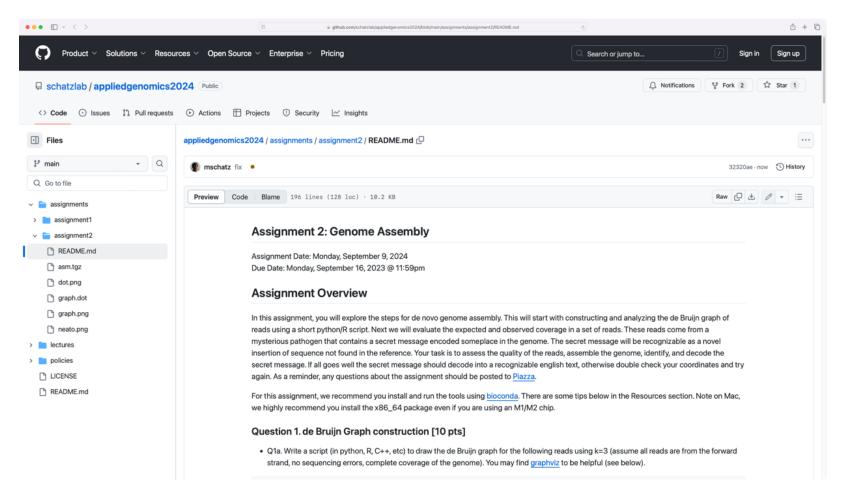
## Read Mapping

Michael Schatz

Sept 16, 2024 Lecture 6: Applied Comparative Genomics



# Assignment 2: Genome Assembly Due Monday Sept 16 by 11:59pm



https://github.com/schatzlab/appliedgenomics2024/tree/main/assignments/assignment2



The Sequence of the Human Genome Venter et al. Science 291. pp 1304-1351 (2001)

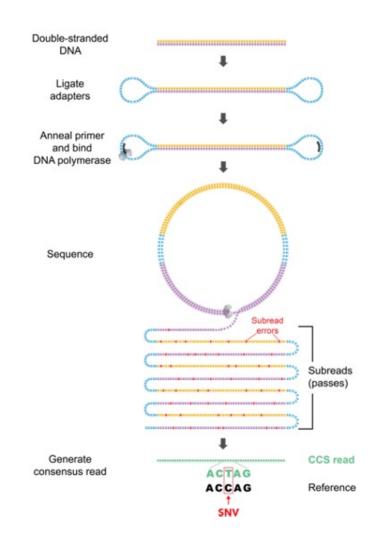
Initial sequencing and analysis of the human genome International Human Genome Sequencing Consortium Nature 409, pp 860–921 (2001)

#### "HiFi" Circular Consensus Reads

High-quality reads produced by sequencing the same molecule multiple times

Higher accuracy for low-coverage sequences like somatic variants or lowly expressed transcripts in RNA-seq, more interpretable alignments, better & faster assembly

Limits read length, used to be very expensive but more manageable now

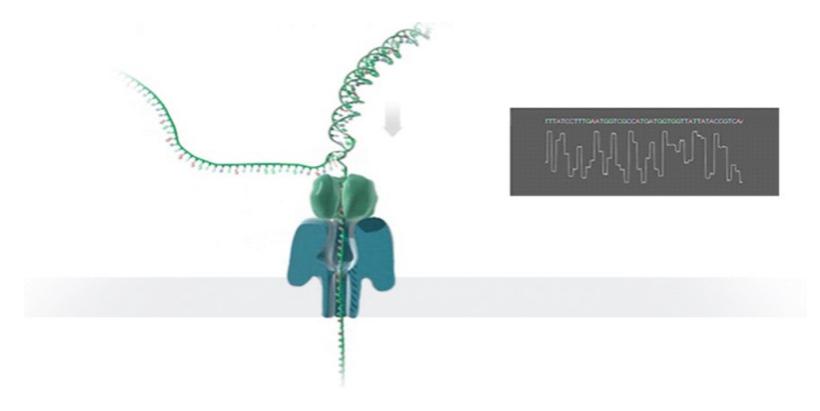


Accurate circular consensus long-read sequencing improves variant detection and assembly of a human genome

Wenger et al (2019) Nature Biotechnology doi:10.1038/s41587-019-0217-9

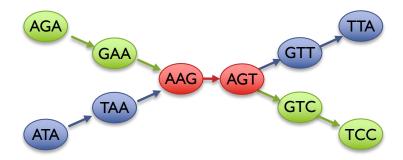
# Nanopore Sequencing

Sequences DNA/RNA by measuring changes in ionic current as nucleotide strand passes through a pore



