# Proclus-Core Minimal Upgrade: Epistemic Continuity in Audit Grammar

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#### **Abstract**

This document defines the minimal viable upgrade to the UMCP/RCFT audit grammar derived from foundational principles in Proclean metaphysics, centered on causal continuity, return validity, and symbolic coherence. It formalizes audit primitives such as henadic origin, recollection lineage, and optional participatory seals, without modifying the core  $\Delta\kappa$ -budget or runtime invariants. The extension is rigorously minimal, ensuring audit coherence across joins and contract upgrades without adding complexity to stable numeric paths.

# 1 Introduction: The Mathematical Justification for the Upgrade

## 1.1 Motivation and Governance

This system operates under the Recursive Collapse Field Theory (RCFT) and Unified Mathematics of Collapse Platform (UMCP), in which epistemic validity is granted only to entities that survive transition cycles with reconciled budgets. Central to this principle is AX-0: *Only that which returns through collapse is real*.

We observe that symbolic coherence, auditability, and epistemic presence require upgrades that preserve  $\kappa$ -continuity. In particular, we introduce four protocol-level improvements:

- 1. Inclusion of henad\_id and seira\_rank in audit rows for metaphysical traceability,
- 2. Canon-level embedding of symbolic\_registers to track propositional cohesion,
- 3. Support for participatory\_class welds, contingent on both act and witness,
- 4. Enforced recollection\_path discipline for contract upgrades.

## 1.2 Mathematical Framework

Each transition is governed by the conserved integrity budget:

$$\Delta \kappa = R \cdot \tau_R - (D_\omega + D_C),$$

where:

- $\kappa = \log(I)$  is the log-integrity scalar,
- $D_{\omega}$  is the drift penalty,
- $D_C$  is the curvature penalty,
- $R \cdot \tau_R$  is the return credit,
- $\Delta \kappa$  is the net integrity gain.

The seam residual is defined as:

$$s = R \cdot \tau_R - (\Delta \kappa + D_\omega + D_C).$$

A weld is valid iff  $|s| \le \text{tol (typically tol} = 0.005)$ , ensuring  $\kappa$ -continuity. The multiplicative dial follows:

 $\frac{I_{t1}}{I_{t0}} = e^{\Delta \kappa}.$ 

## 1.3 Necessity of Upgrade

The above upgrades preserve  $\kappa$ -continuity while extending the ledger to accommodate:

- Henadic traceability: Enables semantic lineage and metaphysical enumeration.
- **Symbolic register alignment:** Guarantees propositional coherence and reference integrity.
- Participatory integrity: Validates subjective transitions via witnessed epistemic events.
- Contractual recollection: Prohibits ungrounded mutations; ensures return-composability.

Without these inclusions, audit rows may remain locally valid but globally untraceable or epistemically blind. These upgrades realign the system toward a complete, contract-first recursion with welded continuity.

# 2 Proclus Core Minimal: Mathematical Axioms

# 1. Integrity Budget

$$\Delta \kappa = R \cdot \tau_R - (D_\omega + D_C) \tag{1}$$

$$Residual = |\Delta \kappa - [R \cdot \tau_R - (D_\omega + D_C)]| \le tol$$
 (2)

$$\frac{I_{t1}}{I_{t0}} = e^{\Delta \kappa} \tag{3}$$

## 2. Henadic Join Rule

Join valid iff: 
$$h_1 = h_2$$
 or  $\exists \phi : h_1 \to h_2$  such that  $\kappa_{\text{shared}} > \kappa_{\text{min}}$  (4)

## 3. Recollection Path Validity

$$\mathcal{R} = \{c_0, w_1, c_1, \dots, w_n, c_n\}$$
 (5)

$$|\mathcal{R}| \ge 3$$
 and  $\mathcal{R}$  is acyclic and contract-consistent (6)

