

Language Models



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Language Models

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Language Models



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Acoustic Confusions

the station signs are in deep in english
the stations signs are in deep in english
the station signs are in deep into english
the station 's signs are in deep in english
the station signs are in deep in the english
the station signs are indeed in english
the station 's signs are indeed in english
the station signs are indians in english

-14732
-14735
-14739
-14740
-14741
-14757
-14760
-14790

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Noisy Channel Model: ASR

■ We want to predict a sentence given acoustics:

$$w^* = \arg \max_w P(w|a)$$

■ The noisy-channel approach:

$$\begin{aligned} w^* &= \arg \max_w P(w|a) \\ &= \arg \max_w P(a|w)P(w)/P(a) \\ &\propto \arg \max_w P(a|w)P(w) \end{aligned}$$

Acoustic model: score fit between sounds and words Language model: score plausibility of word sequences



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Noisy Channel Model: Translation

"Also knowing nothing official about, but having guessed and inferred considerable about, the powerful new mechanized methods in cryptography—methods which I believe succeed even when one does not know what language has been coded—one naturally wonders if the problem of translation could conceivably be treated as a problem in cryptography. When I look at an article in Russian, I say: 'This is really written in English, but it has been coded in some strange symbols. I will now proceed to decode.' "

Warren Weaver (1947)

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Perplexity

■ How do we measure LM “goodness”?

- The Shannon game: predict the next word
When I eat pizza, I wipe off the _____
- Formally: test set log likelihood

$$\log P(X|\theta) = \sum_{w \in X} \log(P(w|\theta))$$

■ Perplexity: “average per word branching factor” (not per-step)

$$\text{perp}(X, \theta) = \exp\left(\frac{\log P(X|\theta)}{|X|}\right)$$

grease 0.5
sauce 0.4
dust 0.05
...
mice 0.0001
...
the 1e-100

3516	wipe off the excess
1034	wipe off the dust
547	wipe off the sweat
513	wipe off the mouthpiece
...	
120	wipe off the grease
0	wipe off the sauce
0	wipe off the mice
28048	wipe off the *

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N-Gram Models

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N-Gram Models

- Use chain rule to generate words left-to-right

$$P(w_1 \dots w_n) = \prod_i P(w_i | w_1 \dots w_{i-1})$$

- Can't condition atomically on the entire left context

$P(\text{???} | \text{The computer I had put into the machine room on the fifth floor just})$

- N-gram models make a Markov assumption

$$P(w_1 \dots w_n) = \prod_i P(w_i | w_{i-k} \dots w_{i-1})$$

$$P(\text{please close the door}) = P(\text{please}|\text{START})P(\text{close}|\text{please}) \dots P(\text{STOP}|\text{door})$$

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Empirical N-Grams

- Use statistics from data (examples here from Google N-Grams)

Training Counts	198015222 the first 194623024 the same 168504105 the following 158562063 the world ... 14112454 the door ----- 23135851162 the *
-----------------	---

$$\hat{P}(\text{door}|\text{the}) = \frac{14112454}{23135851162} = 0.0006$$

- This is the maximum likelihood estimate, which needs modification

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Increasing N-Gram Order

- Higher orders capture more correlations

Bigram Model

198015222	the first
194623024	the same
168504105	the following
158562063	the world
...	
14112454	the door

23135851162	the *

$$P(\text{door} | \text{the}) = 0.0006$$

Trigram Model

197302	close the window
191125	close the door
152500	close the gap
116451	close the thread
87298	close the deal

3785230	close the *

$$P(\text{door} | \text{close the}) = 0.05$$

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Increasing N-Gram Order

Bigram
 To him swallowed countless bear both Which Of save on trail for are my device and
 note life have
 Every enter now severely so let
 • Will be late speaks, or a more to last less first you enter
 • Are where oceans and sights have rise excellency took of... Sleep know we near, vicle
 hic

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What's in an N-Gram?

- Just about every local correlation!
 - Word class restrictions: "will have been ____"
 - Morphology: "she ____", "they ____"
 - Semantic class restrictions: "danced a ____"
 - Idioms: "add insult to ____"
 - World knowledge: "ice caps have ____"
 - Pop culture: "the empire strikes ____"
- But not the long-distance ones
 - "The computer which I had put into the machine room on the fifth floor just ____."

