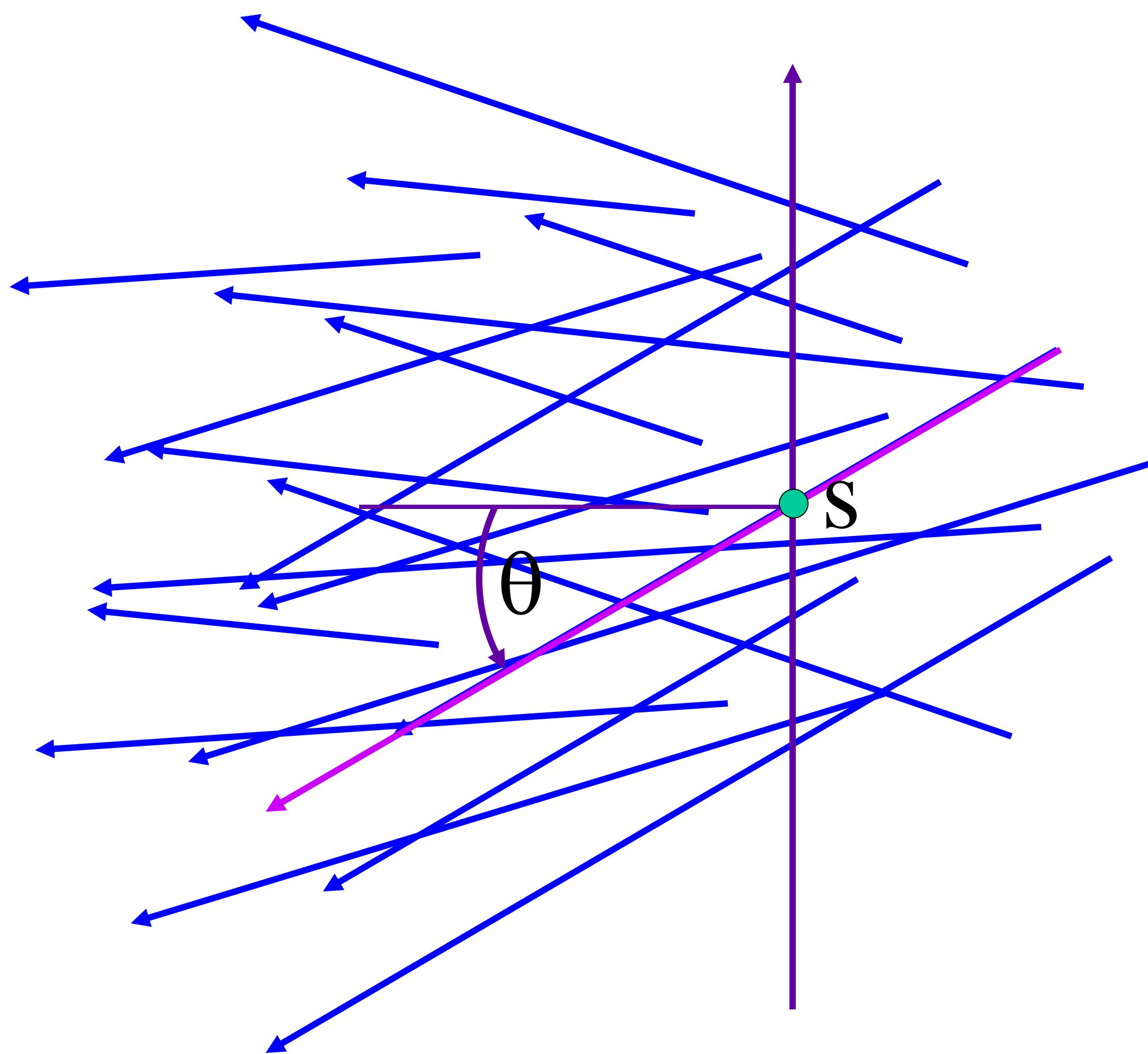


# Lumigraph - Organization

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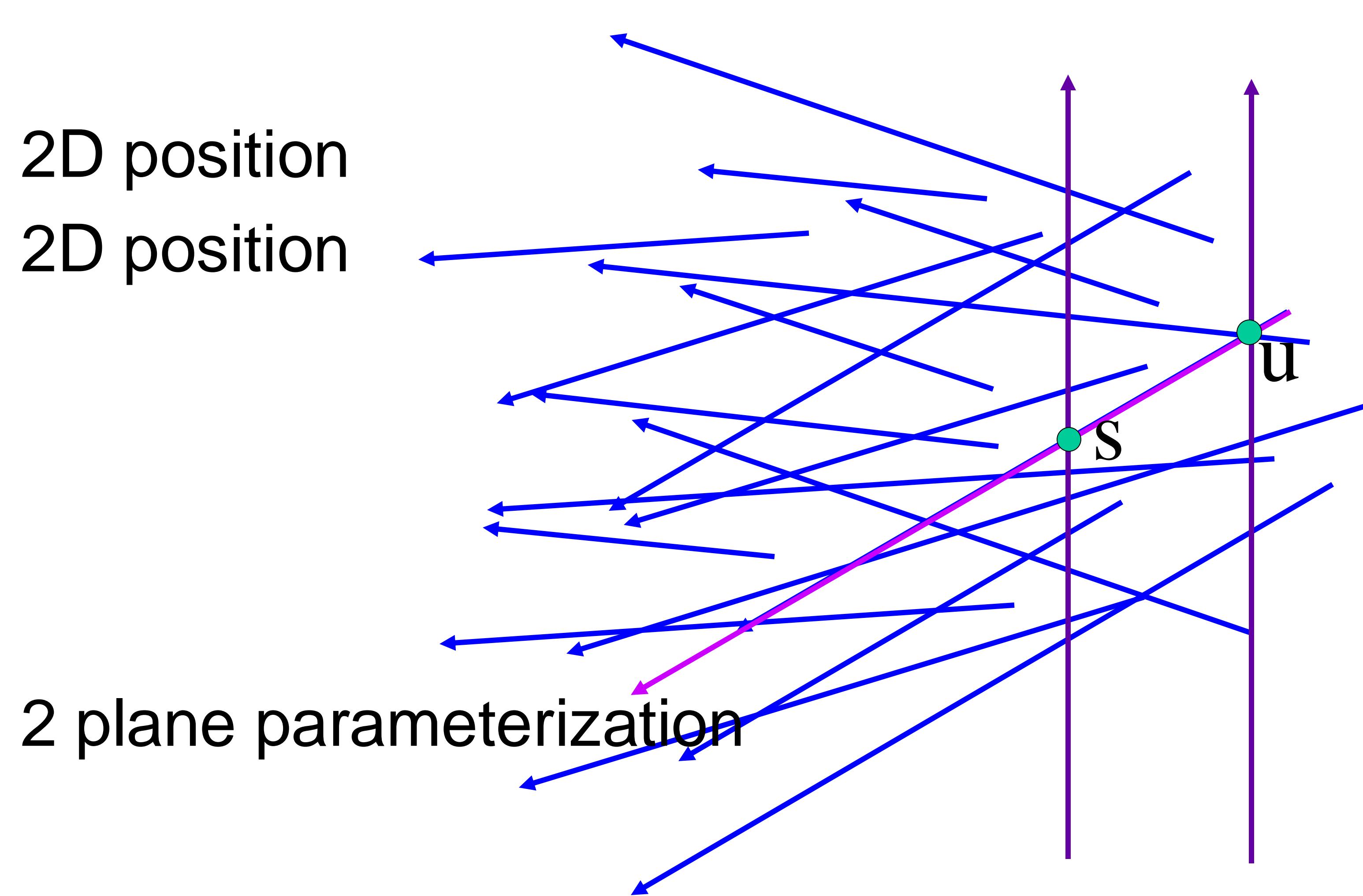
2D position

2D direction



# Lumigraph - Organization

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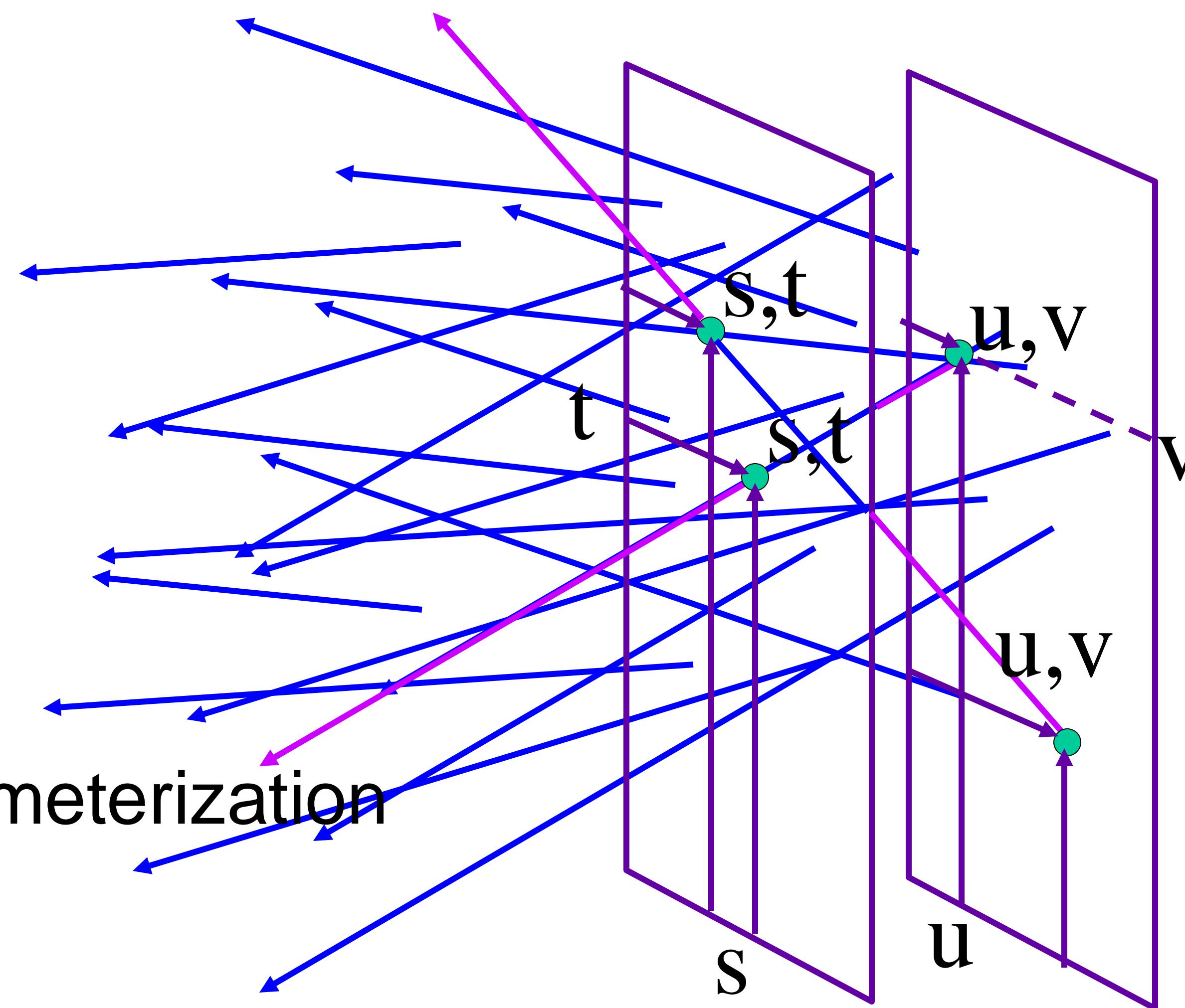
# Lumigraph - Organization

