

Language Models



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Acoustic Confusions

the station signs are in deep in english	-14732
the stations signs are in deep in english	-14735
the station signs are in deep into english	-14739
the station 's signs are in deep in english	-14740
the station signs are in deep in the english	-14741
the station signs are indeed in english	-14757
the station 's signs are indeed in english	-14760
the station signs are indians in english	-14790



Noisy Channel Model: ASR

- We want to predict a sentence given acoustics:

$$w^* = \arg \max_w P(w|a)$$

- The noisy-channel approach:

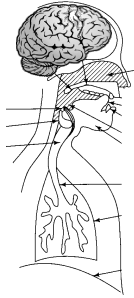
$$w^* = \arg \max_w P(w|a)$$

$$= \arg \max_w P(a|w)P(w)/P(a)$$

$$\propto \arg \max_w P(a|w)P(w)$$

Acoustic model: score fit between
sounds and words

Language model: score
plausibility of word sequences



Noisy Channel Model: Translation

"Also knowing nothing official about, but having guessed and inferred considerable about, the powerful new mechanized methods in cryptography—methods which I believe succeed even when one does not know what language has been coded—one naturally wonders if the problem of translation could conceivably be treated as a problem in cryptography. When I look at an article in Russian, I say: 'This is really written in English, but it has been coded in some strange symbols. I will now proceed to decode.' "

Warren Weaver (1947)



Perplexity

- How do we measure LM "goodness"?

- The Shannon game: predict the next word

When I eat pizza, I wipe off the _____

- Formally: test set log likelihood

$$\log P(X|\theta) = \sum_{w \in X} \log(P(w|\theta))$$

- Perplexity: "average per word branching factor" (not per-step)

$$\text{perp}(X, \theta) = \exp\left(-\frac{\log P(X|\theta)}{|X|}\right)$$

grease 0.5
sauce 0.4
dust 0.05
.....
mice 0.0001
.....
the 1e-100

3516 wipe off the excess
1034 wipe off the dust
547 wipe off the sweat
518 wipe off the mouthpiece
...
120 wipe off the grease
0 wipe off the sauce
0 wipe off the mice

28048 wipe off the *

N-Gram Models



N-Gram Models

- Use chain rule to generate words left-to-right

$$P(w_1 \dots w_n) = \prod_i P(w_i | w_1 \dots w_{i-1})$$

- Can't condition atomically on the entire left context

$P(??? \mid \text{The computer I had put into the machine room on the fifth floor just})$

- N-gram models make a Markov assumption

$$P(w_1 \dots w_n) = \prod_i P(w_i | w_{i-k} \dots w_{i-1})$$

$P(\text{please close the door}) = P(\text{please}|\text{START})P(\text{close}|\text{please}) \dots P(\text{STOP}|\text{door})$



Empirical N-Grams

- Use statistics from data (examples here from Google N-Grams)

Training Counts	198015222 the first	$\hat{P}(\text{door} \text{the}) = \frac{14112454}{23135851162}$ $= 0.0006$
	194623024 the same	
	168504105 the following	
	158562063 the world	
	...	
	14112454 the door	

	23135851162 the *	

- This is the maximum likelihood estimate, which needs modification



Increasing N-Gram Order

- Higher orders capture more correlations

Bigram Model	Trigram Model
198015222 the first	197302 close the window
194623024 the same	191125 close the door
168504105 the following	152500 close the gap
158562063 the world	116451 close the thread
...	87298 close the deal
14112454 the door	-----
23135851162 the *	3785230 close the *
$P(\text{door} \mid \text{the}) = 0.0006$	$P(\text{door} \mid \text{close the}) = 0.05$



Increasing N-Gram Order

Unigram	<ul style="list-style-type: none"> To him swallowed confess hear both. Which. Of save on trail for are ay device and rote life have Every enter now severally so. let Hill he late speaks. or! a more to leg less first you enter Are where exeunt and sighs have rise excellency took of. Sleep knave we. near. vile like
---------	--



What's in an N-Gram?

- Just about every local correlation!
 - Word class restrictions: "will have been ____"
 - Morphology: "she ____", "they ____"
 - Semantic class restrictions: "danced a ____"
 - Idioms: "add insult to ____"
 - World knowledge: "ice caps have ____"
 - Pop culture: "the empire strikes ____"
- But not the long-distance ones
 - "The **computer** which I had put into the machine room on the fifth floor just ____."



Linguistic Pain

- The N-Gram assumption hurts your inner linguist
 - Many linguistic arguments that language isn't regular
 - Long-distance dependencies
 - Recursive structure
 - At the core of the early hesitance in linguistics about statistical methods
- Answers
 - N-grams only model local correlations... but they get them all
 - As N increases, they catch even more correlations
 - N-gram models scale much more easily than combinatorially-structured LMs
 - Can build LMs from structured models, eg grammars (though people generally don't)



Structured Language Models

- Bigram model:
 - [texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen]
 - [outside, new, car, parking, lot, of, the, agreement, reached]
 - [this, would, be, a, record, november]
- PCFG model:
 - [This, quarter, 's, surprisingly, independent, attack, paid, off, the, risk, involving, IRS, leaders, and, transportation, prices, .]
 - [It, could, be, announced, sometime, .]
 - [Mr., Toseland, believes, the, average, defense, economy, is, drafted, from, slightly, more, than, 12, stocks, .]

