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ECE 4300

Professor Aly

Homework 1

1.3 Describe the steps that transform a program written in a high-level language such as C into a representation that is directly executed by a computer processor.

1. Preprocessing: The preprocessor handles directives, expands macros, and includes header files, producing a preprocessed version of the code.

2. Compilation: The compiler translates the preprocessed code into assembly language which then checks for any errors and may optimize the code, then generates an assembly code file.

3. Assembly: The assembler converts the assembly code into machine code, producing an object file.

4. Linking: The linker combines the object files and external libraries into a single executable file, resolving function and variable references.

5. Execution: The operating system loads the executable into memory, and the processor executes the machine code.

1.4 Assume a color display using 8 bits for each of the primary colors (red, green, blue) per pixel and a frame size of 1280 x 1024

a. What is the minimum size in bytes of the frame buffer to store a frame?
- 1 byte = 8 bits
- 8 bits for red + 8 bits for green _ 8 bits for blue = 24 bits per pixel
- Frame size = 1280 x 1024 = 1,310,720 pixels
- Minimum Size of the Frame Buffer = 3 x 1,310,720 = 3,932,160 bytes

b. How long would it take, at a minimum, for the frame to be sent over a 100 Mbit/s network?
- 100 Mbits/s = 100 x 10^6
- 100 Mbit/s = 100 x 10^6 bit/s = 10^2 x 1^6 bit/s = 10^8 bit/s
- Memory Size of the Frame (in bits) = 3,932,160 x 8 = 31,457,280 bits
- Time $= \frac{size}{speed} = \frac{31,457,280\ bits}{10^8 bit/s} \simeq 0.315\ s$

1.5 Consider three different processors P1, P2, and P3 executing the same instruction set. P1 has a 3 GHz clock rate and a CPI of 1.5. P2 has a 2.5 GHz clock rate and a CPI of 1.0. P3 has a 4.0 GHz clock rate and has a CPI of 2.2

a. Which processor has the highest performance expressed in instructions per second?

- CPU Time = $\frac{instructions \times CPI}{clock\ rate}$
- IPS = $\frac{instructions}{CPU\ time}$ = $\frac{clock\ rate}{CPI}$
- 1 GHz = 10^9 Hz
- $IPS_1 = \frac{clock\ rate_1}{CPI_1}$ = $\frac{3GHz}{1.5}$ = 2×10^9
- $IPS_2 = \frac{clock\ rate_2}{CPI_2}$ = $\frac{2.5GHz}{1}$ = 2.5×10^9
- $IPS_3 = \frac{clock\ rate_3}{CPI_3}$ = $\frac{4GHz}{2.2}$ = 1.82×10^9
- Processor 2 is the highest performance

b. If the processors each execute a program in 10 seconds, find the number of cycles and the number of instructions.

- CPU time = 10 seconds
- Clock Cycles = CPU time Clock Rate
- Instructions = IPS CPU Time

- Processor 1
  - Clock Cycles$_1$ = 10 x 3 GHz = 10 x 3 x 10^9 = 3 x 10^9 = 3 x 10^{10}
  - Instructions$_1$ = 2 x 10^{10}
- Processor 2
  - Clock Cycles$_2$ = 10 x 2.5GHz = 2.5 x 10^{10}
  - Instructions$_2$ = 2.5 x 10^{10}
- Processor 3
  - Clock Cycles$_3$ = 10 x 4GHz = 4 x 10^{10} +
  - Instructions$_3$ = 1.82 x 10^{10}

c. We are trying to reduce the execution time by 30% but this leads to an increase of 20% in the CPI. What clock rate should we have to get this time reduction?