# Two Paradigms for Assembly

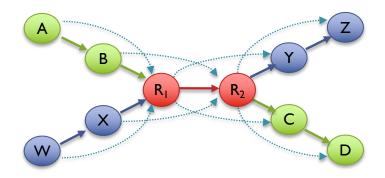
#### de Bruijn Graph



#### Short read assemblers

- Repeats depends on word length
- Read coherency, placements lost
- Robust to high coverage

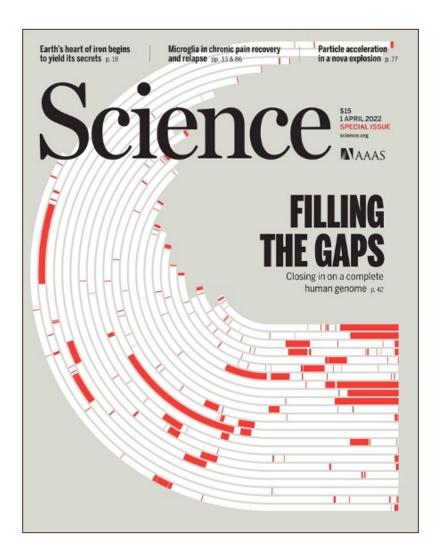
#### **Overlap Graph**

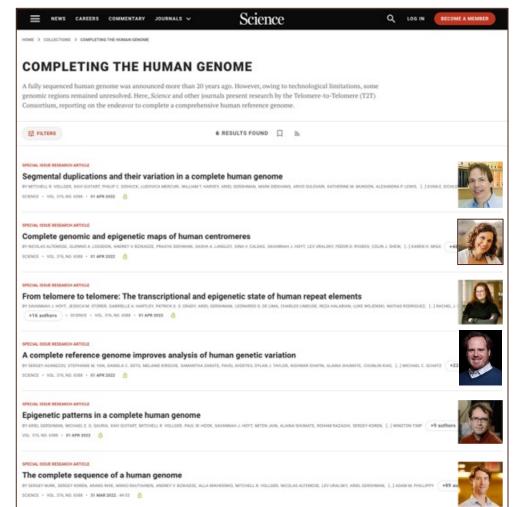


#### Long read assemblers

- Repeats depends on read length
- Read coherency, placements kept
- Tangled by high coverage

Assembly of Large Genomes using Second Generation Sequencing Schatz MC, Delcher AL, Salzberg SL (2010) *Genome Research*. 20:1165-1173.





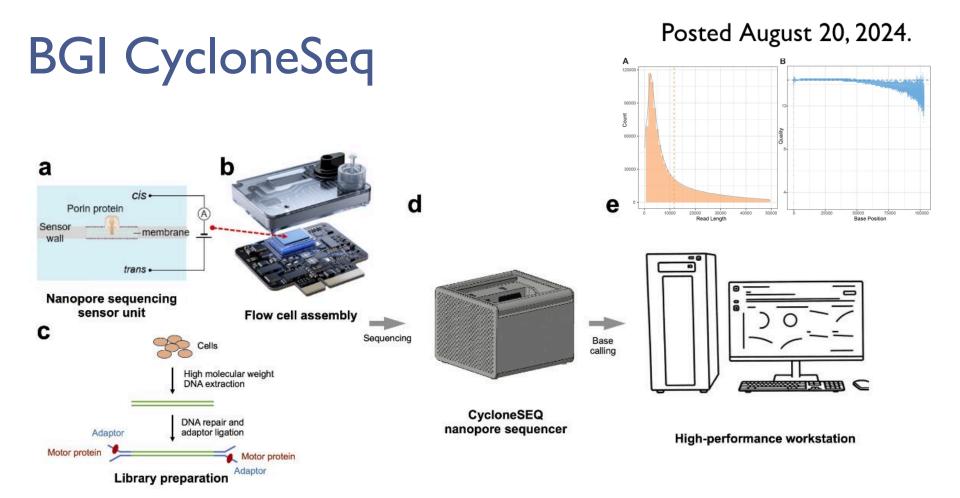
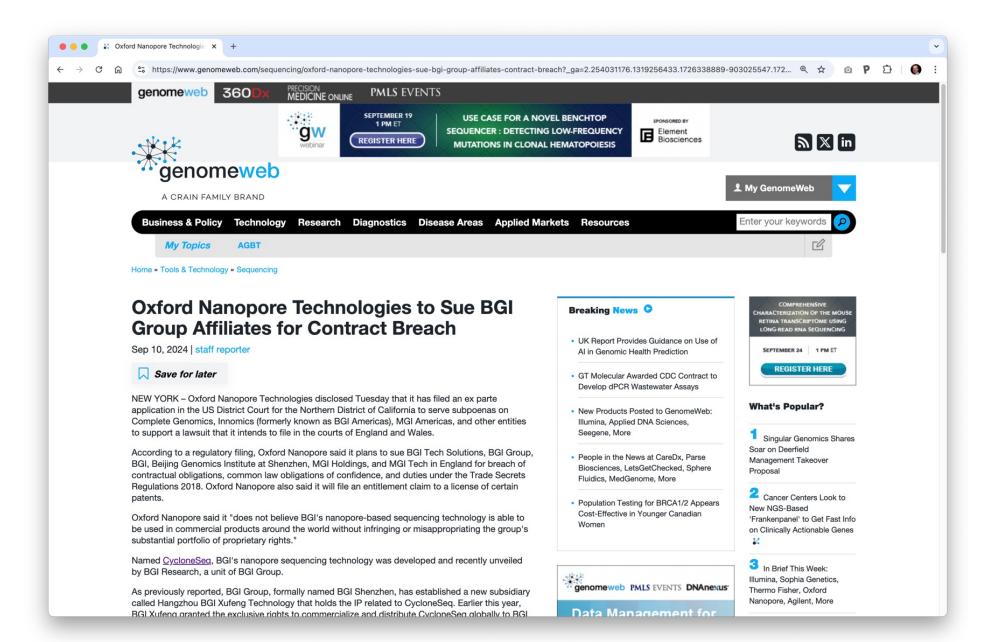


