Input: Two matroids  $(E, \mathcal{F}_1), (E, \mathcal{F}_2)$  given by independence oracles. Weights  $c: E \to \mathbb{R}$ . Output: A set  $X \in \mathcal{F}_1 \cap \mathcal{F}_2$  whose weight c(X) is maximum.

- 1. Set k := 0 and  $X_0 := \emptyset$ . Set  $c_1(e) := c(e)$  and  $c_2(e) := 0$  for all  $e \in E$ .
- 2. For each  $y \in E \setminus X_k$  and  $i \in \{1, 2\}$  compute

$$C_i(X_k, y) := \{x \in X_k \cup \{y\} : X_k \cup \{y\} \notin \mathcal{F}_i, (X_k \cup \{y\}) \setminus \{x\} \in \mathcal{F}_i\}$$

3. Compute

$$A^{(1)} := \{(x, y) : y \in E \setminus X_k, x \in C_1(X_k, y) \setminus \{y\}\}$$

$$A^{(2)} := \{(y, x) : y \in E \setminus X_k, x \in C_2(X_k, y) \setminus \{y\}\}\}$$

$$S := \{y \in E \setminus X_k : X_k \cup \{y\} \in \mathcal{F}_1\}$$

$$T := \{y \in E \setminus X_k : X_k \cup \{y\} \in \mathcal{F}_2\}$$

4. Compute

$$m_{1} := \max\{c_{1}(y) : y \in S\}$$

$$m_{2} := \max\{c_{2}(y) : y \in T\}$$

$$\bar{S} := \{y \in S : c_{1}(y) = m_{1}\}$$

$$\bar{T} := \{y \in T : c_{2}(y) = m_{2}\}$$

$$\bar{A}^{(1)} := \{(x, y) \in A^{(1)} : c_{1}(x) = c_{1}(y)\}$$

$$\bar{A}^{(2)} := \{(y, x) \in A^{(2)} : c_{2}(x) = c_{2}(y)\}$$

$$\bar{G} := (E, \bar{A}^{(1)} \cup \bar{A}^{(2)})$$

- 5. Apply BFS to compute the set R of vertices reachable from  $\bar{S}$  in  $\bar{G}$ .
- 6. If  $R \cap \overline{T} \neq \emptyset$ , then find an  $\overline{S} \overline{T}$  path P in  $\overline{G}$  with a minimum number of edges, set  $X_{k+1} := X_k \triangle V(P)$  and k := k+1 and go to 2.
- 7. Compute

$$\varepsilon_{1} := \min\{c_{1}(x) - c_{1}(y) : (x, y) \in \delta_{A^{(1)}}^{+}(R)\}$$

$$\varepsilon_{2} := \min\{c_{2}(x) - c_{2}(y) : (y, x) \in \delta_{A^{(2)}}^{+}(R)\}$$

$$\varepsilon_{3} := \min\{m_{1} - c_{1}(y) : y \in S \setminus R\}$$

$$\varepsilon_{4} := \min\{m_{2} - c_{2}(y) : y \in T \cap R\}$$

$$\varepsilon := \min\{\varepsilon_{1}, \varepsilon_{2}, \varepsilon_{3}, \varepsilon_{4}\}$$

where  $\min \emptyset := \infty$ .

8. If  $\varepsilon < \infty$  then set  $c_1(x) := c_1(x) - \varepsilon$  and  $c_2(x) := c_2(x) + \varepsilon$  for all  $x \in R$  and go to 4. If  $\varepsilon = \infty$ , then among  $X_0, X_1, \ldots, X_k$ , let X be the one with maximum weight. Stop and output X.