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Linguistic Pain

- The N-Gram assumption hurts your inner linguist
 - Many linguistic arguments that language isn't regular
 - Long-distance dependencies
 - Recursive structure
 - At the core of the early hesitance in linguistics about statistical methods
- Answers
 - N-grams only model local correlations... but they get them all
 - As N increases, they catch even more correlations
 - N-gram models scale much more easily than combinatorially-structured LMs
 - Can build LMs from structured models, eg grammars (though people generally don't)

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Structured Language Models

- Bigram model:
 - [texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen]
 - [outside, new, car, parking, lot, of, the, agreement, reached]
 - [this, would, be, a, record, november]
- PCFG model:
 - [This, quarter, 's, surprisingly, independent, attack, paid, off, the, risk, involving, IRS, leaders, and, transportation, prices, .]
 - [It, could, be, announced, sometime, .]
 - [Mr., Toseeland, believes, the, average, defense, economy, is, drafted, from, slightly, more, than, 12, stocks, .]

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N-Gram Models: Challenges

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Sparsity

Please close the first door on the left.

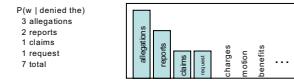
```
3380 please close the door
1601 please close the window
1164 please close the new
1159 please close the gate
...
0 please close the first
13951 please close the *
```

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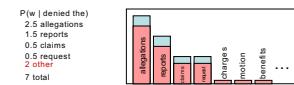


Smoothing

- We often want to make estimates from sparse statistics:



- Smoothing flattens spiky distributions so they generalize better:



- Very important all over NLP, but easy to do badly

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Back-off

Please close the first door on the left.

4-Gram

```
3380 please close the door
1601 please close the window
1164 please close the new
1159 please close the gate
...
0 please close the first
13951 please close the *
```

0.0

3-Gram

```
197302 close the window
191125 close the door
192500 close the gap
116451 close the thread
...
8662 close the first
3785230 close the *
```

0.002

2-Gram

```
198015222 the first
194623024 the same
168504105 the following
158562063 the world
...
29135851162 the *
```

0.009

Specific but Sparse



Dense but General

$$\lambda \hat{P}(w|w_{-1}, w_{-2}) + \lambda' \hat{P}(w|w_{-1}) + \lambda'' \hat{P}(w)$$

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Discounting

- Observation: N-grams occur more in training data than they will later
Empirical Bigram Counts (Church and Gale, 91)

Count in 22M Words	Future c* (Next 22M)
1	
2	
3	
4	
5	

- Absolute discounting: reduce counts by a small constant, redistribute "shaved" mass to a model of new events

$$P_{\text{ad}}(w|w') = \frac{c(w', w) - d}{c(w')} + \alpha(w') \hat{P}(w)$$

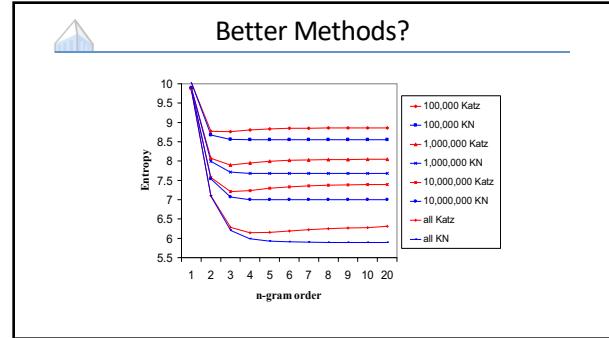
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Fertility

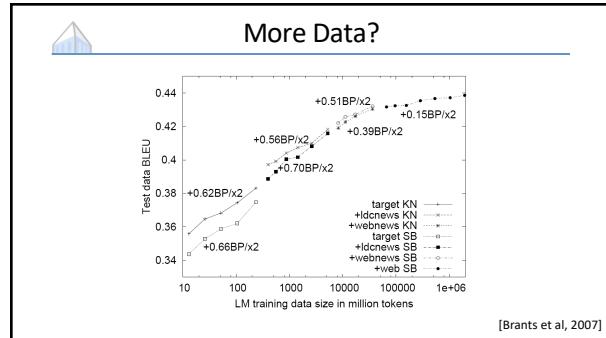
- Shannon game: "There was an unexpected _____"
 - delay? Francisco?
- Context fertility: number of distinct context types that a word occurs in
 - What is the fertility of "delay"?
 - What is the fertility of "Francisco"?
 - Which is more likely in an arbitrary new context?
- Kneser-Ney smoothing: new events proportional to context fertility, not frequency [Kneser & Ney, 1995]

$$P(w) \propto |\{w': c(w', w) > 0\}|$$
- Can be derived as inference in a hierarchical Pitman-Yor process [Teh, 2006]

