

---

1.

a.

```
In[4]:= DSolve[c'[t] ==  $\frac{F}{V}$  cin -  $\frac{F}{V}$  c[t], c[t], t]
```

```
Out[4]= {{c[t] -> cin +  $e^{-\frac{F t}{V}}$  C[1]}}
```

b.

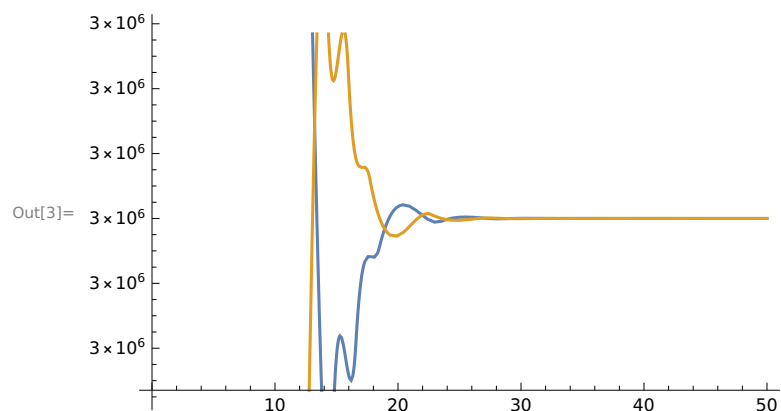
```
Module[{F, V, cin},  
  F =  $48 \times 10^6$ ;  
  V =  $28 \times 10^6$ ;  
  cin =  $3 \times 10^6$ ;  
  sol1[t_] = c[t] /. NDSolve[{c'[t] ==  $\frac{F}{V}$  cin -  $\frac{F}{V}$  c[t], c[0] ==  $6 \times 10^6$ }, c[t], {t, 0, 50}];]
```

c.

```
Module[{F, V, cin},  
  F =  $48 \times 10^6$ ;  
  V =  $28 \times 10^6$ ;  
  cin =  $3 \times 10^6$ ;  
  sol2[t_] = c[t] /. NDSolve[{c'[t] ==  $\frac{F}{V}$  cin -  $\frac{F}{V}$  c[t], c[0] ==  $1 \times 10^6$ }, c[t], {t, 0, 50}];]
```

d.

```
In[3]:= Plot[{sol1[t], sol2[t]}, {t, 0, 50}]
```



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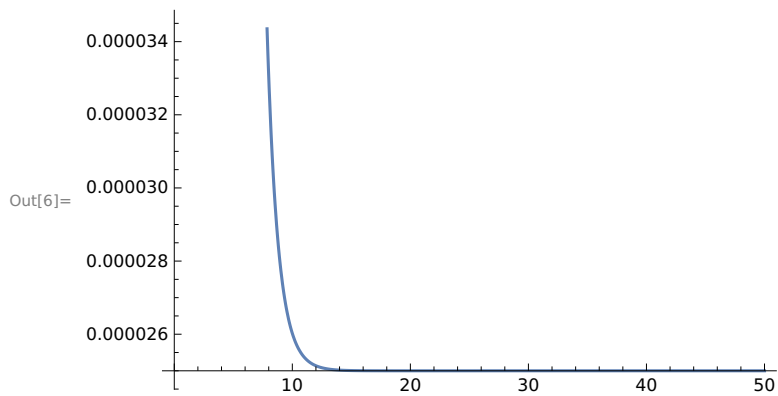
2.

a.

DSolve cannot find an analytical solution but NDSolve can approximate a solution given all conditions and can be seen below.

b.

```
In[6]:= Module[{s, α, n, sol},
  s = 0.01;
  α =  $\frac{1}{2}$ ;
  n = 2;
  sol[t_] = r[t] /. NDSolve[{r'[t] == s (r[t])α - n r[t], r[0] == 5}, r[t], {t, 0, 50}];
  Plot[sol[t], {t, 0, 50}]
```

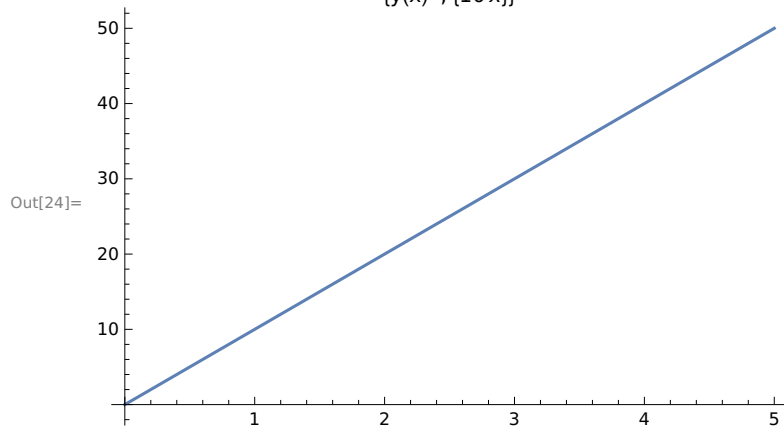


## 3.

a.

```
In[24]:= Module[{sol},
  sol[x_] = y[x] /. DSolve[{x y'[x] == y[x], y[1] == 10}, y[x], x];
  Plot[sol[x], {x, 0, 5}, PlotLabel -> {"y(x)=", sol[x]}]]
```

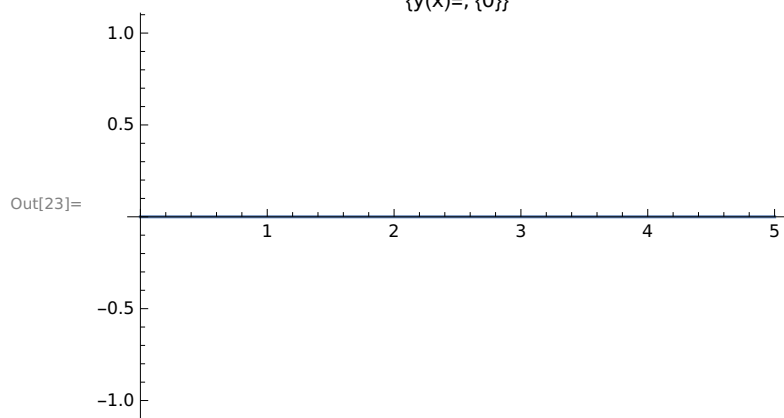
{y(x)=, {10 x}}



b.

```
In[23]:= Module[{sol},
  sol[x_] = y[x] /. DSolve[{x y'[x] == y[x], y[1] == 0}, y[x], x];
  Plot[sol[x], {x, 0, 5}, PlotLabel -> {"y(x)=", sol[x]}]]
```

{y(x)=, {0}}



C.

```
In[26]:= Module[{sol},
  sol[x_] = y[x] /. DSolve[{x y'[x] == y[x], y[0] == 1}, y[x], x];
  Plot[sol[x], {x, -1, 5}, PlotLabel -> {"y(x)=", sol[x]}]]
```

**DSolve:** For some branches of the general solution, the given boundary conditions lead to an empty solution.

