

# Designing a Calculator Using MIPS in MARS

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**Abstract**—This report goes over the steps to implement the basic operations of a calculator; addition, subtraction, multiplication and division. The program will be written MIPS normal and logical operations in MARS.

## I. INTRODUCTION

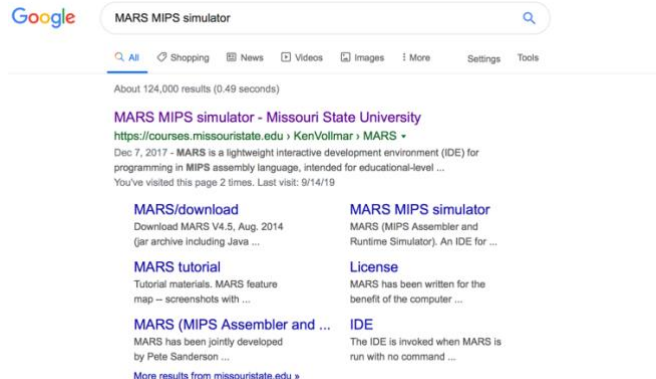
We will be using MIPS to implement our code in MARS which is also known as MIPS Assembler and Runtime Simulator. Then using MIPS assembly language and the MARS platform we will design a code to run addition, subtraction, multiplication, and division problems; both using normal and logical operations. Throughout the process of this project we will complete the following:

- 1) Install MARS and learn the basic functionalities of the assembler
- 2) Implement the basic calculator functions using normal operations
- 3) Implement the basic calculator functions using logical operations
- 4) Test the code we designed to confirm our program performs as expected

## II. INSTALLING MARS AND THE BASICS

### A. Installation

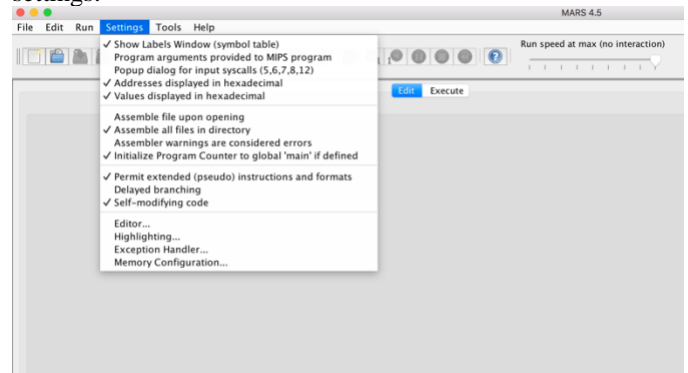
To install MARS, begin by doing a simple Google search for “MARS MIPS Simulator. The first link should be the one you need.



However, if this does not show up for you please visit <https://courses.missouristate.edu/KenVollmar/MARS/>. On the left-hand side of the website you will find a button that says “download.” Click that button and then click the option that says, “Download MARS.”

### B. The Setup

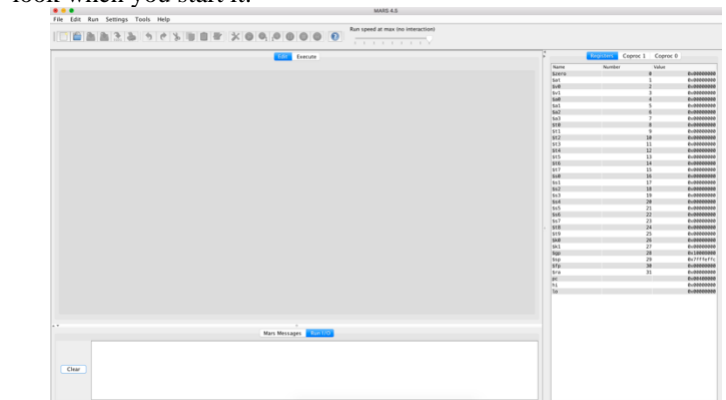
Once MARS is installed you will be able to launch the jar file to begin programming. However, before you begin programming you should make sure that you have the correct settings.



Make sure to have the following settings checked; show labels window (symbol table), addresses displayed in hexadecimal, values displayed in hexadecimal, assemble all files in directory, initialize program counter to global ‘main’ if defined, permit extended (pseudo) instructions and formats, and self-modifying code.

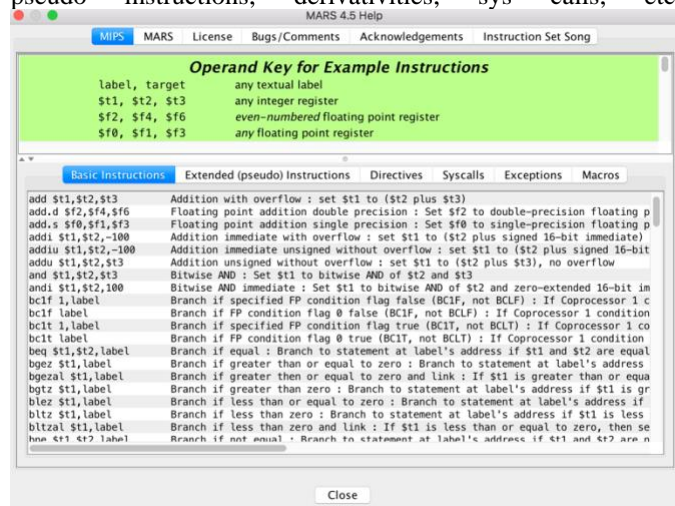
### C. The Basics of MARS

In order to program a calculator on the MARS assembler we just downloaded we must go over the basics of how to use and navigate MARS. To begin with, this is how the assembler will look when you start it:



Going across the top you have your basics, easy to navigate buttons: File, Edit, Settings, Tools, and Help. Help is a very useful and important button that we will get back to. Right below this set of buttons you have another row. From left to right the buttons are used to; create a new file for editing, open

a file for editing, save the current file, save the current file with a different name, dump machine code or data in available format, print current file, undo last edit, redo last edit, cut, copy, past, find/replace, run the current program, run one step at a time, undo the last step, pause the currently running program, stop the currently running program, reset MIPS memory and registers, and lastly, help once again. Below these buttons you have an edit view and an execution view which are used as needed (for editing and execution). On the bottom of the assembler, there is a rectangular box which gives your any messages from MARS, run time errors, and the run time output. Lastly, on the right side there is an option which allows you to view the values in your registers and coprocessors. An important feature of MARS that you must know before you begin your project is the “Help” button. Clicking this button will bring up all the basic instructions used in MIPS, as well as pseudo instructions, derivatives, sys calls, etc.



### III. INSTALLING/OPENING STARTER FILES AND UNDERSTANDING PROJECT INSTRUCTIONS

Now that we know the basics of MARS, we can begin programming the calculator. To start, visit the “Project 1” assignment on canvas and download the zip file. If you cannot find the assignment use the following link: [https://sjsu.instructure.com/courses/1324477/assignments/5056985?module\\_item\\_id=10137487](https://sjsu.instructure.com/courses/1324477/assignments/5056985?module_item_id=10137487). However, this link will only work if the project is open to you. After installing the zip file make sure to extract it. Doing so should give you an extracted file including: cs47\_common\_macro.asm, CS47\_proj\_alu\_logical.asm, CS47\_proj\_alu\_normal.asm, cs47\_proj\_macro.asm, cs47\_proj\_procs.asm, proj-auto-test.asm.

Now that we got the starter files installed, we should go over the instructions of what exactly needs to be done. The only files that need to be (or should be) edited during the process of writing this program are CS47\_proj\_alu\_logical.asm, CS47\_proj\_alu\_normal.asm, and cs47\_proj\_macro.asm. The other files are important to testing and running your code, however you must make sure that you do not edit or change these files. The

#### A. Instructions for Normal

You must edit CS47\_proj\_alu\_normal.asm which takes three arguments \$a0 first operand, \$a1 second operand, and \$a2 the operation code. This part of the program should use normal math operations in MIPS (add, sub, mul and div). to make the basic functions of the calculator. The result of operation will be stored into register \$v0 for addition and subtraction. For multiplication, the result of HI will be stored into \$v1 and LO will be stored into \$v0. Lastly, for division, the quotient will be stored into \$v0 and the remainder will be stored into \$v1.

#### B. Instructions for Logical

For this step you must edit CS47\_proj\_alu\_logical.asm which also take the same three arguments as the normal implementation. The outputs should also be the same as the normal implementation. However, the difference between alu\_normal and alu\_logical is the implementation itself. In alu\_logical you may not use MIPS mathematical operations, but instead use only MIPS logic. Alu\_logical may use regular math operations for uses such as incrementing and initializing.

- Complete the following two procedures in CS47\_proj\_alu\_normal.asm and CS47\_proj\_alu\_logical.asm. You may include your required macros (those you write) in the cs47\_proj\_macro.asm. **Do not update proj-auto-test.asm or cs47\_proj\_procs.asm or cs47\_common\_macro.asm.**
  - au\_normal (in CS47\_proj\_alu\_normal.asm): It takes three arguments as \$a0 (First operand), \$a1 (Second operand), \$a2 (Operation code '+', '-', '\*', '/' - ASCII code). It returns result in \$v0 and \$v1 (for multiplication \$v1 it will contain HI, for division \$v1 will contain remainder). This procedure uses normal math operations of MIPS to compute the result (add, sub, mul and div).
  - au\_logical (in CS47\_proj\_alu\_logical.asm): It takes three arguments as \$a0 (First operand), \$a1 (Second operand), \$a2 (Operation code '+', '-', '\*', '/' - ASCII code). It returns result in \$v0 and \$v1 (for multiplication \$v1 it will contain HI, for division \$v1 will contain remainder). The evaluation of mathematical operations should use MIPS logic operations only (result should not be generated directly using MIPS mathematical operations). The implementation needs to follow the digital algorithm implemented in hardware to implement the mathematical operations.

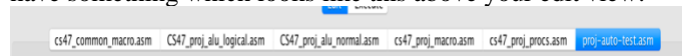
Before writing the code, you will get a 0/40 on the test cases and after the code is written correctly, you should receive a 40/40.

#### C. Opening Starter Files

Since we know the instructions and know what we have to do, let's begin with opening the starter files. To open the files, begin with starting up MARS. Once you are there, choose the button which is used to “Open a file for editing”.



After this, navigate to the unzipped folder and open each asm file one by one. After opening each file in MARS, you should have something which looks like this above your edit view:



#### IV. IMPLEMENTATION OF THE NORMAL PROCEDURE

In this part we will cover how to implement the `alu_normal` part of this project.

##### A. Creating the differnet operation symbols

Begin with creating a frame and then an if statement which will do the following: “if `$a2` (operation symbol) = ‘+’ then jump to add”. Do this for all operation symbols (+, -, \*, and /).