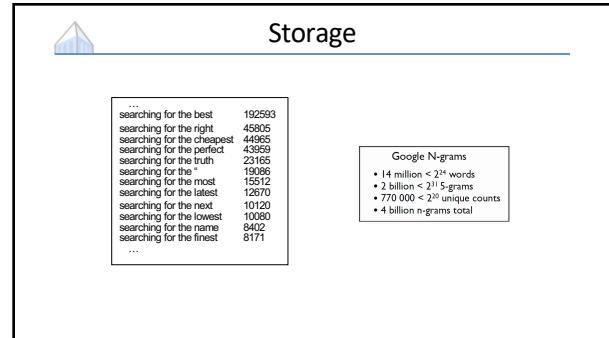
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Storage

For 5+gram models, need to store between 100M and 10B context-word-count triples

Make it fit in memory by *delta encoding* scheme: store deltas instead of values and use variable-length encoding

Pauls and Klein (2011), Heafield (2011)

Slide: Greg Durrett

(a) Context-Encoding			(b) Context Deltas			(c) Bits Required		
w	c	val	Δw	Δc	val	$ \Delta w $	$ \Delta c $	$ val $
1931	15176585	3	1933	15176585	3	24	40	3
1931	15176587	2	+0	+2	1	2	3	3
1931	15176593	1	+0	+5	1	2	3	3
1931	15176613	8	+0	+40	8	2	9	6
1931	15179801	1	+0	+188	1	2	12	3
1985	15176585	298	+2	15176585	298	4	36	15
1985	15176589	1	+0	+4	1	2	6	3

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Graveyard of Correlations

- Skip-grams
- Cluster models
- Topic variables
- Cache models
- Structural zeros
- Dependency models
- Maximum entropy models
- Subword models
- ...

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Entirely Unseen Words

- What about totally unseen words?
- Classical real world option: systems are actually closed vocabulary
 - ASR systems will only propose words that are in their pronunciation dictionary
 - MT systems will only propose words that are in their phrase tables (modulo special models for numbers, etc)
- Classical theoretical option: build open vocabulary
 - Models over character sequences rather than word sequences
 - N-Grams: back-off needs to go down into a "generate new word" model
 - Typically if you need this, a high-order character model will do
- Modern approach: syllable-sized subword units (more later)

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Neural LMs: Preview

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A GPT2 Continuation

■ **The computer I had put into the machine room on the fifth floor just outside our landing was taken by a lot of people.** It was going to be recovered from outside the machine room as soon as we could, but after the machine room was shut down, we had to open all of the windows and doors to save ourselves, and the computer would have been lost. Luckily we are prepared for this. We had five steel doors on each side of the landing to hold any rain and wind that might have hit, so we weren't affected by the storm.

The situation was really grim for days. A few days before, the Apache at Qush Tefah had been shot. This was the most damaged machine in the Armies Corps. The command was only meant to repair Qush

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A GPT2 Continuation

■ **I shall go seek the traitor Gloucester,** when he hath declared his vengeance. Cunegund Shall I back her to kill my cousin in my stead? Witbane Far first shall the brother take his Queen's soul and that in the flames. Clotilda For to slay the King of Scotland with, the blood of my cousin, lie true; And she shall have the right to my feather." Sefton leapt into the rushes, and stole along in the sunlight: the small figure flashed like lightning in the west. In the likeness of a snare he had laid to catch the rushes and made of them a snares, a road to flee from his pursuers; but he now came to an oak where the branches were wreathed in an oak-

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Words: Clusterings and Embeddings

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Stuffing Words into Vector Spaces?



Cartoon: Greg Durrett

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Distributional Similarity

- Key idea in clustering and embedding methods: characterize a word by the words it occurs with (cf Harris' distributional hypothesis, 1954)
- "You can tell a word by the company it keeps." [Firth, 1957]
- Harris / Chomsky divide in linguistic methodology

the president said that the downturn was over

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Clusterings

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Clusterings

- Automatic (Finch and Chater 92, Shuetze 93, many others)

word	nearest neighbors
accompanied	technician banned financed developed authorized headed canceled awarded barred
almost	virtually merely formally fully quite officially just nearly only less
causing	reflecting forcing providing creating producing becoming carrying particularly
classes	elections courses payments loans computers performances violations levels pictures
directors	professionals investigations materials computers agreements papers transactions
goal	target role objective target role objective
japanese	chinese iraq american western arab foreign european federal soviet indian
represent	reveal attend deliver reflect choose contain impose manage establish retain
think	believe wish know realize wonder assume feel say mean bet
you	she he we they i it we you i he she nobody who it everybody there
on	through in at over into with from for by across
must	might would could cannot will should can may does helps
they	we you i he she nobody who it everybody there

- Manual (e.g. thesauri, WordNet)

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"Vector Space" Methods

- Treat words as points in \mathbb{R}^n (eg Shuetze, 93)
- Form matrix of co-occurrence counts
- SVD or similar to reduce rank (cf LSA)
- Cluster projections
- People worried about things like: log of counts, U vs $U\Sigma$

w *M* context counts

w *U* *Σ* *V* context counts

This is actually more of an embedding method (but we didn't want that in 1993)

Cluster these 50-200 dim vectors instead.