N-Gram Models: Challenges

Sparsity

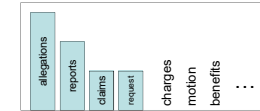
Please close the first door on the left.

```
3380 please close the door
1601 please close the window
1164 please close the new
1159 please close the gate
...
0 please close the first
-----
13951 please close the *
```

Smoothing

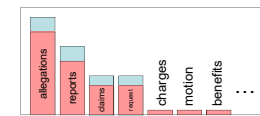
- We often want to make estimates from sparse statistics:

$P(w \mid \text{denied the})$
 3 allegations
 2 reports
 1 claims
 1 request
 7 total



- Smoothing flattens spiky distributions so they generalize better:

$P(w \mid \text{denied the})$
 2.5 allegations
 1.5 reports
 0.5 claims
 0.5 request
 2 other
 7 total



- Very important all over NLP, but easy to do badly

Back-off

Please close the first door on the left.

4-Gram

```
3380 please close the door
1601 please close the window
1164 please close the new
1159 please close the gate
...
0 please close the first
-----
13951 please close the *
```

0.0

3-Gram

```
197302 close the window
191125 close the door
152500 close the gap
116451 close the thread
...
8662 close the first
-----
3785230 close the *
```

0.002

2-Gram

```
198015222 the first
194623024 the same
168504105 the following
158562063 the world
...
23135851162 the *
```

0.009

Specific but Sparse



Dense but General

$$\lambda \hat{P}(w|w_{-1}, w_{-2}) + \lambda' \hat{P}(w|w_{-1}) + \lambda'' \hat{P}(w)$$

Discounting

- Observation: N-grams occur more in training data than they will later

Empirical Bigram Counts (Church and Gale, 91)

Count in 22M Words	Future c^* (Next 22M)
1	
2	
3	
4	
5	

- Absolute discounting: reduce counts by a small constant, redistribute "shaved" mass to a model of new events

$$P_{\text{ad}}(w|w') = \frac{c(w', w) - d}{c(w')} + \alpha(w') \hat{P}(w)$$



Fertility

- Shannon game: "There was an unexpected ____"
delay? Francisco?
- Context fertility: number of distinct context types that a word occurs in
 - What is the fertility of "delay"?
 - What is the fertility of "Francisco"?
 - Which is more likely in an arbitrary new context?

- Kneser-Ney smoothing: new events proportional to context fertility, not frequency

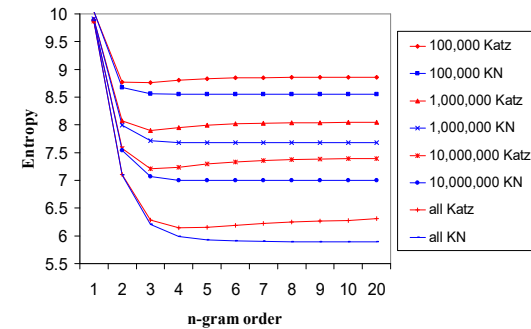
[Kneser & Ney, 1995]

$$P(w) \propto |\{w': c(w', w) > 0\}|$$

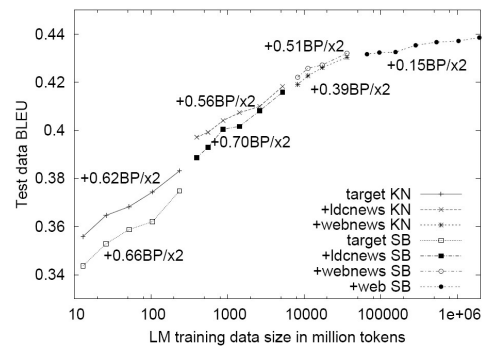
- Can be derived as inference in a hierarchical Pitman-Yor process [Teh, 2006]



Better Methods?



More Data?



[Brants et al, 2007]



Storage

```
...
searching for the best      192593
searching for the right    45805
searching for the cheapest 44965
searching for the perfect  43959
searching for the truth    23165
searching for the "        19086
searching for the most     15512
searching for the latest   12670
searching for the next     10120
searching for the lowest   10080
searching for the name     8402
searching for the finest   8171
...
```

Google N-grams

- 14 million < 2²⁴ words
- 2 billion < 2³¹ 5-grams
- 770 000 < 2²⁰ unique counts
- 4 billion n-grams total



Storage

- For 5+-gram models, need to store between 100M and 10B context-word-count triples

(a) Context-Encoding			(b) Context Deltas			(c) Bits Required		
w	c	val	Δw	Δc	val	$ \Delta w $	$ \Delta c $	$ val $
1933	15176585	3	1933	15176585	3	24	40	3
1933	15176587	2	+0	+2	1	2	3	3
1933	15176593	1	+0	+5	1	2	3	3
1933	15176613	8	+0	+40	8	2	9	6
1933	15179801	1	+0	+188	1	2	12	3
1935	15176585	298	+2	15176585	298	4	36	15
1935	15176589	1	+0	+4	1	2	6	3

- Make it fit in memory by *delta encoding* scheme: store deltas instead of values and use variable-length encoding

Pauls and Klein (2011), Heafield (2011)

Slide: Greg Durrett



Graveyard of Correlations

- Skip-grams
- Cluster models
- Topic variables
- Cache models
- Structural zeros
- Dependency models
- Maximum entropy models
- Subword models
- ...



Entirely Unseen Words

- What about totally unseen words?
- Classical real world option: systems are actually closed vocabulary
 - ASR systems will only propose words that are in their pronunciation dictionary
 - MT systems will only propose words that are in their phrase tables (modulo special models for numbers, etc)
- Classical theoretical option: build open vocabulary LMs
 - Models over character sequences rather than word sequences
 - N-Grams: back-off needs to go down into a "generate new word" model
 - Typically if you need this, a high-order character model will do
- Modern approach: syllable-sized subword units (more later)