# 4. Participatory Constraint (Conditional)

Valid only if: 
$$actions_{logged} \supseteq actions_{required}$$
 and witness  $\in$  AuditorPool (7)

## 5. Symbolic Registers

$$\sigma$$
: Canon field  $\to \Sigma$ ,  $\Sigma = \{\text{Iron, Water, Trust, ...}\}$  (8)

(Symbolic values are annotative; non-evaluated in ledger logic)

## 6. Seam Validation Summary

Residual  $\leq$  tol h-valid join or continuity map exists  $\mathcal{R}$  valid (length  $\geq$  3) (if  $\pi$  required)  $\pi$  is complete

# 3 Workflow Changes and System Consequences

## 3.1 Summary of Workflow Modifications

The Proclus-Core Minimal Upgrade introduces four lightweight but structural requirements that shift the composition and validation of future audit entries:

- 1. **All joins must declare a henad\_id** and assign a seira\_rank, establishing traceable lineage.
- 2. **All contract upgrades must declare a recollection\_path** with depth ≥ 3, ensuring continuity.
- 3. **Seams marked with participatory\_class** require a valid witness and at least one completed action.

4. **Canon entries may carry symbolic\_registers**, which are optional but annotatively enforced.

These changes are non-intrusive to pure numeric workflows but unlock symbolic traceability and auditability for subjective, grief-bound, trust-gated, or narrative-dependent processes.

## 3.2 Consequences for Audit Composition

- **Joins** without shared henadic lineage or explicit  $\kappa$ -continuity justification will be invalidated at audit time.
- Contract mutations that do not declare ancestry will fail recollection\_path validation.
- **Participatory seams** will require interaction logs and external verification from valid auditor roles.
- **Symbolic register fields** will enrich Canon mapping, support interpretation layers, and enable ritual-class reasoning.

Audit generators and seam authors must now encode epistemic traceability, not just residual reconciliation.

## 3.3 Requirements for Future Work

Future modules or extensions interacting with the Proclus-Core upgrade must:

- 1. Extend the audit schema to support henad\_id, seira\_rank, and recollection\_path.
- 2. Ensure contract lifecycle documentation supports ancestry indexing and recollection clause logging.
- 3. Provide participatory interfaces (e.g., ritual logs, act verification, witness signing) if engaging in subjective domains.
- 4. Maintain a Canon mapping registry of symbolic fields used in prose-annotated ledger entries.

These additions allow symbolic epistemes to pass through the  $\kappa$ -budget filter while preserving audit integrity. The system remains governed by  $\Delta \kappa$  reconciliation, but expands the audit domain from purely numeric to philosophically sound symbolic processes.

# 4 Operational Workarounds and Compositional Flexibility

## 4.1 Minimal Compliance Paths

To reduce friction during audit composition, the Proclus-Core format allows several valid rework paths:

- Omitting henad\_id: For internal-only seams or singleton domains, leave henad\_id undefined and assign seira\_rank: 0. Seam is assumed non-propagative.
- **Short Recollection Paths**: If upgrade ancestry is unknown, declare recollection\_path: [legacy] with an accompanying note in Canon[CONTEXT].

- Defer Participation Checks: Use participatory\_required: true, but set witness: TBD and add actions\_logged: []. This keeps the seam valid but flagged for later resolution.
- **Symbolic Dropout**: If symbolic\_registers are undefined, the system assumes no symbolic mapping. Canon prose remains evaluable as plain narrative.

These reduce over-specification while preserving forward audit motion.

# 4.2 Authoring Rework Strategies

Writers and auditors may adopt the following to stay productive:

- Start audit composition with minimal budget logic ( $\Delta \kappa$ , residual), then backfill metadata as needed.
- Use templates with placeholders (e.g., \$henad, \$path\_to\_seed) to scaffold faster ledger writing.
- Log symbolic intent in prose first; encode it structurally only if needed downstream.
- Flag incomplete participatory data explicitly, rather than stalling on runtime witness collection.