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Models: Brown Clustering

- Classic model-based clustering (Brown et al, 92)

- Each word starts in its own cluster
- Each cluster has co-occurrence stats
- Greedily merge clusters based on a mutual information criterion
- Equivalent to optimizing a class-based bigram LM.

$$P(w_i|w_{i-1}) = P(c_i|c_{i-1})P(w_i|c_i)$$

- Produces a dendrogram (hierarchy) of clusters



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Embeddings

Most slides from Greg Durrett

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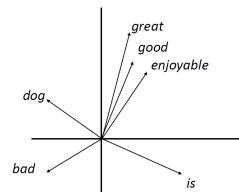


Embeddings

- Embeddings map discrete words (eg $|V| = 50k$) to continuous vectors (eg $d = 100$)

- Why do we care about embeddings?
 - Neural methods want them
 - Nuanced similarity possible; generalize across words

- We hope embeddings will have structure that exposes word correlations (and thereby meanings)



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Embedding Models

- Idea: compute a representation of each word from co-occurring words

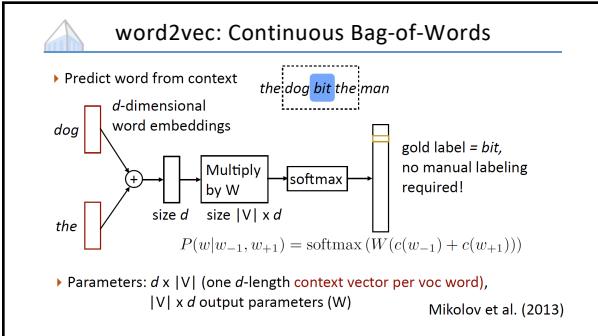
the dog bit the man



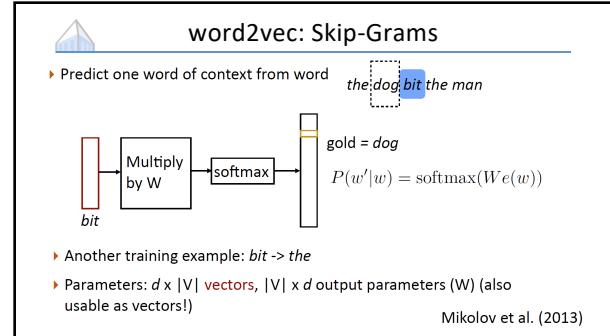
Token-Level

- We'll build up several ideas that can be mixed-and-matched and which frequently get used in other contexts

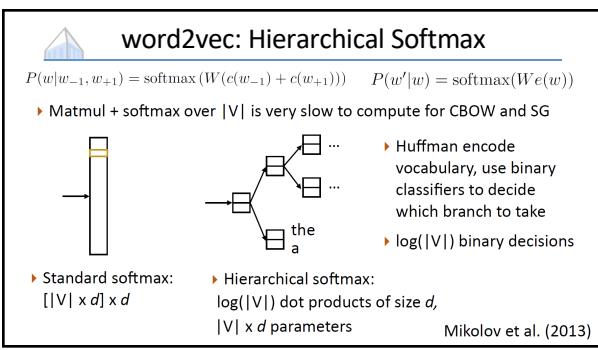
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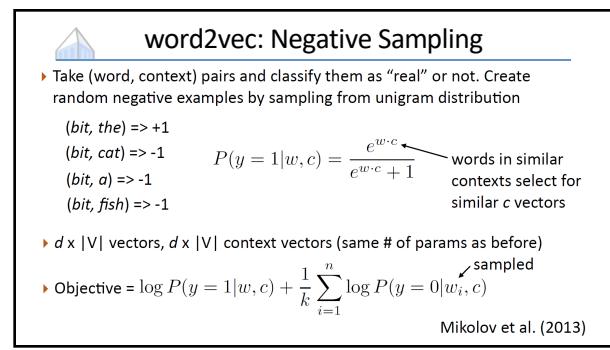
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fastText: Character-Level Models

- Same as SGNS, but break words down into n-grams with $n = 3$ to 6 where:

3-grams: <wh, whe, her, ere, re>
 4-grams: <whe, wher, here, ere>,
 5-grams: <wher, where, here,>,
 6-grams: <where, where>

► Replace $w \cdot c$ in skip-gram computation with $\left(\sum_{g \in \text{igrams}} w_g \cdot c \right)$

- Advantages?