---

2D position

2D position

2 plane parameterization



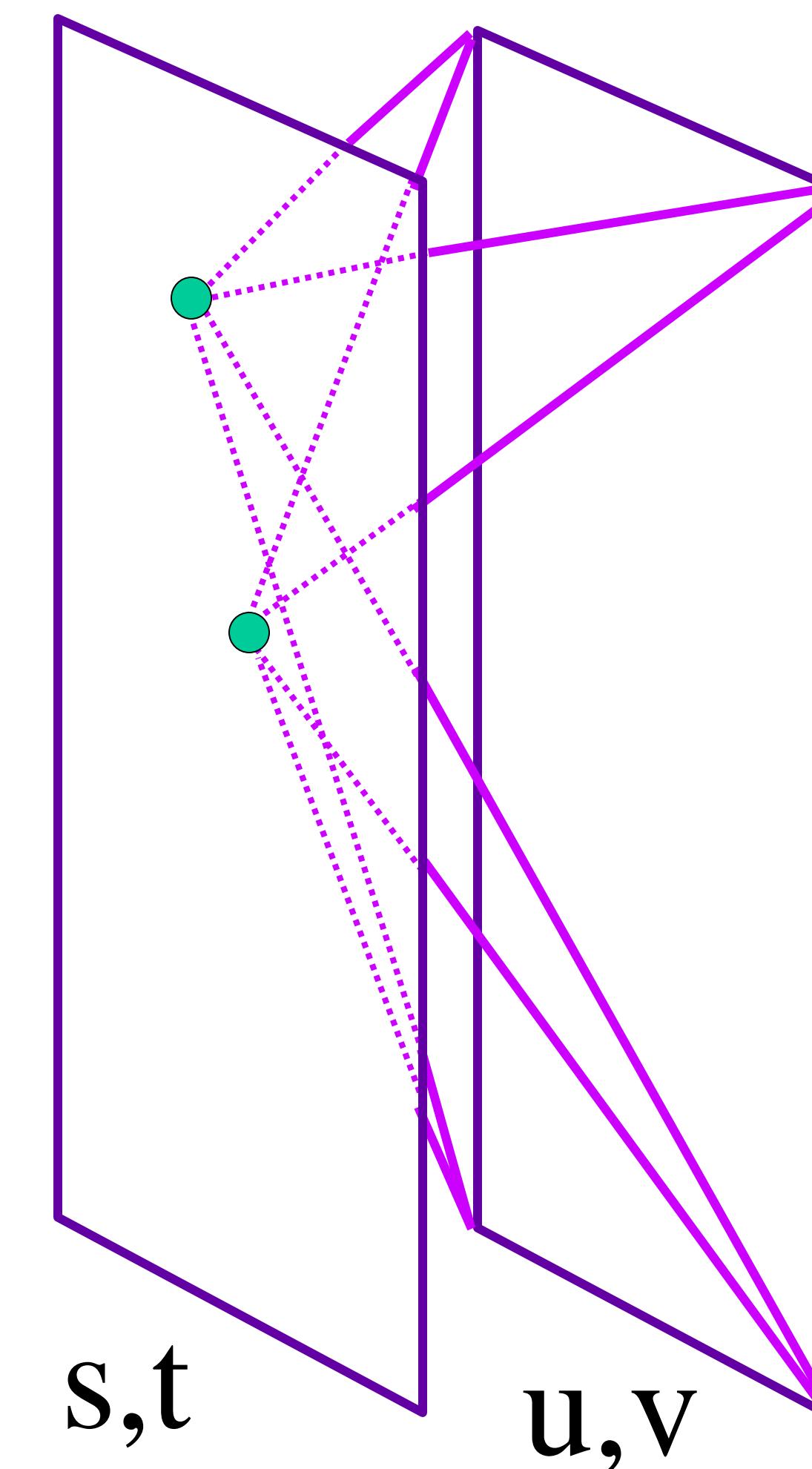
# Lumigraph - Organization

---

Hold  $s, t$  constant

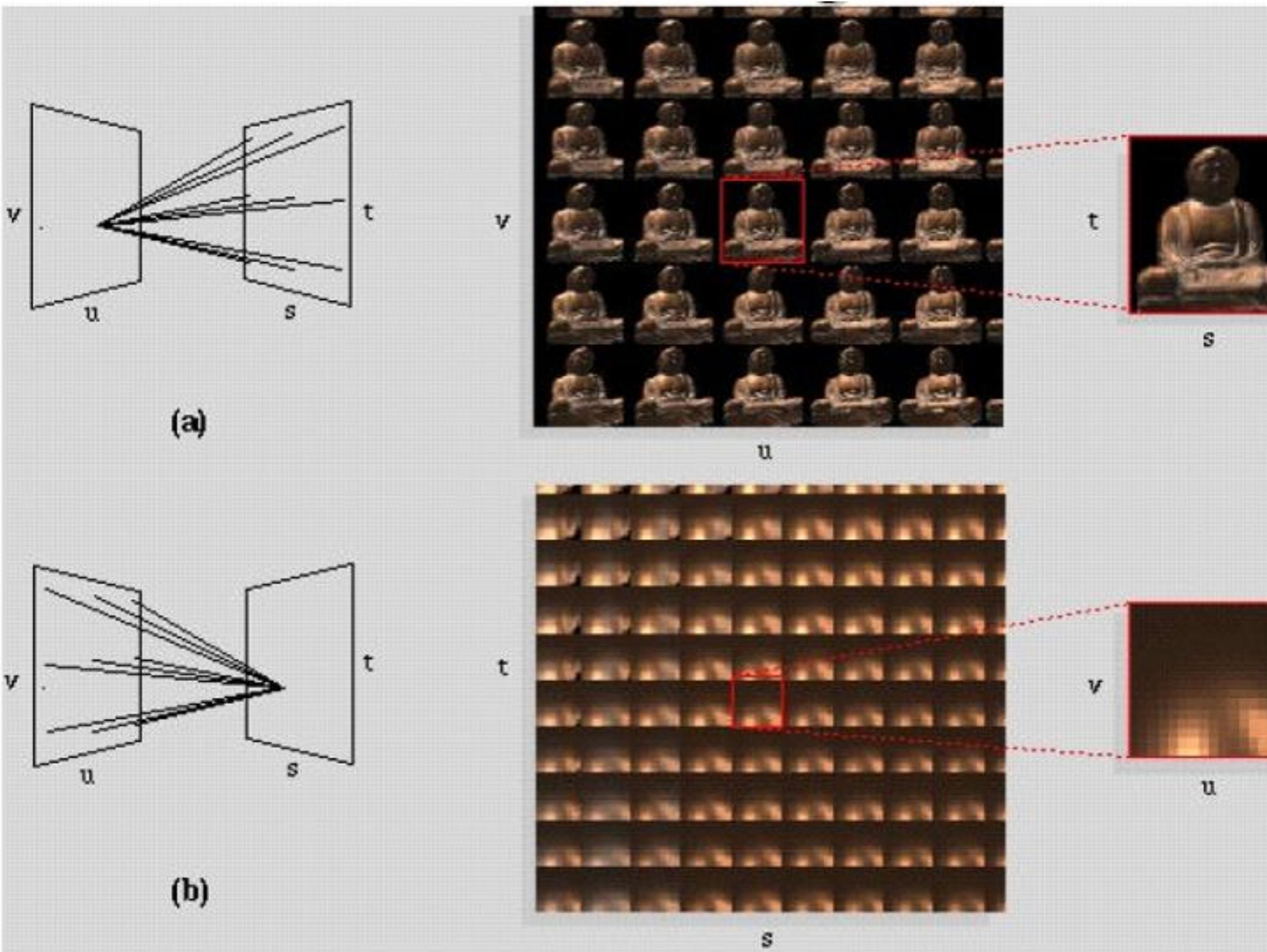
Let  $u, v$  vary

An image



# Lumigraph / Lightfield

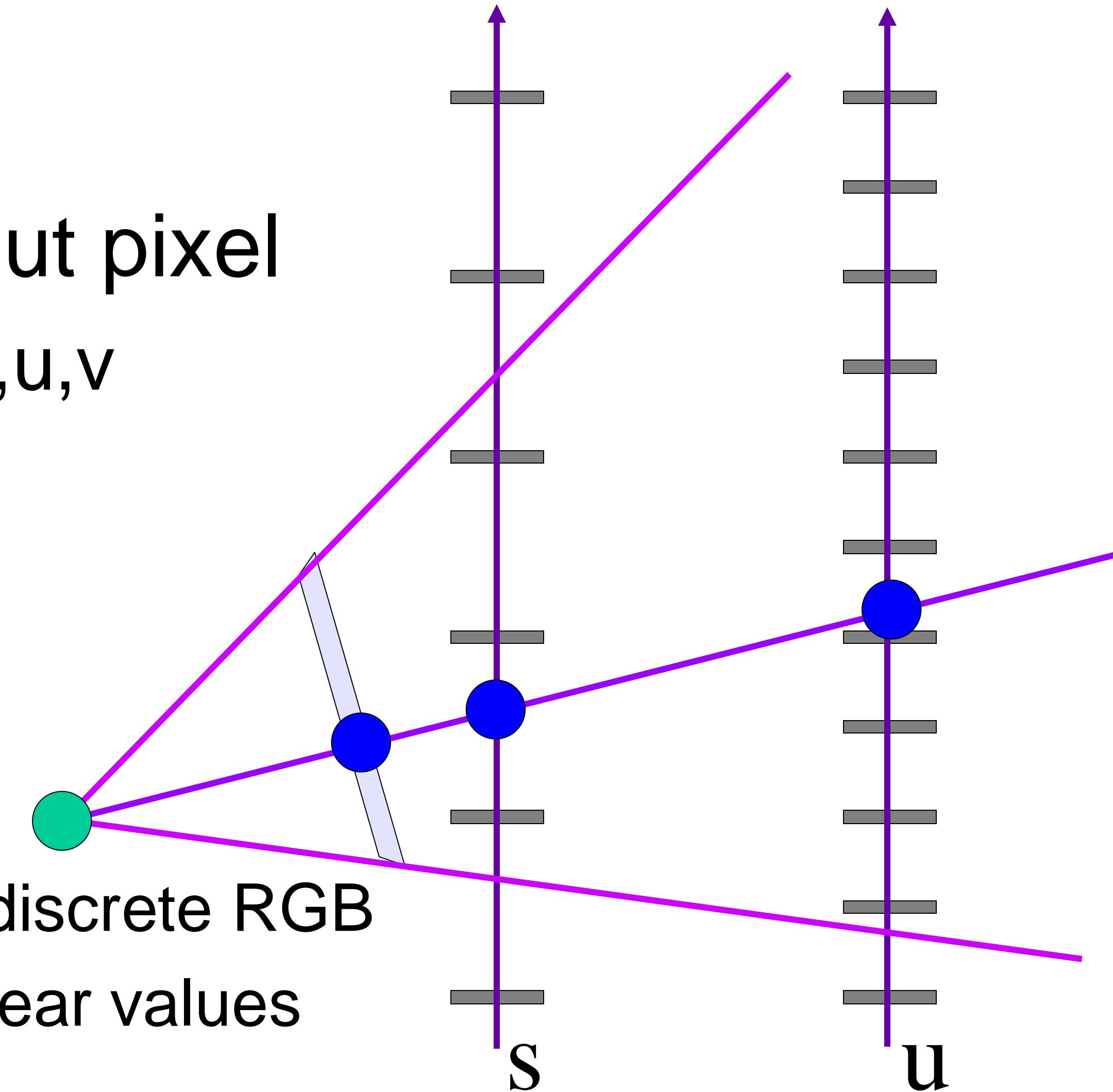
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# Novel View Synthesis