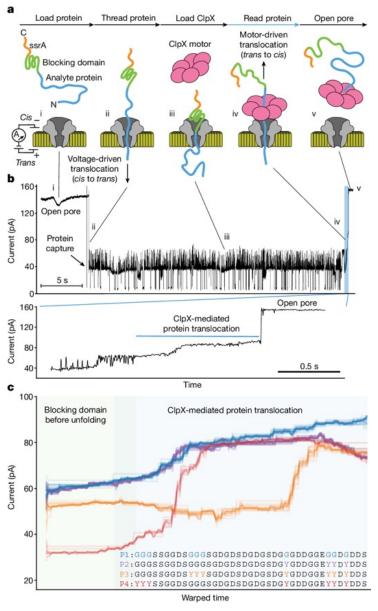
Figure 4: A single-molecule nanopore sequencing platform.

(a) Schematic representation of a sensor unit constructed with an insulating membrane containing an inserted nanopore, along with *cis* and *trans* chambers and corresponding electrodes. (b) Exploded view diagram of a flow cell. (c) Library preparation process for nanopore sequencing. (d) CycloneSEQ nanopore sequencer. (e) High-performance workstation and operating software for the CycloneSEQ nanopore sequencing platform.

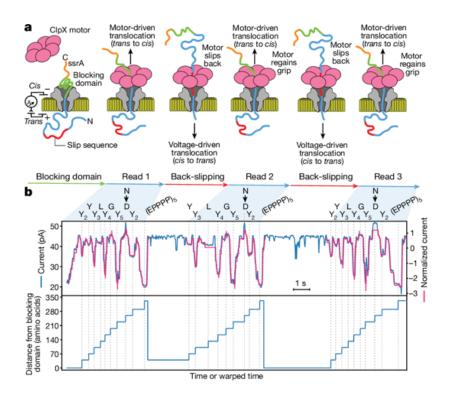
#### A single-molecule nanopore sequencing platform

Zhang et al (2024) bioRxiv. doi: 10.1101/2024.08.19.608720





Rereading single protein molecules multiple times with an unfoldase slip sequence.