Bojanowski et al. (2017)

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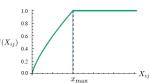


GloVe

- Idea: Fit co-occurrence matrix directly (weighted least squares)



$$J = \sum_{i,j=1}^V f(X_{ij}) (w_i^T \bar{w}_j + b_i + \bar{b}_j - \log X_{ij})^2$$



- Type-level computations (so constant in data size)
- Currently the most common word embedding method

Pennington et al, 2014

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Bottleneck vs Co-occurrence

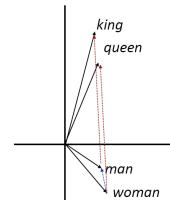
- Two main views of inducing word structure
 - Co-occurrence: model which words occur in similar contexts
 - Bottleneck: model latent structure that mediates between words and their behaviors
- These turn out to be closely related!

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Structure of Embedding Spaces

- How can you fit 50K words into a 64-dimensional hypercube?
- Orthogonality: Can each axis have a global "meaning" (number, gender, animacy, etc)?
- Global structure: Can embeddings have algebraic structure (eg king – man + woman = queen)?



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Bias in Embeddings

- Embeddings can capture biases in the data! (Bolukbasi et al 16)

$$\overrightarrow{\text{man}} - \overrightarrow{\text{woman}} \approx \overrightarrow{\text{king}} - \overrightarrow{\text{queen}}$$

- Debiasing methods (as in Bolukbasi et al 16) are an active area of research

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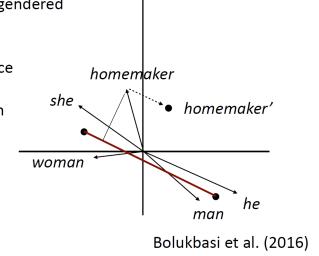


Debiasing?

- ▶ Identify gender subspace with gendered words

- ▶ Project words onto this subspace

- ▶ Subtract those projections from the original word



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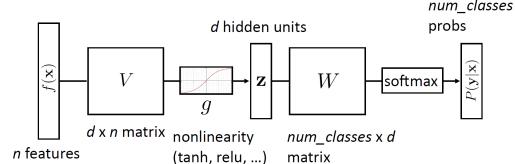
Neural Language Models

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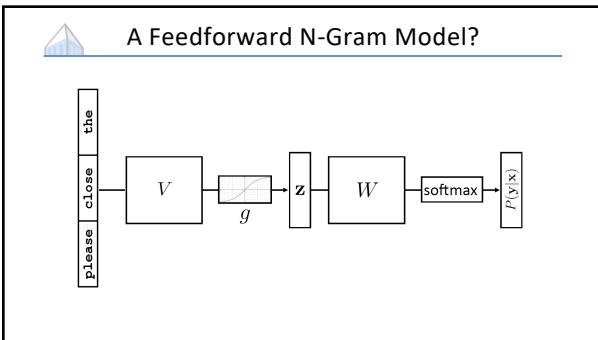


Reminder: Feedforward Neural Nets

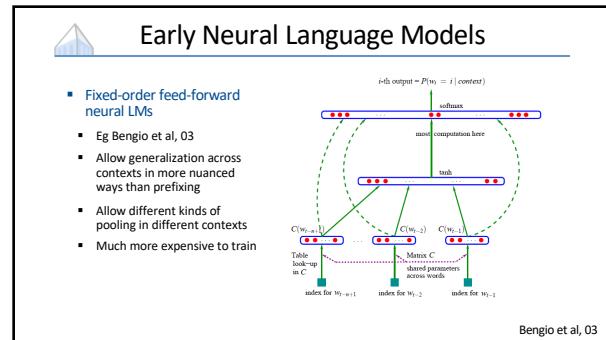
$$P(\mathbf{y}|\mathbf{x}) = \text{softmax}(Wg(Vf(\mathbf{x})))$$



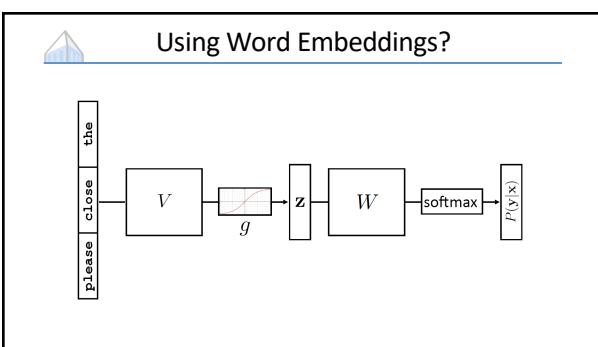
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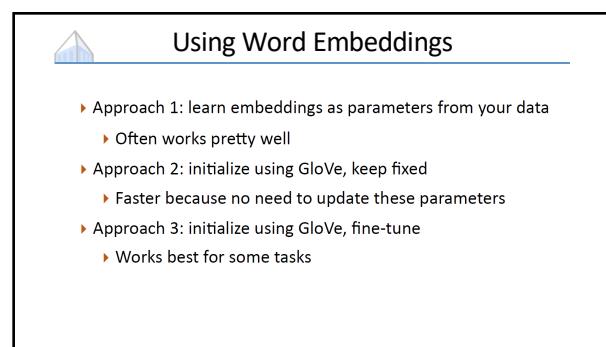
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Limitations of Fixed-Window NN LMs?