- ‘+’ represents additions
- ‘-’ represents subtractions
- ‘\*’ represents multiplication
- ‘/’ represents division

`au_normal:`

```
# TBD: Complete it
#create frame
addi $sp, $sp, -24
sw $fp, 24($sp)
sw $ra, 20($sp)
sw $a0, 16($sp)
sw $a1, 12($sp)
sw $a2, 8($sp)
addi $fp, $sp, 24

#body
beq $a2, '+', add #if operation is + jump to add
beq $a2, '-', subtract #if operation is - jump to subtract
beq $a2, '*', multiply #if operation is * jump to multiply
beq $a2, '/', divide #if operation is / jump to divide
```

##### B. Add

For the addition, simply use the MIPS instruction ‘add’ and store the addition into `$v0`.

##### C. Subtract

For the subtraction, use the MIPS instruction ‘sub’ and store the subtraction into `$v0`.

##### D. Multiply

For multiplication, multiply the operands together using ‘mult’ which will automatically store the HI value into HI and the LO value into LO. The ‘mflo’ (move from lo) and ‘mfhi’ (move from hi) to be the values into `$v0` and `$v1` as instructed.

##### E. Divide

For division, divide the operands using ‘div’ which will automatically move the quotient to LO and the remainder to HI. Then, as you did in multiply, use ‘mflo’ and ‘mfhi’ to move the values into `$v0` and `$v1`.

```
add:
    add $v0, $a0, $a1 #v0=$a0+$a1
    j end #jump to end where program restores frame

subtract:
    sub $v0, $a0, $a1 #v0=$a0-$a1
    j end #jump to end where program restores frame

multiply:
    mult $a0, $a1 #multiply $a0 and $a1
    mflo $v0 #v0 = LO
    mfhi $v1 #v1 = HI
    j end #jump to end where program restores frame

divide:
    div $a0, $a1 #divide $a0 by $a1 where LO is quotient and HI is remainder
    mflo $v0 #quotient
    mfhi $v1 #remainder
    j end #jump to end where program restores frame

end:
    #restore frame
    lw $fp, 24($sp)
    lw $ra, 20($sp)
    lw $a0, 16($sp)
    lw $a1, 12($sp)
    lw $a2, 8($sp)
    addi $sp, $sp, 24
    jr $ra
```

Once you have completed the implementation of `alu_normal` you should be able to get 1/40 on the test case.

#### V. IMPLEMENTATION OF THE LOGICAL PROCEDURE

In this part we will go over the implementation of `alu_logical`.

##### A. Macros

To make the process a little simpler we will create some macros: `extract_nth_bit($regD,$regS,$regT)` and `insert_to_nth_bit($regD,$regS,$regT,$maskReg)`.

`Extract_nth_bit($regD,$regS,$regT)` should be able to extract the bit at the `$regT` position (0-31) from `$regS` (the source bit pattern) and this should result into `$regD` being 0x1 or 0x0. To implement this macro use ‘srlv’ to shift right on `$regS` by `$regT` and store that value into `$regD`. Then you AND that value with 0x1 to get the value of the bit. This macro should look something like this:

```
.macro extract_nth_bit($regD, $regS, $regT) #as described in video
    srlv $regD, $regS, $regT
    and $regD, $regD, 1
.end_macro
```

`Insert_to_nth_bit($regD,$regS,$regT,$maskReg)` should insert the value from `$regT` (register containing the bit to insert, 0 or 1) into `$regD` at `$regS` (the nth position). `$regMask` is used to hold a temporary mask. Begin by initializing the `$regMask` to 1. Then, left shifting mask by n bits. After you have done that, invert `$maskReg`. Next, do an AND operation with your new `$maskReg` and `$regD`. After this, you shift `$regT` n times and then perform an OR operation with `$regD`.

```

      1
      v
1 1 1 1 0 1 1 0 <--- D; n=3; b=1

-----
0 0 0 0 0 0 1 <--- M == Mask
0 0 0 0 1 0 0 0 <--- M = M << n

1 1 1 1 0 1 1 1 <--- M = !M
& 1 1 1 1 0 1 1 0 <--- D

-----
1 1 1 1 0 1 1 0
| 0 0 0 0 1 0 0 0 <--- b = b << n

-----
1 1 1 1 1 1 1 0
```

After following these steps, you should get a macro looking like this:

```
.macro insert_to_nth_bit ($regD, $regS, $regT, $maskReg) #as described in video
    li $maskReg, 1
    sllv $maskReg, $maskReg, $regS
    not $maskReg, $maskReg
    and $regD, $regD, $maskReg
    sllv $regT, $regT, $regS
    or $regD, $regD, $regT
.end_macro
```

##### B. Creating the differnet operation symbols

Similar to the way we created if then statements using `beq` in the `alu_normal`, we will do the same here.

```
au_logical:
# TBD: Complete it
#body
beq $a2, '+', addition #if operation is + jump to add_sub
beq $a2, '-', subtract #if operation is - jump to add_sub
beq $a2, '*', multiply #if operation is * jump to multiply
beq $a2, '/', divide #if operation is / jump to divide
.....
```



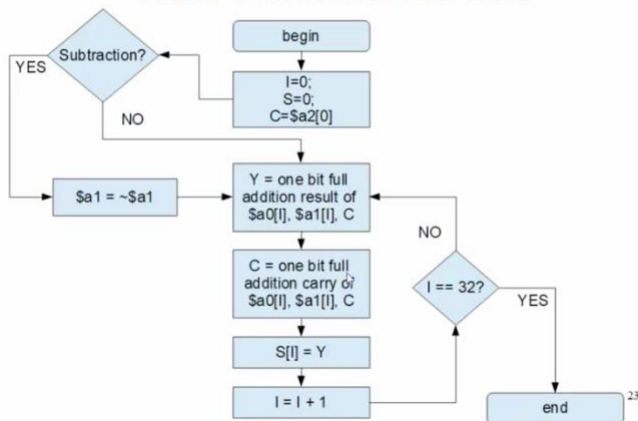
### C. Addition and Subtraction

The process for addition and subtraction is very similar, so we will attempt to combine some parts of the process for these two operations.