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- For each output pixel
  - determine  $s, t, u, v$
  - either
    - use closest discrete RGB
    - interpolate near values



# How NeRF models the Plenoptic Function

$$P(\theta, \phi, V_x, V_y, V_z)$$

Look familiar

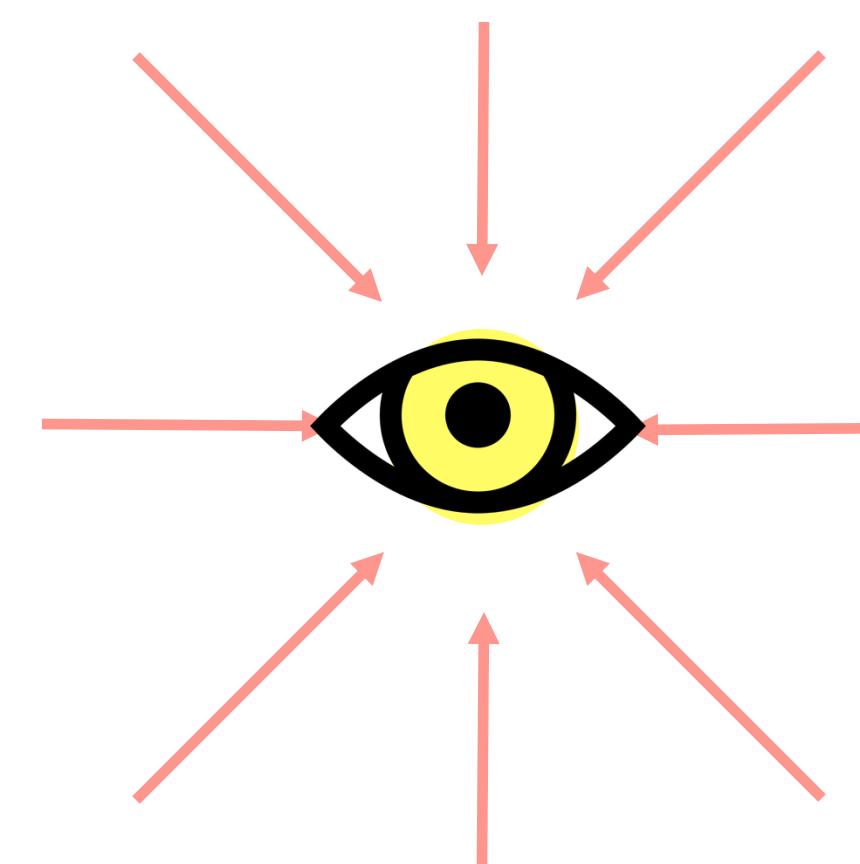


NeRF takes the same input as the Plenoptic Function!

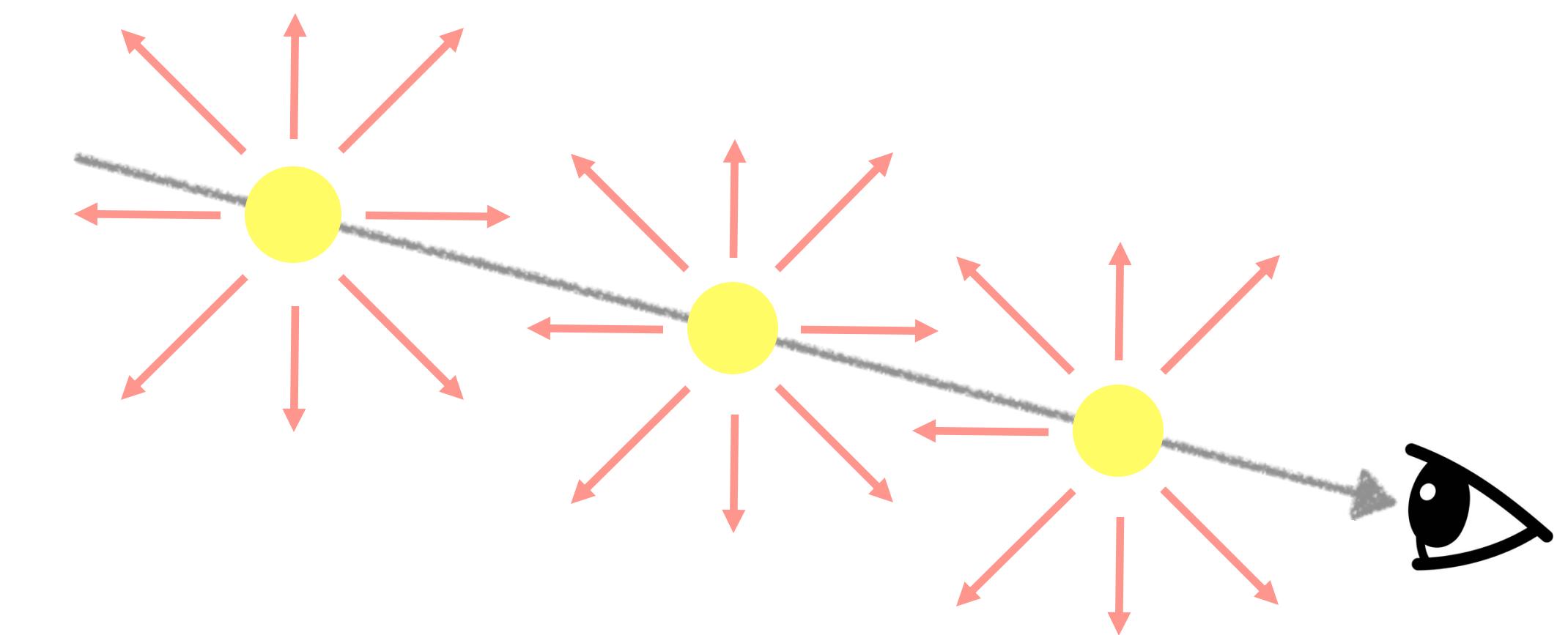
It allows rays to change color. Hence we can fly into the glass bowl (if we had enough observation)