- What have we gained over N-Grams LMs?
- What have we lost?
- What have we not changed?

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Recurrent NNs

Slides from Greg Durrett / UT Austin, Abigail See / Stanford

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RNNs

- ▶ Feedforward NNs can't handle variable length input: each position in the feature vector has fixed semantics



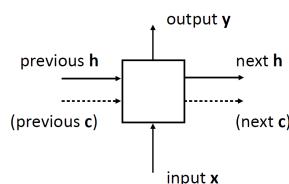
- ▶ These don't look related (*great* is in two different orthogonal subspaces)
- ▶ Instead, we need to:
 - 1) Process each word in a uniform way
 - 2) ...while still exploiting the context that that token occurs in

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General RNN Approach

- ▶ Cell that takes some input x , has some hidden state h , and updates that hidden state and produces output y (all vector-valued)



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RNN Uses

- Transducer: make some prediction for each element in a sequence
- Acceptor/encoder: encode a sequence into a fixed-sized vector and use that for some purpose

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Basic RNNs

$h_t = \tanh(Wx_t + Vh_{t-1} + b_h)$

$y_t = \tanh(Uh_t + b_y)$

- Updates hidden state based on input and current hidden state
- Computes output from hidden state

Long history! (invented in the late 1980s)

Elman (1990)

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Training RNNs

- "Backpropagation through time": build the network as one big computation graph, some parameters are shared
- RNN potentially needs to learn how to "remember" information for a long time!
- it was my favorite movie of 2016, though it wasn't without problems -> +
 - "Correct" parameter update is to do a better job of remembering the sentiment of *favorite*

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Problem: Vanishing Gradients

- Contribution of earlier inputs decreases if matrices are contractive (first eigenvalue < 1), non-linearities are squashing, etc
- Gradients can be viewed as a measure of the effect of the past on the future
- That's a problem for optimization but also means that information naturally decays quickly, so model will tend to capture local information

Next slides adapted from Abigail See / Stanford

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Core Issue: Information Decay

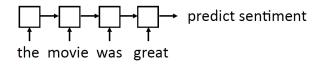
- The main problem is that it's too difficult for the RNN to learn to preserve information over many timesteps.
- In a vanilla RNN, the hidden state is constantly being rewritten

$$h^{(t)} = \sigma(W_h h^{(t-1)} + W_x x^{(t)} + b)$$
- How about a RNN with separate memory?

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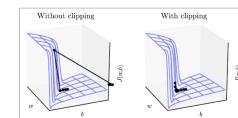


Problem: Exploding Gradients



Gradients can also be too large

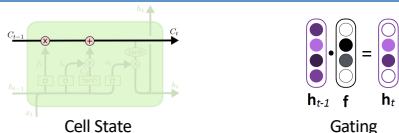
- Leads to overshooting / jumping around the parameter space
- Common solution: gradient clipping



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Key Idea: Propagated State



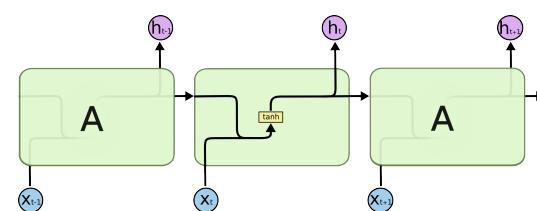
- Information decays in RNNs because it gets multiplied each time step
- Idea: have a channel called the *cell state* that by default just gets propagated (the "conveyer belt")
- Gates make explicit decisions about what to add / forget from this channel