\$a0 is the first operand, \$a1 is the second operand and \$a2 is a “mode” where it is set to 0x00000000 if the operation is addition and 0xFFFFFFFF if the operation is subtraction. To begin with, the if statement should branch to a label called addition or subtraction depending on the operation which should alter the value in \$a2 register as needed. These two should come back together by branching to a label, ‘add\_sub’ which initializes the counter, summation, and C (the first bit of \$a2). Check to see what the value of C is. If C is 0 then the procedure addition, so jump to ‘add\_sub\_process’. On the other hand, if C is 1 then the procedure is subtraction, so invert the second operand and then jump to ‘add\_sub\_process’.

Inside of the ‘add\_sub\_process’ you perform one-bit full addition. One-bit full addition is where you pick up one bit at a time from each operand and from C and then XOR between them. C is the carry bit of the XOR between the previous one-bit addition. Since you are doing one bit at a time for the entire number you should have a loop going from 0 to 31. Use the macros created to extract one bit at a time, add them and then insert each bit where it belongs inside of \$v0, which should include your final answer. Repeat this process by incrementing I until you finish with the MSB (Incrementor = 31). Once I = 31 branch to ‘add\_sub\_end’ where you restore the frame. The algorithm of this process is visualized as the following:

#### Write common Add/Sub



Once completed, your implementation should look similar to the one shown below. However, it may or may not differ depending on if you followed this algorithm or not. Also, it may differ depending on the instructions and pseudo instructions you used and in what order you performed your operations.

```

24 addition:
25     li     $a2, 0x00000000
26
27     j      add_sub
28
29 subtract:
30     li     $a2, 0xFFFFFFFF
31
32     j      add_sub
33
34 add_sub:
35     #create frame
36     addi   $sp, $sp, -32
37     sw     $fp, 32($sp)
38     sw     $ra, 28($sp)
39     sw     $t0, 24($sp)
40     sw     $t1, 20($sp)
41     sw     $t2, 16($sp)
42     sw     $t3, 12($sp)
43     sw     $t4, 8($sp)
44     addi   $fp, $sp, 32
45
46     li     $t0, 0x0 #index=0
47     li     $v0, 0x0 #summation = 0
48
49     extract_nth_bit($t1, $a2, $t0) #c=$a2[0]
50
51     beq     $a2, 0x0, add_sub_process
52
53     j      invert
54

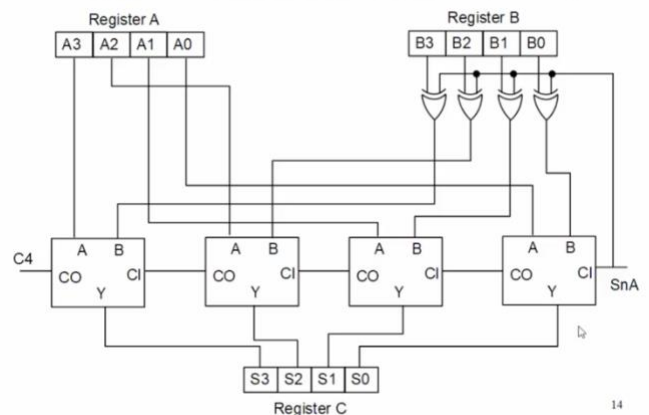
```

```

55 invert:
56     nor     $a1, $a1, $zero
57
58     j      add_sub_process
59
60 add_sub_process:
61     extract_nth_bit($t2, $a0, $t0)
62     extract_nth_bit($t3, $a1, $t0)
63
64     xor     $t4, $t2, $t3 #op 1 xor op 2
65     and     $t5, $t2, $t3
66     xor     $t6, $t4, $t1 #c xor (op1 xor op 2)
67     and     $t1, $t1, $t4
68
69     or      $t1, $t1, $t5
70
71     insert_to_nth_bit($v0, $t0, $t6, $t3)
72
73     addi    $t0, $t0, 0x1 #increment index
74     beq     $t0, 32, add_sub_end #if index = 32 then break loop
75
76     j      add_sub_process #loop
77
78 add_sub_end:
79     #restore frame
80     lw      $fp, 32($sp)
81     lw      $ra, 28($sp)
82     lw      $t0, 24($sp)
83     lw      $t1, 20($sp)
84     lw      $t2, 16($sp)
85     lw      $t3, 12($sp)
86     lw      $t4, 8($sp)
87     addi    $sp, $sp, 32
88
89     jr      $ra
90

```

The multi bit addition and subtraction diagram/flow chart looks as shown below:



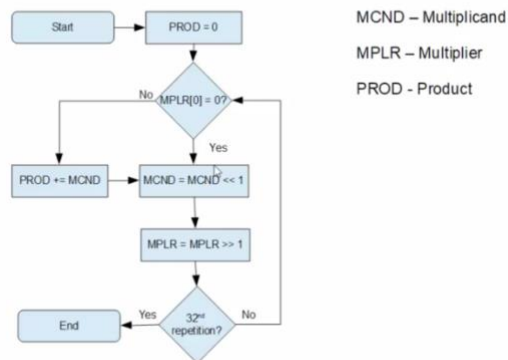
Once you have completed the implementation of the alu\_normal and the alu\_logical addition and subtraction part you should be able to get a 20/40 on the test cases. You should be halfway done with the project (P.S this was the easier half, the next part gets crazy).

