Caleb Logemann MATH 565 Continuous Optimization Homework 1

- 1. Problem 6
- 2. Problem 8
- 3. Problem 12
- 4. For the quadractic function

$$f(\underline{x}) = \frac{1}{2} \underline{\underline{x}}^T \underline{\underline{B}} \underline{x} - \underline{x}^T \underline{b}$$

where $\underline{\underline{B}} \in \mathbb{R}^{n \times n}$ is symmetric positive definite, show that the Newton search direction with $\alpha = 1$ satisfies the sufficient decrease assumption (3.4) for any $c_1 \leq \frac{1}{2}$ and the curvature conditions (3.5) for any $c_2 > 0$.

5. Consider the function:

$$f(\underline{x}) = 20(x_2 - x_1^2)^2 + (1 - x_1)^2$$

Write a MATLAB steepest descent code to find the minimizer of this function. The function be in the form

xstar = SteepestDescent(f, x0, TOL, MaxIters)

Use
$$\underline{x_0} = (1.2, 1.2)^T$$

6.