Image: <https://colah.github.io/posts/2015-08-Understanding-LSTMs/>

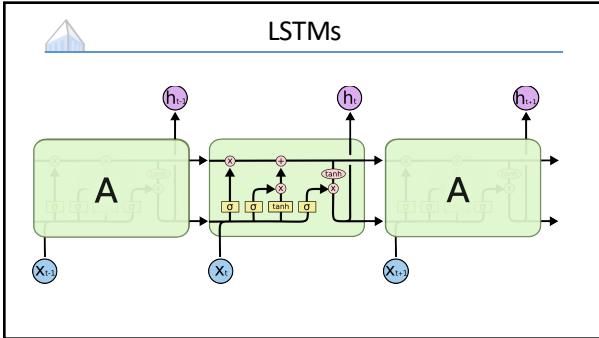
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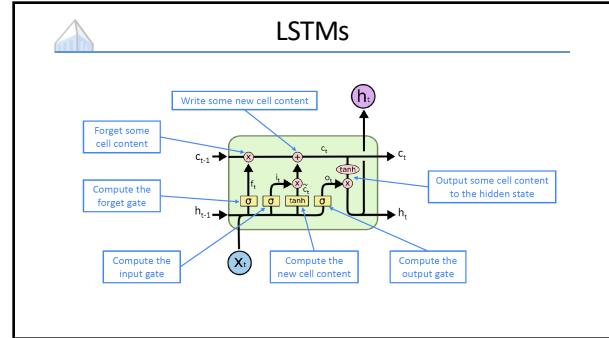
RNNs



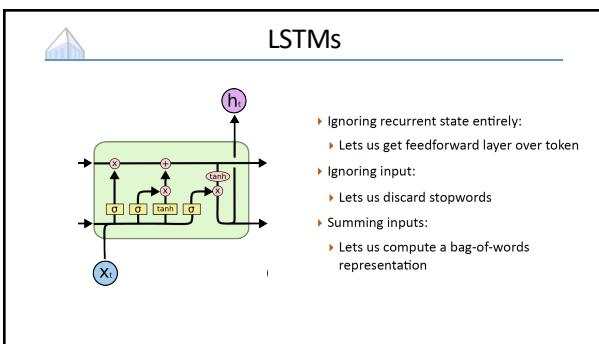
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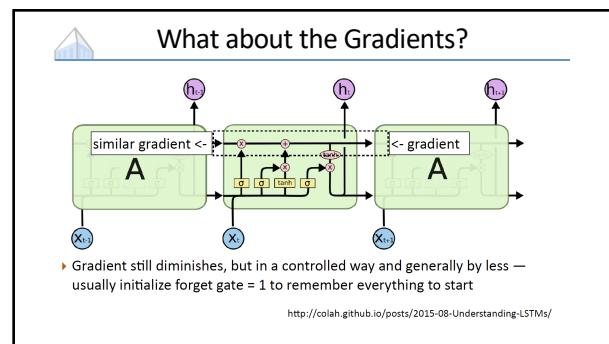
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Gated Recurrent Units (GRUs)

Update gate: controls what parts of hidden state are updated vs preserved

$$u^{(t)} = \sigma(W_u h^{(t-1)} + U_u x^{(t)} + b_u)$$

Reset gate: controls what parts of previous hidden state are used to compute new content

$$r^{(t)} = \sigma(W_r h^{(t-1)} + U_r x^{(t)} + b_r)$$

New hidden state content: reset gate selects useful parts of prev hidden state. Use this and current input to compute new hidden content.

$$\tilde{h}^{(t)} = \tanh(W_h(r^{(t)} \circ h^{(t-1)}) + U_h x^{(t)} + b_h)$$

Hidden state: update gate simultaneously controls what is kept from previous hidden state, and what is updated to new hidden state content

$$h^{(t)} = (1 - u^{(t)}) \circ h^{(t-1)} + u^{(t)} \circ \tilde{h}^{(t)}$$

How does this solve vanishing gradient?
Like LSTM, GRU makes it easier to retain info long-term (e.g. by setting update gate to 0)

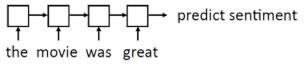
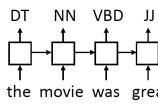
73

Uses of RNNs

Slides from Greg Durrett / UT Austin

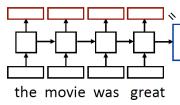
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Reminder: Tasks for RNNs

- Sentence Classification (eg Sentiment Analysis)
 
- Transduction (eg Part-of-Speech Tagging, NER)
 
- Encoder/Decoder (eg machine translation)

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Encoder / Decoder Preview



Encoding of the sentence — can pass this to a decoder or make a classification decision about the sentence

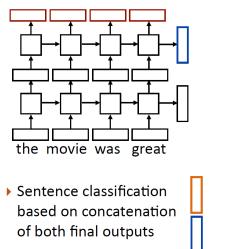
Encoding of each word — can pass this to another layer to make a prediction (can also pool these to get a different sentence encoding)

RNN can be viewed as a transformation of a sequence of vectors into a sequence of context-dependent vectors

