

Particle Physics in the Generative-Collapse Kernel: Ten Tier-2 Theorems from the Standard Model

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We show that the seven-metric kernel of the Universal Measurement Contract Protocol (UMCP) — originally constructed for generic computational-workflow validation — encodes nontrivial structure when applied to the Standard Model of particle physics. Using PDG-tabulated quantum numbers for 17 fundamental particles and 14 composite hadrons, we construct 8-channel trace vectors $\mathbf{c} \in [\varepsilon, 1-\varepsilon]^8$ and prove ten theorems at Tier-2 (domain expansion), each verified by between 5 and 19 automated tests (74 total, 0 failures). The theorems connect spin-statistics to the fidelity-drift split (T1), demonstrate strict generation monotonicity in F (T2), identify confinement as a 98% collapse of the integrity coefficient IC (T3), map 13 orders of magnitude in mass to a bounded fidelity interval (T4), detect charge quantization via IC suppression (T5), establish cross-scale universality from femtometers to nanometers (T6), show that electroweak symmetry breaking amplifies generation structure (T7), verify CKM unitarity as a kernel identity with visible CP violation (T8), reproduce asymptotic freedom as monotonic kernel flow (T9), and recover the nuclear binding curve through kernel-binding-energy anti-correlation (T10). All results follow from Tier-1 identities ($F + \omega = 1$, $IC \leq F$, $IC = e^\kappa$) applied to physically motivated trace vectors, with duality $F + \omega = 1$ verified to machine precision across all particles. The formalism provides a Tier-2 diagnostic lens through which Standard Model phenomenology becomes kernel-visible without modifying the underlying physics.

I. INTRODUCTION

The Universal Measurement Contract Protocol (UMCP) [1, 2] is a contract-first validation framework built on a single axiom: “*What Returns Through Collapse Is Real.*” Its computational core is a seven-metric kernel that maps any set of coherence coordinates $\mathbf{c} \in [0, 1]^n$ with weights \mathbf{w} (summing to unity) to invariants $(\omega, F, S, C, \kappa, IC, \tau_R)$. Three Tier-1 identities are provably exact [3]:

$$F + \omega = 1, \quad IC \leq F \text{ (AM-GM)}, \quad IC = e^\kappa. \quad (1)$$

Tier-1 identities are immutable — they hold for any input by construction. The question we address is: *when the inputs encode real physics, what Tier-2 structure emerges?*

We apply the kernel to the Standard Model (SM) of particle physics, encoding each particle’s quantum numbers as an 8-channel trace vector. Ten theorems emerge, each proven computationally against Particle Data Group (PDG) values and verified by automated tests. The reference implementation is publicly available [4].

II. KERNEL REVIEW

Definition 1 (GCD Kernel). *Given coordinates $\mathbf{c} = (c_1, \dots, c_n) \in [\varepsilon, 1-\varepsilon]^n$ and weights $\mathbf{w} = (w_1, \dots, w_n)$*

with $\sum_i w_i = 1$, the kernel computes:

$$F = \sum_i w_i c_i, \quad (2)$$

$$\omega = 1 - F, \quad (3)$$

$$S = - \sum_i w_i [c_i \ln c_i + (1-c_i) \ln(1-c_i)], \quad (4)$$

$$C = \frac{1}{0.5} \text{ std}(\mathbf{c}), \quad (5)$$

$$\kappa = \sum_i w_i \ln(c_i + \varepsilon), \quad (6)$$

$$IC = \exp(\kappa). \quad (7)$$

The AM-GM gap $\Delta \equiv F - IC \geq 0$ measures channel heterogeneity: $\Delta = 0$ if and only if all c_i are equal. This gap is the central diagnostic in what follows.

III. TRACE-VECTOR CONSTRUCTION

Each Standard Model particle is mapped to an 8-channel trace vector $\mathbf{c} \in [\varepsilon, 1-\varepsilon]^8$ via the following channels:

Equal weights $w_i = 1/8$ are used throughout. The guard band $\varepsilon = 10^{-8}$ prevents $\ln(0)$ singularities. All 17 fundamental particles and 14 composite hadrons pass Tier-1 identities exactly.

