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# Polar Stratospheric Clouds Microphysical and optical models

Addendum

Ву

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#### Polar Stratospheric Clouds Microphysical and optical models

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The PSC model is continuously being updated with new experimental data and microphysical processes. This addendum describes those changes made to the model since the publication of Scientific Report 00-06 (Larsen, 2000).

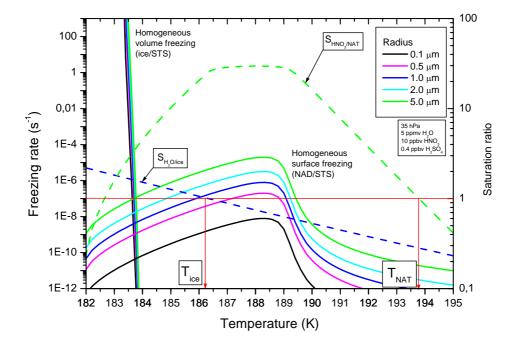
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Updated homogeneous freezing rates have been applied in the latest model versions.

At 3-4 K below T<sub>ice</sub>, freezing of ice out of STS become possible. The model applies homogeneous volume-proportional ice freezing rates, derived from experimental data, as given by Koop et al. [2000]. The much slower homogeneous surfaceproportional freezing of NAD out of solution at temperatures between T<sub>NAT</sub> and T<sub>ice</sub> [Tabazadeh et al., 2002] is also included in the model, assuming an instant conversion to stable NAT after freezing. The freezing rate for the two processes are illustrated in Figure 3.4.1 below, calculated for different particle sizes. The left-hand side of Figure 3.4.1 shows the ice freezing rates. Assuming a critical freezing rate of 1 s<sup>-1</sup>, the ice freezing occurs in a very narrow temperature interval of 0.1-0.2 K at temperatures roughly 3 K below T<sub>ice</sub> at an H<sub>2</sub>O/ice saturation ratio around 1.7. In comparison with ice freezing, the NAD homogeneous freezing rates peak a few K above T<sub>ice</sub> at HNO<sub>3</sub>/NAT saturation ratios around 30 with much lower freezing rates and a more pronounced size dependence. The NAD freezing rates and saturation ratios shown in Figure 3.4.1 have been calculated for equilibrium STS compositions at decreasing temperatures, taking account of the uptake of HNO<sub>3</sub> and H<sub>2</sub>O in the STS.

It should be noticed that to simulate a partial ice freezing of only the larger particles in a size distribution, temperature histories would be needed with an accuracy of a tenth of a degree (which is unrealistic in any meteorological model). It should also be noted that once a fraction of the large-size end of the distribution is frozen into ice particles, fast condensation of water vapor to these particles will decrease the partial water pressure towards equilibrium with ice and thereby require even lower temperatures to freeze the remaining smaller particles. This will cause a substantial broadening of the temperature interval in which freezing of the full range of particles may take place. Therefore accurate cooling rates are also required. The NAD freezing will be much more size selective than ice freezing.

Comparison between observations and model simulations of the formation of solid particles in synoptic Arctic PSCs led Larsen et al. (2004) to conclude that the homogeneous surface-proportional freezing rates of NAD out of solution at temperatures between  $T_{\rm NAT}$  and  $T_{\rm ice}$  [Tabazadeh et al., 2002] were too high, recommending that the freezing rates be reduced by a factor 20 (i.e. multiplied by an adjustment factor of 0.05). The PSCBOX model currently takes this adjustment factor as a free parameter in the model code.

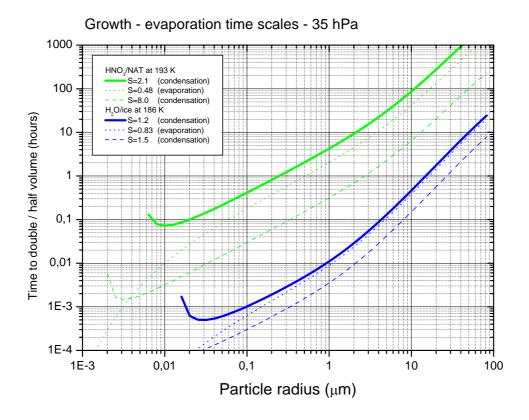


**Figure 3.4.**1 Homogeneous volume-proportional freezing rates of ice (nearly vertical solid color-coded curves in the left-hand side of the diagram) [*Koop et al.*, 2000] and surface proportional NAD (solid color-coded curves) [*Tabazadeh et al.*, 2002] in STS solution for different particle sizes as indicated in the legend. The NAT freezing rates are calculated for STS equilibrium compositions as function of temperature, assuming 10 ppbv HNO<sub>3</sub>, 5 ppmv H<sub>2</sub>O, and 0.4 ppbv H<sub>2</sub>SO<sub>4</sub> at 35 hPa pressure altitude (no adjustment factors applied, cf. text). The partial pressure of HNO<sub>3</sub> is reduced at lower temperatures, corresponding to the uptake in STS, giving rise to a maximum in the saturation ratio over NAT. T<sub>NAT</sub> and T<sub>ice</sub> are indicated corresponding to saturation ratios (dashed curves) over NAT (S<sub>HNO3/NAT</sub>) and ice (S<sub>H2O/ice</sub>) equal to 1.

