Panel Data Analysis of Interactive Effects between High-Danger Shots, Rebounds, and Secondary Skills on NHL Goal Production

1. Introduction

Modern hockey analytics has moved beyond traditional statistics to examine the complex factors driving goal production. High-danger shots, defined as shots taken from within 29 feet of the center of the goal and bounded by imaginary lines drawn from the face-off dots to 2 feet outside the goalpost [1] are strong predictors of goal scoring. However, secondary skills like rebound generation, physical play, and puck management may amplify or diminish their effectiveness [2]. Understanding these interactive relationships is crucial for player evaluation and team strategy. Despite advances in hockey analytics, limited research has systematically examined how high-danger shooting combines with complementary skills to influence goal production. Previous research predominantly treats these factors independently, possibly missing critical interactive

relationships. This study addresses this gap by analyzing five seasons of NHL data (2020-21 through 2024-25) using fixed-effects panel regression to control for unobserved player characteristics and examine skill complementarity in offensive production. 1.1 Research Question

How do high-danger shooting opportunities and rebound generation jointly influence goal production in hockey, and how do secondary skills (hits, takeaways, giveaways) interact with this relationship? 2. Methodology

2.1 Data Sources

This study utilizes comprehensive player-level performance data [3], covering five complete NHL regular seasons from 2020-21 through 2024-25. The dataset includes game-by-game statistics for all NHL players across multiple performance dimensions, providing detailed metrics on shooting, defensive actions, and situational factors. #load the libraries

library(ggplot2) library(GGally) ## Registered S3 method overwritten by 'GGally': ## method from +.gg ggplot2 library(corrplot)

corrplot 0.95 loaded library(plm)

library(dplyr)

Attaching package: 'dplyr' ## The following objects are masked from 'package:plm': between, lag, lead ## The following objects are masked from 'package:stats': ## filter, lag ## The following objects are masked from 'package:base': ## intersect, setdiff, setequal, union library(lmtest) ## Loading required package: zoo

Attaching package: 'zoo' ## The following objects are masked from 'package:base': ## as.Date, as.Date.numeric library(sandwich) #load files and add season indicator data_24_25 <- read.csv("D:/hockey-skill-interactions-analysis/dataset/2024_2025.csv") %>% mutate(season = "2024_2 data_23_24 <- read.csv("D:/hockey-skill-interactions-analysis/dataset/2023_2024.csv") %>% mutate(season = "2023_2 data_22_23 <- read.csv("D:/hockey-skill-interactions-analysis/dataset/2022_2023.csv") %>% mutate(season = "2022_2 data_21_22 <- read.csv("D:/hockey-skill-interactions-analysis/dataset/2021_2022.csv") %>% mutate(season = "2021_2 data_20_21 <- read.csv("D:/hockey-skill-interactions-analysis/dataset/2020_2021.csv") %>% mutate(season = "2020_2 #merge all seasons data_all <- bind_rows(data_24_25, data_23_24, data_22_23, data_21_22, data_20_21)

data_all <- data_all %>% mutate(hd_rate = I_F_highDangerShots / icetime, goals_rate = I_F_goals / icetime, mom_diff = (xGoalsForAfterShifts - xGoalsAgainstAfterShifts) / icetime, reb_rate = I_F_xGoals_with_earned_rebounds / icetime, phys_rate = I_F_hits / icetime, o_d_start_diff = I_F_oZoneShiftStarts - I_F_dZoneShiftStarts) #remove missing values data_clean <- na.omit(data_all)</pre> 2.3 Exploratory Data Analysis Prior to model estimation, correlation analysis was conducted to examine the relationships between key variables and identify potential multicollinearity concerns. #compute correlation matrix

All performance metrics were standardized as per-minute rates to ensure comparability across players with varying ice time allocations. The dependent variable, goal production rate (goals_rate), represents goals scored per minute of ice time. Primary independent variables include

high-danger shot rate (hd_rate) and rebound rate (reb_rate), while secondary skills encompass physical engagement (phys_rate),

hd_rate goals_rate mom_diff reb_rate phys_rate take_rate give_rate ## hd_rate 0.186 -0.006 0.459 -0.029

round(cor_matrix, 3)

goals_rate

mom_diff

reb_rate

take_rate

df_games,

drop.index = TRUE

model = "within")

Residuals:

Coefficients:

Unbalanced Panel: n = 1460, T = 2-25, N = 22117

Min. 1st Qu. Median 3rd Qu.

