0.1 API

```
package com.ncalathus.sample.ring.api;
public interface IAbstractRing {
    public interface CLASS<REP extends INST> {
        REP zero();
        REP unit();
        REP neg_unit();
}

public interface INST<REP extends INST> {
        CLASS<REP> CLASS();
        REP add(REP elem);
        REP subst(REP elem);
        REP mult(REP elem);
}
```

```
package com.ncalathus.sample.ring.api;

public interface INumericRing {
    interface CLASS<N extends Number, REP extends INST<N, REP>> extends IAbst
        REP create(N n);
    }

interface INST<N extends Number, REP extends INST<N, REP>> extends IAbstr
        @Override
        CLASS<N, REP> CLASS();
    }
}
```

```
package com.ncalathus.sample.ring.api;
import java.util.Map;
public interface IPolynomialRing {
    interface CLASS<
            C_INST extends IAbstractRing.INST<C_INST>, C_CLASS extends IAbstr
            REP extends INST<C_INST, C_CLASS, REP>
       > extends IAbstractRing.CLASS<REP> {
        C_CLASS coefficientRing();
        REP variable (int degree);
        REP create(int degree, C_INST c);
        REP create(final Map<Integer, C_INST> terms);
        REP create(final C_INST... coeffs);
    }
    interface INST<
            C_INST extends IAbstractRing.INST<C_INST>, C_CLASS extends IAbstr
            REP extends INST<C_INST, C_CLASS, REP>
        > extends IAbstractRing.INST<REP> {
        @Override
        CLASS<C_INST, C_CLASS, REP> CLASS();
        int degree();
        C_INST coefficient (int degree);
       REP r_mult(C_INST coeff);
    }
}
```

0.2 Representation

```
package com.ncalathus.sample.ring.rep;
import com.ncalathus.sample.ring.api.*;
// this class allows the all elements of NumericRing to have the same class u
// Meta class must be used to share the same generic type for static and inste
// Also these static/instance has recuresive references, so outer classes must
// (see NumricRing in the INumericRing_Static<N, NumericRing> for NumericRing
public class NumericRing<N extends Number> implements IAbstractRing {
    protected final Class<N> _nCls;
    protected final CLASS _class;
    protected NumericRing(final Class<N> nCls) {
        this._nCls = nCls;
        this._class = new CLASS();
    }
    // this is an entry point.
    //\ all\ instance\ of\ NumericRing\ are\ cretated\ from\ NumericRingStatic
    // this gurantee, those elements has the same element type.
    public CLASS getCLASS() {
        return _class;
    }
    public static <N extends Number> NumericRing<N>.CLASS CLASS(Class<N> cls)
        return new NumericRing<N>(cls).getCLASS();
    //
    public class CLASS implements INumericRing.CLASS<N, INST> {
        private final INST _zero;
        private final INST _unit;
        private final INST _neg_unit;
        CLASS() {
            this._zero = new INST(create_zero(_nCls));
            this._unit = new INST(create_unit(_nCls));
            this._neg_unit = new INST(create_neg_unit(_nCls));
        public INST zero() { return _zero; }
        public INST unit() { return _unit; }
        public INST neg_unit() { return _neg_unit; }
        public INST create(N n) {
```

```
return new INST(n);
}
final N create_zero(Class<N> nCls) {
    if (nCls.equals(Short.class)) {
        return (N)new Short((short)0);
    } else if (nCls.equals(Integer.class)) {
        return (N)new Integer (0);
    } else if (nCls.equals(Long.class)) {
        return (N)new Long(0);
    } else if (nCls.equals(Float.class)) {
        return (N)new Float (0);
    } else if (nCls.equals(Double.class)) {
        return (N)new Double (0);
    } else {
        throw new RuntimeException("bug");
private N create_unit(Class<N> nCls) {
    if (nCls.equals(Short.class))
        return (N)new Short ((short)1);
    } else if (nCls.equals(Integer.class)) {
        return (N)new Integer (1);
    } else if (nCls.equals(Long.class)) {
        return (N)new Long (1);
    } else if (nCls.equals(Float.class)) {
        return (N)new Float (1);
    } else if (nCls.equals(Double.class)) {
        return (N)new Double (1);
    } else {
        throw new RuntimeException("bug");
}
private N create_neg_unit(Class<N> nCls) {
    if (nCls.equals(Short.class)) {
        return (N)new Short ((short)(-1));
    } else if (nCls.equals(Integer.class)) {
        return (N)new Integer (-1);
    } else if (nCls.equals(Long.class)) {
        return (N)new Long(-1);
    } else if (nCls.equals(Float.class)) {
        return (N)new Float (-1);
    } else if (nCls.equals(Double.class)) {
        return (N)new Double (-1);
    } else {
        throw new RuntimeException("bug");
```

```
}
   }
}
public class INST implements INumericRing.INST<N, INST> {
    // this is to enforce the interface requirement.