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# Figure 3.8 Notice that the correct unit on the particle radius axis in $\mu m$ .

As a supplement to Figure 3.8, Figure 3.8.1 below shows the time to grow/evaporate PSC particles to double/half sizes.



**Figure 3.8.1** Time to grow (solid curves) or evaporate (dashed curves) NAT (green) and ice (blue) particles to double, half sizes respectively, calculated at the same atmospheric conditions as in Figure 3.8.

#### **Page 36.**

#### Diffusion coefficient of HNO<sub>3</sub> in air (D<sub>n</sub>).

$$D_n = 0.559 D_w$$

where D<sub>w</sub> is the diffusion coefficient of water vapor in air, calculated from *Pruppacher & Klett* [1997, formula 13-3] as function of air temperature and pressure.

The coefficient of proportionality, 0.559 is calculated as follows (suffix n refers to HNO<sub>3</sub>, w to H<sub>2</sub>O and a to air molecules):

 $D_n = \frac{v_{th,n}l_n}{3}$  where  $v_{th,n}$  is the thermal speed of HNO<sub>3</sub> and  $l_n$  is the mean free path of HNO<sub>3</sub> [e.g. *Turco et al.*, 1989, formula 8].

 $v_{th,n} = \sqrt{\frac{8RT}{\pi M_n}}$  where R is the universal gas constant, T is the air temperature, and M<sub>n</sub>

is the molar mass of HNO<sub>3</sub> [*Pruppacher & Klett*, 1997, formula 5-49]. Similar formula for air molecules, i.e.

$$v_{th,n} = \left(\frac{M_a}{M_n}\right)^{1/2} v_{th,a}$$

 $l_n = \frac{4(M_a + M_n)^{1/2}}{\pi n(d_a + d_n)^2 M_a^{1/2}}$  where n is the number density of air molecules, and d is the molecular diameter [Hamill et al., 1977, formula 6], i.e.

$$\frac{l_n}{l_a} = \frac{2\sqrt{2}(M_a + M_n)^{1/2} d_a^2}{M_a^{1/2} (d_a + d_n)^2} = \Theta_n, \text{ and likewise } \frac{l_w}{l_a} = \frac{2\sqrt{2}(M_a + M_w)^{1/2} d_a^2}{M_a^{1/2} (d_a + d_w)^2} = \Theta_w$$

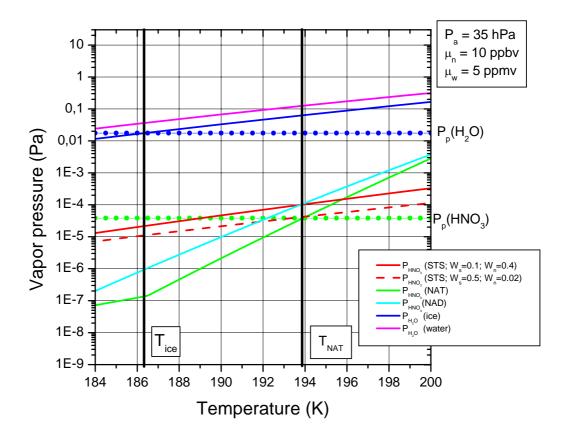
Using the above expressions

$$\frac{D_n}{D_w} = \frac{v_{th,n}l_n}{v_{th,w}l_w} = \left(\frac{M_w}{M_n}\right)^{1/2} \frac{\Theta_n}{\Theta_w} = 0.559, \text{ assuming d}_a = 3.65 \text{ Å}, d_n = 5.2 \text{ Å}, \text{ and d}_w = 4.0 \text{ Å}.$$

The diffusion coefficient is corrected for discontinuity effects at distances near the surfaces of the small particles smaller than the mean free path [*Pruppacher & Klett*, 1997, cp. 5].

#### Page 18, Figure 3.2

The plot is supplemented with the vapor pressure of HNO<sub>3</sub> over nitric acid dihydrate (NAD).



**Figure 3.2.** Examples of HNO<sub>3</sub> vapor pressures over STS (red), NAT (green), and NAD (cyan) and H<sub>2</sub>O vapor pressures over ice (blue) and water (magenta). Partial pressures of HNO<sub>3</sub> and H<sub>2</sub>O at 35 hPa at typical mixing ratios of 10 ppbv HNO<sub>3</sub> and 5 ppmv H<sub>2</sub>O are indicated by green and blue dotlines.