-1.9073e-02 -7.8727e-05 8.0314e-05 2.3081e-04 1.1962e-01

phys_rate 2.7689e-02 4.7661e-03 5.8096 6.354e-09 ***

index = c("playerId", "season_game"),

0.19

-0.01

0.46

0.00

0.00

0.70

-0.02

0.00

cor_matrix <- cor(data_clean[, cor_vars])</pre>

cor_vars <- c("hd_rate", "goals_rate", "mom_diff",</pre>

"reb_rate", "phys_rate", "take_rate", "give_rate")

0.00

-0.01

0.01

0.00

0.70

-0.01

-0.04

0.00

-0.02

0.01

-0.04

0.00

2.2 Variable Construction

#create rate variables per minutes

defensive takeaways (take_rate), and puck management (give_rate).

goals_rate 0.186 1.000 -0.005 0.704 -0.019 -0.001 -0.002 ## mom_diff -0.006 -0.005 1.000 -0.010 0.006 -0.001 0.011 0.459 0.704 -0.010 1.000 -0.043 0.000 -0.009 ## reb_rate -0.004 ## phys_rate -0.029 -0.019 0.006 -0.043 1.000 0.018

-0.003

-0.010

0.6

0.4

0.2

-0.2

-0.4

take_rate -0.003 -0.001 -0.001 0.000 -0.0040.002 1.000 ## give_rate -0.010 -0.002 0.011 -0.0091.000 0.018 0.002 #compute correlation matrix (heatmap) corrplot(cor_matrix, method = "color", addCoef.col = "black") hd_rate 0.19 -0.03 0.00 -0.01 0.46

0.00

0.00

0.00

0.00

0.01

-0.01

0.02

0.00

-0.6 8.0give_rate -0.01 0.00 0.01 -0.01 0.02 0.00 2.4 Panel Data Structure The analysis utilized a balanced panel design where individual players observed across multiple games within each season. To create unique time identifiers, games were sequentially numbered within each season for each player, then combined with season indicators to generate unique season_game identifiers. #create an unique identifier for each game within each player for each season df_games <- data_clean %>% arrange(playerId, season) %>% group_by(playerId, season) %>% mutate(game_row = row_number()) %>% ungroup() #create a new columns that merge season and game_row to become season_game that uniquely identifies each game ins ide a season df_games <- df_games %>% mutate(season_game = paste(season, game_row, sep = "_")) #build panel data frame on playerId and season_game so that the fixed effects with plm can be conducted df_panel_games <- pdata.frame(</pre>

#check for duplicate pairs which should be zero df_check <- df_games %>% count(playerId, season_game) %>% filter(n > 1) df_check ## # A tibble: 0 × 3 ## # i 3 variables: playerId <int>, season_game <chr>, n <int> 2.5 Model Specification The primary approach utilizes fixed-effects panel regression to investigate both main effects and interaction patterns between high-danger shooting and complementary skills. The fixed-effects ("within") estimator controls for unobserved player-specific characteristics that remain constant over time, such as innate shooting ability or positional tendencies. #built model with interaction terms fe_goals_model <- plm(goals_rate ~ hd_rate * reb_rate + hd_rate * phys_rate + hd_rate * take_rate + hd_rate * giv e_rate, data = df_panel_games, model = "within") #look at the summary summary(fe_goals_model) ## Oneway (individual) effect Within Model ## ## plm(formula = goals_rate ~ hd_rate * reb_rate + hd_rate * phys_rate +

hd_rate * take_rate + hd_rate * give_rate, data = df_panel_games,

Estimate Std. Error t-value Pr(>|t|)