# A subtle difference

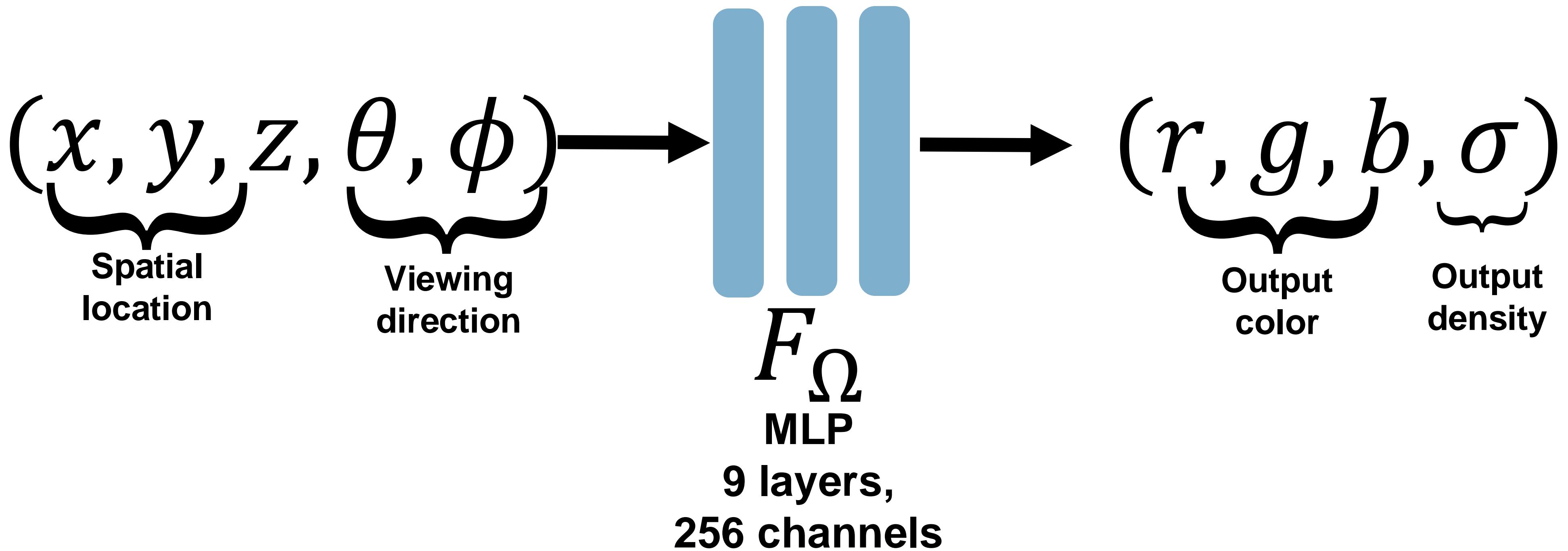
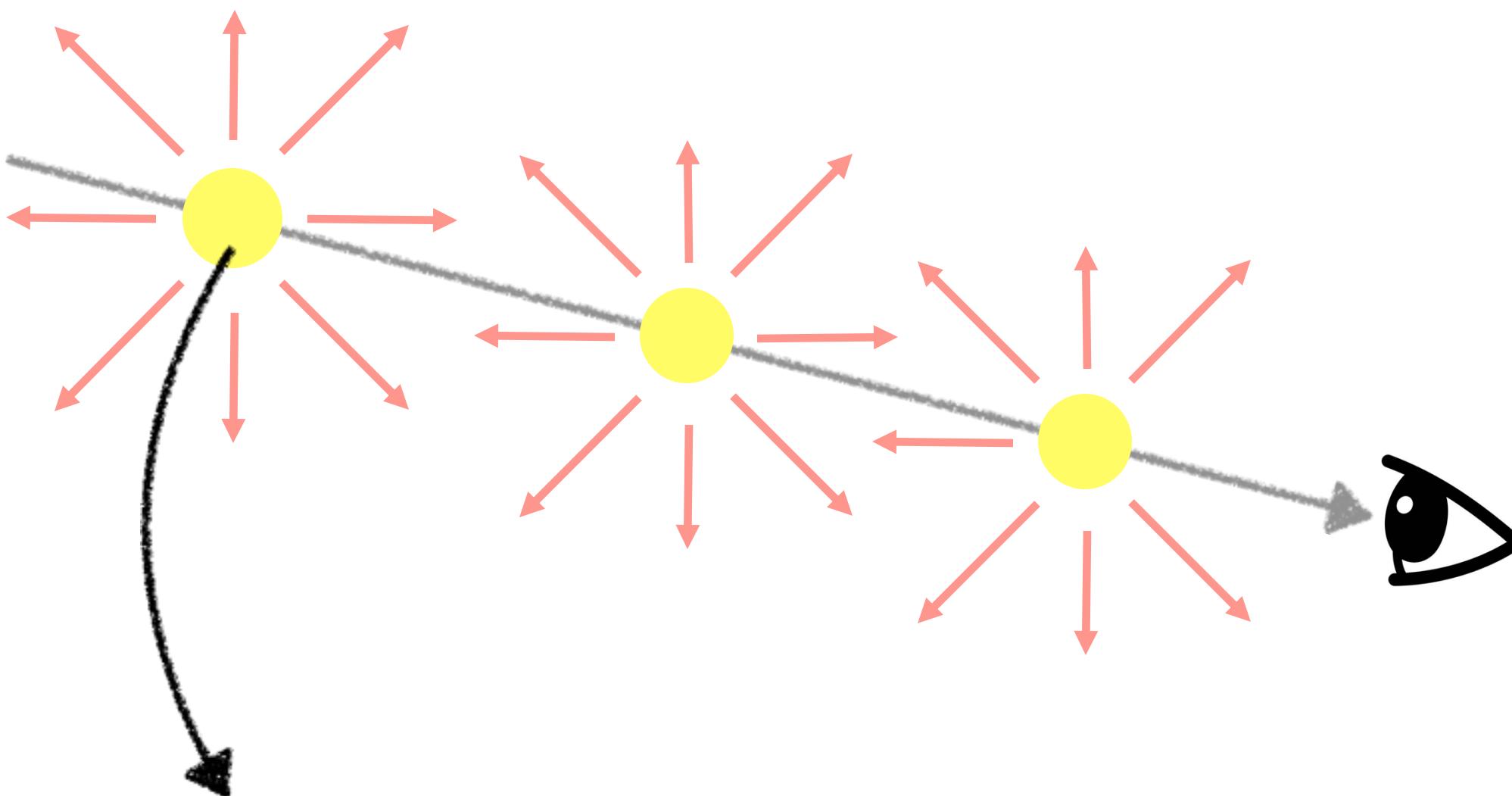


**Plenoptic Function**



**NeRF**

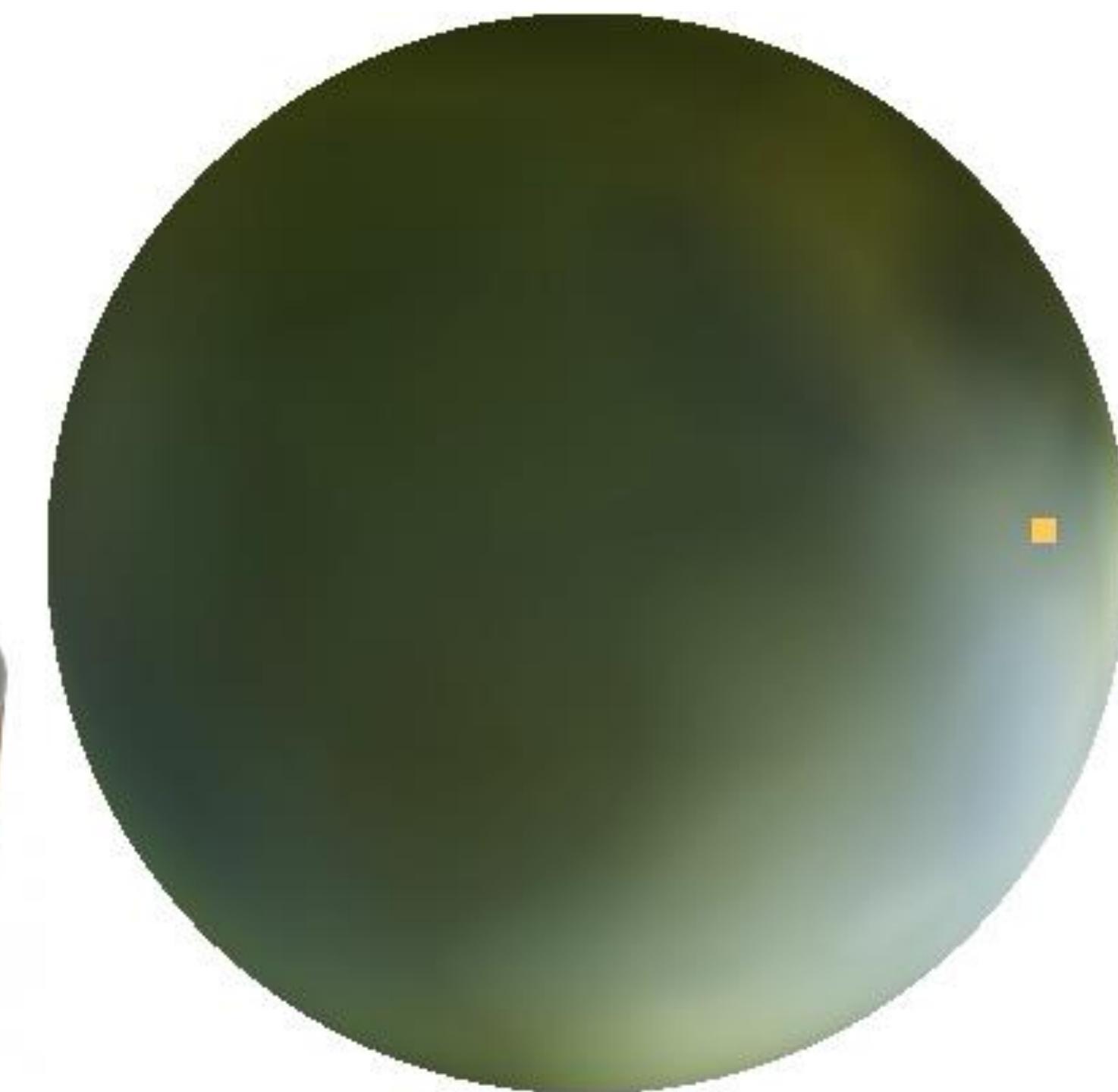
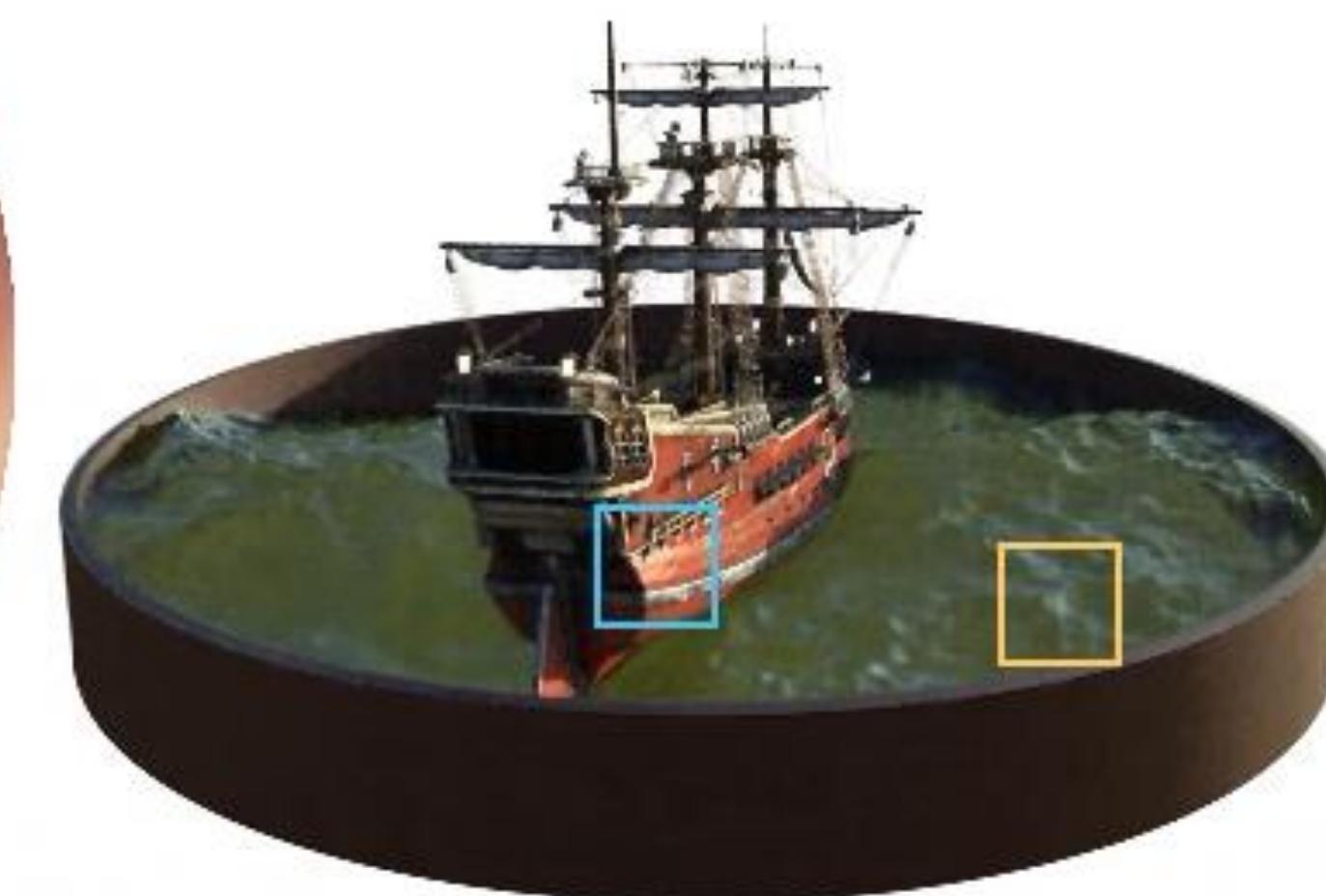
So NeRF requires the integration along the viewing ray to compute the Plenoptic Function  
Bottom line: it models the full (5D) plenoptic function!