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Further to T-matrix calculations:

The aerosol backscatter ratio R is defined as

$$R = \frac{B_a}{B_m} = \frac{\beta_a^{\text{II}} + \beta_a^{\perp}}{\beta_m^{\text{II}} + \beta_m^{\perp}} = \frac{\int_0^{\infty} n(r) \frac{d\sigma_b}{d\Omega} dr}{n_g \frac{d\sigma}{d\Omega}_{Ray}} = \frac{\int_0^{\infty} n(r) \frac{d\sigma_b}{d\Omega} dr}{\frac{P_a}{kT} \frac{d\sigma}{d\Omega}_{Ray}}$$

where Ba is the total particle volume backscattering coefficient, and Bm is the total molecular (Rayleigh) volume backscattering coefficient, and  $\beta^{II}$  and  $\beta^{\perp}$  are the corresponding parallel and

perpendicular components of the volume backscatter coefficients.  $\frac{d\sigma_b}{d\Omega}$  and  $\frac{d\sigma}{d\Omega_{Ray}}$  are the

particulate and molecular backscattering cross sections, n the number density of particles, ng the number density of gas molecules, P, T, and k the air pressure, temperature and Boltzmann's constant

The backscattering differential cross section is calculated from the scattering matrix element F<sub>11</sub> at 180° as

$$\frac{d\sigma_b}{d\Omega} = \frac{F_{11}Q}{4\pi}$$

where Q is the scattering cross section averaged over the uniform orientation distribution of a (non)spherical particle.

The aerosol depolarisation ratio  $\delta_a$  and volume depolarisation ratio  $\delta$  are defined as

$$\delta_a = \frac{\beta_a^{\perp}}{\beta_a^{\coprod}}$$
 and  $\delta = \frac{\beta_a^{\perp} + \beta_m^{\perp}}{\beta_a^{\coprod} + \beta_m^{\coprod}}$ 

The aerosol depolarisation ratio  $\delta_a$  is calculated from the scattering matrix elements  $F_{i,j}$  at  $180^\circ$  as

$$\delta_{a} = \frac{\int_{0}^{\infty} n(r) \frac{F_{11} - F_{22}}{F_{11} + F_{22} + 2F_{12}} \frac{d\sigma_{b}}{d\Omega} dr}{\int_{0}^{\infty} n(r) \frac{d\sigma_{b}}{d\Omega} dr}$$

The volume depolarisation ratio 
$$\delta$$
 is related to the aerosol depolarisation ratio  $\delta_{\rm a}$  as 
$$\delta = \frac{\delta_a \left[ \left( R+1 \right) \! \delta_m + R \right] + \delta_m}{\left[ \delta_m R + R + 1 + \delta_a \right]}$$

where  $\delta_{\rm m}$  is the molecular depolarisation,  $\delta_{m} = \frac{\beta_{m}^{\perp}}{\beta_{m}^{\perp \perp}}$ , assumed to 1.4%.

The model applies the T-matrix code of Mishchenko and Travis (1998), using a pre-calculated database of expansions of the elements of the scattering matrix in generalised spherical functions  $(\alpha_1..\alpha_4, \beta_1, \beta_2)$  in Mishchenko's notation). The data base spans the particle aspect ratio range 0.50 to 2.00 in steps of 0.05 and real part refractive indices in the range 1.29 to 1.61 in steps of 0.02. The model calculates the differential back scattering cross section, extinction cross section, and depolarisation for a given wavelength, angel, refractive index, and aspect ratio. The recommendations of Mishchenko for input parameter settings have been followed. The data base is calculated for volume-equivalent sizes (RAT=1D0 in Mishchenko's notation) and imaginary refractive index 1E-8. See further description in the original Mishchenko code (Mishchenko and Travis, 1998).

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The internal structure of the Eulerian model version has been changed. In the new version the number density of the four different particle type together with the condensed masses of H<sub>2</sub>SO<sub>4</sub>, HNO<sub>3</sub>, and H<sub>2</sub>O per particle of each type constitute the integration variables.

```
***********************
    SUBROUTINE PSCBOX(
                         ***********
            DTIME.
            THKNES
            NBINS, TYPES, NWORK,
            TAIR, PAIR, PPWV, PPNA,
            ND,
            MCS, MCN, MCW,
            SDND, SDMCS, SDMCN, SDMCW,
            PRESENCE, SEDMNT,
            PTSIZE, WORK)
    Declaration of input/output variables:
    INTEGER NBINS, TYPES, NWORK
    REAL(KIND=4)
            DTIME.
            THKNES
            TAIR, PAIR, PPWV, PPNA,
            ND(NBINS, TYPES),
            MCS(NBINS, TYPES), MCN(NBINS, TYPES), MCW(NBINS, TYPES),
            SDND (NBINS, TYPES),
            SDMCS(NBINS, TYPES), SDMCN(NBINS, TYPES), SDMCW(NBINS, TYPES),
            PTSIZE(NBINS,8), WORK(NBINS, NWORK)
    LOGICAL PRESENCE (TYPES), SEDMNT (TYPES)
    Input:
        DTIME:
                               Integration time step
        THKNES:
                               Vertical thickness of layer
                 (m)
                               Number of particle radii bins
        NBINS:
        TYPES:
                               Number of particle types comprehended by the model
        NWORK:
                               2nd dimension of work array
        TAIR:
                 (K)
                               Ambient air temperature
        PAIR:
                               Ambient air pressure
                 (Pa)
    Input/output:
        PPWV:
                               Ambient partial pressure of water vapor
                 (Pa)
        PPNA:
                               Ambient partial pressure of nitric acid
                 (Pa)
        ND:
                               Number density of particles per kg of air
                 (par/kg air)
        MCS:
                 (kg/particle)
                              Mass of condensed sulfuric acid per particle
        MCN:
                 (kg/particle) Mass of condensed nitric acid per particle
        MCW:
                 (kg/particle) Mass of condensed water per particle
                  (par/m**3)
        SDND:
                                  Sedimentation flow of particles in time interval
DTTME
        SDMCS:
                   (kg/particle)
                                  Mass of condensed sulfuric acid in sedimenting
particles
        SDMCN:
                   (kg/particle)
                                   Mass of condensed nitric acid in sedimenting
particles
        SDMCW:
                 (kg/particle) Mass of condensed water in sedimenting particles
        PRESENCE:(logical)
                               Indicator of presence of different types of particles
        SEDMNT:
                                  Indicator of sedimentation of different types of
                 (logical)
particles
    Work array:
        PTSIZE:
                 (m,m**2,m**3)
                              Particle radii, surface, volume, etc.
                               (not to be changed)
        WORK:
                               Work array (allowed to be changed)
******************
```