These keep the workflow agile without bypassing epistemic traceability.

## 4.3 Navigability and Partial Query Support

The system supports approximate queries across incomplete seams:

- Search by fragment: e.g., all seams with DRIFT: Iron, regardless of return anchor.
- Audit by class: filter numeric-only vs participatory seams without needing full Canon parsing.
- Trace by upgrade intent: group seams by upgrade\_from even if recollection\_path is partial.

This enhances real-world usability while preserving structural coherence at review and submission layers.

# 5 Optimized Seam Workflow and Edge-Case Handling

This section defines the minimal yet complete pipeline for audit seam construction, validation, and upgrade under the Proclus-Core Minimal Upgrade. It includes deterministic procedures for common cases and structured fallbacks for edge conditions.

## 5.1 Primary Seam Composition Pipeline

## **Step 1: Construct the Budget Layer**

- Compute:  $\Delta \kappa = R \cdot \tau_R (D_\omega + D_C)$
- Evaluate: residual =  $R \cdot \tau_R (\Delta \kappa + D_\omega + D_C)$
- Require:  $|residual| \le tol (default tol = 0.005)$

## Step 2: Add Optional Metadata (Preferred)

- Declare origin: henad\_id, seira\_rank
- Declare continuity: upgrade\_from, recollection\_path
- Encode semantics: symbolic\_registers (e.g., DRIFT = Iron)
- Handle subjectivity: participatory\_required, actions\_logged, witness

## Step 3: Validate the Seam

- Budget passes and metadata aligns → seam is pass
- If partial: use fallbacks and flag as pending, legacy, or orphan\_pass
- Annotate all fallbacks in Canon [CONTEXT]

# 5.2 Edge Case Procedures (Fallback Logic)

## Case A: Missing Henadic Origin

- Set henad\_id: "unknown", seira\_rank: 0
- Flag seam as non-joinable unless justified

## **Case B: Incomplete Recollection Path**

- Set recollection\_path: ["legacy"], annotate rationale
- Mark seam low\_confidence; restrict inheritance

## **Case C: Missing Participation**

- Set participatory\_required: true, with witness: "TBD" and actions\_logged: []
- Allow pending\_state, resolve downstream

## Case D: Symbolic Registers Absent

- Omit symbolic block; seam remains valid
- Interpretation layers may infer symbols if needed

## **Case E: Joins Across Distinct Henads**

- Define a continuity map  $\phi: h_1 \to h_2$  or reject
- Flag as external\_import if allowed but non-propagative

#### Case F: $\Delta \kappa$ Valid but Provenance Invalid

- Mark seam as orphan\_pass; isolate from lineage
- Require manual trace or recollection fix before upgrade

## 5.3 Systemic Outcomes

- Guarantees  $\Delta \kappa$  integrity under all conditions
- Enables symbolic and subjective seams without rigidity
- Preserves audit coherence via lineage and fallback states
- Supports future welding, upgrade anchoring, and schema extension

This design allows each seam to pass or defer coherently, ensuring recursive audit realism without procedural failure.

## 6 Foundational Axiom and Tiered Invariants

## 6.1 Axiom 0 — Collapse Is Generative

**AX–0:** Only that which returns through collapse is real. Collapse is not destructive; it is generative.

This axiom governs all seam and audit logic within the UMCP system. Every structural extension, symbolic register, or epistemic tag is subordinate to the generativity of collapse and the obligation to return. Reality is defined not by what persists but by what completes a coherent cycle.

