

# Principles of Electrical Engineering Cheat Sheet

## Basics

- $V = IR \mid P = IV \mid P = \frac{V^2}{R}$
- $R_a \parallel R_b = \frac{R_a R_b}{R_a + R_b}$
- Absorbed power =  $\frac{V^2}{R}$

## Circuit Analysis/Simplification

### Superposition

- For **Independent** Sources only:
- Current sources  $\rightarrow$  OC | Voltage sources  $\rightarrow$  SC
- Deactivate all but **1** source and solve the circuit. Repeat with a different source. Add the values for each component

### Thevenin/Norton with respect to a & b

- $V_{Th}$  is open circuit voltage between a and b
- Find  $R_{Th}$  by removing sources like in superposition and find equivalent resistance between a and b
- Find  $I_{SC}$  by shorting across a and b.  $V_{Th} = I_{sc} R_{Th}$
- Norton: Take Thevenin and source transform into current source parallel to  $R_{Th}$

### Source Transformation

- $V_s$  in series with R  $\leftrightarrow$   $I_s$  in parallel with R

### Delta-Wye ( $\Delta - Y$ )

$\Delta$  to Y

$$R_A = \frac{R_{AB} R_{AC}}{R_{AB} + R_{AC} + R_{BC}}$$

$$R_B = \frac{R_{AB} R_{BC}}{R_{AB} + R_{AC} + R_{BC}}$$

$$R_C = \frac{R_{AC} R_{BC}}{R_{AB} + R_{AC} + R_{BC}}$$

Y to  $\Delta$

$$R_{AB} = \frac{R_A R_B + R_A R_C + R_B R_C}{R_C}$$

$$R_{BC} = \frac{R_A R_B + R_A R_C + R_B R_C}{R_A}$$

$$R_{AC} = \frac{R_A R_B + R_A R_C + R_B R_C}{R_B}$$

## Maximum Power Transfer

- $R_L = R_{Th} \mid P = \frac{V_{Th}^2}{4R_L}$

## Op Amps

- Linear Region:  $-V_{cc} \leq V_o \leq V_{cc}$
- $I_n = I_p = 0 \mid V_n = V_p$
- Perform KCL @ inputs, Node voltage method

## Time Varying Sources

- $v(t) = V_m \cos(\omega t + \phi) \mid V_m$  is the amplitude, DC
- RMS for cos:  $V_{rms} = \frac{V_m}{\sqrt{2}}$

## Inductors and Capacitors

- Capacitor:
  - $I = C \frac{dv}{dt} \mid C = \frac{q}{v}$
  - $v(t) = \frac{1}{C} \int_{t_0}^t i dt + v(t_0)$
  - $P = v C \frac{dv}{dt} \mid w = \frac{1}{2} C v^2$
- Series
  - $\frac{1}{C_{eq}} = \sum \frac{1}{C_n}$
- Parallel
  - $C_{eq} = \sum C_n$
- Inductor:
  - $v dt = L di$
  - $i(t) = \frac{1}{L} \int_{t_0}^t v dt + i(t_0)$
  - $P = L i \frac{di}{dt} \mid w = \frac{1}{2} L i^2$
  - Series
    - \*  $L_{eq} = \sum L_n$
    - \*  $v = \sum L_n \frac{di}{dt}$
  - Parallel
    - \*  $\frac{1}{L_{eq}} = \sum \frac{1}{L_n}$
    - \*  $i(t_0) = \sum i_n(t_0)$

## Trig Relationships and Angles

- $\cos(\omega t) = \sin(\omega t + \frac{\pi}{2}) = -\sin(\omega t - \frac{\pi}{2})$
- $\sin(\omega t) = \cos(\omega t - \frac{\pi}{2}) = -\cos(\omega t + \frac{\pi}{2})$
- In an inductor the current lags voltage 90 degrees
- In a capacitive circuit, current leads voltage by 90 degrees

## Mutual Inductance

- Mutually induced voltage =  $M \frac{di_2}{dt}$  where  $I_2$  is the current in the other coil

- Dot convention:
  - When the reference direction for a current enters the dotted terminal of a coil, the reference polarity of the voltage that it induces in the other coil is positive at its dotted terminal

## Impedance (Z)

Ohm's Law:  $V=IZ$

- Resistor:  $Z_R = R$
- Inductor:  $Z_L = j\omega L$
- Capacitor:  $Z_C = \frac{1}{j\omega C}$

Admittance is the reciprocal of impedance

## Phasors

$$C = M\angle\theta = M \cos(t\omega + \theta) = Me^{j\theta}$$

## Forms

- Phasor:  $C = M\angle\theta$
- Rectangular:  $C = A + jB$

## Conversion

- $M = \sqrt{A^2 + B^2}$ ,  $\theta = \arctan(\frac{B}{A})$
- $A = M \cos \theta$ ,  $B = M \sin \theta$

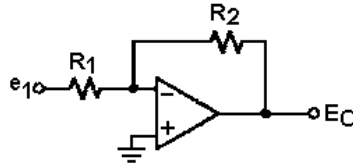
## Phasor Math

Let  $C_1 = M_1\angle\theta_1$  and  $C_2 = M_2\angle\theta_2$

- $C_1 \times C_2 = M_1 \times M_2 \angle(\theta_1 + \theta_2)$
- $C_1 \div C_2 = \frac{M_1}{M_2} \angle(\theta_1 - \theta_2)$

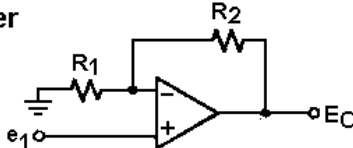
### (a) Inverting Amplifier

$$e_o = e_1 \left( \frac{R_2}{R_1} \right)$$



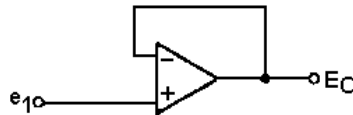
### (b) Non-Inverting Amplifier

$$e_o = e_1 \left( \frac{R_2 + R_1}{R_1} \right)$$



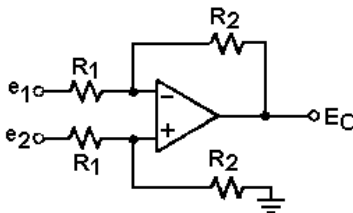
### (c) Voltage Follower

$$e_o = e_1$$



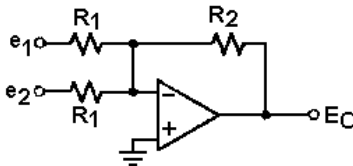
### (d) Differential Amplifier (Subtractor)

$$e_o = (e_2 - e_1) \frac{R_2}{R_1}$$



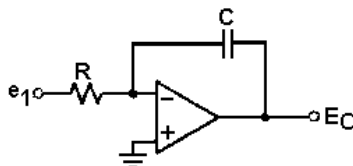
### (e) Adder

$$e_o = -(e_1 + e_2) \frac{R_2}{R_1}$$



### (f) Integrator

$$e_o = \frac{-1}{RC} \int e_1 dt$$



### (g) Differentiator

$$e_o = -RC \frac{de_1}{dt}$$

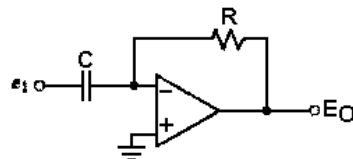


Figure 1: Types of Op Amps