- Execution Time = $\frac{clock\ cycles}{clock\ rate}$ = $\frac{instructions \times CPI}{clock\ rate}$
- Clock Cycles = instructions x CPI
- Execution Time$_{new}$ = 0.7 Execution Time$_{old}$

- $\dfrac{instructions_{new} \; x \; CPI_{new}}{clock\,rate_{new}} = 0.7\,x\,\dfrac{CPI_{old}}{clock\,rate_{old}} = 1.2\,CPI_{old}$

- $\dfrac{1.2}{clock\,rate_{new}} = \dfrac{0.7}{clock\,rate_{old}}$

- $clock\,rate_{new} = \dfrac{1.2}{0.7}\,x\,clock\,rate_{old} = 1.71\,clock\,rate_{old}$

- The clock rate must increase by 71%

1.6 Consider two different implementations of the same instruction set architecture. The instructions can be divided into four classes according to their CPI (class A, B, C, and D). P1 with a clock rate of 2.5 GHz and CPIs of 1, 2, 3, and 3, and P2 with a clock rate of 3 GHz and CPIs of 2, 2, 2, and 2. Given a program with a dynamic instruction count of 1.0E6 instructions divided into classes as follows: 10% class A, 20% class B, 50% class C, and 20% class D, which implementation is faster?

a. What is the global CPI for each implementation?
- CPU Time $= \dfrac{CPU\;clock\;cycle}{Clock\;rate}$
- CPU Clock Cylces $= \sum_{i=1}^{n}(CPI_i)\;x\;C_i$
- Class A = Program Executes 10^6 x 10% = 10^5
- Class B = 10^6 x 20% = 2 x 10^5
- Class C = 10^6 x 50% = 5 x 10^5
- Class D = 10^6 x 20% = 2 x 10^5
- CPU clock cycles$_{p1}$ = (10^5) ((1) +(2x2) +(3x5) +(3x2)) = 2.6 x 10^6
- CPU clock cycles$_{p2}$ = (10^5) ((2) +(2x2) +(2x5) +(2x2)) = 2 x 10^6
- CPU Times$_{p1}$ = $\dfrac{2.6\;x\;10^5}{2.5\;x\;GHz}$ = $1.04ms$
- CPU Times$_{p2}$ = $\dfrac{2\;x\;10^5}{3\;x\;GHz}$ = $666.66ms$
- Processor P2 is the faster processor.
  - CPI$_{p1}$ = $\dfrac{CPU\;clock\;cycles_{p1}}{\#\;of\;instructions}$ = $\dfrac{2.6\;x\;10^6}{10^6}$ = 2.6
  - CPI$_{p2}$ = $\dfrac{CPU\;clock\;cycles_{p2}}{\#\;of\;instructions}$ = $\dfrac{2\;x\;10^6}{10^6}$ = 2

b. Find the clock cycles required in both cases.
- CPU clock cycles$_{p1}$ = (10^5) ((1) +(2x2) +(3x5) +(3x2)) = 2.6 x 10^6
- CPU clock cycles$_{p2}$ = (10^5) ((2) +(2x2) +(2x5) +(2x2)) = 2 x 10^6

1.7 Compilers can have a profound impact on the performance of an application. Assume that for a program, compiler A results in a dynamic instruction count of 1.0E9 and has an execution time of 1.1 s, while compiler B results in a dynamic instruction count of 1.2E9 and an execution time of 1.5 s

a. Find the average CPI for each program given that the processor has a clock cycle time of 1 ns

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$$CPI_A = \frac{CPU\ time_A}{instructions_A \times cycle\ time} = \frac{1.1s}{10^9 x\ 10^{-9}s} = 1.1$$

- $CPI_B = \frac{CPU\ time_B}{instructions_B \times cycle\ time} = \frac{1.5s}{1.2x10^9 x\ 10^{-9}s} = 1.1$

b. Assume the compiled programs run on two different processors. If the execution times on the two processors are the same, how much faster is the clock of the processor running compiler A's code versus the clock of the processor running compiler B's code?

- Clock rate$_A = \frac{instructions_A \times CPI_A}{instructions_B \times CPI_B} \times clock\ rate_B = \frac{10^9 \times 1.1}{1.2 \times 10^9 x\ 1.25} \times clock\ rate_B = 0.73\ clock\ rate_B$

- Processor A is 27% slower than Processor B.

c. A new compiler is developed that uses only 6.0E8 instructions and has an average CPI of 1.1. What is the speedup of using this new compiler versus using compiler A or B on the original processor?