This subroutine calculates the particle size distributions and chemical compositions in an ensemble of liquid supercooled ternary solution (STS) stratospheric particles (type 1b PSC at low temperatures), frozen stratospheric sulfate aerosols, and polar stratospheric clouds (PSC) of type 1a and 2 in a SINGLE point in space (box) and time. Individual PSC-box models can be placed in grid-points of a larger model, or can be used for air parcel trajectory

calculations, or can be stacked to form a column model. The placement of the box-model within a larger model (geographical/vertical) is referred to as the location of the box-model.

At each location the PSC-box model takes as input the ambient air state variables: temperature (TAIR), pressure (PAIR), partial pressure of water vapor (PPWV), and partial pressure of nitric acid vapor (PPNA).

The particle size distribution of each particle type is divided into a number of bins (NBINS) on a geometrically increasing volume scale. It is required, that NBINS > 2. NBINS must be the same for all locations of the PSC-box model.

The number density (ND - particles per unit air mass), i.e. the the particle size distributions, are stored in the following arrays:  $\begin{array}{c} \text{ND(i,1), i=1,...NBINS} \\ \text{Liquid sulfate aerosols which, at low temperatures,} \\ \text{take up nitric acid and water, turning into} \\ \text{supercooled ternary solution Type 1b PSC} \\ \end{array}$ 

ND(i,2), i=1,...NBINS Frozen sulfuric acid tetrahydrate particles (SAT) ND(i,3), i=1,...NBINS Nitric acid trihydrate (NAT) type la PSC

ND(i,4), i=1,...NBINS Water ice type 2 PSC

ND-array element no. i holds the particles per unit air mass in the particle radius interval spanned by bin no. i.

The subroutine calculates the differential size distribition ND(i,1) of liquid ternary sulfuric-nitric acid solution aerosol particles, assuming the ternary aerosols to be in equilibrium with the water and nitric acid vapor at an arbitrary ambient atmospheric state, specified as input (TAIR, PPWV, and PPNA).

For each type (j=1,2,3,4) of particle, the condensed masses are stored as follows:

condensed sulfuric acid mass per particle, MCS(i,j), i=1,...NBINS, j=1,2,3,4 condensed nitric acid mass per particle, MCN(i,j), i=1,...NBINS, j=1,2,3,4 condensed water per particle, MCW(i,j), i=1,...NBINS, j=1,2,3,4

Currently, the phase transition between liquid/solid PSCs is unknown. The model applies homogeneous volume dependent freezing of ice in HNO3/H2O supercooled solutions according to Koop et al. (2000). Homogeneous freezing of NAT (NAD) in supercooled solution according to Tabazadeh et al. (2002) can also be simulated if the common block variable TABA\_COR > 0.0, set in calling program.

Upon freezing of a STS particle all the nitric acid together with water is deposited as nitric acid trihydrate (NAT) and all sulfuric acid together with water

as sulfuric acid tetrahydrate (SAT). Any unbound water in hydrates are assumed to form

ice. Upon heating an ice PSC the ice evaporates, turning into a type 1a NAT PSC. Upon further heating the NAT will evaporate, whereby the frozen sulfate aerosol core is released (SAT particle).

Any frozen SAT particles are assumed to melt when the air temperature is above the SAT melting temperature. SAT melting (deliquescence) upon cooling (Koop and Carslaw, 1996) can also be simulated if the logical parameter SAT\_DELI is be set to .TRUE. When melting a SAT paticle the number density is transferred from the frozen to the liquid particle category and the equilibrium composition and ternary density is recalculated.