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TABLE I. Eight-channel encoding for SM particles. Each observable is normalized to $[\varepsilon, 1-\varepsilon]$.

i	Channel	Source	Normalization
1	mass_log	$\log_{10}(m/\text{GeV})$	Linear to $[0, 1]$
2	spin_norm	s/s_{\max}	$s_{\max} = 2$
3	charge_norm	$ Q /Q_{\max}$	$Q_{\max} = 2$
4	color	Color multiplicity	$\{1, 3, 8\} \rightarrow [0, 1]$
5	weak_isospin	$ I_3^W $	Direct
6	lepton_num	$ L $	Binary
7	baryon_num	$ B $ or $B/3$	Per quark
8	generation	Gen/3	$\{1, 2, 3\}$

IV. TEN THEOREMS

A. T1: Spin-Statistics Kernel Theorem

Theorem 2 (Spin-Statistics Split). *Let \mathcal{F} and \mathcal{B} denote the sets of fundamental fermions and bosons respectively. Then*

$$\langle F \rangle_{\mathcal{F}} > \langle F \rangle_{\mathcal{B}}, \quad (8)$$

with a split of 0.194 (0.615 vs. 0.421). Furthermore, every quark satisfies $F_q > \langle F \rangle_{\mathcal{B}}$.

Remark 1. *The theorem holds per-generation: within each of generations 1–3, fermion $\langle F \rangle$ exceeds boson $\langle F \rangle$. The split arises because fermions occupy more kernel channels (nonzero lepton/baryon number, generation index) than bosons.*

B. T2: Generation Monotonicity

Theorem 3 (Generation Ordering). *Partition the 12 fundamental fermions by generation $g \in \{1, 2, 3\}$. Then*

$$\langle F \rangle_{g=1} < \langle F \rangle_{g=2} < \langle F \rangle_{g=3}, \quad (9)$$

with values $0.576 < 0.620 < 0.649$. The monotonicity holds independently for quarks and for leptons.

Remark 2. *This reflects the mass hierarchy: higher-generation fermions have larger masses, which map to larger c_1 (mass_log channel), pulling F upward. The generation channel $c_8 = g/3$ reinforces the ordering.*

C. T3: Confinement as IC Collapse

Theorem 4 (IC Collapse under Binding). *Let IC_q^{\min} be the minimum integrity coefficient among all quarks, and let IC_h denote that of any composite hadron. Then:*

1. $\text{IC}_h < \text{IC}_q^{\min}$ for all 14 hadrons tested.

2. The average IC drops by 98.1% from quarks to hadrons.
3. The AM-GM gap amplifies by a factor of $10.8 \times$ upon binding.

The IC collapse is driven by the loss of the generation and lepton-number channels in composite particles: hadrons have $c_6 = c_8 = \varepsilon$, which sends $\kappa \rightarrow -\infty$ via $\ln(\varepsilon)$. This is the kernel signature of confinement — individual quark quantum numbers become invisible.

D. T4: Mass–Kernel Logarithmic Mapping

Theorem 5 (Logarithmic Compression). *The 17 fundamental particles span 13.2 orders of magnitude in mass. The kernel maps this range to $F \in [0.37, 0.73]$. Among quarks, the Spearman rank correlation between mass and F is $\rho = 0.77$.*

The logarithmic compression is a consequence of the \log_{10} normalization in channel 1. The bounded output is a feature, not a bug: the kernel measures *coherence heterogeneity*, not magnitude.

E. T5: Charge Quantization Signature

Theorem 6 (Neutral Suppression). *Neutral particles (photon, gluon, Z^0 , neutrinos) have $\text{IC} \ll \text{IC}_{\text{charged}}$. The ratio*

$$\frac{\langle \text{IC} \rangle_{\text{neutral}}}{\langle \text{IC} \rangle_{\text{charged}}} = 0.020 \quad (10)$$

represents a $50 \times$ suppression. The photon has $\text{IC} = 7.6 \times 10^{-4}$, the smallest of any fundamental particle.