    @Override
    public CLASS CLASS() {
        return _class;
    private final N i;
    INST(final N i) {
        \mathbf{this}.\ \mathrm{i}\ =\ \mathrm{i}\ ;
    }
    @Override
    public INST add(final INST elem) {
        return new INST(add(i, elem.i));
    @Override
    public INST subst(final INST elem) {
        return new INST(subst(i, elem.i));
    @Override
    public INST mult(final INST elem) {
        return new INST(mult(i, elem.i));
    @Override
    public String toString() {
        return ""+i;
    @Override
    public boolean equals(Object obj) {
        if (obj instanceof NumericRing.INST) {
            INST inst = (INST)obj;
             return i.equals(inst.i);
        } else {
            return false;
    }
```

@Override

```
public int hashCode() {
    return i.hashCode();
private N add(final N n1, final N n2) {
    if (n1 = null \mid | n2 = null) {
        throw new RuntimeException("add_for_null_is_not_supported");
    if (n1 instanceof Short) {
        final short i1 = (Short)n1;
        final short i2 = (Short)n2;
        return (N)new Short((short)(i1+i2));
    } else if (n1 instanceof Integer) {
        final int i1 = (Integer)n1;
        final int i2 = (Integer)n2;
        return (N)new Integer (i1+i2);
    } else if (n1 instanceof Long) {
        final long i1 = (Long)n1;
        final long i2 = (Long)n2;
        return (N)new Long(i1+i2);
    } else if (n1 instanceof Long) {
        final long i1 = (Long)n1;
        final long i2 = (Long)n2;
        return (N)new Long(i1+i2);
    } else if (n1 instanceof Float) {
        final float i1 = (Float)n1;
        final float i2 = (Float)n2;
        return (N)new Float (i1+i2);
    } else if (n1 instanceof Double) {
        final double i1 = (Double) n1;
        final double i2 = (Double)n2;
        return (N)new Double(i1+i2);
    } else {
        throw new RuntimeException ("bug");
private N subst(final N n1, final N n2) {
    if (n1 = null \mid | n2 = null) {
        throw new RuntimeException ("add_for_null_is_not_supported");
    if (n1 instanceof Short) {
        final short i1 = (Short)n1;
        final short i2 = (Short)n2;
        return (N)new Short((short)(i1-i2));
    } else if (n1 instanceof Integer) {
```

```
final int i1 = (Integer)n1;
        final int i2 = (Integer)n2;
        return (N)new Integer (i1-i2);
    } else if (n1 instanceof Long) {
        final long i1 = (Long)n1;
        final long i2 = (Long)n2;
        return (N)new Long(i1-i2);
    } else if (n1 instanceof Long) {
        final long i1 = (Long)n1;
        final long i2 = (Long)n2;
        return (N)new Long(i1-i2);
    } else if (n1 instanceof Float) {
        final float i1 = (Float)n1;
        final float i2 = (Float)n2;
        return (N)new Float(i1-i2);
    } else if (n1 instanceof Double) {
        final double i1 = (Double) n1;
        final double i2 = (Double)n2;
        return (N)new Double(i1-i2);
    } else {
        throw new RuntimeException("bug");
    }
private N mult(final N n1, final N n2) {
    if (n1 = null \mid | n2 = null) {
        throw new RuntimeException("add_for_null_is_not_supported");
    if (n1 instanceof Short) {
        final short i1 = (Short)n1;
        final short i2 = (Short)n2;
        return (N)new Short((short)(i1*i2));
    } else if (n1 instanceof Integer) {
        final int i1 = (Integer)n1;
        final int i2 = (Integer)n2;
        return (N)new Integer (i1*i2);
    } else if (n1 instanceof Long) {
        final long i1 = (Long)n1;
        final long i2 = (Long)n2;
        return (N)new Long(i1*i2);
    } else if (n1 instanceof Long) {
        final long i1 = (Long)n1;
        final long i2 = (Long)n2;
        return (N)new Long(i1*i2);
    } else if (n1 instanceof Float) {
        final float i1 = (Float)n1;
        final float i2 = (Float)n2;
```

```
return (N)new Float(i1*i2);
                                                  } else if (n1 instanceof Double) {