The SAT particle may also act as nucleation center for type 1a NAT PSC formation upon subsequent cooling, simulating preactivated SAT (Zhang et al., 1996).

 ${\tt HNO3}$  condensation on ice is included if logical parameter  ${\tt HNO3\_ON\_ICE}$  is set to .TRUE.

The logical input/output variables PRESENCE(j), (j=1,2,3,4) can be used in the calling program to test whether particles of a given type are present.

The number density of particles (ND), and the masses of condensed substances (MCS, MCN, MCW)) constitute the integration variables of the model. When the subroutine is called, these variables must hold the values, calculated by the routine in the previous time step (or the initial values, cf. below). Upon exit these variables will hold the new values at a time DTIME later. The new values are calculated by a first order explicit Euler expression within the routine. The ambient air state variables (TAIR, PAIR) are assumed to be constant during the time interval DTIME. In order to perform calculations at different geographical locations and altitudes (grid points), these variables must be defined at each point.

Nitric acid and water are taken up or released from/to the air during condensation/evaporation. On exit new values of gas phase partial pressures of nitric acid (PPNA) and water (PPWV) are recalculated.

The balance calculations of particle number density and masses of condensed substance use as input the sedimentation flow of particles (SDNA). The variables SDMCS, SDMCN, AND SDMCW hold the masses of condensed H2SO4, HNO3, and H2O of the particles falling in from the layer above. The routine will return as output, in the same variables, the flow to be used in the box-calculations in the layer below.

The logical array SEDMNT(j), (j=1,2,3,4) indicate, if there is a sedimentation flow of particles of type j from the layer above on entry, and indicate, in the same variable, if there is a sedimentation flow to the layer below on exit.

Thus, for the calculations in a column, the subroutine should be called in a sequence from the top-layer to the bottom-layer. At the top layer, the sedimentation input variables should be set equal to zero; the logical sedimentation indicator (SEDMNT) should be set to .FALSE., and the calling program should not change the values of these variables between calls in the column sequence. The sedimentation variables will hold the fall out of particles in the bottom layer after the last call of the subroutine in the column sequence. The same array for storing the sedimentation flows and logical indicators can be used at different locations, if the calculations are performed column-wise.

A positive vertical extent (THKNES) of the PSC-box (vertical distance between layers) must be given as input to the subroutine. This extent need not be the same, neither at all locations, nor at all times.

The subroutine uses adjustable array dimensions of all arrays. The parameter NBINS and the arrays in the argument list of the subroutine must be set and dimensioned (cf. above) in the calling program.

The minimum and maximum particle radius are given as parameters to SUBROUTINE SETBIN, which must be called once before any call to PSCBOX (cf. below). Subroutine SETBIN will store the values of the particle radius, surface area, and volume of each bin in the array PTSIZE. This array PTSIZE must be used at all locations, and the array must not be changed between the calls of subroutine PSCBOX.

Subroutine PSCBOX\_START can be used to initialise PSCBOX, including a call to subroutine SETBIN. PSCBOX\_START can be used to calculate initial values of particle number density and chemical composition of a liquid stratospheric sulfuric acid particle ensemble with an initial log-normal size distribution (parameters given to the suboutine). Under warmer stratospheric conditions with no PSCs this distribution could normally be used as initial values of the PSC-box model. In addition PSCBOX\_START will initialise sedimentation variables.

The total particle surface area density of a given particle type can be calculated by SUBROUTINE SURFCE. The condensed phase mixing ratios of sulfuric acid, nitric acid, and water can be calculated by SUBROUTINE MIXCON. Parameters of log-normal distribution fits to individual particle distribitions can be calculated by SUBROUTINE LGNPAR (cf. below).

The array WORK can be be used by the calling program unit between calls of the subroutine, and the same array WORK can be used at all locations.

The PSC-box model uses a number of named common blocks, holding values which can be also be utilised in the calling program unit:

#### COMMON /TAU/TAUMAX

holding the following REAL value:

TAUMAX:

Inverse of minimum time constant encountered in the microphysical processes (1/s); Subroutine PSCBOX will integrate the state variables forward in time and return after DTIME seconds. During DTIME the air temperature and pressure are assumed to be constant. PSCBOX will try to integrate the state variables in one integration step of DTIME seconds; however, if the microphysical minimum time constants encountered are smaller than DTIME, the actual integration step will be reduced to 1/TAUMAX in order to make a stable integration; in this case PSCBOX will

use more than one step to integrate DTIME seconds forward. A minimum time step DTMIN, defined as a parameter below, is used.

COMMON /SED/SEDI

holding the following LOGICAL value:

SEDI:

A logical flag to indecate, if particle sedimentation calculations are to be performed by PSCBOX. This flag will be set to .TRUE. initially by subroutine SETBIN; however, this value can be changed to .FALSE. by the calling program unit (after the call to SETBIN), if sedimentation calculations are not wanted.