take_rate 3.1708e-03 3.4303e-03 0.9244 0.35531 ## give_rate 1.8637e-02 1.3265e-02 1.4050 0.16004 ## hd_rate:reb_rate -4.6847e+01 9.7533e-01 -48.0322 < 2.2e-16 *** ## hd_rate:phys_rate -1.8026e+02 1.0019e+01 -17.9920 < 2.2e-16 *** ## hd_rate:take_rate -3.2542e+02 2.1708e+01 -14.9909 < 2.2e-16 *** ## hd_rate:give_rate -5.7993e+01 9.8285e+00 -5.9005 3.680e-09 *** ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 ## Total Sum of Squares: 0.072433 ## Residual Sum of Squares: 0.030644 ## R-Squared: 0.57694 ## Adj. R-Squared: 0.54686 ## F-statistic: 3128.67 on 9 and 20648 DF, p-value: < 2.22e-16 2.6 Statistical Inference Standard errors were adjusted for heteroscedasticity and within-player correlation using the HC1 robust variance estimator with clustering at the player level. This approach accounts for potential correlation of error terms within players across games while allowing for heteroscedastic residuals. #computes robust standards error that adjust for clustering by the player and run t-test coeftest(fe_goals_model, vcov = vcovHC(fe_goals_model, type = "HC1", cluster = "group")) ## t test of coefficients: ## Estimate Std. Error t value Pr(>|t|)
hd_rate -1.5518e-02 1.3153e-01 -0.1180 0.90608 2.7941e+00 1.1962e+00 2.3358 0.01951 * ## reb_rate ## phys_rate 2.7689e-02 1.7879e-02 1.5487 0.12148 ## take_rate 3.1708e-03 4.0254e-03 0.7877 0.43088 ## give_rate 1.8637e-02 1.6248e-02 1.1471 0.25137 ## hd rate:reb rate -4.6847e+01 3.8458e+01 -1.2182 0.22318 ## hd_rate:phys_rate -1.8026e+02 1.1909e+02 -1.5137 0.13012

2.7 Model Simplification Following estimation of the full interactive model, a simplified specification was developed focusing on statistically significant relationships, retaining the theoretically important high-danger shot and rebound interaction while including secondary skills as direct effects. #simplified model focusing on significant relationships

s, model = "within") summary(fe_goals_simple)

Residuals:

Coefficients:

Total Sum of Squares: 0.072433 ## Residual Sum of Squares: 0.031631

R-Squared: 0.5633 ## Adj. R-Squared: 0.53232

hd_rate:take_rate -3.2542e+02 2.3096e+02 -1.4090 0.15885 ## hd_rate:give_rate -5.7993e+01 8.8481e+01 -0.6554 0.51220

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

give_rate, data = df_panel_games, model = "within")

-1.8200e-02 -6.9390e-05 8.1712e-05 2.3740e-04 1.2508e-01

F-statistic: 4439.68 on 6 and 20651 DF, p-value: < 2.22e-16

3.2 Fixed-effects Panel Regression Results

plm(formula = goals_rate ~ hd_rate * reb_rate + hd_rate * phys_rate + hd_rate * take_rate + hd_rate * give_rate, data = df_panel_games,

Median

hd_rate:reb_rate -4.6847e+01 9.7533e-01 -48.0322 < 2.2e-16 *** hd_rate:take_rate -3.2542e+02 2.1708e+01 -14.9909 < 2.2e-16 *** hd_rate:give_rate -5.7993e+01 9.8285e+00 -5.9005 3.680e-09 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

difference from adjusted R² (0.547) indicating robust explanatory power.

Figure 3. Fixed-effects coefficients with robust standard errors.

1st Qu.

Coefficients:

hd_rate

reb_rate

engagement (p = 0.12), takeaways (p = 0.43), and giveaways (p = 0.25).

Median 3rd Qu.

Estimate Std. Error t-value Pr(>|t|) -5.8885e-02 7.4299e-03 -7.9254 2.388e-15 ***

2.6679e+00 1.7719e-02 150.5689 < 2.2e-16 ***

Figure 4. Simplified fixed-effects model retaining only significant interaction.

-1.8200e-02 -6.9390e-05 8.1712e-05 2.3740e-04 1.2508e-01

-1.9073e-02 -7.8727e-05 8.0314e-05 2.3081e-04 1.1962e-01

3rd Qu.