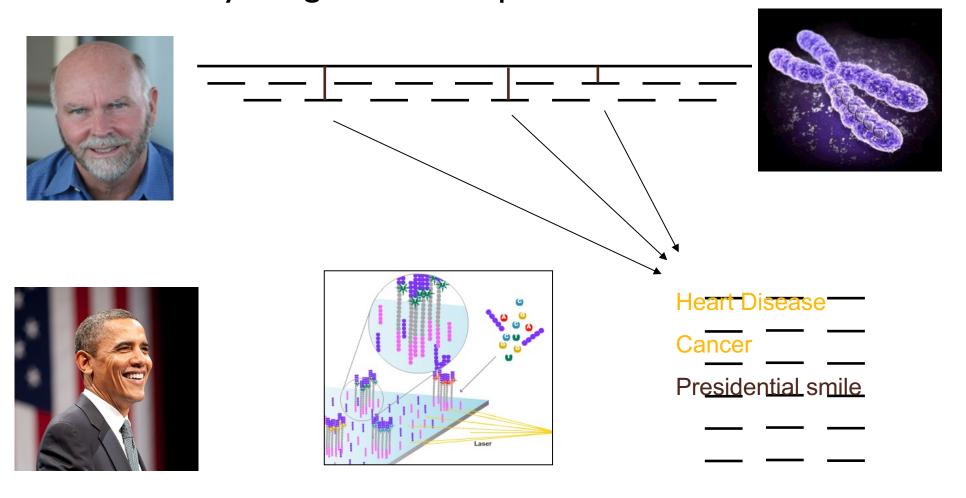


Multi-pass, single-molecule nanopore reading of long protein strands Motone *et al* (2024) Natue. https://doi.org/10.1038/s41586-024-07935-7

# Read Mapping

#### Personal Genomics

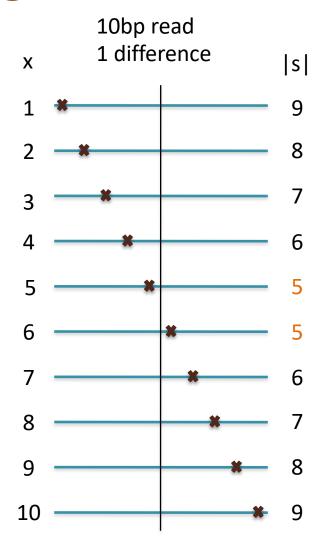
How does your genome compare to the reference?



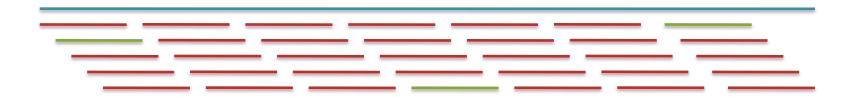
# Seed-and-Extend Alignment

Theorem: An alignment of a sequence of length m with at most k differences must contain an exact match at least s=m/(k+1) bp long (Baeza-Yates and Perleberg, 1996)

- Proof: Pigeonhole principle
  - I pigeon can't fill 2 holes
- Seed-and-extend search
  - Use an index to rapidly find short exact alignments to seed longer in-exact alignments
    - BLAST, MUMmer, Bowtie, BWA, SOAP, ...
  - Specificity of the depends on seed length
    - Guaranteed sensitivity for k differences
    - Also finds some (but not all) lower quality alignments <- heuristic</li>



#### Brute Force Analysis



- Brute Force:
  - At every possible offset in the genome:
    - Do all of the characters of the query match?
- Analysis
  - Simple, easy to understand

<ul><li>Genome length = n</li></ul>	[3B]
— Query length = m	[7]
<ul><li>Comparisons: (n-m+1) * m</li></ul>	[21B]

Overall runtime: O(nm)

[How long would it take if we double the genome size, read length?] [How long would it take if we double both?]

#### **Brute Force Reflections**

#### Why check every position?

GATTACA can't possibly start at position 15

[WHY?]

I	2	3	4	5	6	7	8	9	10	П	12	13	14	15	•••
Т	G	Α	Т	Т	Α	С	Α	G	Α	Т	Т	Α	С	С	•••
								G	Α	Т	Т	Α	С	Α	

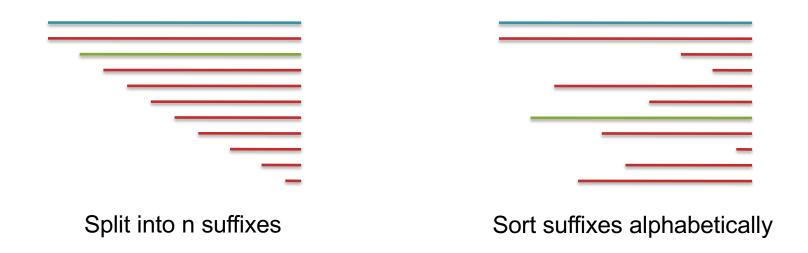
Improve runtime to O(n + m)

[3B + 7]

- If we double both, it just takes twice as long
- Knuth-Morris-Pratt, 1977
- Boyer-Moyer, 1977, 1991
- For one-off scans, this is the best we can do (optimal performance)
  - We have to read every character of the genome, and every character of the query
  - For short queries, runtime is dominated by the length of the genome

#### Suffix Arrays: Searching the Phone Book

- What if we need to check many queries?
  - We don't need to check every page of the phone book to find 'Schatz'
  - Sorting alphabetically lets us immediately skip 96% (25/26) of the book without any loss in accuracy
- Sorting the genome: Suffix Array (Manber & Myers, 1991)
  - Sort every suffix of the genome



[Challenge Question: How else could we split the genome?]

- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = 1; Hi = 15;



#	Sequence	Pos
	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
П	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	I
14	TTACAGATTACC	4
15	TTACC	П





- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (I+I5)/2 = 8
  - Middle = Suffix[8] = CC



#	Sequence	Pos
	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
П	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	Ī
14	TTACAGATTACC	4
15	TTACC	Ш





- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC => Higher: Lo = Mid + I



#	Sequence	Pos
_	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
П	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	I
14	TTACAGATTACC	4
15	TTACC	Ш





- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC=> Higher: Lo = Mid + I
  - Lo = 9; Hi = 15;

#	Sequence	Pos
I	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
Ш	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	I
14	TTACAGATTACC	4
15	TTACC	П

Lo



- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC => Higher: Lo = Mid + I
  - Lo = 9; Hi = 15; Mid = (9+15)/2 = 12
  - Middle = Suffix[12] = TACC

#	Sequence	Pos
I	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
П	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	Ι
14	TTACAGATTACC	4
15	TTACC	Ш

Lo



- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC=> Higher: Lo = Mid + I
  - Lo = 9; Hi = 15; Mid = (9+15)/2 = 12
  - Middle = Suffix[12] = TACC=> Lower: Hi = Mid I
  - Lo = 9; Hi = 11;





#	Sequence	Pos
I	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
П	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	I
14	TTACAGATTACC	4
15	TTACC	П

- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC=> Higher: Lo = Mid + I
  - Lo = 9; Hi = 15; Mid = (9+15)/2 = 12
  - Middle = Suffix[12] = TACC=> Lower: Hi = Mid I
  - Lo = 9; Hi = 11; Mid = (9+11)/2 = 10
  - Middle = Suffix[10] = GATTACC

#	Sequence	Pos
I	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
Ш	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	T
14	TTACAGATTACC	4

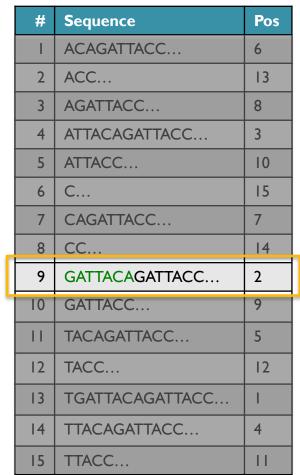
Hi

- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = I5; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC=> Higher: Lo = Mid + I
  - Lo = 9; Hi = 15; Mid = (9+15)/2 = 12
  - Middle = Suffix[12] = TACC=> Lower: Hi = Mid I
  - Lo = 9; Hi = 11; Mid = (9+11)/2 = 10
  - Middle = Suffix[10] = GATTACC=> Lower: Hi = Mid I
  - Lo = 9; Hi = 9;



#	Sequence	Pos
_	ACAGATTACC	6
2	ACC	13
3	AGATTACC	8
4	ATTACAGATTACC	3
5	ATTACC	10
6	C	15
7	CAGATTACC	7
8	CC	14
9	GATTACAGATTACC	2
10	GATTACC	9
П	TACAGATTACC	5
12	TACC	12
13	TGATTACAGATTACC	I
14	TTACAGATTACC	4
15	TTACC	Ш

- Strategy 2: Binary search
  - Compare to the middle, refine as higher or lower
- Searching for GATTACA
  - Lo = I; Hi = 15; Mid = (1+15)/2 = 8
  - Middle = Suffix[8] = CC
     => Higher: Lo = Mid + I
  - Lo = 9; Hi = 15; Mid = (9+15)/2 = 12
  - Middle = Suffix[12] = TACC=> Lower: Hi = Mid I
  - Lo = 9; Hi = 11; Mid = (9+11)/2 = 10
  - Middle = Suffix[10] = GATTACC=> Lower: Hi = Mid I
  - Lo = 9; Hi = 9; Mid = (9+9)/2 = 9
  - Middle = Suffix[9] = GATTACA...=> Match at position 2!