COMMON /CONTRL/TEST

holding the following INTEGER value:

TEST:

The value of TEST indicates, if values of local variables in various sub-programmes, used in the PSC-box model, should be printed to a file. This facility is mainly used to test the program. If TEST is equal to zero, no printing will take place. TEST is initially set to zero by subroutine SETBIN. If this detailed (voluminous) output is needed, TEST must be set to a positive value ( >= 50 ) in the calling program unit, and a formatted file with unit number TEST must be opened from the calling program unit. Values of local variables will then be printed on file unit TEST as long as TEST is non-zero. The file must also be closed from the calling program unit. TEST must be >= 60 for very detailed output, and 50 <= TEST < 60 for moderate detailed output.

COMMON /BINS/VR,ZERO,D1,LOGVR holding the following REAL values:

VR: VRATIO

ZERO: Smallest significant number density of particles

in a single bin (1/kg air)

D1: Parameter, related to VRATIO, used in log-normal dist.

LOGVR: ALOG(VR)

Values in common /BINS/ are set by subroutine SETBIN, and must not be changed by the calling program.

Multiplication factor for Tabazadeh freezing rates (if =0, no freezing): REAL TABA\_CORR COMMON /CORRECT/TABA\_CORR

All calculations are performed in SI units.

The entire PSC-box model is written in ANSI fortran 90.

#### Page 71-74:

#### Eulerian PSCMODEL version:

PROGRAM PSC\_MODEL\_E

Main program used to run the PSCBOX model in the Eulerian-radius-space version, i.e. using fixed size bins.

The program file PSCMODEL.FOR must be linked to PSCBOX.FOR holding the microphysical, thermodynamical, and optical subroutines of the PSC box model.

A few lines of code in this program must be changed, depending on the computer (operative system) to be used and where input/output files are stored. The statements of the program, which have to be changed, are all preceded by a comment line, starting with 'CMP'. All instructions in comment lines, starting with 'CMP', should be invoked, before compiling and running the program. Comment lines starting with 'CMP' are only found in this main program file.

Input/Output files:

\_\_\_\_\_

The program uses a simple self-explaining ASCII input file, stored in the associated input file directory. The input file can have any name with extension '.INP'. Output file names are generated from the applied input file name, all with extension .DAT and stored in the associated output file directory. The input/output directories must be specified in the main program before compiling (cf. CMP comment lines).

Time units.

The model performs all calculations internally in SI units, i.e. time in seconds. However, other units for input/output can be required. The units (Days, Hours, Minutes, Seconds) of the time specifications in the input file and the tempetature table file can be set in the input file. These units are also used for output.

Computing control:

\_\_\_\_\_

Two numbers can be set in the input file to control the integration of the PSC-model:

Maximum integration step size (s)

Integration start and stop time (Days, Hours, Minutes, Seconds); when the integration has reached the stop time, the program is terminated (in batch mode), or control is transferred to the interactive routine (using the interactive mode on a PC).

Output control:

-----

A number can be set in the input file to control the frequency of output from the PSC-model (Days, Hours, Minutes, Seconds).

Model structure:

-----

The number of layers in the vertical direction is specified in the input file. A maximum of MAXLAY layers can be used. If a negative number is specified, the absolute value is used as the number of layers, but no sedimentation of particles between the layers is calculated. The layers are numbered from the top to the bottom, and the top layer is no. 1.

The potential temperature THETA (K) of the bottom layer and the layer thickness dPOT (K) (delta-potential temperature) are specified in the input file which, together with temperature/pressure specification in the input fili, will have the following influence:

Temperature, pressure, and potential temperature:

\_\_\_\_\_

The temperature can be calculated from a function of time as

TAIR(time) = RAMP-function(time)

The RAMP-function is a continuous piece-wise linear function, specified by 4 coordinate pairs: { (ramp time i, temperature i); i=1..4 }; i.e. the graph of this function is made up of 3 straight line segments between the 4 coordinate points. For time values less than ramp time 1, the function is constant equal to temperature 1, and for time values greater than ramp time 4, the function is constant equal to temperuture 4. The 4 coordinate pairs are specified in the input file. The same temperatur applies for all layers when using the RAMP-function. Isentropic conditions are assumed and pressures are calculated from temperatures and the specified potenteal temperatures in each layer. If the RAMP temperature function is to be used, the temperature calculation method flag in the input file must be specified as 0 (zero).

Alternatively, the temperature history may be specified individually in each layer from a time table of the temperature. The table must be stored in the input directory as an ASCII file with 1+NLAYER columns (time,temp1,temp2...temp-nlayer), (Kelvin), using the above speficied time units. Cubic spline interpolation will be used between the table entries. Time values in the table must be strictly increasing. The name of the temperature table file is specified in the input file, residing in the input directory. Isentropic conditions are assumed and pressures are calculated from temperatures and the specified potential temperatures in each layer. If the temperature table is to be used, the temperature calculation method flag in the input file must be specified as 1 (one).