### D. Multiplication

The algorithm of the multiplication processes goes as follows. You start and assign product (a 64-bit output) as 0. Then, you look at the LSB of the multiplier and test if it is 0 or not. If the multiplier is 1, add the product with the multiplicand, so product = product + multiplicand and then left shift multiplicand by one bit. If the multiplier is 0 then skip straight

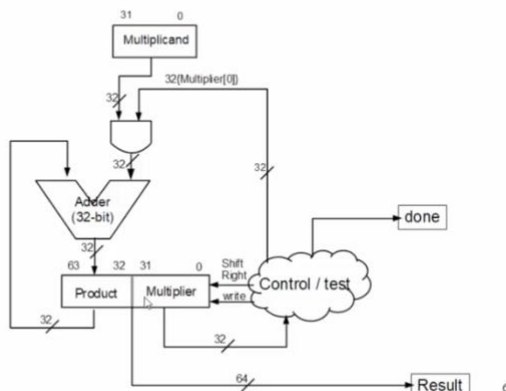
to shifting the multiplicand by one bit. Next, you shift the multiplier to the right by one bit. You do this on a loop, with an incrementor. Once, you hit 31 you stop. The visual representation of the algorithm looks like this:

## Binary Multiplication Algorithm



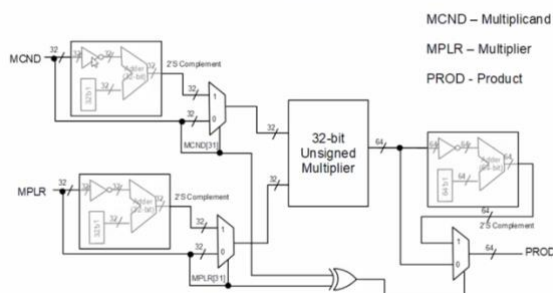
A 32-bit unsigned multiplier has a diagram which make it a lot easier to visualize what the multiplier is actually doing.

## Simplified Sequential Multiplier



However, this is only for a 32-bit unsigned multiplier. We also want to construct signed multiplication. Unsigned multiplication will ignore the signs of the operands and only give you a positive answer, thus having a signed multiplier in our program is essential. A signed multiplier visual looks like the following:

## Signed Multiplication Circuit



To implement this in MARS we must create a few procedures:

1) *Twos\_complement*- This procedure should return the twos complement of the argument (\$a0). In this procedure you use 'NOT' and your previously designed addition procedure to compute  $\sim a0 + 1$ .

```
205 twos_complement:
206     not    $a0, $a0
207     li     $a1, 1
208     j      addition #~$a0 + 1
209
```

2) *Twos\_complement\_if\_negative*- Depending on if the bit pattern is negative use this procedure. It should return the twos complement of \$a0 if \$a0 is negative. If the incoming bit pattern is negative then do twos\_complement otherwise do not. This procedure should simply call twos\_complement if necessary.

```
210 twos_complement_if_negative:
211     bltz   $a0, twos_complement
212     jr     $ra
213
```

3) *Twos\_comp\_64bit*- the argument \$a0 is the lower half of the address and the argument \$a1 is the hi of the number. It should return \$v0, the lo part of the 2s complement 64 bit and \$v1, the hi part of the the 2s complement 64 bit. First invert both \$a0 and \$a1. Then, use your previously created addition procedure to add 1 to \$a0. Lastly, add carry from previous step to \$a1 (also using the addition procedure you created). Make sure to not just take the complement of the upper and lower half because this will not work.

```
214 twos_comp_64bit:
215     #create frame
216     addi   $sp, $sp, -16
217     sw     $fp, 16($sp)
218     sw     $ra, 12($sp)
219     sw     $t0, 8($sp)
220     addi   $fp, $sp, 16
221
222     nor    $t0, $a1, $zero
223     nor    $a0, $a0, $zero
224     add    $a1, $zero, 1
225
226     jal    addition
227
228     move   $a0, $t0
229     move   $t0, $v0
230     move   $a1, $v1
231
232     jal    addition
233
234     move   $v1, $v0
235     move   $v0, $t0
236
237     #restore frame
238     lw     $fp, 16($sp)
239     lw     $ra, 12($sp)
240     lw     $t0, 8($sp)
241     addi   $sp, $sp, 16
242
243     jr     $ra
244
```

4) *Bit\_replicator*- replicates a given bit value to 32 times. This takes an argument of \$a0 which is 0x0 or 0x1 and sets \$v0 to 0x00000000 if \$a0 is 0x0 or 0xFFFFFFFF if \$a0 is 0x1.

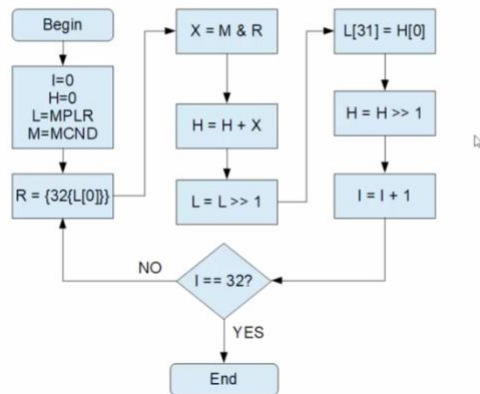
```

245 bit_replicator:
246     beq    $a0, 0x0, replicate_0
247     li     $v0, 0xFFFFFFFF
248     jr     $ra
249
250 replicate_0:
251     li     $v0, 0
252     jr     $ra
253

```

5) *Multiply\_unsigned*- this should take \$a0 (the multiplicand) and \$a1 (the multiplier) as arguments. Its should return lo through \$v0 and high through \$v1. The algorithm looks like this:

### Unsigned Multiplication



The code for unsigned multiply should look like the following:

```

139 multiply_unsigned:
140     #create frame
141     addi   $sp, $sp, -48
142     sw     $fp, 48($sp)
143     sw     $ra, 44($sp)
144     sw     $s0, 40($sp)
145     sw     $s1, 36($sp)
146     sw     $s2, 32($sp)
147     sw     $s3, 28($sp)
148     sw     $s4, 24($sp)
149     sw     $s5, 20($sp)
150     sw     $t0, 16($sp)
151     sw     $t1, 12($sp)
152     sw     $t2, 8($sp)
153     addi   $fp, $sp, 48
154
155     add    $s0, $zero, $zero #I
156     add    $s1, $zero, $zero #H
157     move   $s2, $a0 # $a0 is multiplicand = M
158     move   $s3, $a1 # $a1 is multiplier = L
159
160     j      multiply_process
161

```

6) *Signed Multiplication*: Set n1 to \$a0 and n2 to \$a1. Make n1 and n2 twos complement if they are negative. Then, call unsigned multiplication using n1 and n2. Then determine the sign of the bit by extracting the MSB of \$a0 and \$a and xor between them. The xor result is S. If S is 1 then use

twos\_comp\_64bit to determine the twos complement of the number.

Following the algorithms and diagrams above your code for multiplication should appear as this:

```

91 multiply:
92     #create frame
93     addi   $sp, $sp, -28
94     sw     $fp, 28($sp)
95     sw     $ra, 24($sp)
96     sw     $s2, 20($sp)
97     sw     $s1, 16($sp)
98     sw     $s0, 12($sp)
99     sw     $t0, 8($sp)
100    addi   $fp, $sp, 28
101
102    move    $s0, $a0 #n1
103    move    $s1, $a1 #n2
104    move    $v0, $a0
105
106    jal     twos_complement_if_negative #if negative returns in $v0
107
108    move    $s2, $v0 #n1 is stored in s2
109    move    $a0, $s1
110    move    $v0, $s1
111
112    jal     twos_complement_if_negative
113
114    move    $a1, $v0 #n2 = a1
115    move    $a0, $s2
116
117    jal     multiply_unsigned #calls unsigned multiplication with $a1 and $a0
118
119    move    $a0, $v0 #quotient
120    move    $a1, $v1 #remainder
121    add     $t0, $zero, 31
122
123    extract_nth_bit($s0, $s0, $t0) #sign of a0 in s0
124    extract_nth_bit($s1, $s1, $t0) #sign of a1 in s1
125
126    xor     $s0, $s0, $s1 #s in s0
127    beq     $s0, 1, twos_comp_64bit #get complement if s is 1
128
129    #restore frame
130    lw      $fp, 28($sp)
131    lw      $ra, 24($sp)
132    lw      $s2, 20($sp)
133    lw      $s1, 16($sp)
134    lw      $s0, 12($sp)
135    lw      $t0, 8($sp)
136    addi    $sp, $sp, 28
137    jr      $ra
138

```

```

162 multiply_process:
163     extract_nth_bit($s4, $s3, $zero)
164
165     move    $a0, $s4
166
167     jal     bit_replicator #replicate the value in R 32 times, returns in $v0
168
169     move    $s4, $v0
170     and     $s5, $s2, $s4 #X = M & R
171     add     $s1, $s1, $s5 #H = H + X
172     srl     $s3, $s3, 1 #L = L >> 1
173
174     extract_nth_bit($t0, $s1, $zero) #extract 0th bit from H
175
176     add     $t1, $zero, 31
177
178     insert_to_nth_bit($s3, $t1, $t0, $t2) #L[31] = H[0]
179
180     srl     $s1, $s1, 1 #H = H >> 1
181     add     $s0, $s0, 1 #increment counter
182     beq     $s0, 32, multiply_end #if index = 32 then break loop
183
184     j      multiply_process #loop
185

```

```

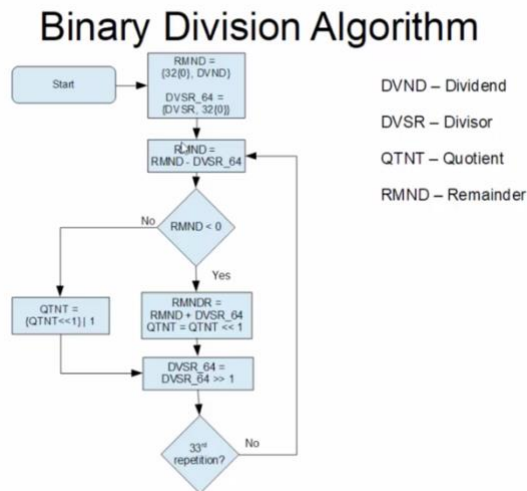
186 multiply_end:
187     move    $v0, $s3 #lo
188     move    $v1, $s1 #hi
189
190     #restore frame
191     lw      $fp, 48($sp)
192     lw      $ra, 44($sp)
193     lw      $s0, 40($sp)
194     lw      $s1, 36($sp)
195     lw      $s2, 32($sp)
196     lw      $s3, 28($sp)
197     lw      $s4, 24($sp)
198     lw      $s5, 20($sp)
199     lw      $t0, 16($sp)
200     lw      $t1, 12($sp)
201     lw      $t2, 8($sp)
202     addi    $sp, $sp, 48
203     jr      $ra
204