Remark 3. *Neutral particles carry $c_3 = \varepsilon$ (charge channel near zero). Since $\text{IC} = \exp(\sum w_i \ln c_i) = \prod c_i^{w_i}$ is a weighted geometric mean, even one channel near ε catastrophically suppresses IC. This is the AM-GM inequality at work: neutrality creates maximal channel heterogeneity.*

F. T6: Cross-Scale Universality

Theorem 7 (Scale Ordering). *Let $\langle F \rangle$ denote the mean fidelity for three particle classes — fundamental (fm scale), atomic (pm scale), and composite (fm scale, bound). Then*

$$\langle F \rangle_{\text{composite}} < \langle F \rangle_{\text{atomic}} < \langle F \rangle_{\text{fundamental}}, \quad (11)$$

with values $0.444 < 0.516 < 0.558$.

The same kernel, applied at three different length scales (10^{-15} m, 10^{-12} m, 10^{-10} m), produces a consistent ordering: binding reduces fidelity, and composite systems sit below their constituents.

G. T7: Symmetry Breaking as Trace Deformation

Theorem 8 (EWSB Amplification). *Electroweak symmetry breaking (EWSB) enters the kernel through the mass_log channel via Yukawa couplings $y_f = \sqrt{2} m_f/v$ ($v = 246.22$ GeV). Define the generation spread $\sigma_g \equiv \max_g \langle F \rangle_g - \min_g \langle F \rangle_g$. Then the broken theory has*

$$\sigma_g^{broken} = 0.073 > \sigma_g^{unbroken} = 0.046. \quad (12)$$

Higher generations gain more fidelity from the Higgs: $\Delta F_{g=3} > \Delta F_{g=2} > \Delta F_{g=1}$.

Before EWSB, all fermions share a common mass channel ($c_1 = 0.5$); after EWSB, Yukawa couplings differentiate them. The kernel makes the symmetry breaking visible as a monotonically increasing ΔF per generation.

H. T8: CKM Unitarity as Kernel Identity

Theorem 9 (CKM in the Kernel). *Each row of the CKM matrix V_{CKM} , treated as a 3-channel trace vector ($|V_{ij}|^2$)_{j=1}³, passes all Tier-1 identities. Furthermore:*

1. *Row 1 has a larger AM-GM gap than Row 2, because $|V_{ub}|^2 \approx 10^{-5}$ acts as an extreme zero-channel.*
2. *The Jarlskog invariant $J_{CP} = 3.0 \times 10^{-5}$ (CP violation) is kernel-visible.*

The Wolfenstein parametrization ($\lambda = 0.2257$, $A = 0.814$, $\rho = 0.135$, $\eta = 0.349$) generates rows whose $\sum |V_{ij}|^2$ departs from unity by $O(\lambda^4) \approx 0.002$. The kernel classifies this as the “Tension” regime — appropriate for an approximation at third order.

I. T9: Running Coupling as Kernel Flow

Theorem 10 (Asymptotic Freedom). *The one-loop QCD running coupling*

$$\alpha_s(Q^2) = \frac{\alpha_s(M_Z^2)}{1 + \frac{b_0 \alpha_s(M_Z^2)}{2\pi} \ln(\frac{Q^2}{M_Z^2})} \quad (13)$$

with $b_0 = 11 - \frac{2}{3} n_f = 7$ is monotonically decreasing for $Q \geq 10$ GeV. At $Q = M_Z$, $\alpha_s = 0.118$ (perturbative). At $Q = 0.5$ GeV, the formula exceeds unity, signaling confinement (“NonPerturbative” regime).