# Visualizing the 2D function on the sphere



Outgoing radiance distribution  
for point on side of ship



Outgoing radiance distribution  
for point on water's surface

# Baking in Light



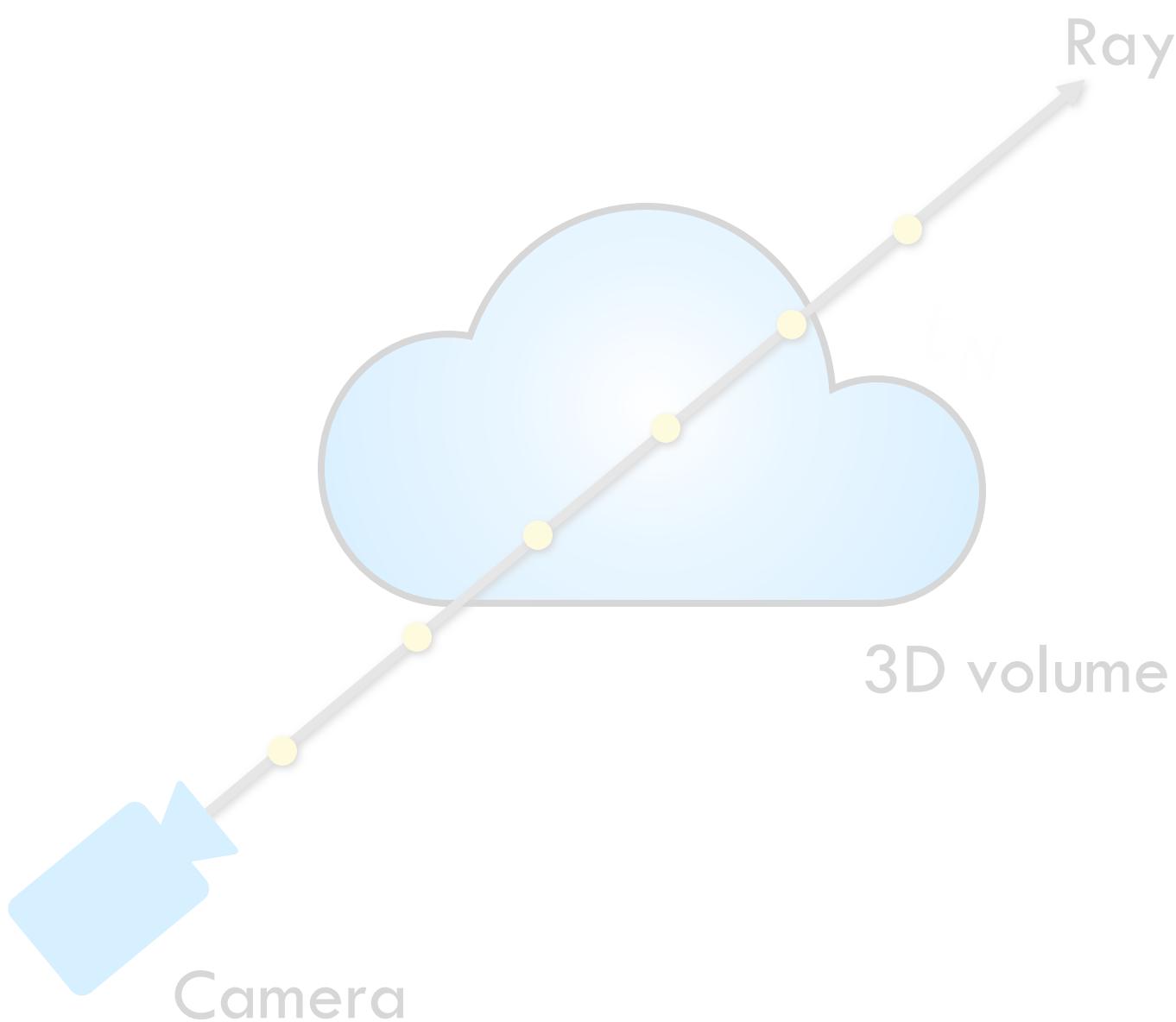
- NeRF can capture non-Lambertian (specular, shiny surfaces) because it models the color in a view-dependent manner
- This is hard to do with meshes unless you model the physical materials & lighting interactions
- But, with Image Based Rendering — All lighting effects are baked in

# NeRF in a Slide

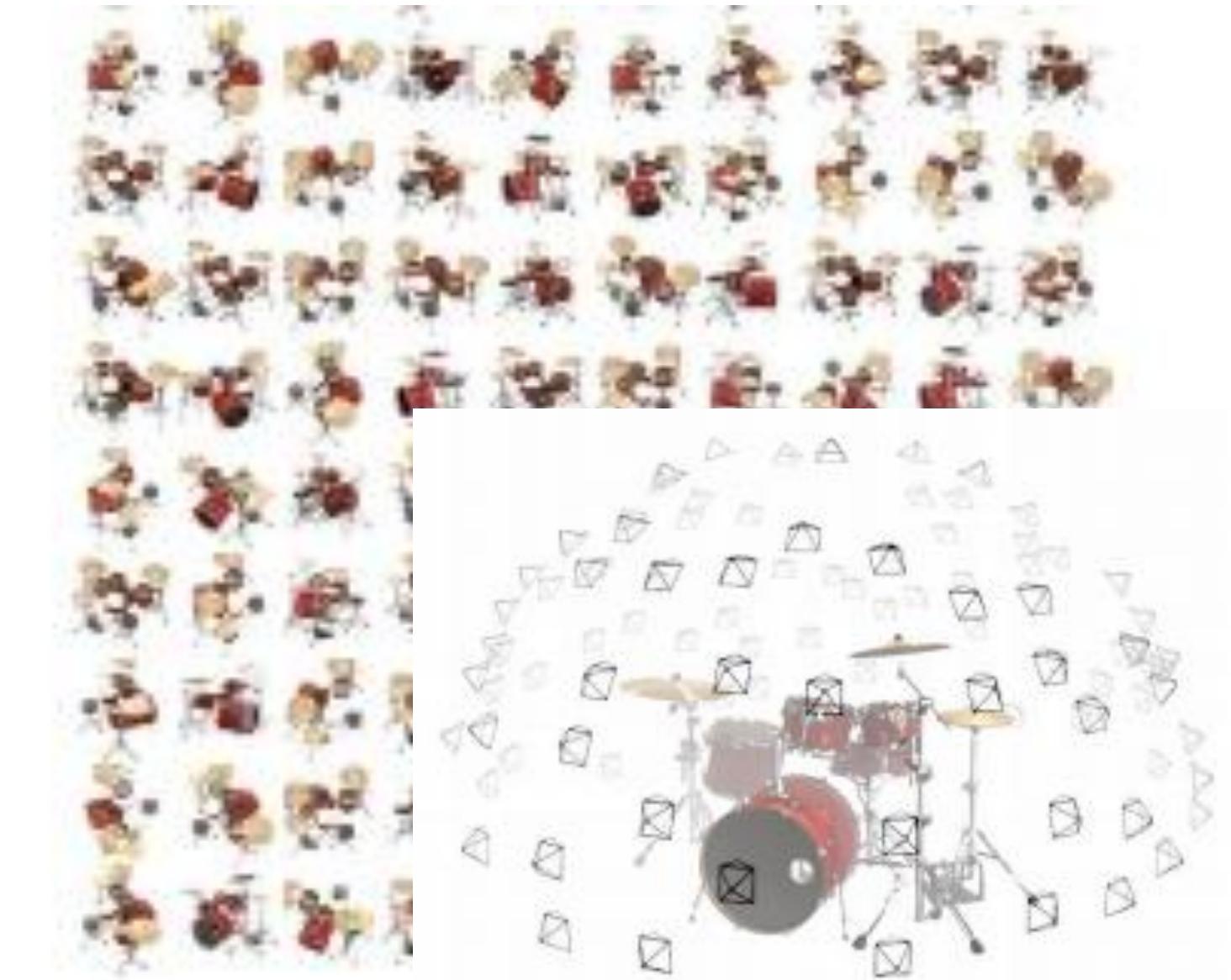
Objective: Reconstruct  
all training views



Volumetric 3D Scene  
Representation



Differentiable Volumetric  
Rendering Function



Optimization via  
Analysis-by-Synthesis

# Unmentioned caveat so far

- Training a NeRF requires a **calibrated camera!!!**
- Need to know the camera parameters: extrinsic (viewpoint) & intrinsics (focal length, distortion, etc)



**How do we get this from images?**

# Structure from Motion

Or Photogrammetry (1850~)  
Long history in Computer Vision

*Proc. R. Soc. Lond. B.* 203, 405–426 (1979)

*Printed in Great Britain*

The interpretation of structure from motion

BY S. ULLMAN

*Artificial Intelligence Laboratory, Massachusetts Institute of Technology,  
545 Technology Square (Room 808), Cambridge, Massachusetts 02139 U.S.A.*