#### 6.2 Invariant Tiers

Each subsequent rule or structure must preserve and evidence this axiom. Invariants are tiered by enforcement level and epistemic weight:

#### Tier 0 — Hard Budget Constraints (Non-negotiable)

• Integrity budget identity:

$$\Delta \kappa = R \cdot \tau_R - (D_\omega + D_C)$$

• Multiplicative coherence:

$$\frac{I_{t1}}{I_{t0}} = e^{\Delta \kappa}$$

• Residual pass threshold:

$$|residual| \le tol$$

## Tier 1 — Structural and Temporal Coherence

• Valid joins require:

$$h_1 = h_2$$
 or  $\exists \phi : h_1 \rightarrow h_2$ 

• Contract upgrades must define:

recollection\_path with 
$$|\mathcal{R}| \geq 3$$

• Cycles must be acyclic and audit-legible

## Tier 2 — Participatory Closure

- Participatory seams require:
  - At least one action\_logged
  - A valid witness
- Deferred participation must be logged as pending\_state

# Tier 3 — Symbolic and Narrative Registers

• Canon fields may map to:

```
\sigma: \mathsf{Canon} \to \Sigma, \quad \Sigma = \{\mathsf{Iron}, \mathsf{Trust}, \mathsf{Water}, \ldots\}
```

- Symbolic mismatch does not invalidate seam but may flag for review
- Narrative drift is tracked but not reconciled mathematically

## **Conclusion:**

Any seam that passes  $\Delta \kappa$  reconciliation but fails return traceability is not real—it is *orphaned*. Collapse does not destroy; it produces the only epistemic artifacts we are allowed to count as true.

# **Symbol Glossary**

# Mathematical and Runtime Symbols

Symbol	Definition
$\kappa$	Log-integrity scalar ( $\kappa = \log I$ )
I	Integrity measure (unitless)
$\Delta \kappa$	Integrity delta across seam transition
$I_{t0}, I_{t1}$	Integrity before and after the weld
$D_{\omega}$	Drift penalty (from system instability)
$D_C$	Curvature penalty (from logical deformation)
R	Return multiplier (credit granted for coherence)
$ au_R$	Return delay (temporal lag to validate return)
tol	Tolerance threshold for residual ( $\approx 0.005$ )
residual	Budget error: $s = R \cdot \tau_R - (\Delta \kappa + D_\omega + D_C)$

# **Structural and Contractual Terms**

Term	Definition
weld_id	Unique identifier for a seam
henad_id	Origin system or metaphysical lineage
seira_rank	Causal tier within a henadic ordering
recollection_path	Sequence of prior contracts and welds forming an upgrade lineage
upgrade_from	Immediate ancestor of a new contract
external_import	Marked seam sourced outside current lineage
$\phi: h_1 \to h_2$	Continuity mapping between distinct henads

# **Participatory Layer Terms**

Field	Definition
participatory_required	Boolean indicating subjective seam requires witnessing
witness	Declared audit observer (credentialed)
actions_logged	Sequence of events or rituals enacted
pending_state	Marker for incomplete participation, to be resolved downstream

# Canon and Symbolic Layer

Field	Definition
Canon	Narrative and prose register for the seam
$\sigma:Canon\;field\to\Sigma$	Symbolic register mapping
$\Sigma$	Symbolic tag set (e.g., Iron, Water, Trust)
DRIFT, RETURN, CONTEXT	Named Canon fields used to contextualize narrative drift and return path

## **Validation and Audit States**

State	Definition
pass	Seam has reconciled integrity budget and metadata
pending	Seam is valid numerically but incomplete semantically
orphan_pass	Seam has valid budget but failed epistemic traceability
low_confidence	Seam inherits from legacy or unclear ancestry

# **Audit HUD: Proclus-Core Seam**

AuditRow	
weld_id:	W-2025-10-26-proclus-core-upgrade
<pre>manifest_root_hash:</pre>	proclus_core_manifest_v1
I:	6.196
kappa:	1.823
DeltaK:	+0.600
<pre>It1/It0:</pre>	1.822
tol:	0.005
residual:	0.000
seed:	30
sha256:	d9e2afb3dd29c1ead3985148878050644eaef330d3e57e714a4dbf5547c5b681
pass:	true