#### Binary Search Analysis

Binary Search

```
Initialize search range to entire list

mid = (hi+lo)/2; middle = suffix[mid]

if query matches middle: done

else if query < middle: pick low range

else if query > middle: pick hi range

Repeat until done or empty range
```

[WHEN?]

- Analysis
  - More complicated method
  - How many times do we repeat?
    - How many times can it cut the range in half?
    - Find smallest x such that:  $n/(2^x) \le 1$ ;  $x = \lg_2(n)$

[32]

- Total Runtime: O(m lg n)
  - More complicated, but much faster!
  - Looking up a query loops 32 times instead of 3B

[How long does it take to search 6B or 24B nucleotides?]



#### Binary Search Analysis

Binary Search

```
Initialize search range to entire list

mid = (hi+lo)/2; middle = suffix[mid]

if query matches middle: done

else if query < middle: pick low range

else if query > middle: pick hi range

Repeat until done or empty range
```

[WHEN?]

- Analysis
  - More complicated method
  - How many times do we repeat?
    - How many times can it cut the range in half?
    - Find smallest x such that:  $n/(2^x) \le 1$ ;  $x = \lg_2(n)$

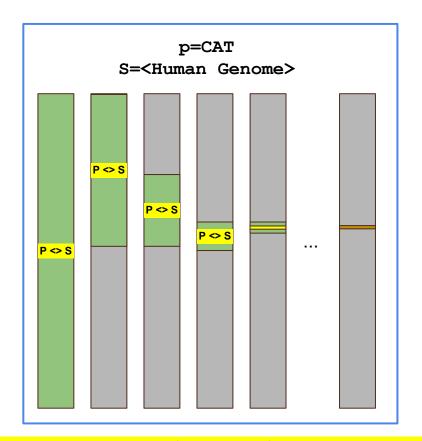
[32]

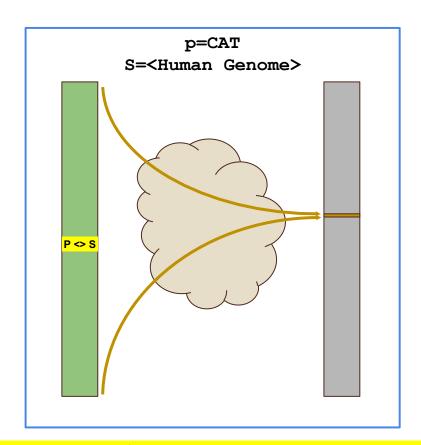
- Total Runtime: O(m lg n)
  - More complicated, but much faster!
  - Looking up a query loops 32 times instead of 3B

Can be reduced to O(m + lg n) using an auxiliary data structure called the LCP array



# Sapling: Accelerating Suffix Array Queries with Learned Data Models





What if instead of a slow algorithmic approach to find the correct rows, we could somehow quickly guess/predict the correct rows?

Kirsche, M, Das, A, Schatz, MC (2020) Bioinformatics doi: https://doi.org/10.1093/bioinformatics/btaa911

# Algorithmic challenge

How can we combine the speed of a suffix array O(m + lg(n)) (or even O(m)) with the size of a brute force analysis (n bytes)?

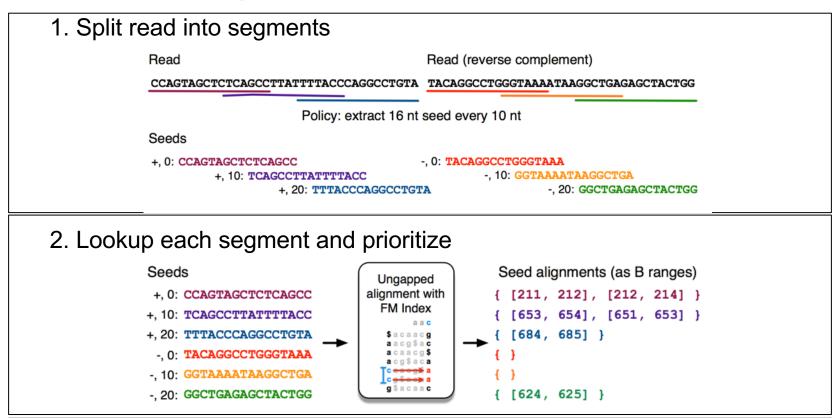
What would such an index look like?