# NeRF is AFTER Structure from Motion

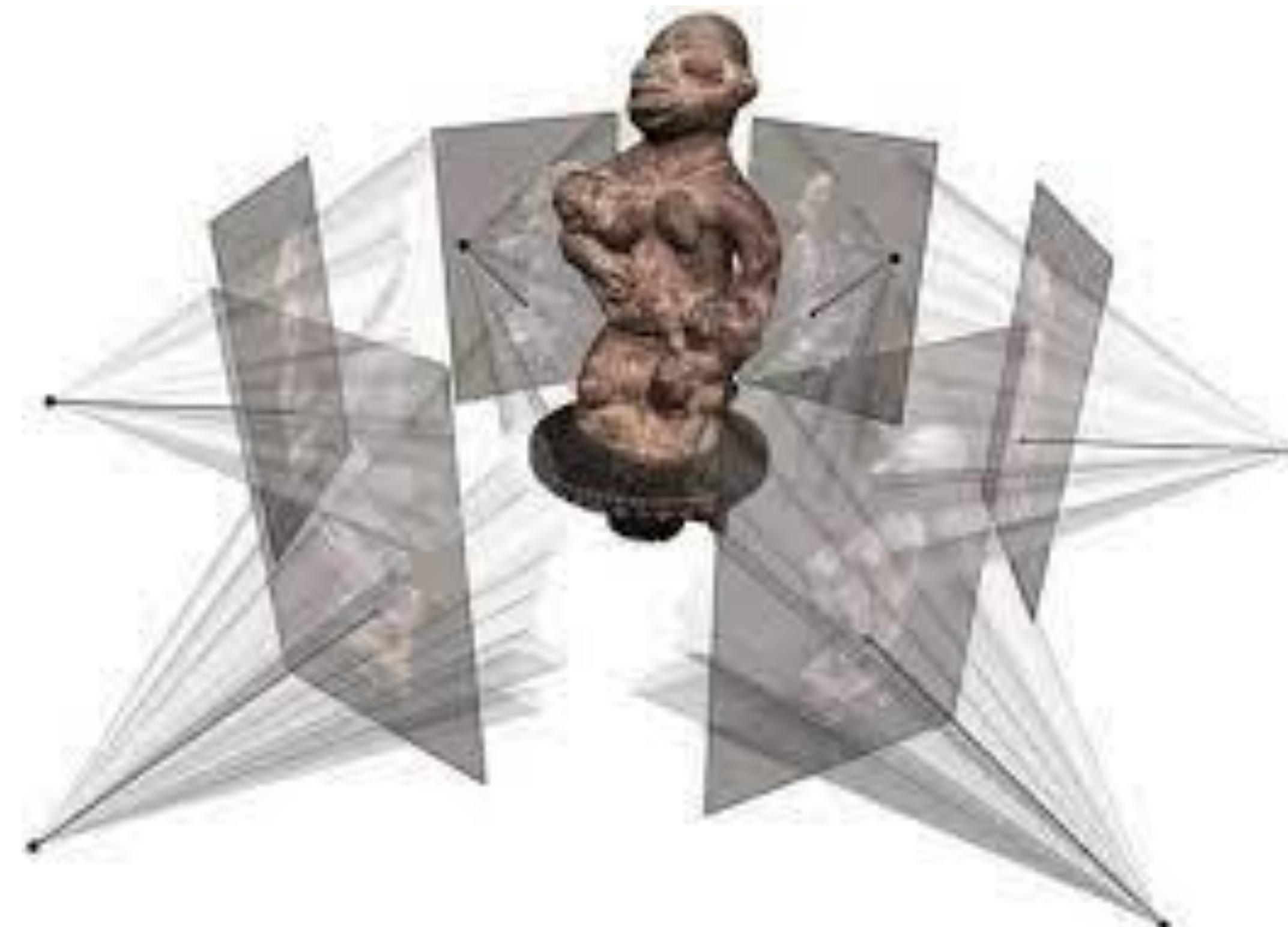
- In order to train NeRF you need to run SfM/SLAM on the images to estimate the camera parameters
- In this sense, the problem category is same as that of **Multi-view Stereo**



Colmap: Schönberger et al. 2016

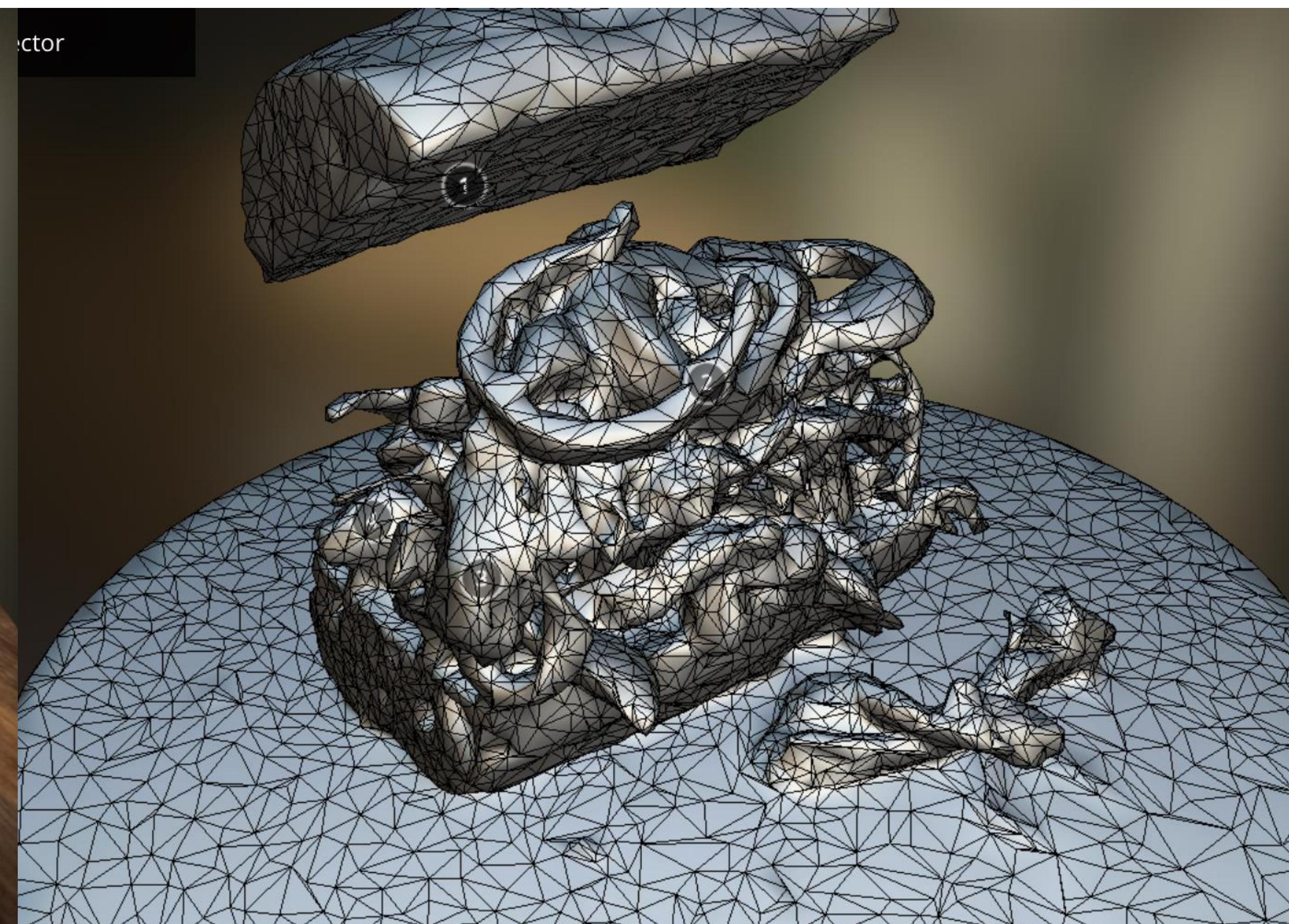
# Multi-view Stereo

- Problem: Given calibrated cameras, recover highly detailed 3D **surface** model
- Dense photogrammetry, often the output is textured meshes



# Multi-View Stereo

Solutions to MVS is what you see for any existing 3D scanning system, ie sketchfab, or what's in your video game