```

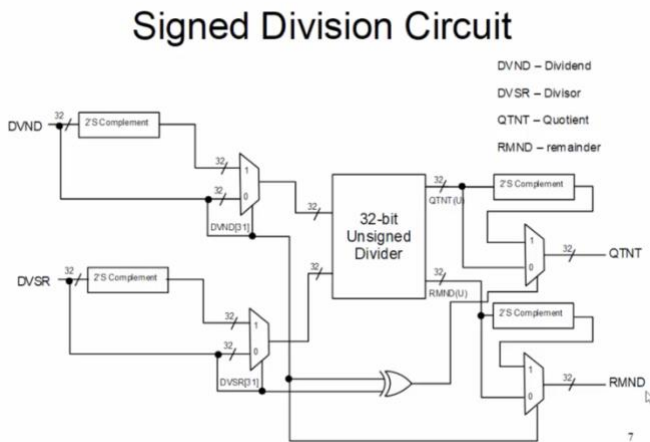
This code above should be accompanied with the procedures we went over.

### E. Division

The algorithm should begin by loading the remainder register (64 bits) with the dividend in the lower half and 32 0's in the upper half and loading the divisor register (64 bits) with the divisor in the upper half and 32 0's in the lower half. Next, you do remainder = remainder - divisor (64) using a 64-bit subtractor. Next, if the remainder is not less than 0 then left shift quotient by one and then OR with 1. On the other hand, if the remainder is less than one after doing remainder = remainder - divisor, then you do remainder = remainder + divisor and then left shift quotient by 1. Then, we right shift divisor by 1. You do this until 33<sup>rd</sup> repetition. The visual representation of the algorithm looks as following:



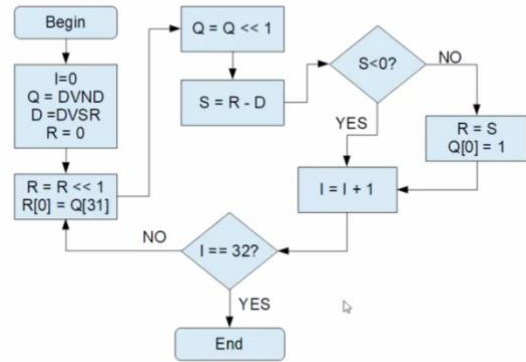
A visual representation of a signed division circuit looks like this:



Your code for alu\_divide should include the following procedures:

1) *Divide\_unassigned*- this takes the arguments \$a0 (dividend) and \$a1 (divisor) and returns \$v0 (quotient) and \$v1 (remainder). The approach to writing the algorithm for *divide\_unassigned* is as follows:

## Unsigned Division



The steps of signed division are as follows:

## Signed Division

### • Steps

- N1 = \$a0, N2 = \$a1
- Make N1 two's complement if negative
- Make N2 two's complement if negative
- Call unsigned Division using N1, N2. Say the result is Q and R
- Determine sign S of Q
  - Extract \$a0[31] and \$a1[31] bits and xor between them. The xor result is S.
  - If S is 1, use the 'twos\_complement' to determine two's complement form of Q.
- Determine sign S of R
  - Extract \$a0[31] and assign this to S
  - If S is 1, use the 'twos\_complement' to determine two's complement form of R.

Once completed, your code for divide should look like this:

```

206 divide:
207     #create frame
208     addi $sp, $sp, -28
209     sw $fp, 28($sp)
210     sw $ra, 24($sp)
211     sw $s2, 20($sp)
212     sw $s1, 16($sp)
213     sw $s0, 12($sp)
214     sw $t0, 8($sp)
215     addi $fp, $sp, 28
216
217     la $s0, ($a0) #N1
218     la $s1, ($a1) #N2
219     move $v0, $a0
220
221     jal twos_complement_if_negative #if negative then take complement
222
223     move $s2, $v0 #N1 = s2
224     move $a0, $s1
225     move $v0, $s1
226
227     jal twos_complement_if_negative #if negative then take complement
228
229     move $a1, $v0 #N2 = a1 divisor
230     move $a0, $s2 #N1 = a0 dividend
231
232     jal divide_unsigned #returns $v0 quotient and $v1 remainder
233
234     move $a0, $v0 #Q
235     move $a1, $v1 #R
236
237     #determine sign
238     add $t0, $zero, 31
239
240     extract_nth_bit($s0, $s0, $t0) #sign of a0 in t2
241     extract_nth_bit($s1, $s1, $t0) #sign of a1 in s1
242
243     xor $t6, $s0, $s1 #S in t2
244     and $t7, $t6, $s0
245     beq $t7, 1, complement2 #if both are 1 then negate both
246     beq $t6, 1, twos_complement
247     beq $s0, 1, complement
248
249     #restore frame
250     lw $fp, 28($sp)
251     lw $ra, 24($sp)
252     lw $s2, 20($sp)
253     lw $s1, 16($sp)
  