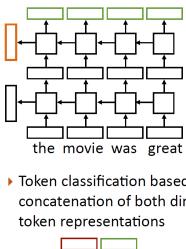
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Multilayer and Bidirectional RNNs



- ▶ Sentence classification based on concatenation of both final outputs

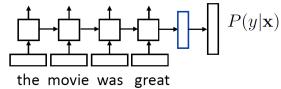


- ▶ Token classification based on concatenation of both directions' token representations

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Training for Sentential Tasks

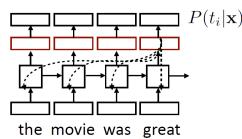


- ▶ Loss = negative log likelihood of probability of gold label (or use SVM or other loss)
- ▶ Backpropagate through entire network
- ▶ Example: sentiment analysis

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Training for Transduction Tasks



- ▶ Loss = negative log likelihood of probability of gold predictions, summed over the tags
- ▶ Loss terms filter back through network
- ▶ Example: language modeling (predict next word given context)

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Example Sentential Task: NL Inference

Premise		Hypothesis
A boy plays in the snow	<i>entails</i>	A boy is outside
A man inspects the uniform of a figure	<i>contradicts</i>	The man is sleeping
An older and younger man smiling	<i>neutral</i>	Two men are smiling and laughing at cats playing

- ▶ Long history of this task: "Recognizing Textual Entailment" challenge in 2006 (Dagan, Glickman, Magnini)
- ▶ Early datasets: small (hundreds of pairs), very ambitious (lots of world knowledge, temporal reasoning, etc.)

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SNLI Dataset

- ▶ Show people captions for (unseen) images and solicit entailed / neutral / contradictory statements
- ▶ >500,000 sentence pairs
- ▶ Encode each sentence and process
- 100D LSTM: 78% accuracy
- 300D LSTM: 80% accuracy
(Bowman et al., 2016)
- 300D BiLSTM: 83% accuracy
(Liu et al., 2016)
- ▶ Later: better models for this

Bowman et al. (2015)

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Visualizing RNNs

Slides from Greg Durrett / UT Austin

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LSTMs Can Model Length

- ▶ Train *character* LSTM language model (predict next character based on history) over two datasets: War and Peace and Linux kernel source code
- ▶ Visualize activations of specific cells (components of c) to understand them
- ▶ Counter: know when to generate $\backslash n$

The sole importance of the crossing of the Seerine lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the impossibility of the only possible line of action--the one which the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at the first alarm, and the Russian army, instead of pursuing them, reached its goal. It fled like a wounded animal and it was impossible to stop it. The French had no time to make any preparations for crossing as by what took place at the bridges. When the bridges were broken, all the transports, all the horses, all the men, all the women who were with the French transport, all...carried on by vis inertiae...pressed forward into boats and into the ice-covered water and did not...surrender.

Karpathy et al. (2015)

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LSTMs Can Model Long-Term Bits

- ▶ Train *character* LSTM language model (predict next character based on history) over two datasets: War and Peace and Linux kernel source code
- ▶ Visualize activations of specific cells to see what they track
- ▶ Binary switch: tells us if we're in a quote or not

"You seem to imply that I have nothing to eat out of....on the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he uttered to win over his audience and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."

Karpathy et al. (2015)

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 **LSTMs Can Model Stack Depth**

- ▶ Train *character* LSTM language model (predict next character based on history) over two datasets: War and Peace and Linux kernel source code
- ▶ Visualize activations of specific cells to see what they track
- ▶ Stack: activation based on indentation

```
#ifdef CONFIG_AUDIT_SYSCALL
static inline int audit_watch_bits(int class, int mask)
{
    if (class >= AUDIT_WATCH_MAX)
        return -1;
    if (task->audit_watches[class] & mask)
        return 0;
    task->audit_watches[class] |= mask;
    return 1;
}
#endif
```

Karpathy et al. (2015)

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 **LSTMs Can Be Completely Inscrutable**

- ▶ Train *character* LSTM language model (predict next character based on history) over two datasets: War and Peace and Linux kernel source code
- ▶ Visualize activations of specific cells to see what they track
- ▶ Uninterpretable: probably doing double-duty, or only makes sense in the context of another activation

```
/* Unpack a filter face's string representation from user-space
 * buffer */
char audit_unpack_string(void *buffer, size_t remain, size_t len)
{
    char *buf = (char *)buffer;
    if (len == 0 || (len <= 0) || (len <= remain))
        return ERR_PTR(-EINVAL);
    /* Of the currently implemented string fields, PATH_MAX
     * defines the longest valid length */
}
```

Karpathy et al. (2015)

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