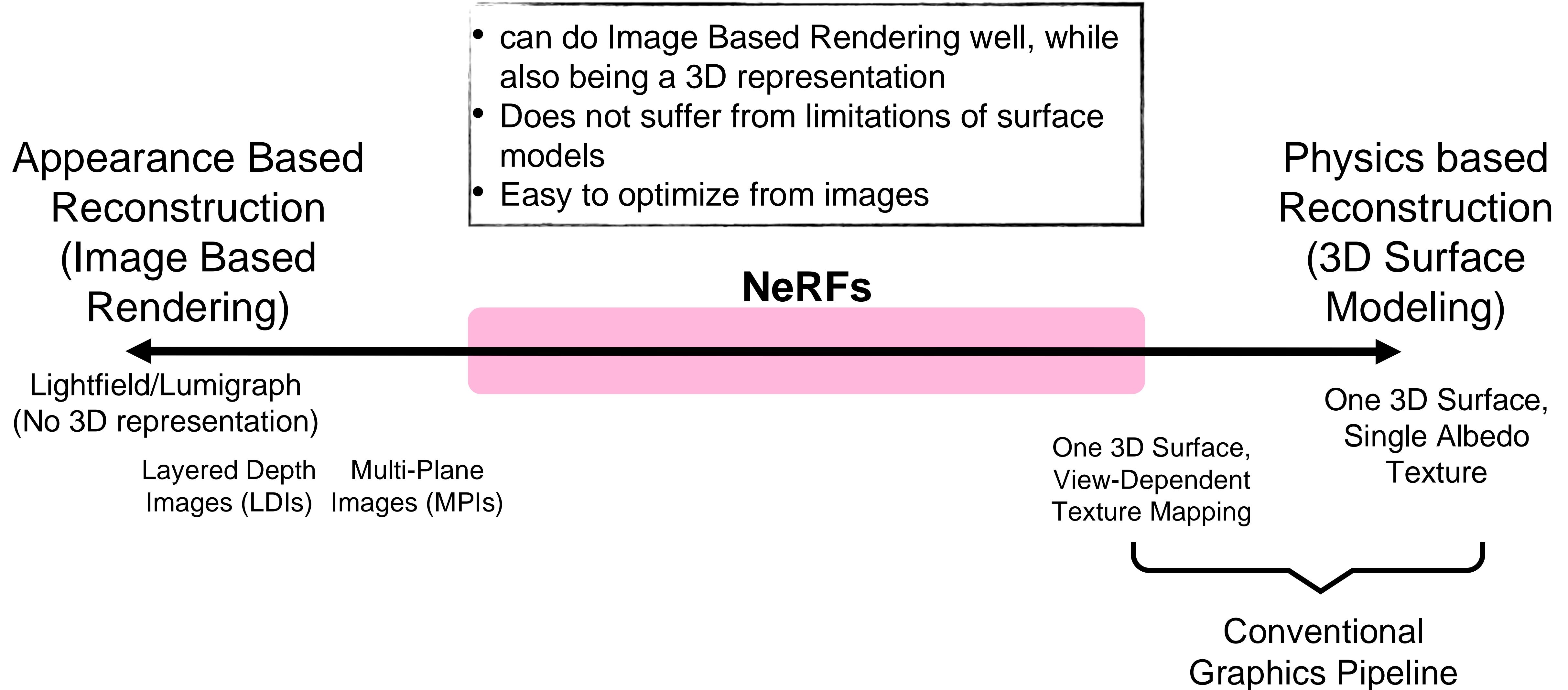
# Multi-View Stereo

Because they often model surfaces, struggles on Thin / Amorphus / Shiny objects





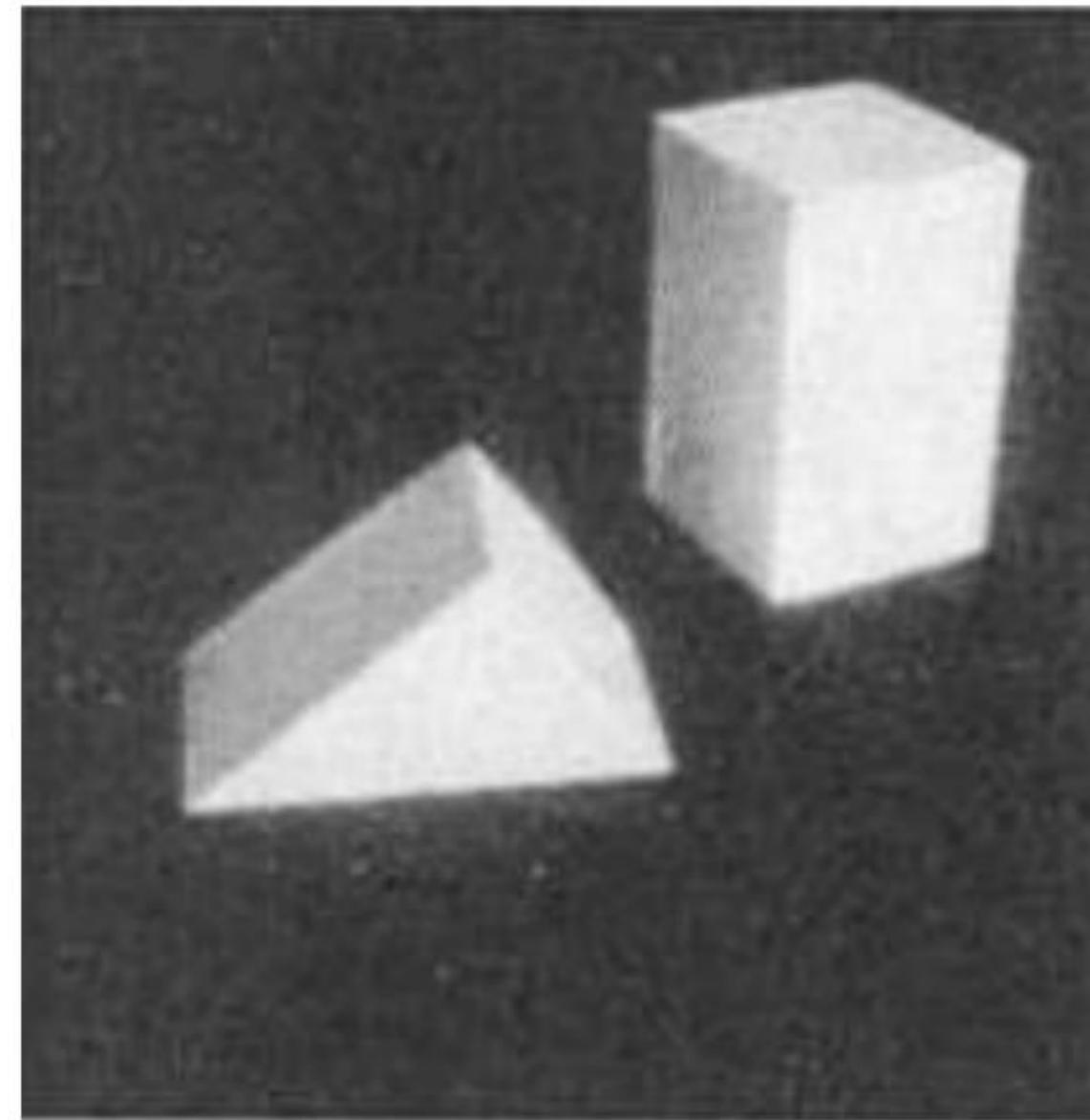
# Where NeRF stands



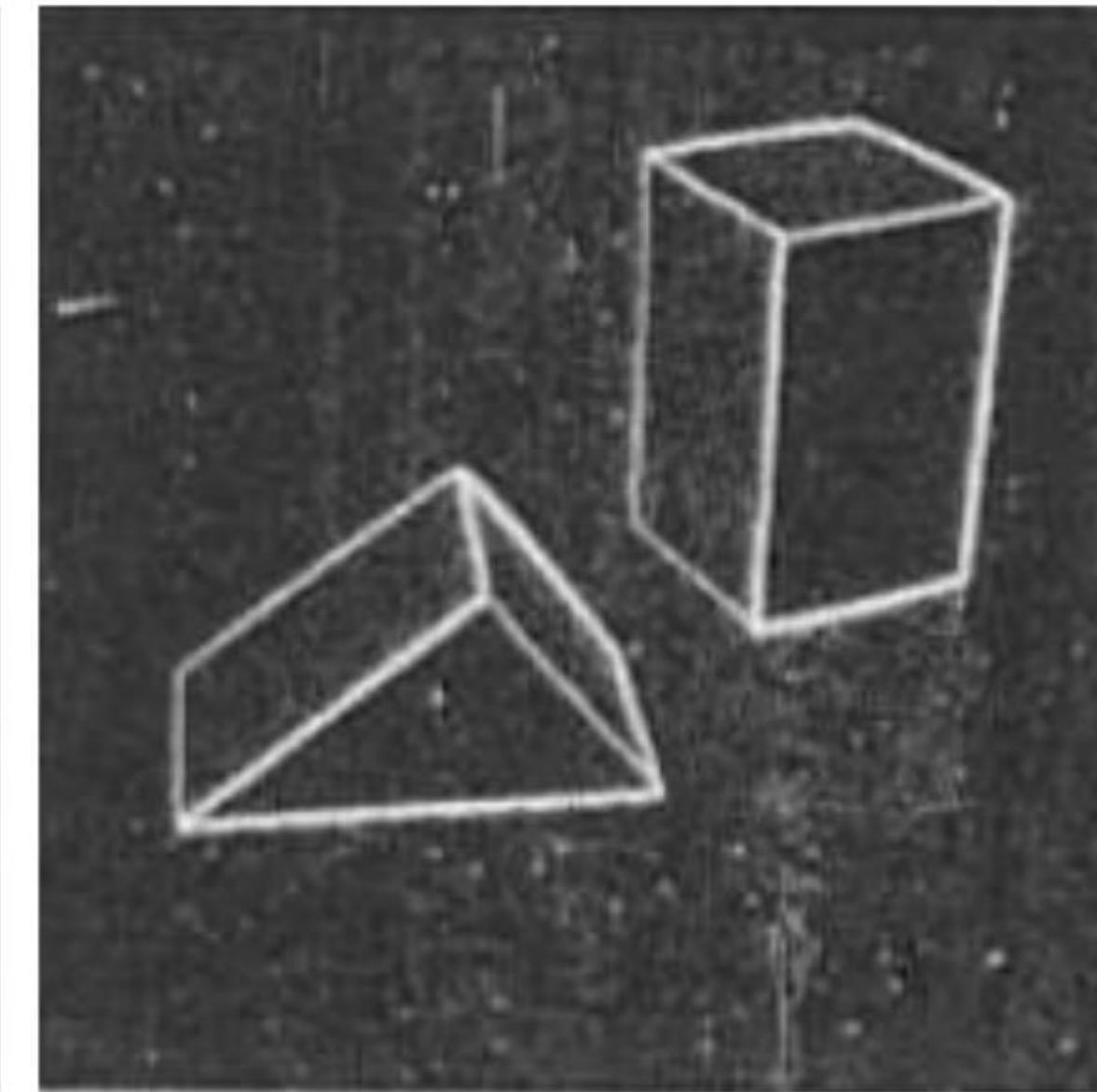
# Analysis-by-Synthesis



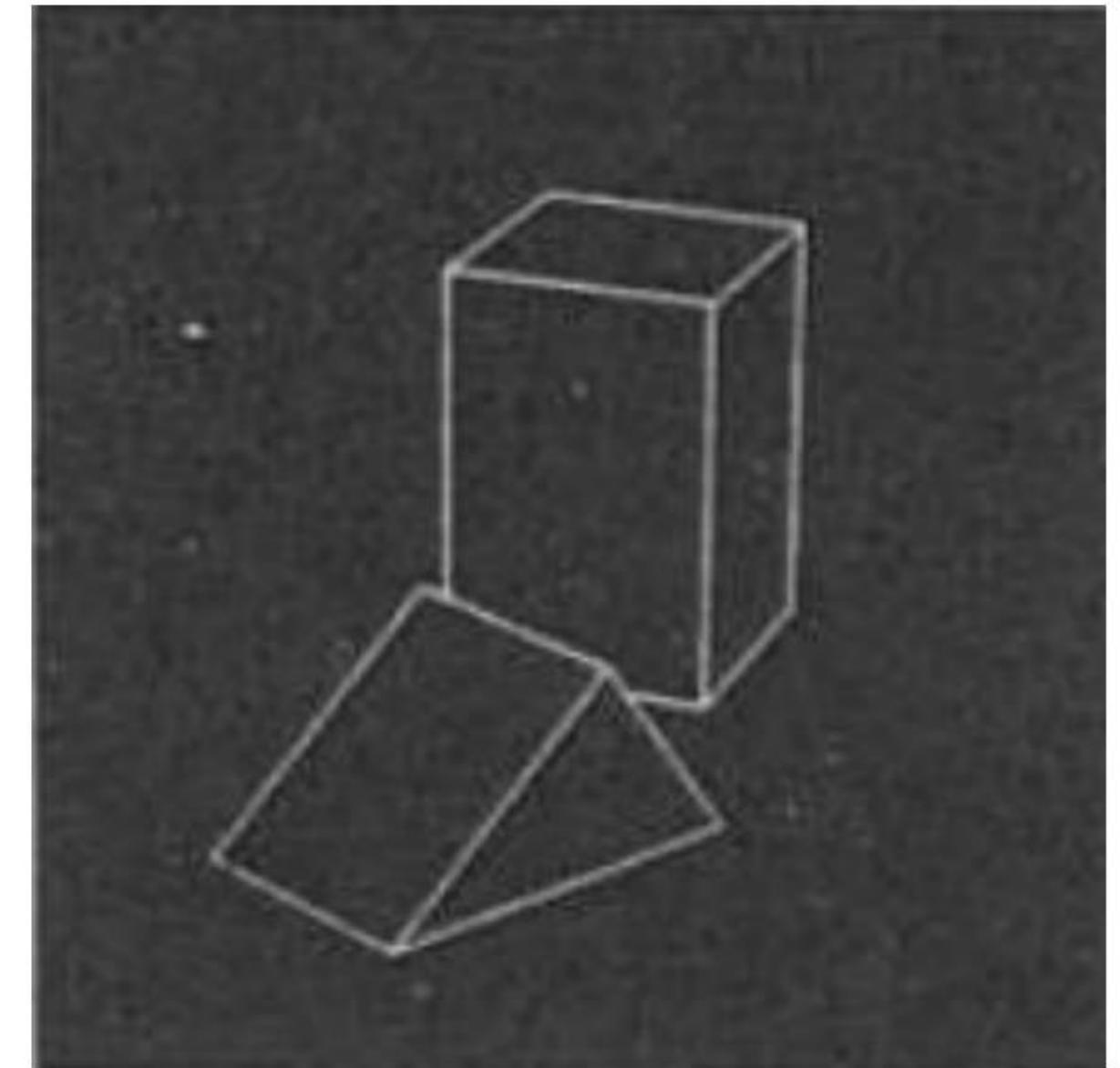
Larry Roberts  
“Father of Computer Vision”