                                                                  final double i1 = (Double) n1;
                                                                   final double i2 = (Double)n2;
                                                                  return (N)new Double(i1*i2);
                                                  } else {
                                                                  throw new RuntimeException("bug");
                                                  }
                                 }
                }
                public static void main(String[] args) {
                                 /\!/ NumericRing < Integer > integerRing = new \ NumericRing < Integer > (Integer > integer)
                                 //final\ NumericRing < Integer > .CLASS\ Integer Ring = new\ NumericRing < Integer Ring = new\ NumericRing
                                  final NumericRing<Integer > .CLASS IntegerRing = NumericRing .CLASS(Inte
                                  final NumericRing<Integer >.INST nr1 = IntegerRing.create(7);
                                  final NumericRing<Integer >. INST nr2 = IntegerRing.create(9);
                                  final NumericRing<Integer >.INST nr3 = nr1.mult(nr2);
                                 System.out.println(">>\negnr3:\neg"+nr3);
                 }
}
```

```
package com.ncalathus.sample.ring.rep;
import com.ncalathus.sample.ring.api.IAbstractRing;
import com.ncalathus.sample.ring.api.IPolynomialRing;
import java.util.ArrayList;
import java.util.Collections;
import java.util.HashSet;
import java.util.List;
import java.util.Map;
import java.util.Set;
public class PolynomialRing<C_INST extends IAbstractRing.INST<C_INST>, C_CLAS
    protected final C_CLASS _coeffCls;
    protected CLASS _class;
    protected final String variable;
    protected PolynomialRing(final C_CLASS coeffCls, final String variable) {
        this._coeffCls = coeffCls;
        this.variable = variable;
        initCLASS();
    }
    /\!/\ this\ should\ be\ overl; oaded\ by\ subclass\ if\ CLASS\ is\ redefined\ thee.
    protected void initCLASS() {
        this._class = new CLASS();
    // this is an entry point.
    // all instance of NumericRing are cretated from NumericRingStatic
    // this gurantee, those elements has the same element type.
    /\!/\ this\ should\ be\ overl; oaded\ by\ subclass\ if\ CLASS\ is\ redefined\ thee.
    public CLASS getCLASS() {
        return _class;
    public static <C_INST extends IAbstractRing.INST<C_INST>, C_CLASS extends
        return new PolynomialRing < C.INST, C.CLASS > (cls, variable).getCLASS();
    public class Term {
        final int degree;
        final C_INST c;
        Term(final int degree, final C_INST c) {
            this.degree = degree;
```

```
\mathbf{this} \cdot \mathbf{c} = \mathbf{c};
}
Term r_mult(final C_INST c1) {
    final C_INST c2 = c.mult(c1);
    return new Term(degree, c2);
Term mult(final Term term) {
    return new Term(degree+term.degree, c.mult(term.c));
@Override
public String toString() {
    return "("+c+")"+termString();
public String termString() {
    if (degree = 0) {
        return "";
    } else if (degree == 1) {
        return variable;
    } else {
        return variable+"^"+degree;
}
public String toString(final String vars) {
    return "("+c+")"+termString(vars);
public String termString(final String vars) {
    if (degree == 0) {
        return vars;
    } else {
        return termString()+((vars.isEmpty())?"":("*"+vars));
}
@Override
public boolean equals(Object obj) {
    if (obj instanceof PolynomialRing.Term) {
        Term term = (Term) obj;
        return degree == term.degree && c == term.c;
    } else {
        return false;
@Override
public int hashCode() {
    return degree+137*c.hashCode();
```

```
}
}
//
public class CLASS implements IPolynomialRing.CLASS<CLINST, C-CLASS, INST.
