

(101) (5)

$$W = \vec{F} \cdot \vec{s}$$

$$\vec{F} = \langle 2t, t^2 \rangle \text{ N}$$

$$\vec{s} = \langle 3, t/2 \rangle \text{ m}$$

$$\frac{dW}{dt} = \vec{F} \frac{d\vec{s}}{dt} + \vec{s} \frac{d\vec{F}}{dt}$$

$$W = \langle 2t, t^2 \rangle \cdot \langle 3, t/2 \rangle$$

$$W(t) = 6t + \frac{t^3}{2}$$

$$W(1) = 6.5 \text{ N}\cdot\text{m} = 6.5 \text{ J}$$

$$\frac{dw}{dt} = \vec{F} \frac{d}{dt}(\vec{s}) + \vec{s} \frac{d}{dt}(\vec{F})$$

$$\frac{dw}{dt} = \langle 2t, t^2 \rangle \cdot \langle 0, 1/2 \rangle + \langle 3, t/2 \rangle \cdot \langle 2, \pi \rangle$$

$$= (0 + t^2/2) + (6 + t^2)$$

$$= \frac{3t^2}{2} + 6$$

$$\frac{dw}{dt}(1) = 7.5 \frac{\text{m} \cdot \text{m}}{\text{s}} = 7.5 \frac{\text{J}}{\text{s}} = 7.5 \text{ W}$$

$$(6) \quad w = \int \vec{F} \cdot d\vec{s} \quad \text{lb} \quad \vec{F} = 6x\hat{i} - 2y\hat{j}$$

$$\text{ft} \quad d\vec{s} = dx\hat{i} + dy\hat{j}$$

$$\vec{F} \cdot d\vec{s} = \langle 6x, -2y \rangle \cdot \langle dx, dy \rangle$$

$$\vec{F} \cdot d\vec{s} = 6x dx - 2y dy$$

$$\int \vec{F} \cdot d\vec{s} = \int 6x dx - \int 2y dy$$

$$\int \vec{F} \cdot d\vec{s} = 3x^2 - y^2 + C$$

$$\int_0^5 \vec{F} \cdot d\vec{s} = 3x^2 \Big|_0^5 = 75 \text{ ft} \cdot \text{lb}$$

$$\int_0^5 \vec{F} \cdot d\vec{s} = -y^2 \Big|_0^5 = -25 \text{ ft} \cdot \text{lb}$$

$$(102) \text{ ① } \vec{u} = \langle 1, -2, 5 \rangle \quad \vec{u} + \vec{v} = \langle -2, -1, 4 \rangle$$

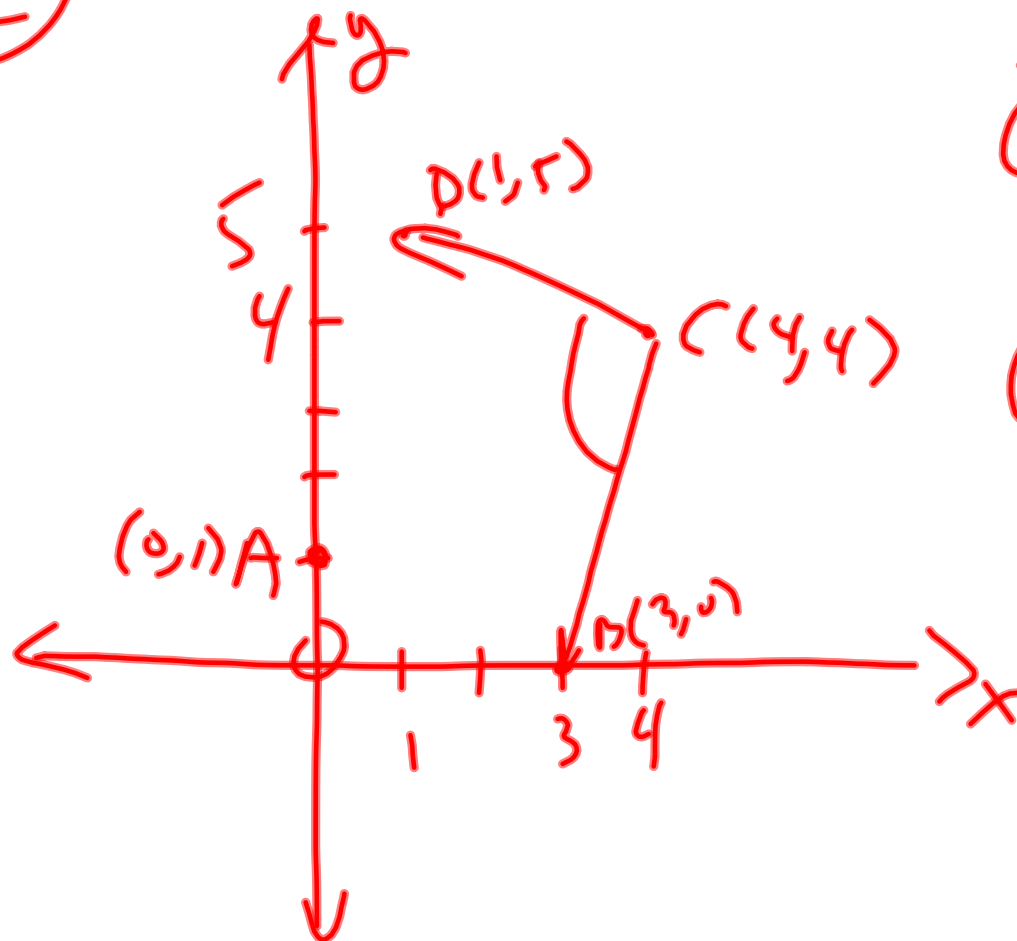
$$\vec{v} = \langle -3, 1, -1 \rangle \quad 2(\vec{u} + \vec{v}) = \langle -4, -2, 8 \rangle$$

$$2\vec{u} = \langle 2, -4, 10 \rangle \quad 2\vec{v} = \langle -6, 2, -2 \rangle$$

$$2\vec{u} + 2\vec{v} = \langle -4, -2, 8 \rangle$$

DISTRIBUTION OF SCALAR MULTIPLICATION  
OVER VECTOR ADDITION.

(2)



$$\vec{AD} = \langle -3, 1 \rangle$$

$$\vec{AB} = \langle -1, -4 \rangle$$

$$\vec{C} \times \vec{B} = \langle -3, 1 \rangle \times \langle -1, -4 \rangle$$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ -3 & 1 & 0 \\ -1 & -4 & 0 \end{vmatrix}$$

$$\langle 0, 0, 13 \rangle$$

$$= (0 - 0)\hat{i} - (0 - 0)\hat{j} + (12 + 1)\hat{k} = 13\hat{k}$$