- CPU Time$_{new}$ = instructions$_{new}$ x CPI$_{new}$ x cycle time = 6 x 10^8 x 1.1 x 10^{-9}s = 0.66s
- $\frac{performance_{new}}{performance_A} = \frac{CPU\ Time_A}{CPU\ Time_{New}} = \frac{1.1s}{0.66s} = 1.67$
- $\frac{performance_{new}}{performance_B} = \frac{CPU\ Time_B}{CPU\ Time_C} = \frac{1.5s}{0.66s} = 2.27$

The new compiler will be 1.67x faster than complier A and 2.27x times faster than compiler B.

1.11 The results of the SPEC CPU2006 bzip2 benchmark running on an AMD Barcelona has an instruction count of 2.389E12, an execution time of 750 s, and a reference time of 9650 s.

1.11.1 Find the CPI if the clock cycle time is 0.333 ns.

- $\text{CPI} = \dfrac{clock\ cycles}{number\ of\ instructions} = \dfrac{2.25\ x\ 10^{12}}{2.389\ x\ 10^{12}} = 0.94$

1.11.2 Find the SPECratio.

- $\text{SPEC ratio} = \dfrac{Reference\ Time}{Execution\ Time} = \dfrac{9650}{750} = 12.87$

1.11.3 Find the increase in CPU time if the number of instructions of the benchmark is increased by 10% without affecting the CPI.

- Clock Cycle = new number of instructions x CPI $=2.628\ x\ 10^{12}\ x\ 0.94\ = 2.47\ x\ 10^{12}$
- CPU Time = clock cycles x cycle time = 2.47 x 10^{12} x 0.33 x 10^{-9} s = 822.51 s

1.11.4 Find the increase in CPU time if the number of instructions of the benchmark is increased by 10% and the CPI is increased by 5%.

- New CPI = 1.05 x 0.94 = 0.987
- Clock Cycle = new number of instructions x CPI = 2.6278 x 10^{12} x 0.987 = 2.59 x 10^{12}
- CPU Time = Clock cycles x cycle time = 2.59 x 10^{12} 0.333 x 10^{-9}s = 862.47 s

1.11.5 Find the change in the SPECratio for this change.

- $\text{SPECratio} = \dfrac{Reference\ Time}{Execution\ Time} = \dfrac{9659}{862.47} = 11.19$

1.11.6 Suppose that we are developing a new version of the AMD Barcelona processor with a 4 GHz clock rate. We have added some additional instructions to the instruction set in such a way that the number of instructions has been reduced by 15%. Th e execution time is reduced to 700 s and the new SPECratio is 13.7. Find the new CPI.

- Cycle time = 0.25 x 10^{-9}s
- Clock cycles = $\dfrac{Execution\ time}{cycle\ time} = \dfrac{700}{0.25\ x\ 10^{-9}} = 2.8\ x\ 10^{12}$
- Number of instructions = 2.389 x 10^{12} x 0.85 = 2.03 x 10^{12}
- Clock cycles = number of instructions x CPI
- $\text{CPI} = \dfrac{clock\ cycles}{number\ of\ istructions} = \dfrac{2.8 x 10^{12}}{2.03\ x\ 10^{12}} = 1.38$

1.11.7 This CPI value is larger than obtained in 1.11.1 as the clock rate was increased from 3 GHz to 4 GHz. Determine whether the increase in the CPI is similar to that of the clock rate. If they are dissimilar, why?

- Increased clock rate: 1.333
- Increased CPI = $\frac{1.38}{0.94}$ = 1.468

The CPI has increased by 1.33x more given the reduction in number of instructions.