# Bowtie: Ultrafast and memory efficient alignment of short DNA sequences to the human genome

Slides Courtesy of Ben Langmead

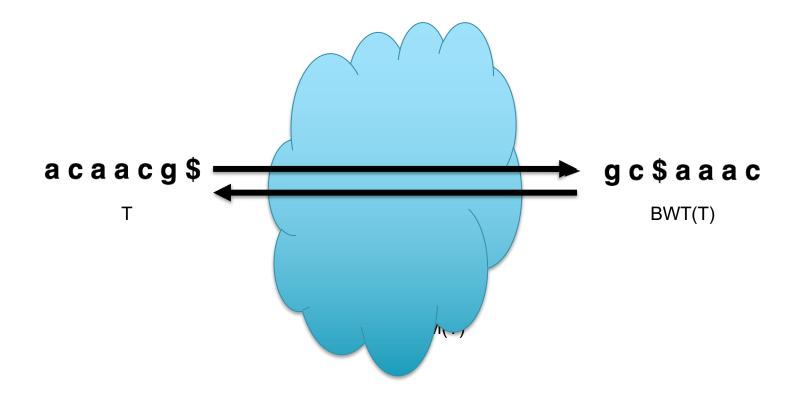
## Algorithm Overview



3. Evaluate end-to-end match

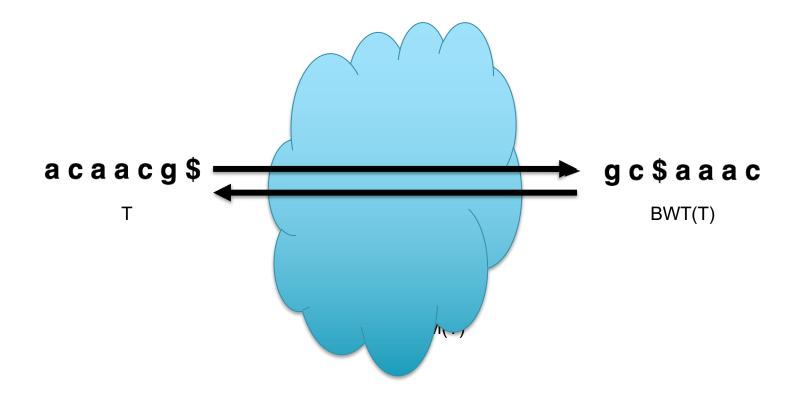
```
Extension candidates
                                        SAM alignments
                         SIMD dynamic
                                                chr12
                         programming
                                                         1936
SA:684, chr12:1955
                            aligner
SA:624, chr2:462
SA:211: chr4:762
                                                    XS:i:-2 XN:i:0
                                            XM:i:0
                                                            XG:i:0
SA:213: chr12:1935
                                            NM:i:0
                                                    MD:Z:36 YT:Z:UU
SA:652: chr12:1945
                                            YM:i:0
                                                        (Langmead & Salzberg, 2012)
```

Reversible permutation of the characters in a text



A block sorting lossless data compression algorithm.

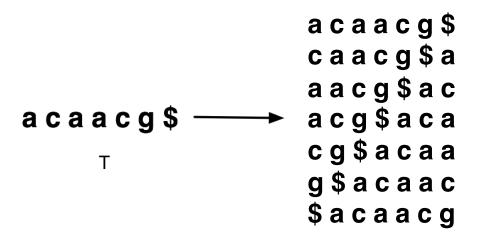
Reversible permutation of the characters in a text



A block sorting lossless data compression algorithm.

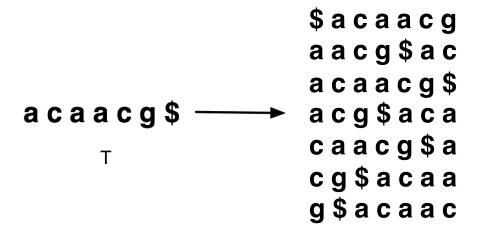
Permutation of the characters in a text

Permutation of the characters in a text



All cyclic permutations

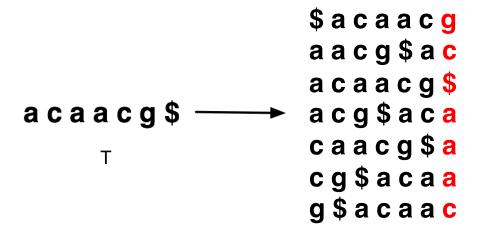
Permutation of the characters in a text



Sorted cyclic permutations AKA Burrows Wheeler Matrix

A block sorting lossless data compression algorithm.