Estimate Std. Error t-value Pr(>|t|)

2.7689e-02 4.7661e-03 5.8096 6.354e-09 ***

-1.5518e-02 7.5151e-03 -2.0649 0.03894 2.7941e+00 1.8134e-02 154.0833 < 2.2e-16 ***

3.1708e-03 3.4303e-03 0.9244 0.35531

1.8637e-02 1.3265e-02 1.4050 0.16004

3.2.1 Full Interactive Model

model = "within")

Residuals:

Coefficients:

hd_rate

reb_rate

phys_rate

take_rate give_rate

Oneway (individual) effect Within Model

1st Qu.

Unbalanced Panel: n = 1460, T = 2-25, N = 22117

both simultaneously, indicating distinct pathways to of

3.2.2 Robust Standard Error Analysis

t test of coefficients:

Estimate Std. Error t-value Pr(>|t|)

Unbalanced Panel: n = 1460, T = 2-25, N = 22117

Min. 1st Qu. Median 3rd Qu.

Oneway (individual) effect Within Model ## ## Call: ## plm(formula = goals_rate ~ hd_rate * reb_rate + phys_rate + take_rate +

fe_goals_simple <- plm(goals_rate ~ hd_rate * reb_rate + phys_rate + take_rate + give_rate, data = df_panel_game</pre>

take_rate 2.2228e-04 3.4799e-03 0.0639 0.949070 ## give_rate 2.6385e-03 1.3230e-02 0.1994 0.841922 ## hd_rate:reb_rate -4.0512e+01 9.5795e-01 -42.2909 < 2.2e-16 *** ## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

3. Results & Discussion 3.1 Correlation Analysis 0.19 -0.01 0.46 -0.03 0.00 -0.01 goals_rate 0.19 0.00 0.70 -0.02 0.00 0.00 -0.01 0.01 0.00 0.01 mom_diff -0.01 0.00 reb_rate 0.46 0.70 -0.01 -0.04 0.00 -0.01 -0.2 phys_rate -0.03 -0.02 0.01 -0.04 0.00 0.02 -0.4 take_rate 0.00 0.00 0.00 0.00 0.00 0.00 -0.6 give_rate -0.01 0.00 0.01 -0.01 0.02 0.00 Figure 1. Correlation matrix of the variables. Darker blue indicates stronger positive relationships and red indicates negative relationships. Based on the correlation matrix above (Figure 1), the rebound shows the strongest association with goal production (r = 0.70), while high-danger shots demonstrate a moderate correlation with goal production (r = 0.19). The two primary skills are moderately linked (r = 0.46), suggesting skilled shooters often generate rebounds. Furthermore, the secondary skills exhibit negligible correlations with goals, where hits, takeaways, and giveaways all show |r| < 0.03. These near-zero relationships indicate that physical engagement and puck management do not directly influence scoring output.

Total Sum of Squares: 0.072433 Residual Sum of Squares: 0.030644 R-Squared: 0.57694 Adj. R-Squared: 0.54686 F-statistic: 3128.67 on 9 and 20648 DF, p-value: < 2.22e-16 Figure 2. Fixed-effects model with full interaction terms. The full fixed-effects model provides definitive answers to both components of the research question (Figure 2). Regarding how high-danger shots and rebounds jointly influence goal production, the strongly negative interaction coefficient ($\beta = -46.847$, p < 0.001) reveals that these skills operate as substitutes rather than complements. Players achieve optimal goal production through specialization in one primary skill rather than maximizing

Addressing how secondary skills interact with this relationship, all interaction terms are statistically significant: physical engagement (β = -180.26, p

< 0.001), takeaways ($\beta = -325.42$, p < 0.001), and giveaways ($\beta = -57.993$, p < 0.001). These universally negative coefficients reveal that secondary skills diminish rather than amplify high-danger shooting effectiveness, suggesting resource allocation trade-offs where focusing on secondary activities reduces high-danger shooting efficiency. The model explains 57.7% of within-player variation in goal production, with minimal