Finally, both temperature and pressure can be specified for each layer in an input table file, giving 1+(2\*NLAYER) columns (time, temp1, pres1, temp2, pres2,...,temp-nlayer,pres-nlayer)(Kelvin,Pa) The temperature calculation method flag must set to 2 (two). In this case the specified potential temperature is ignored, but dPOT is used to specify the top layer thickness.

If a temperature (pressure) input file is used the ramp temperature information in the input file is ignored. If a ramp temperature function is used the specification of temperature table file name is ignored.

The temperature calculations as described above may be overlayed by adding a sinosoidal temperature oscillation. Amplitude (K) and period (user units) are specified in the input file. If no oscilations are to be used, specify amplitude AND period equal to zero. To apply a constant temperature correction in all layers, specify the amplitude with sign, and set the period equal to zero.

#### Initial values:

-----

Initial values of water vapor (ppmv) is specified in the input file, one value for each layer.

Initial values of nitric acid (ppbv) is specified in the input file, one value for each layer. If a positive value is given, this value is used; if zero is specified, an observed vertical profile of nitric acid from LIMS-data is used, (cf. JGR 89,5125,1984), either from a northern (positive latitude) hemisphere or southern (negative latitude) hemisphere data set.

Initial values of the total number density of sulfuric aerosols (1/ccm) is specified in the input file (same for all layers). If a positive value is given, this value is used for all levels; if zero is specified, number density is derived in consistency with SAGE I and II aerosol surface climatology (Hitchman et al., JGR 99,20689, 1994).

Median radius and geometric standard deviation of the initial lognormal distribution is given in the input file (same for all altitudes).

#### Optical calculations:

\_\_\_\_\_

Calculation of particle backscatter ratios, extinction coefficients and depolarisation (Mie scattering or T-matrix) can be specified by a logical

flag in the input file. Directory of T-matric coeffifients must be specified in the main program before compiling (cf. CMP comment lines). Wavelengths are speficied as parameters in the main programme and must be set before compilation. The number of size bins must be large to obtain reliable backscatter values. IF(OPTICS)-ENDIF blocks in the main program and subroutine DUMP should also be inspected and changed according to the actual optical parameters required.

```
Output on files:
```

Three types of ASCII output files can be created by the program:

- 1: Historical output files
- 2: Distribution output file
- 3: Vertical profile output file

The output file names are generated from the input file name (e.g. XXXXX.INP) and stored in the specified output file directory:

HISTORICAL OUTPUT FILE is always created for each layer, named XXXXX-Hyy.DAT, where yy is the layer number. The historical output files hold a number of records; one record for each output time, as specified in the input file. Each record holds the following values:

```
Time (Days, Hours, Minutes, Seconds; as specified in the input file)
B: Temperature (K)
   Total number density of frozen sulfate particles (1/ccm)
   Total number density of PSC 1 particles (1/ccm)
E:
   Total number density of PSC 2 particles (1/ccm)
    Saturation ratio of nitric acid over NAT
F:
G: Saturation ratio of water vapor over ice
   Mixing ratio of water vapor (ppmv)
Η:
т:
   Mixing ratio of nitric acid vapor (ppbv)
J: Total (gas phase and condensed phase) mix. ratio, water (ppmv)
   Total (gas phase and condensed phase) mix. ratio, nitric acid (ppbv)
L:
   Ratio of total to initial mixing ratio of water (%)
м:
   Ratio of total to initial mixing ratio of nitric acid (%)
N:
   Total volume of frozen sulfate particles (micron**3/ccm)
   Total volume of PSC la particles (micron**3/ccm)
   Total volume of PSC 2 particles (micron**3/ccm)
   Total volume of all particles (micron**3/ccm)
R:
   Total number density of PSC 1b (STS) particles (1/ccm)
   Total volume of PSC 1b (STS) particles (micron**3/ccm)
   Sulfuric acid weight fraction liquid PSC 1b aerosols [0;1]
IJ:
   Mean radius liquid PSC 1b aerosols (micron)
v:
   Median radius frozen sulfate aerosols (micron)
X: Median radius PSC 1 (micron)
   Median radius PSC 2 (micron)
Z: Nitric acid weight fraction liquid PSC 1b aerosols [0;1]
AA: NAT condensation temperature (K)
BB: Ice frost point temperature (K)
CC: Air pressure (hPa)
DD: Total mixing ration of sulfuric acid (ppb)
EE: Optical parameter 1
FF: Optical parameter 2
GG: Optical parameter 3
HH: Moleratio
II-UU: Cumulated size distribution
({\tt AEROSOL\_BACKSCATTER\_RATIO(J,L),J=1,N\_WAVE),!
                                                   (47 - 53)
(EXTINCTION(J,L),J=1,N_WAVE),
                                                   (54-60)
(DEPOL(J,L),J=1,N_WAVE)
```