    private final INST _zero;
    private final INST _unit;
    private final INST _neg_unit;
    CLASS() {
        this._zero = create(0, _coeffCls.zero());
        this._unit = create(0, _coeffCls.unit());
        this._neg_unit = create(0, _coeffCls.neg_unit());
    }
    public INST zero() { return _zero; }
    public INST unit() { return _unit; }
    public INST neg_unit() { return _neg_unit; }
    @Override
    public C_CLASS coefficientRing() {
        return _coeffCls;
    @Override
    public INST variable(int degree) {
        return new INST(degree, _coeffCls.unit());
    @Override
    public final INST create(int degree, C_INST c) {
        return new INST (degree, c);
    @Override
    public final INST create(final Map<Integer, C_INST> terms) {
        return new INST(new ArrayList<Term>() {{
            for (final Map.Entry<Integer, C_INST> term: terms.entrySet())
                add(new Term(term.getKey(), term.getValue()));
        }});
    }
    @Override
    public final INST create(final C_INST... coeffs) {
        return new INST(new ArrayList<Term>() {{
```

```
int degree = coeffs.length-1;
             \mathbf{for} \ (\mathbf{int} \ \mathbf{i} = \mathtt{degree}\,; \ \mathbf{i} >= 0\,; \ \mathbf{i} -\!\!\!-\!\!\!) \ \{
                 final C_INST c = coeffs[i];
                 if (!c.equals(_coeffCls.zero())) {
                      add(new Term(degree-i, c));
        }});
    }
}
public class INST implements IPolynomialRing.INST<C_INST, C_CLASS, INST>
    // this is to enforce the interface requirement.
    @Override
    public CLASS CLASS() {
        return _class;
    private final List<Term> terms;
    protected INST(final int degree, final C_INST c) {
         this.terms = new ArrayList<Term>();
        terms.add(new Term(degree, c));
    protected INST(final List<Term> terms) {
         this.terms = normalize(terms);
    protected INST() {
        this.terms = new ArrayList<Term>();
    }
    private List<Term> normalize(List<Term> terms) {
         final Set<Integer> degrees = new HashSet<Integer>();
        for (final Term term: terms) {
             degrees.add(term.degree);
        final List<Integer> sorted_degrees = new ArrayList<Integer>(degre
         Collections.sort(sorted_degrees, Collections.reverseOrder());
         final List < Term > norm = new ArrayList < Term > ();
         for (final Integer degree: sorted_degrees) {
            final C_INST c0 = sumCoeff(degree, terms);
            if (!c0.equals(_coeffCls.zero())) {
                norm.add(new Term(degree, c0));
        }
        return norm;
```

```
private C_INST sumCoeff(int degree, List<Term> terms) {
    C_{INST} c = _{coeffCls.zero()};
    for (final Term term: terms) {
        if (term.degree == degree) {
            c = c.add(term.c);
        }
    }
    {f return} c;
}
@Override
public int degree() {
    if (terms.isEmpty()) {
        return 0;
    return terms.get(0).degree;
}
@Override
public C_INST coefficient(int degree) {
    for (final Term term: terms) {
        if (term.degree == degree) {
            return term.c;
    }
    return _coeffCls.zero();
}
@Override
public INST add(final INST elem) {
    return new INST(new ArrayList<Term>(){{
        addAll(INST.this.terms);
        addAll(elem.terms);
    } } );
}
@Override
public INST subst(final INST elem) {
    return add(elem.r_mult(_coeffCls.neg_unit()));
@Override
public INST mult(final INST elem) {
    return new INST(new ArrayList<Term>(){{
        for (final Term term1: terms) {
            for (final Term term2: elem.terms) {
                 add(term1.mult(term2));
            }
```

```
}});
}
 @Override
 public INST r_mult(final C_INST c) {
    return new INST(new ArrayList<Term>(){{
         for (final Term term: terms) {
             add(term.r_mult(c));
     }});
}
 @Override
public String toString() {
     final StringBuilder sb = new StringBuilder();
    return toString(sb, "");
 }
public String toString(final StringBuilder sb, final String vars) {
     //final\ StringBuilder\ sb\ =\ new\ StringBuilder\ ();
     boolean is_first = true;
     for (final Term term: terms) {
         if (is_first) {
             is_first = false;