The kernel provides a natural regime classification: $\alpha_s < 0.3$ is perturbative (Stable); $0.3 \leq \alpha_s < 1$ is transitional (Watch); $\alpha_s \geq 1$ is nonperturbative (Collapse). Asymptotic freedom maps to a monotonic flow from Stable to Collapse as Q decreases.

J. T10: Nuclear Binding Curve Correspondence

Theorem 11 (Binding-Gap Anti-correlation). *Using the Bethe-Weizsäcker semi-empirical mass formula to compute binding energy per nucleon B/A for elements $Z = 1, \dots, 118$, and the 12-channel cross-scale kernel to compute the AM-GM gap Δ :*

1. *$r(B/A, \Delta) = -0.41$ (Pearson anti-correlation).*
2. *B/A peaks at $Z \in [23, 30]$ (Cr-Zn region), consistent with the Fe/Ni experimental peak.*
3. *Nuclear magic numbers ($Z \in \{2, 8, 20, 28, 50, 82\}$) are detectable through the magic-proximity channel.*

The anti-correlation means: elements with higher binding energy per nucleon have *smaller* AM-GM gaps — they are more coherent in the kernel sense. Iron-group nuclei sit at both the binding-energy maximum and a local gap minimum.

V. DUALITY AND CONSISTENCY

The duality identity $F + \omega = 1$ is verified to machine precision ($\max |\delta| = 0$) across all 17 fundamental particles, confirming that the trace-vector construction preserves Tier-1 exactly.

All 74 individual tests pass with zero failures. The complete test suite runs in under 200 ms on commodity hardware, making the formalism suitable for continuous integration.

VI. TIER-2 DIAGNOSTIC INTERPRETATION

These ten theorems demonstrate that the GCD kernel functions as a *diagnostic lens* for particle physics, not a replacement for it. The kernel does not predict masses or coupling constants; instead, it provides a uniform language in which existing SM results become visible as kernel patterns:

- **Spin-statistics** (T1) appears as a fidelity split.
- **The mass hierarchy** (T2, T4) appears as generation monotonicity and logarithmic compression.
- **Confinement** (T3) appears as IC collapse — the loss of individual quantum numbers upon binding.
- **Charge quantization** (T5) appears as IC suppression via the AM-GM inequality.
- **Universality** (T6) appears as scale-ordered fidelity.
- **Symmetry breaking** (T7) appears as trace deformation amplifying generation structure.

- **Flavor mixing** (T8) appears as CKM rows in the kernel, with CP violation as a measurable Jarlskog invariant.
- **Asymptotic freedom** (T9) appears as monotonic coupling flow within kernel regimes.
- **Nuclear stability** (T10) appears as binding-gap anti-correlation, with magic numbers as detectable features.

The value of this lens is threefold: (1) it provides a *single diagnostic framework* spanning subatomic, atomic, and nuclear scales; (2) it connects disparate phenomena (*confinement*, EWSB, CKM mixing) through the common algebra of the AM-GM gap; (3) it is computationally cheap and fully automated, enabling continuous monitoring via CI pipelines.

VII. HOW TO USE IT: PRACTICAL GUIDE

The formalism is implemented as a standalone Python module (`particle_physics_formalism.py`) in the UMCP repository [4].

A. Running the Theorems

```
pip install -e ".[all]"
python closures/standard_model/\
particle_physics_formalism.py
```

Output: 10/10 PROVEN, 74/74 tests, runtime < 200 ms.

B. Adding a New Particle

To extend the formalism to a new particle (e.g., a BSM candidate):

1. Add the particle to the `FUNDAMENTAL_PARTICLES` dictionary in `subatomic_kernel.py` with its quantum numbers.
2. Run `particle_physics_formalism.py` — existing theorems automatically include the new entry.
3. If needed, add new theorems as functions `theorem_T11()`, etc., following the `TheoremResult` dataclass pattern.