Permutation of the characters in a text

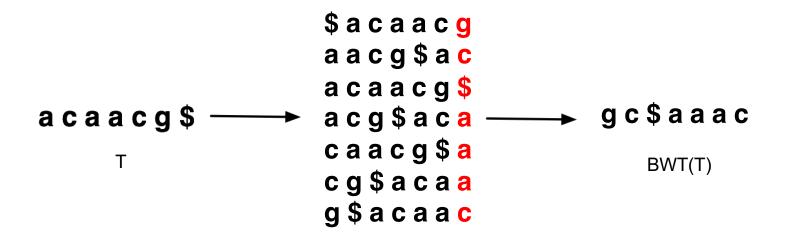


Sorted cyclic permutations
AKA Burrows Wheeler Matrix

Last Column = Burrows Wheeler Transform

A block sorting lossless data compression algorithm.

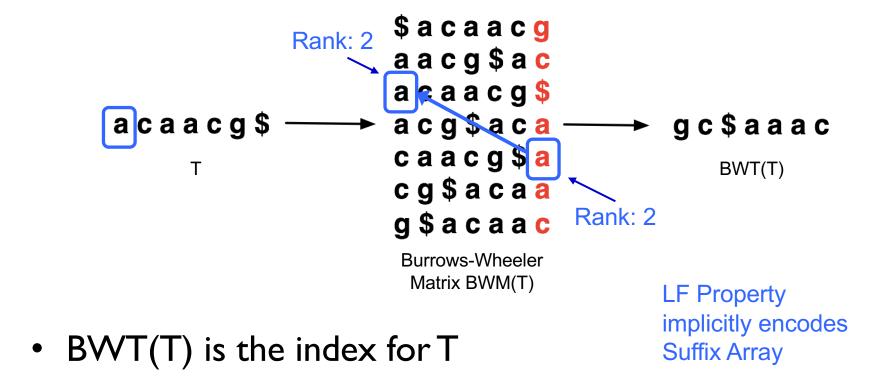
Permutation of the characters in a text



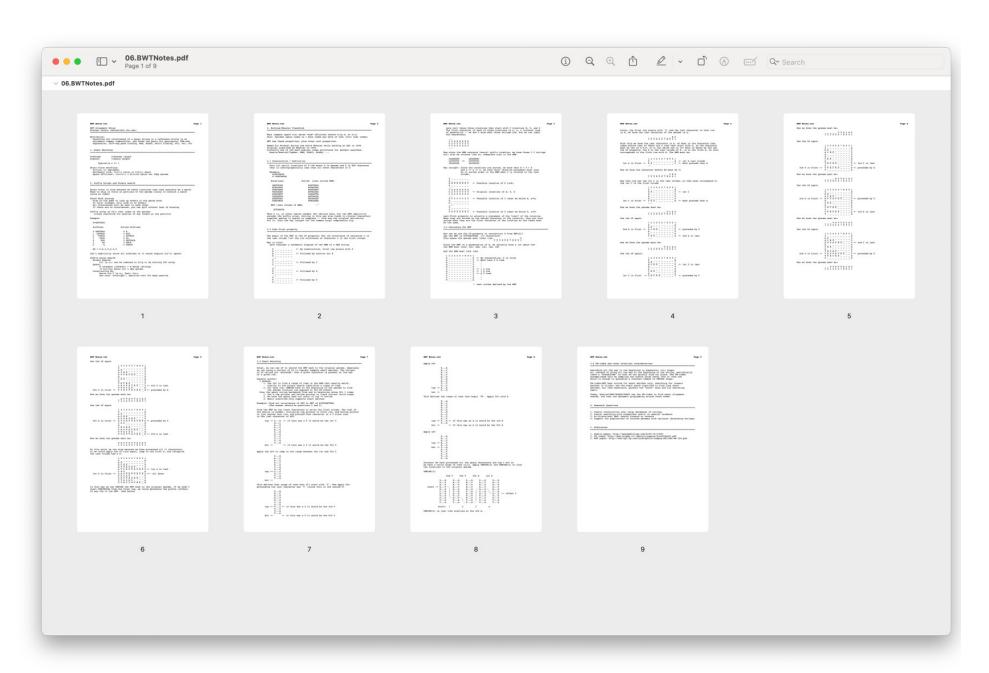
BWT(T) is the index for T

A block sorting lossless data compression algorithm.

Reversible permutation of the characters in a text



A block sorting lossless data compression algorithm.



Recompute the original text when the BWT is ACTTGA\$TTAA