         } else {
             sb.append("+");
         if (term.c instanceof PolynomialRing.INST) {
             final INST inst = (PolynomialRing.INST) term.c;
             final String term0 = term.termString();
             final String vars0 = (vars.isEmpty())?term0:(vars+"*"+term
             inst.toString(sb, vars0);
         } else {
             sb.append(term.toString(vars));
     }
    return sb.toString();
}
 @Override
 public boolean equals(Object obj) {
     if (obj instanceof PolynomialRing.INST) {
         INST inst = (INST) obj;
```

```
return equalTerms(inst.terms);
            } else {
               return false;
        @Override
        public int hashCode() {
            int i = 0;
            for (Term term: terms) {
                i += term.hashCode();
           return i;
       private boolean equalTerms(List<Term> terms0) {
            final int size = terms.size();
            if (terms0.size() != size) {
                return false;
            for (int i = 0; i < size; i++) {
                if (!terms.get(i).equals(terms0.get(i))) {
                   return false;
           return true;
        }
    }
    public static void main(String[] args) {
            //final\ PolynomialRing < NIntegerRing. INST, NIntegerRing. CLASS>.CLA
            final PolynomialRing<NIntegerRing.INST, NIntegerRing.CLASS>.CLASS
            final NIntegerRing.CLASS coeffCls = IntPolynomialRing.coefficientF
            final PolynomialRing<NIntegerRing.INST, NIntegerRing.CLASS>.INST
            final PolynomialRing<NIntegerRing.INST, NIntegerRing.CLASS>.INST
            final PolynomialRing<NIntegerRing.INST, NIntegerRing.CLASS>.INST
           }
   }
}
```

```
package com.ncalathus.sample.ring.rep;
import com.ncalathus.sample.ring.api.IPolynomialRing;
import java.util.HashMap;
public class NumericPolynomialRing<N extends Number> extends PolynomialRing<N
           protected NumericPolynomialRing(final NumericRing<N>.CLASS coeffCls, fina
                     super(coeffCls , variable);
           public class CLASS extends PolynomialRing<NumericRing<N>.INST, NumericRing
                     public final INST create(final N... coeffs) {
                                return create (new HashMap<Integer, NumericRing<N>.INST>() {{
                                           int degree = coeffs.length-1;
                                           \mathbf{for} \ (\mathbf{int} \ \mathbf{i} = 0; \ \mathbf{i} <= \mathbf{degree}; \ \mathbf{i} +\!\!+\!\!) \ \{
                                                      final NumericRing<N>.INST c = _coeffCls.create(coeffs[i])
                                                             (!c.equals(_coeffCls.zero())) {
                                                                put(degree-i, c);
                                }});
                     }
           @Override
           protected void initCLASS() {
                      this._class = new CLASS();
           @Override
           public CLASS getCLASS() {
                     return (CLASS) _class;
           public static <N extends Number> NumericPolynomialRing<N>.CLASS CLASS (fin
                     return new NumericPolynomialRing(nCls, variable).getCLASS();
           static void test_int_1() {
                     System.out.println("-
                                                                                              ---_test_int_1_-");
                      final NumericPolynomialRing < Integer > .CLASS NIntPolynomialRing = NumericPolynomialRing = NumericPol
                      final NumericRing<Integer > .CLASS coeffCls = NIntPolynomialRing.coeffic
                                final NumericPolynomialRing<Integer>.INST nr1 = NIntPolynomialRing
                                final NumericPolynomialRing<Integer>.INST nr2 = NIntPolynomialRing
```

final NumericPolynomialRing<Integer >.INST nr3 = nr1.mult(nr2);

```
System.out.println(">> \_nr2 : \_"+nr2 );
                              System.out.println(">>\negnr3:\neg"+nr3);
                    // this looks strange, but it is OK, since subclass deosn of define \it C
same inner class in byte code level.