Estimate Std. Error t value Pr(>|t|)take_rate 3.1708e-03 4.0254e-03 0.7877 0.43088 give_rate 1.8637e-02 1.6248e-02 1.1471 0.25137 hd_rate:reb_rate -4.6847e+01 3.8458e+01 -1.2182 0.22318 hd_rate:phys_rate -1.8026e+02 1.1909e+02 -1.5137 0.13012 hd_rate:take_rate -3.2542e+02 2.3096e+02 -1.4090 0.15885 hd_rate:give_rate -5.7993e+01 8.8481e+01 -0.6554 0.51220 Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

This pattern suggests that rebound generation represents the most reliable predictor of goal production, while the evidence for interactive effects is more fragile than initially indicated. The loss of interaction significance under robust standard errors indicates that conclusions about skill substitutability and secondary skill moderation should be interpreted with appropriate caution, highlighting the importance of statistical robustness in sports analytics. 3.2.3 Simplified Model Oneway (individual) effect Within Model plm(formula = goals_rate ~ hd_rate * reb_rate + phys_rate + take_rate + give_rate, data = df_panel_games, model = "within") Unbalanced Panel: n = 1460, T = 2-25, N = 22117

The robust standard error analysis reveals important nuances in the reliability of these findings (Figure 3). While rebound rate maintains strong significance (p < 0.02), the high-danger shot and rebound interaction loses statistical significance (p = 0.22) under heteroscedasticity-adjusted

standard errors. Similarly, all secondary skill interactions become non-significant when accounting for within-player clustering: physical

1.4487e-02 4.7863e-03 3.0267 0.002475 ** phys_rate 2.2228e-04 3.4799e-03 0.0639 0.949070 take_rate 2.6385e-03 1.3230e-02 0.1994 0.841922 hd_rate:reb_rate -4.0512e+01 9.5795e-01 -42.2909 < 2.2e-16 *** Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1 Total Sum of Squares: 0.072433 Residual Sum of Squares: 0.031631 Adj. R-Squared: 0.53232 F-statistic: 4439.68 on 6 and 20651 DF, p-value: < 2.22e-16

offensive skill hierarchy, while the fragility of interaction effects under robust standard errors suggests that individual skill excellence may be more important than skill combinations. This has significant implications for player evaluation and development, supporting focused skill specialization rather than attempting to maximize all abilities simultaneously. 4. Conclusion

Given the robust standard error results, a simplified model focusing on reliable relationships was estimated (Figure 4). The model retains the high-

danger shot and rebound interaction ($\beta = -40.512$, p < 0.001) while treating secondary skills as direct effects. Rebound rate emerges as the

These findings fundamentally address the research question by revealing that goal production operates through a skill specialization framework rather than skill complementarity. The dominance of rebound generation over high-danger shooting challenges conventional assumptions about

dominant predictor (β = 2.6679, p < 0.001), while physical engagement shows a positive direct effect (β = 0.01, p < 0.01).

4.1 Implications These findings challenge conventional assumptions about skill complementarity in hockey analytics and support a skill specialization system for player evaluation. Teams should prioritize players who excel in rebound generation and consider that developing multiple offensive skills simultaneously may yield diminishing returns. The results suggest that effective player development strategies should focus on maximizing specific abilities rather than attempting to enhance all skills equally.

4.2 Limitations

Resources

The analysis focuses on individual-level performance without accounting for team context, linemate effects, or defensive systems that may moderate skill interactions. The loss of interaction significance under robust standard errors highlights the sensitivity of these relationships to statistical assumptions. Additionally, the study examines only offensive skills, excluding defensive contributions that may influence overall player value.

4.3 Future Research Future studies should explore positional differences in skill complementarity, examine how team systems moderate individual skill effectiveness, and investigate the temporal dynamics of skill development. Research incorporating defensive context and team-level factors would provide a more comprehensive understanding of skill interactions in hockey performance.

1. EDGE.NHL.com. NHL edge puck and player tracking statistics - glossary [Internet]. [cited 2025 Jun 27]. Available from: https://edge.nhl.com/en/glossary 2. Cusimano MD, Nastis S, Zuccaro L. Effectiveness of interventions to reduce aggression and injuries among ice hockey players: A systematic review. Canadian Medical Association Journal. 2012 Dec 3;185(1). doi:10.1503/cmaj.112017 3. MoneyPuck.com. Player and Team Data [Internet]. [cited 2025 Jun 27]. Available from: https://moneypuck.com/data.htm