1.11.8 By how much has the CPU time been reduced?

- Ratio of new and old CPU time = $\frac{700}{750}$ = 0.9333
- CPU time has decreased by 6.7%

1.11.9 For a second benchmark, libquantum, assume an execution time of 960 ns, CPI of 1.61, and clock rate of 3 GHz. If the execution time is reduced by an additional 10% without affecting to the CPI and with a clock rate of 4 GHz, determine the number of instructions.
- Execution time = 0.9 x 960ns = 846 x 10^{-9} s
- Number of instructions = $\frac{846 \; x \; 10^{-9} x \; 4 \; x \; 10^9}{1.61}$ = 2147

1.11.10 Determine the clock rate required to give a further 10% reduction in CPU time while maintaining the number of instructions and with the CPI unchanged.

- Execution time = 0.9 x 864 x 10^{-9}s = 77.6 x 10^{-9}s
- New clock rate = $\frac{1.61 \; x \; 2147}{777.6 \; x \; 10^{-9}s}$ = 4.445GHz

1.11.11 Determine the clock rate if the CPI is reduced by 15% and the CPU time by 20% while the number of instructions is unchanged.

- CPI = 0.85 x 1.61 = 1.3585
- Execution time = 0.8 x 777.6 x 10^{-9}s =622.08 x 10^{-9}s
- New clock rate = $\frac{1.3685 \; x \; 2147}{622.08 \; x \; 10^{-9}s}$ = 4.72GHz

1.12 Section 1.10 cites as a pitfall the utilization of a subset of the performance equation as a performance metric. To illustrate this, consider the following two processors. P1 has a clock rate of 4 GHz, average CPI of 0.9, and requires the execution of 5.0E9 instructions. P2 has a clock rate of 3 GHz, an average CPI of 0.75, and requires the execution of 1.0E9 instructions.

1.12.1 One usual fallacy is to consider the computer with the largest clock rate as having the largest performance. Check if this is true for P1 and P2.

- $CPU\ time_{P1} = \frac{5\ x\ 10^9\ x\ 0.9}{4GHz} = \frac{4.5\ x\ 10^9}{4\ x\ 10^9 Hz} = 1.125s$
- $CPU\ time_{P2} = \frac{1\ x\ 10^9\ x\ 0.75}{3GHz} = \frac{0.75\ x\ 10^9}{3\ x\ 10^9 Hz} = 0.25s$

1.12.2 Another fallacy is to consider that the processor executing the largest number of instructions will need a larger CPU time. Considering that processor P1 is executing a sequence of 1.0E9 instructions and that the CPI of processors P1 and P2 do not change, determine the number of instructions that P2 can execute in the same time that P1 needs to execute 1.0E9 instructions.

- $CPU\ time_{P1} = \frac{10^9\ x\ 0.9}{4\ GHz} = \frac{0.9\ x\ 10^9}{4\ x\ 10^9 Hz} = 0.225s$
- $CPU\ time_{P1} = CPU\ time_{P2}$
- Clock rate = 3 GHz
- Number of instructions$_{P2} = \frac{0.225\ x\ 3\ x\ 10^9}{3\ GHz} = 9\ x\ 10^8$

1.12.3 A common fallacy is to use MIPS (millions of instructions per second) to compare the performance of two different processors, and consider that the processor with the largest MIPS has the largest performance. Check if this is true for P1 and P2.

- $MIPS_{P1} = \frac{4\ GHz}{0.9\ x\ 10^6} = \frac{4\ x\ 10^9}{0.9\ x\ 10^6} = 4444$
- $MIPS_{P2} = \frac{3GHz}{0.75\ x\ 10^6} = \frac{3\ x\ 10^9}{0.75\ x\ 10^6} = 4000$

1.12.4 Another common performance figure is MFLOPS (millions of floating-point operations per second), defined as MFLOPS = No. FP operations / (execution time × 1E6) but this figure has the same problems as MIPS. Assume that 40% of the instructions executed on both P1 and P2 are floating-point instructions. Find the MFLOPS figures for the programs.

- $MFLOPS = \dfrac{FLOP\ instructions}{time\ x\ 10^6} = \dfrac{0.4\ x\ instructions}{time\ x\ 10^6} = 0.4M\ MIPS$
- $MFLOPS_{P1} = 0.4(4444) = 1777.6$
- P1 MFLOPS is bigger than P2