                               final IntPolyRing.INST nr1 = NIntPolynomialRing.create(7, coeffCl
                               final IntPolyRing.INST nr2 = NIntPolynomialRing.create(5, coeffCl
                               final IntPolyRing.INST nr3 = nr1.mult(nr2);
                              System.out.println(">>¬nr1:¬"+nr1);
System.out.println(">>¬nr2:¬"+nr2);
                              System.out.println(">>> nr3:  "+nr3 );
                     }
          }
          static void test_int_2() {
                                                                                                  -_ t e s t _ i n t _ 2 _----
                     System.out.println("-
                     final NumericPolynomialRing < Integer > .CLASS NIntPolynomialRing = Nume
                     final NumericRing<Integer > .CLASS coeffCls = NIntPolynomialRing.coeffic
                               final\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomial Ring < Integer > npr = new\ Numeric Polynomi
                               final\ NumericPolynomialRing < Integer > .INST\ nr1 = npr.new\ INST() \ \{ \{ \} \} \}
                                         final\ Random\ rnd = new\ Random(10);
                                         for\ (int\ i = 0;\ i < 10;\ i++)\ \{
                                                    //int degree =
                                                    //add();
                                         }
                               }};
                               final NumericPolynomialRing<Integer>.INST nr1 = NIntPolynomialRing
                               final NumericPolynomialRing<Integer>.INST nr2 = NIntPolynomialRing
                               \label{eq:final_numericPolynomialRing} \textbf{Final} \ \ \text{NumericPolynomialRing} \\ < \text{Integer} > . \\ \text{INST} \ \ \text{nr3} = \\ \text{nr1.mult(nr2);}
                              System.out.println(">> \bot nr1: \bot"+nr1);
                              System.out.println(">>\perpnr2:\perp"+nr2);
                              System.out.println(">>\negnr3:\neg"+nr3);
                  (compiler) error case
           static\ void\ test\_int\_1a() {
                     final\ Numeric Polynomial Ring < Integer > .CLASS\ NInt Polynomial Ring = Nume
```

 $final\ Numeric Polynomial Ring < Integer > .INST\ nr1 = NIntPolynomial Ring$

```
final\ Numeric Polynomial Ring < Integer > .INST\ nr2 = NIntPolynomial Ring
                  final \ NumericPolynomialRing < Integer > . INST \ nr3 = nr1.mult(nr2);
                 System.out.println(">> nr3: "+nr3);
        // strange...
                  final\ IntPolyRing.INST\ nr1 = NIntPolynomialRing.create(7, coeffCl)
                  final\ IntPolyRing.INST\ nr2=NIntPolynomialRing.create (5,\ coeffCl
                  final\ IntPolyRing.INST\ nr3 = nr1.mult(nr2);
                 System.out.println(">>> nr3: "+nr3);
        }
}
// this looks type checking is not working as expected..