Input image



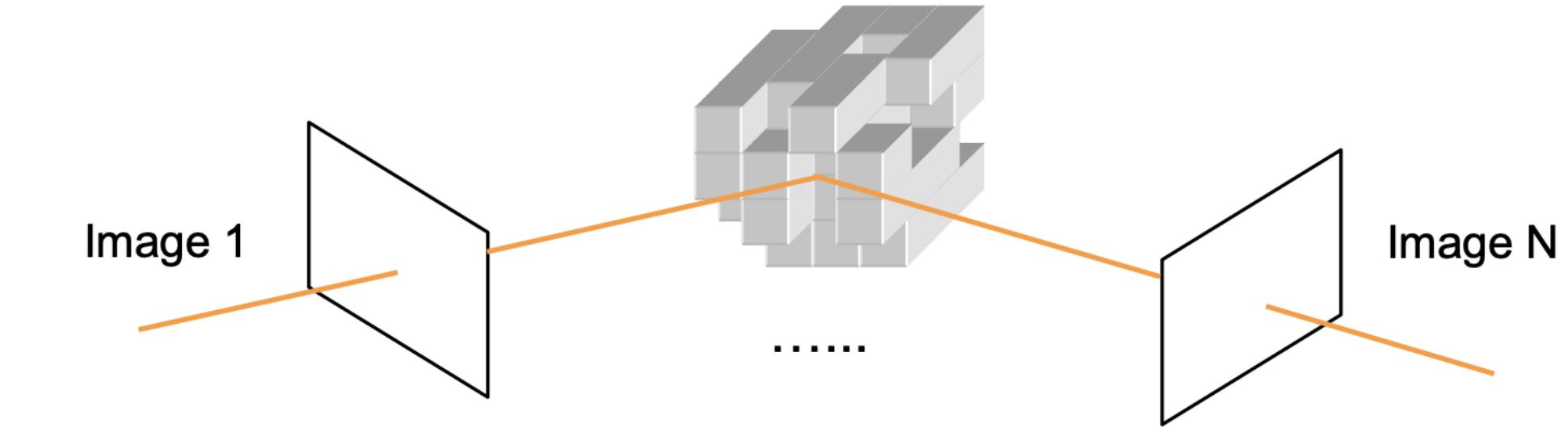
2x2 gradient operator



computed 3D model  
rendered from new viewpoint

- History goes way back to the **first** Computer Vision paper!  
Roberts: Machine Perception of Three-Dimensional Solids, MIT, 1963

# Power of Analysis-by-Synthesis



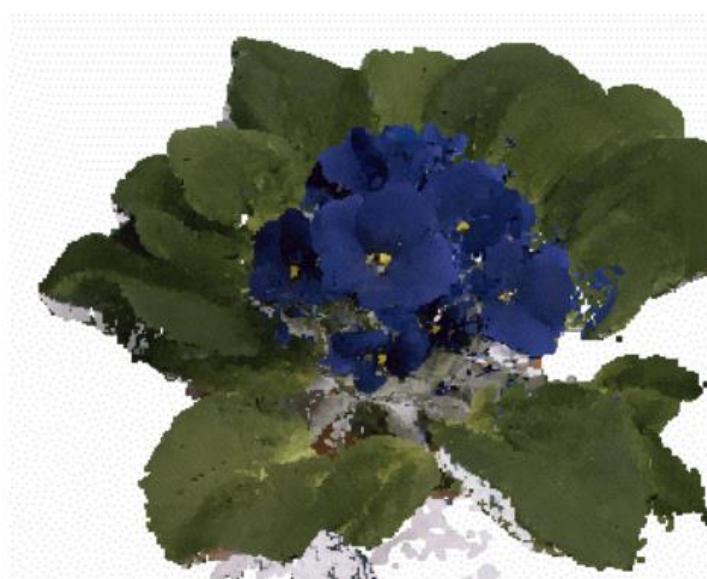
- Space Carving: A MVS method that used Colored voxels
- But the optimization method was bottom up then.
- Key is optimization via Analysis-by-Synthesis [Plenoxels, Yu et al. 2022]



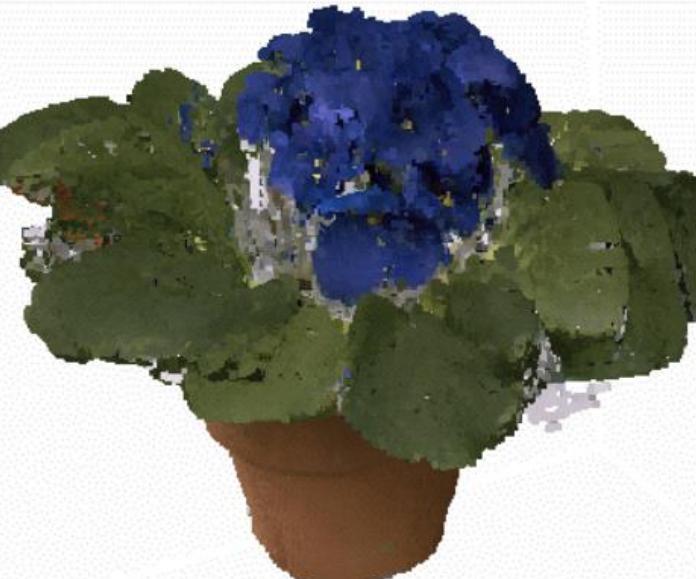
Input Image (1 of 45)



Reconstruction



Reconstruction



Reconstruction



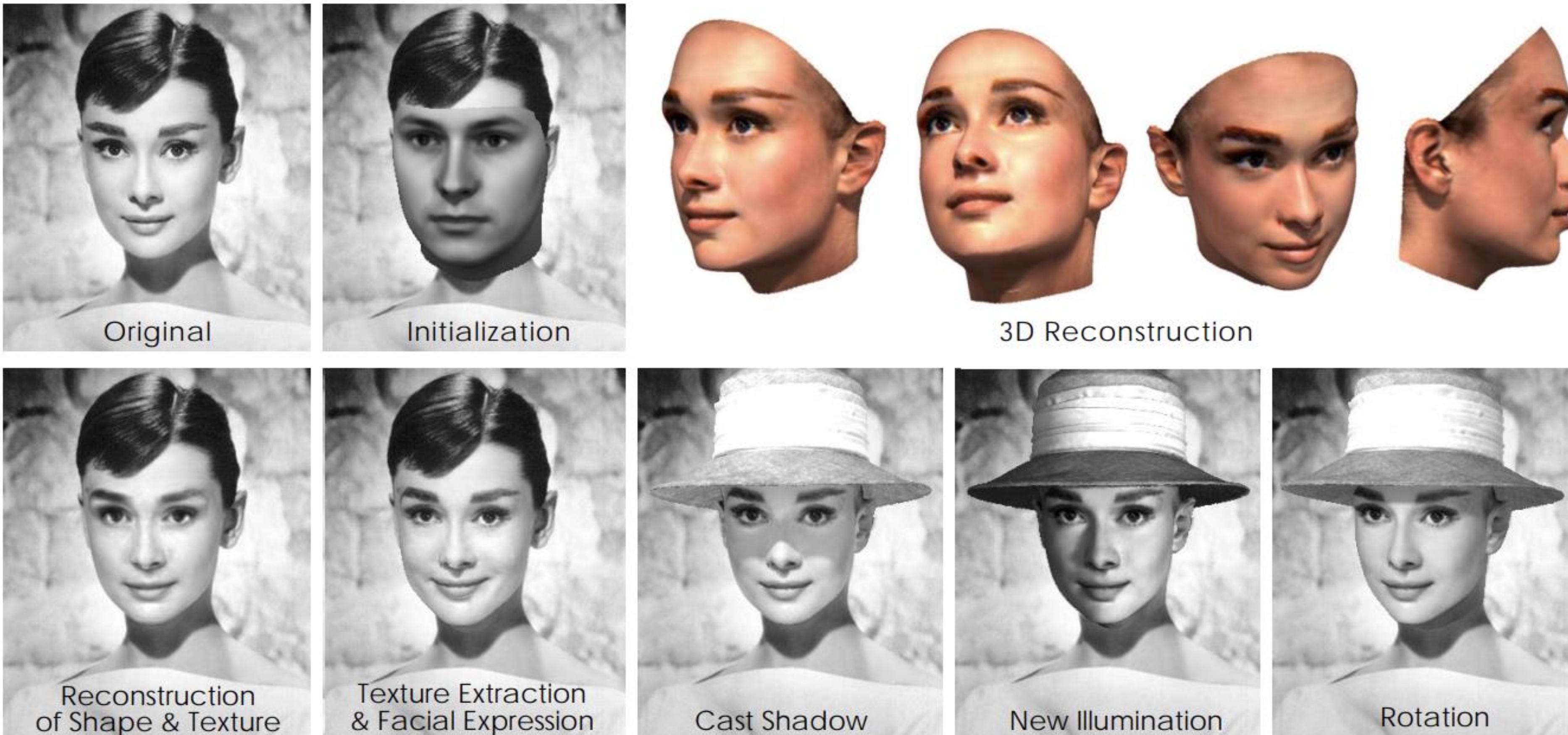
Input Image  
(1 of 100)



Views of Reconstruction



# Analysis-by-Synthesis



Blanz & Vetter 1999

- With custom differentiable renders

# Analysis by Synthesis Requires Differentiable Renderers

Next: Deep dive into Volumetric Rendering Function

# Where we are

1. Birds Eye View & Background
2. **Volumetric Rendering Function**
3. Encoding and Representing 3D Volumes
4. Signal Processing Considerations
5. Challenges & Pointers

# Volume Rendering

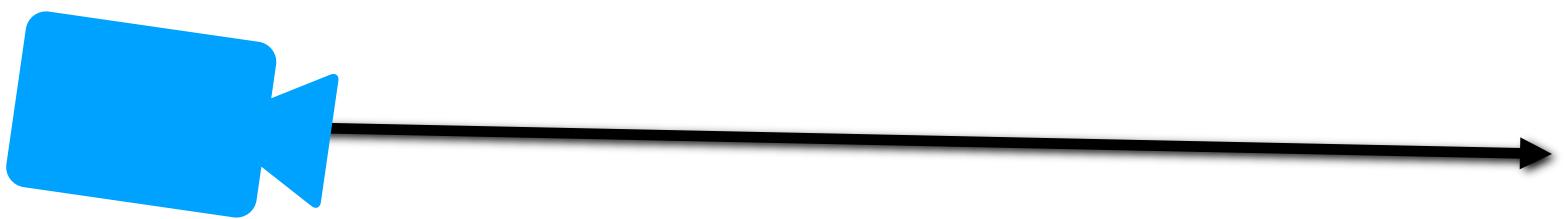
*"... in 10 years, all rendering will be volume rendering."*

Jim Kajiya at SIGGRAPH '91

# Neural Volumetric Rendering

# Neural Volumetric **Rendering**

computing color along rays  
through 3D space



**What color is this pixel?**