```



```

253     lw     $s1, 16($sp)
254     lw     $s0, 12($sp)
255     lw     $t0, 8($sp)
256     addi   $sp, $sp, 28
257     jr     $ra
258
259 divide_unsigned:
260     addi   $sp, $sp, -48
261     sw     $fp, 48($sp)
262     sw     $ra, 44($sp)
263     sw     $s0, 40($sp)
264     sw     $s1, 36($sp)
265     sw     $s2, 32($sp)
266     sw     $s3, 28($sp)
267     sw     $s4, 24($sp)
268     sw     $s5, 20($sp)
269     sw     $t0, 16($sp)
270     sw     $t1, 12($sp)
271     sw     $t2, 8($sp)
272     addi   $fp, $sp, 48
273
274     add     $s0, $zero, $zero # I (counter)
275     add     $s1, $zero, $zero # R Remainder
276     move    $s2, $a0 # Q
277     move    $s3, $a1 # D
278
279     j       divide_process
280
281 divide_process:
282     sll     $s1, $s1, 1 # R = R << 1
283     li      $t0, 31
284
285     extract_nth_bit($s4, $s2, $t0) #extract 31st bit from Q
286     insert_to_nth_bit($s1, $zero, $s4, $t0) #insert at R[0]
287
288     sll     $s2, $s2, 1 # Q = Q << 1
289     move    $a0, $s1 #move R into $a0
290     move    $a1, $s3 #move D into $a1
291
292     jal     subtract
293
294     move    $s5, $v0 #solution stored in $s5 after subtracting S
295     la      $a0, ($s2)
296     bltz    $s5, check_loop
297     move    $s1, $s5
298     li      $t1, 1
299
300     insert_to_nth_bit($s2, $zero, $t1, $t0)
301
302     j       check_loop
303
304 check_loop:
305     addi    $s0, $s0, 1
306     li      $t2, 32
307     beq     $s0, $t2, divide_process_end #if index = 32 then break loop
308     j       divide_process #loop
309
310 divide_process_end:
311     move    $v1, $s1 #remainder
312     move    $v0, $s2 #quotient
313
314     #restore frame
315     lw     $fp, 48($sp)
316     lw     $ra, 44($sp)
317     lw     $s0, 40($sp)
318     lw     $s1, 36($sp)
319     lw     $s2, 32($sp)
320     lw     $s3, 28($sp)
321     lw     $s4, 24($sp)
322     lw     $s5, 20($sp)
323     lw     $t0, 16($sp)
324     lw     $t1, 12($sp)
325     lw     $t2, 8($sp)
326     addi   $sp, $sp, 48
327     jr     $ra
328

```

auto-test.asm file (on MARS) and hit the ‘assemble the current file and clear breakpoints’ button. Then, hit the ‘run the current program’ button. Assuming you did everything correct, your output should be:

```

(4 + 2)    normal => 6    logical => 6    [matched]
(4 + 2)    normal => 2    logical => 2    [matched]
(4 * 2)    normal => HI:0 L0:8    logical => HI:0 L0:8    [matched]
(4 / 2)    normal => R:0 Q:2    logical => R:0 Q:2    [matched]
(16 + -3)  normal => 13    logical => 13    [matched]
(16 - -3)  normal => 19    logical => 19    [matched]
(16 * -3)  normal => HI:-1 L0:-48    logical => HI:-1 L0:-48    [matched]
(16 / -3)  normal => R:1 Q:-5    logical => R:1 Q:-5    [matched]
(-13 + 5)  normal => -8    logical => -8    [matched]
(-13 - 5)  normal => -18    logical => -18    [matched]
(-13 * 5)  normal => HI:-1 L0:-65    logical => HI:-1 L0:-65    [matched]
(-13 / 5)  normal => R:-3 Q:-2    logical => R:-3 Q:-2    [matched]
(-2 + -8)  normal => -10    logical => -10    [matched]
(-2 - -8)  normal => 6    logical => 6    [matched]
(-2 * -8)  normal => HI:0 L0:16    logical => HI:0 L0:16    [matched]
(-2 / -8)  normal => R:-2 Q:0    logical => R:-2 Q:0    [matched]
(-6 + -6)  normal => -12    logical => -12    [matched]
(-6 - -6)  normal => 0    logical => 0    [matched]
(-6 * -6)  normal => HI:0 L0:36    logical => HI:0 L0:36    [matched]
(-6 / -6)  normal => R:0 Q:1    logical => R:0 Q:1    [matched]
(-18 + 18) normal => 0    logical => 0    [matched]
(-18 - 18) normal => -36    logical => -36    [matched]
(-18 * 18) normal => HI:-1 L0:-324    logical => HI:-1 L0:-324    [matched]
(-18 / 18) normal => R:0 Q:-1    logical => R:0 Q:-1    [matched]
(5 + -8)   normal => -3    logical => -3    [matched]
(5 - -8)   normal => 13    logical => 13    [matched]
(5 * -8)   normal => HI:-1 L0:-40    logical => HI:-1 L0:-40    [matched]
(5 / -8)   normal => R:5 Q:0    logical => R:5 Q:0    [matched]
(-19 + 3)  normal => -16    logical => -16    [matched]
(-19 - 3)  normal => -22    logical => -22    [matched]
(-19 * 3)  normal => HI:-1 L0:-57    logical => HI:-1 L0:-57    [matched]
(-19 / 3)  normal => R:-1 Q:-6    logical => R:-1 Q:-6    [matched]
(4 + 3)    normal => 7    logical => 7    [matched]
(4 - 3)    normal => 1    logical => 1    [matched]
(4 * 3)    normal => HI:0 L0:12    logical => HI:0 L0:12    [matched]
(4 / 3)    normal => R:1 Q:1    logical => R:1 Q:1    [matched]
(-26 + -64) normal => -90    logical => -90    [matched]
(-26 - -64) normal => 38    logical => 38    [matched]
(-26 * -64) normal => HI:0 L0:1664    logical => HI:0 L0:1664    [matched]
(-26 / -64) normal => R:-26 Q:0    logical => R:-26 Q:0    [matched]

Total passed 40 / 40
*** OVERALL RESULT PASS ***

-- program is finished running --

```

## F. Testing

Now you should be finished with implementing `alu_normal` and `alu_logical` so we could test if our code works as expected. To test the code, make sure all files are saved as the latest version and then run the code. To run the code, go to the proj-