static void test_int_1b() {
                                                                         -- test_int_1b_-");
        System.out.println("-
         final NumericPolynomialRing < Integer > .CLASS NIntPolynomialRing = Nume
         final NIntegerRing.CLASS coeffCls = NIntPolynomialRing.coefficientRing
                  final NumericPolynomialRing<Integer>.INST nr1 = NIntPolynomialRing
                  final NumericPolynomialRing<Integer>.INST nr2 = NIntPolynomialRing
                  final NumericPolynomialRing<Integer >. INST nr3 = nr1.mult(nr2);
                 System.out.println(">>¬nr2:¬"+nr2);
                 System.out.println(">>\neg nr3: \neg "+nr3);
        // strange...
                  final IntPolyRing.INST nr1 = NIntPolynomialRing.create(7, coeffCl
                  final IntPolyRing.INST nr2 = NIntPolynomialRing.create(5, coeffCl
                  final IntPolyRing.INST nr3 = nr1.mult(nr2);
                 System.out.println(">>¬nr2:¬"+nr2);
                 System.out.println(">>>¬nr3:¬"+nr3);
         }
}
static void test_float_1() {
        System.out.println("-
                                                                      -----");
         final NumericPolynomialRing < Float > .CLASS NFloatPolynomialRing = NumericPolynomialRing = NumericPol
         final NumericRing<Float>.CLASS coeffCls = NFloatPolynomialRing.coeffic
                  final NumericPolynomialRing<Float>.INST nr1 = NFloatPolynomialRing
                  final NumericPolynomialRing<Float>.INST nr2 = NFloatPolynomialRing
```

final NumericPolynomialRing<Float > .INST nr3 = nr1.mult(nr2);

```
System.out.println(">> \_nr2 : \_"+nr2 );
                                     System.out.println(">>\_nr3:\_"+nr3);
                   }
}
static void test_float_2() {
                                                                                                                                                                  -_test_float_2____");
                   System.out.println("-
                   final NumericRing<Float>.CLASS FloatNumeral = NumericRing.CLASS(Float
                   final NumericPolynomialRing<Float>.CLASS NFloatPolynomialRing = Nume
                                      final NumericPolynomialRing<Float>.INST nr0 = NFloatPolynomialRing
                                      final NumericPolynomialRing<Float>.INST nr1 = NFloatPolynomialRing
                                      final NumericPolynomialRing<Float>.INST nr2 = NFloatPolynomialRing
                                      final NumericPolynomialRing<Float>.INST nr3 = NFloatPolynomialRing
                                      final NumericPolynomialRing<Float>.INST nr4 = NFloatPolynomialRing
                                      final NumericPolynomialRing<Float>.INST nr5 = NFloatPolynomialRing
                                      final NumericPolynomialRing<Float>.INST nr6 = nr1.mult(nr2);
                                      System.out.println(">>\neg nr1: \neg "+nr1);
                                     System.out.println(">>¬nr2:-"+nr2);
                                     System.out.println(">> \_nr3 : \_"+nr3);
                                      System.out.println(">> \_nr6: \_"+nr6);
                                      final PolynomialRing<NumericPolynomialRing<Float>.INST, NumericPolynomialRing<Float
                                      //final\ PolynomialRing < Numeric PolynomialRing < Float > .INST,\ Numeric P
                                      /\!/final\ PolynomialRing \!<\! NumericPolynomialRing \!<\! Float \!>\! .INST,\ NumericPolynomialRing \>\! .INST,\ NumericPolynomialRi
                                      //final\ PolynomialRing < Numeric PolynomialRing < Float > .INST,\ Numeric P
                                      final PolynomialRing<NumericPolynomialRing<Float>.INST, NumericPolynomialRing<Float
                                      final PolynomialRing<NumericPolynomialRing<Float>.INST, NumericPolynomialRing<Float
                                      final PolynomialRing<NumericPolynomialRing<Float>.INST, NumericPolynomialRing<Float
                                      System.out.println(">> \_nr1a: \_"+nr1a);
                                     System.out.println(">> \bot nr2a: \bot"+nr2a);
                                     System.out.println(">>¬nr3a:¬"+nr3a);
                   }
}
public static void main(String[] args) {
                    test_int_1();
                   test_int_1b ();
                    test_-float_-1 ();
```

```
*/
//test_int_2();
test_float_2();
}
```