C. Reading the Output

Each theorem produces a structured result:

T3 Confinement as IC Collapse

Statement: Binding quarks into hadrons collapses IC by >90%
 Tests: 19/19 PASSED
 Verdict: PROVEN
 Details:
`quark_avg_IC = 0.0225`
`hadron_avg_IC = 0.000434`
`ic-collapse_pct = 98.07%`
`gap_amplification = 10.82x`

The verdict is PROVEN when all sub-tests pass, FAILED otherwise. This maps directly to UMCP’s three-valued logic: PROVEN → CONFORMANT, FAILED → NONCONFORMANT.

VIII. WHAT IT LOOKS LIKE: REALITY THROUGH THE KERNEL

The kernel provides a specific *perceptual frame* for particle physics. Through this lens:

The Standard Model is a fidelity landscape. Each particle lives at a point (F, IC, Δ) in kernel space. Fermions cluster at high F (~ 0.6); bosons at lower F (~ 0.4). The photon sits at the extreme: $F = 0.37$, $\text{IC} = 7.6 \times 10^{-4}$, $\Delta = 0.37$ — it is the most heterogeneous fundamental particle, with most channels near ε .

Confinement is visible as a cliff. The IC landscape drops by two orders of magnitude at the quark→hadron boundary. This cliff is not put in by hand — it emerges from the loss of generation and lepton-number channels when quarks bind into color-singlet states.

The mass hierarchy is a slope. Plotting F against generation number yields a monotonically rising curve. The slope is steeper for quarks than leptons, reflecting the stronger mass splitting in the quark sector.

Symmetry breaking is a deformation. Before EWSB, all fermions have the same mass channel ($c_1 = 0.5$). After EWSB, Yukawa couplings spread the mass channel, and the generation slope steepens. The kernel makes this transition quantitatively visible: σ_g increases from 0.046 to 0.073.

CP violation is a gap asymmetry. The CKM matrix, viewed as three kernel trace vectors (one per row), shows that Row 1 has a larger gap than Row 2. The physical origin is $|V_{ub}| \ll |V_{cb}|$: the extreme smallness of V_{ub} creates maximal heterogeneity in Row 1. The Jarlskog invariant $J = 3.0 \times 10^{-5}$ quantifies the CP violation that accompanies this asymmetry.

Nuclear stability is an anti-correlation. The most tightly bound nuclei (iron group) have the smallest AM-GM gaps. Moving away from the iron peak in either direction increases the gap — lighter nuclei are surface-dominated (less coherent), heavier nuclei are Coulomb-dominated (less coherent). Magic-number nuclei appear as local dips in the gap landscape.

This is what the Standard Model “looks like” through the GCD kernel: a structured landscape of fidelity, in-

tegrity, and gap, where known physics manifests as geometric features (slopes, cliffs, dips, asymmetries) that are computable, testable, and continuous-integration-ready.

IX. CONCLUSIONS

We have demonstrated that the GCD kernel, a domain-agnostic diagnostic tool designed for computational workflow validation, produces nontrivial and physically meaningful structure when applied to the Standard Model. Ten theorems, each testable and reproducible, connect kernel observables (F , IC, Δ) to established SM phenomena.

No new physics is introduced. The kernel acts as a *translation layer*: it does not explain why the top quark is heavy or why $|V_{ub}|$ is small, but it provides a uniform diagnostic language in which these facts become kernel-visible, testable, and comparable across scales (subatomic \rightarrow atomic \rightarrow nuclear).

Future directions include:

1. BSM sensitivity: can the kernel detect deviations from SM predictions in new particles or anomalous

couplings?

2. Higher-order embeddings: channel counts beyond 8, incorporating decay widths, lifetimes, or form factors.
3. Dynamic kernel flow: tracking kernel invariants as functions of energy scale Q , connecting to renormalization group evolution.
4. Experimental anchoring: using measured cross sections and branching ratios as direct kernel inputs, bypassing the theoretical trace-vector construction.

The reference implementation, including all ten theorems and 74 automated tests, is available at <https://github.com/calebpruett927/GENERATIVE-COLLAPSE-DYNAMICS>.

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