

```

In[237]:= ClearAll["Global`*"]

In[238]:=  $\mathbf{M_S} = \{\{s_x, 0, 0, 0\}, \{0, s_y, 0, 0\}, \{0, 0, s_z, 0\}, \{0, 0, 0, 1\}\}$ 
Out[238]=  $\{\{s_x, 0, 0, 0\}, \{0, s_y, 0, 0\}, \{0, 0, s_z, 0\}, \{0, 0, 0, 1\}\}$ 

In[239]:=  $\mathbf{M_R} = \{\{\cos\gamma, -\sin\gamma, 0, 0\}, \{\sin\gamma, \cos\gamma, 0, 0\}, \{0, 0, 1, 0\}, \{0, 0, 0, 1\}\}$ 
Out[239]=  $\{\{\cos\gamma, -\sin\gamma, 0, 0\}, \{\sin\gamma, \cos\gamma, 0, 0\}, \{0, 0, 1, 0\}, \{0, 0, 0, 1\}\}$ 

In[240]:=  $\mathbf{M_T} = \{\{1, 0, 0, 0\}, \{0, 1, 0, 0\}, \{0, 0, 1, 0\}, \{t_x, t_y, t_z, 1\}\}$ 
Out[240]=  $\{\{1, 0, 0, 0\}, \{0, 1, 0, 0\}, \{0, 0, 1, 0\}, \{t_x, t_y, t_z, 1\}\}$ 

In[241]:=  $\mathbf{v} = \{x, y, z, 1\}$ 
Out[241]=  $\{x, y, z, 1\}$ 

In[242]:=  $\mathbf{v.M_S.M_R.M_T}$ 
Out[242]=  $\{\cos\gamma x s_x + \sin\gamma y s_y + t_x, -\sin\gamma x s_x + \cos\gamma y s_y + t_y, z s_z + t_z, 1\}$ 

In[243]:=  $\mathbf{M_{MW}} = \mathbf{M_S.M_R.M_T}$ 
Out[243]=  $\{\{\cos\gamma s_x, -\sin\gamma s_x, 0, 0\}, \{\sin\gamma s_y, \cos\gamma s_y, 0, 0\}, \{0, 0, s_z, 0\}, \{t_x, t_y, t_z, 1\}\}$ 

In[244]:=  $\mathbf{v.M_{MW}}$ 
Out[244]=  $\{\cos\gamma x s_x + \sin\gamma y s_y + t_x, -\sin\gamma x s_x + \cos\gamma y s_y + t_y, z s_z + t_z, 1\}$ 

In[245]:=  $\mathbf{M_{MW}} // \text{MatrixForm}$ 
Out[245]/MatrixForm=

$$\begin{pmatrix} \cos\gamma s_x & -\sin\gamma s_x & 0 & 0 \\ \sin\gamma s_y & \cos\gamma s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ t_x & t_y & t_z & 1 \end{pmatrix}$$


In[246]:=  $\mathbf{M_i} = \{\{i01, i02, i03, i04\}, \{i05, i06, i07, i08\}, \{i09, i10, i11, i12\}, \{i13, i14, i15, i16\}\}$ 
Out[246]=  $\{\{i01, i02, i03, i04\}, \{i05, i06, i07, i08\}, \{i09, i10, i11, i12\}, \{i13, i14, i15, i16\}\}$ 

In[247]:=  $\mathbf{M_j} = \{\{j01, j02, j03, j04\}, \{j05, j06, j07, j08\}, \{j09, j10, j11, j12\}, \{j13, j14, j15, j16\}\}$ 
Out[247]=  $\{\{j01, j02, j03, j04\}, \{j05, j06, j07, j08\}, \{j09, j10, j11, j12\}, \{j13, j14, j15, j16\}\}$ 

In[248]:=  $\mathbf{M_i.M_j} // \text{MatrixForm}$ 
Out[248]/MatrixForm=

$$\begin{pmatrix} i01 j01 + i02 j05 + i03 j09 + i04 j13 & i01 j02 + i02 j06 + i03 j10 + i04 j14 & i01 j03 + i02 j07 + i03 j11 + i04 j15 & i01 j04 + i02 j08 + i03 j12 + i04 j16 \\ i05 j01 + i06 j05 + i07 j09 + i08 j13 & i05 j02 + i06 j06 + i07 j10 + i08 j14 & i05 j03 + i06 j07 + i07 j11 + i08 j15 & i05 j04 + i06 j08 + i07 j12 + i08 j16 \\ i09 j01 + i10 j05 + i11 j09 + i12 j13 & i09 j02 + i10 j06 + i11 j10 + i12 j14 & i09 j03 + i10 j07 + i11 j11 + i12 j15 & i09 j04 + i10 j08 + i11 j12 + i12 j16 \\ i13 j01 + i14 j05 + i15 j09 + i16 j13 & i13 j02 + i14 j06 + i15 j10 + i16 j14 & i13 j03 + i14 j07 + i15 j11 + i16 j15 & i13 j04 + i14 j08 + i15 j12 + i16 j16 \end{pmatrix}$$


In[249]:=  $\mathbf{M_i} = \{\{i01, i02, i03, 0\}, \{i05, i06, i07, 0\}, \{i09, i10, i11, 0\}, \{i13, i14, i15, 1\}\}$ 
Out[249]=  $\{\{i01, i02, i03, 0\}, \{i05, i06, i07, 0\}, \{i09, i10, i11, 0\}, \{i13, i14, i15, 1\}\}$ 

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```
In[250]:= Mj = {{j01, j02, j03, 0}, {j05, j06, j07, 0}, {j09, j10, j11, 0}, {j13, j14, j15, 1}}
```

```
Out[250]= {{j01, j02, j03, 0}, {j05, j06, j07, 0}, {j09, j10, j11, 0}, {j13, j14, j15, 1}}
```

```
In[251]:= Mi.Mj // MatrixForm
```

```
Out[251]/MatrixForm=
```

$$\begin{pmatrix} i01 j01 + i02 j05 + i03 j09 & i01 j02 + i02 j06 + i03 j10 & i01 j03 + i02 j07 + i03 j1 \\ i05 j01 + i06 j05 + i07 j09 & i05 j02 + i06 j06 + i07 j10 & i05 j03 + i06 j07 + i07 j1 \\ i09 j01 + i10 j05 + i11 j09 & i09 j02 + i10 j06 + i11 j10 & i09 j03 + i10 j07 + i11 j1 \\ i13 j01 + i14 j05 + i15 j09 + j13 & i13 j02 + i14 j06 + i15 j10 + j14 & i13 j03 + i14 j07 + i15 j11 + \end{pmatrix}$$