DISTRIBUTION OUTPUT FILES are created, if a non-zero distribution-dump-frequency is specified in the input file, or if a command is given interactively for this (PC). The names of the distribution output files are XXXXX-Dyy.DAT, where yy is the layer number. The distribution output files holds a number of blocks of records. A block is written to each distribution output file at each distribution output time. The first record in a block holds the time (Seconds, Days or Hours as specified in the input file). Then follows a number of records; one record for each size bin giving the following values:

```
A: Particle radius (micron)
B: Differential concentration of liquid sulfate particles (1/micron ccm)
C: Differential concentration of frozen sulfate particles (1/micron ccm)
D: Differential concentration of PSC 1 particles (1/micron ccm)
E: Differential concentration of PSC 2 particles (1/micron ccm)
F: Differential concentration of all particles (1/icronm ccm)
```

A VERTICAL PROFILE OUTPUT FILE is created, if a non-zero vertical-dump-frequency is specified in the input file, or if a command is given interactively for this (PC). The name of the vertical profile output files is XXXXX-V.DAT. The vertical profile output file holds a number of blocks of records. A block is written to the vertical output file at each vertical output time. The first record in a block holds the time (Days or Hours; as specified in the input file). Then follows a number of records; one record for each layer, starting from the BOTTOM layer. Each record holds the following values:

```
A: Altitude (km)
в:
   Pressure (hPa)
C:
    Temperature (K)
    Total number density of frozen sulfate particles (1/ccm)
   Total number density of PSC 1 particles (1/ccm) Total number density of PSC 2 particles (1/ccm)
G: Saturation ratio of nitric acid over NAT
    Saturation ratio of water vapor over ice
I: Mixing ratio of water vapor (ppmv)
J:
   Mixing ratio of nitric acid vapor (ppbv)
Κ:
    Total (gas phase and condensed phase) mix. ratio, water (ppmv)
   Total (gas phase and condensed phase) mix. ratio, nitric acid (ppbv)
L:
    Ratio of total to initial mixing ratio of water (%)
м:
   Ratio of total to initial mixing ratio of nitric acid (%)
N:
   Total surface area density of frozen sulfate particles (æm**2/ccm)
p:
    Total surface area density of PSC 1 particles (xm**2/ccm)
    Total surface area density of PSC 2 particles (xm**2/ccm)
    Total surface area density of all particles (æm**2/ccm)
R:
   Total number density of liquid sulfate particles (1/ccm)
T:
   Total surface area density of liquid sulfate particles (æm**2/ccm)
    Sulfuric acid weight fraction in LIQUID sulfate aerosols [0;1]
U:
V: Median radius liquid sulfate aerosols (æm)
   Median radius frozen sulfate aerosols (æm)
x:
Υ:
   Median radius PSC 1 (æm)
Z: Median radius PSC 2 (æm)
AA: Nitric acid weight fraction in LIQUID sulfate aerosols [0;1]
AB: NAT condensation temperature (K)
AC: Ice frost point temperature (K)
AD: Air pressure (hPa)
AE: Total mixing ration of sulfuric acid (ppb)
AF: Optical parameter 1
AG: Optical parameter 2
AH: Optical parameter 3
AI: Moleratio
```

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#### Example on input file for the Eulerian PSCMODEL version:

```
Constant cooling - heating, PSC model E version, Homogeneous freezing
                      Number of layers (IF < 0: no sedimentation calculations)
0.001, 100.0
                     Min. max. radius (MICRONS)
360.0
                     Max. integration time step (seconds)
                     Time units (H/D/M) of the following time specifications and I/O
0.0
                     Integration start time (H/D/M)
96.00
                     Integration stop time (H/D/M))
0.1, 0.0, 0.0
                     Time interval between plot/print output (H/D/M), history, vertical,
distribution
475.0, 20.0
                     Bottom layer potential temperature and potential temperature increment (K)
0
                     Temperature calculation (0: ramp; 1: Temp table; 2: Temp/Press table)
                     Temperature/pressure history file
0.0,225.0
                     Ramp time 1 (H/D/M), temperature 1 (K)
48.0,180.0
                     Ramp time 2 (H/D/M), temperature 2 (K)
60.0,180.0
                     Ramp time 3 (H/D/M), temperature 3 (K)
96.0,225.0
                     Ramp time 4 (H/D/M), temperature 4 (K) \,
0.0, 0.0
                     Temperature sine oscillation period (H/D/M); amplitude (K)
5.0, 5.0, 5.0, 5.0
                     Mixing ratio water vapor in each layer, initial value (ppmv)
0.0, 0.0, 0.0, 0.0
                     Mixing ratio nitric acid in each layer, initial value (ppbv);
                                                                                     (IF 0: LIMS-
data)
10.0, 0.0
                     Number density sulf.aerosols (1/ccm);
                                                              (IF 0: Antarctic profile)
0.0725, 0.15
                     Median radius (microns)
1.86, 1.15
                     Geometric std. dev.
80.00
                     Latitude
.t.
                     Optical calculations
2
                     Particle surface area (2) or volume (3)
5.0E-2
                     Correction factor for homogeneous NAT nucleation
```

#### References

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