



# Securing Wireless Networks, COMP4337/9337

## RSA/DH, Certification Authority, Authentication

Never Stand Still

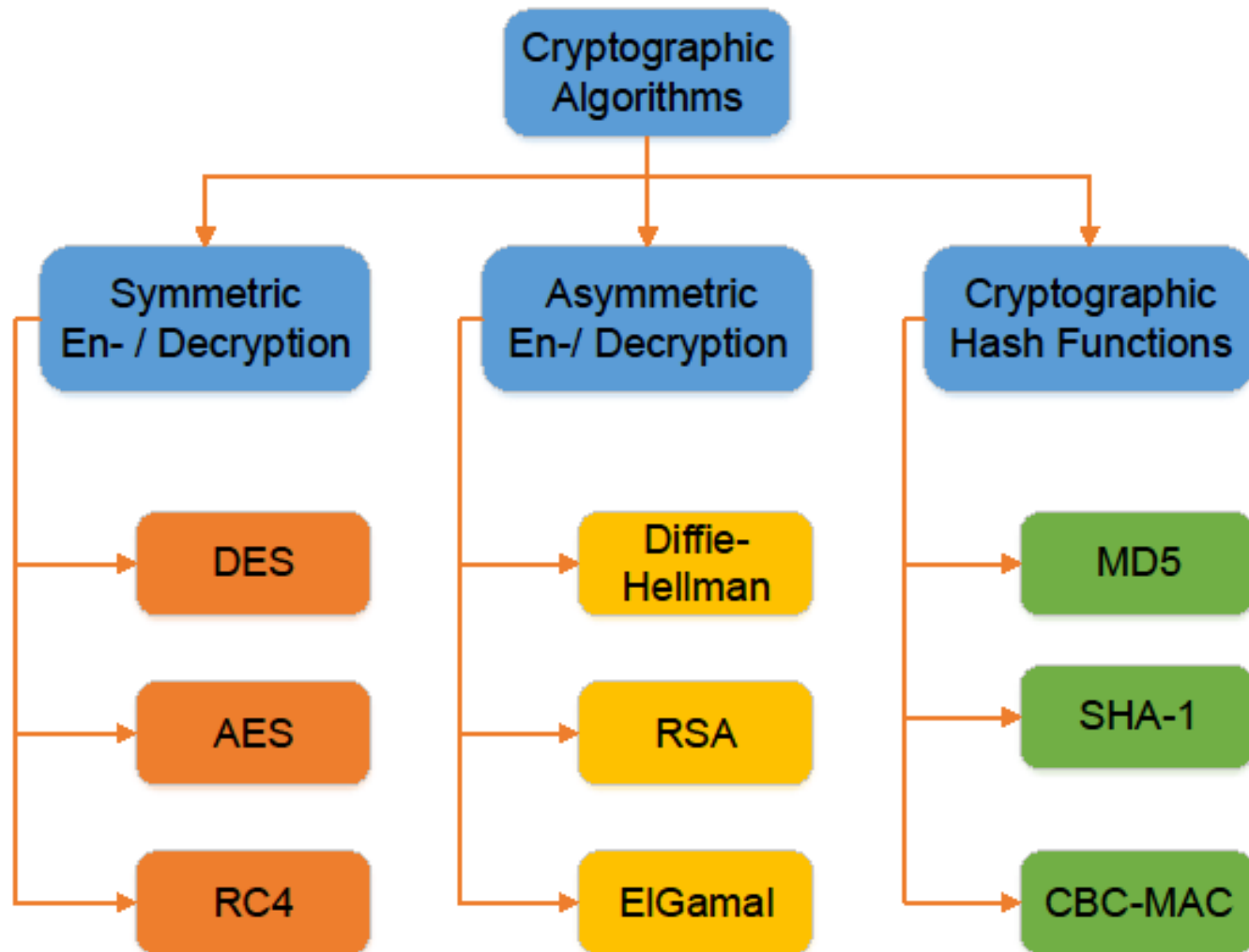
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# Today's Agenda – Part 1

- Key Distribution RSA, Deffie Hellman
- Certification Authority and X.509
- Authentication Recap
- Application Layer Security (PGP)

# Recap



# Public key encryption algorithms

## Requirements:

- ① need  $K_B^+$  and  $K_B^-$  such that

$$K_B^-(K_B^+(m)) = m$$

- ② given public key  $K_B^+$ , it should be impossible to compute private key  $K_B^-$

**RSA:** Rivest, Shamir, Adelson algorithm

# Public Key Cryptography

## *symmetric key crypto*

- requires sender, receiver know shared secret key
- Q: how to agree on key in first place (particularly if never “met”)?

## *public key crypto*

- ❖ radically different approach [Diffie-Hellman76, RSA78]
- ❖ sender, receiver do *not* share secret key
- ❖ *public* encryption key known to *all*
- ❖ *private* decryption key known only to receiver



# RSA: getting ready

- A message is a bit pattern.
- A bit pattern can be uniquely represented by an integer number.
- Thus encrypting a message is equivalent to encrypting a number.

## Example

- $m = 10010001$ . This message is uniquely represented by the decimal number 145.
- To encrypt  $m$ , we encrypt the corresponding number, which gives a new number (the ciphertext).

# RSA: Creating public/private key pair

1. Choose two large prime numbers  $p, q$ .  
(e.g., 1024 bits each)
2. Compute  $n = pq$ ,  $z = (p-1)(q-1)$
3. Choose  $e$  (with  $e < n$ ) that has no common factors with  $z$ . ( $e, z$  are “relatively prime”). E.g.: 4 and 9 are relatively prime. 6 and 9 are not.
4. Choose  $d$  such that  $ed-1$  is exactly divisible by  $z$ .  
(in other words:  $ed \bmod z = 1$  ).
5. Public key is  $(n, e)$ . Private key is  $(n, d)$ .  

$\underbrace{\hspace{1.5cm}}_{K_B^+}$

$\underbrace{\hspace{1.5cm}}_{K_B^-}$

# RSA: Encryption, decryption

0. Given  $(n, e)$  and  $(n, d)$  as computed above

1. To encrypt bit pattern,  $m$  ( $m < n$ ), compute

$$c = m^e \bmod n \quad (\text{i.e., remainder when } m^e \text{ is divided by } n)$$

2. To decrypt received bit pattern,  $c$ , compute

$$m = c^d \bmod n \quad (\text{i.e., remainder when } c^d \text{ is divided by } n)$$

Magic  
happens!

$$m = \underbrace{(m^e \bmod n)}_c^d \bmod n$$



# RSA example

Bob chooses  $p=5$ ,  $q=7$ . Then  $n=35$ ,  $z=24$ .

$e=5$  (so  $e$ ,  $z$  relatively prime).

$d=29$  (so  $ed-1$  exactly divisible by  $z$ ).

	<u>letter</u>	<u>m</u>	<u><math>m^e</math></u>	<u><math>c = m^e \bmod n</math></u>
encrypt:	I	12	1524832	17
	<u>c</u>	<u><math>c^d</math></u>	<u><math>m = c^d \bmod n</math></u>	<u>letter</u>
decrypt:	17	481968572106750915091411825223071697	12	I

# RSA: another important property

The following property will be *very* useful later:

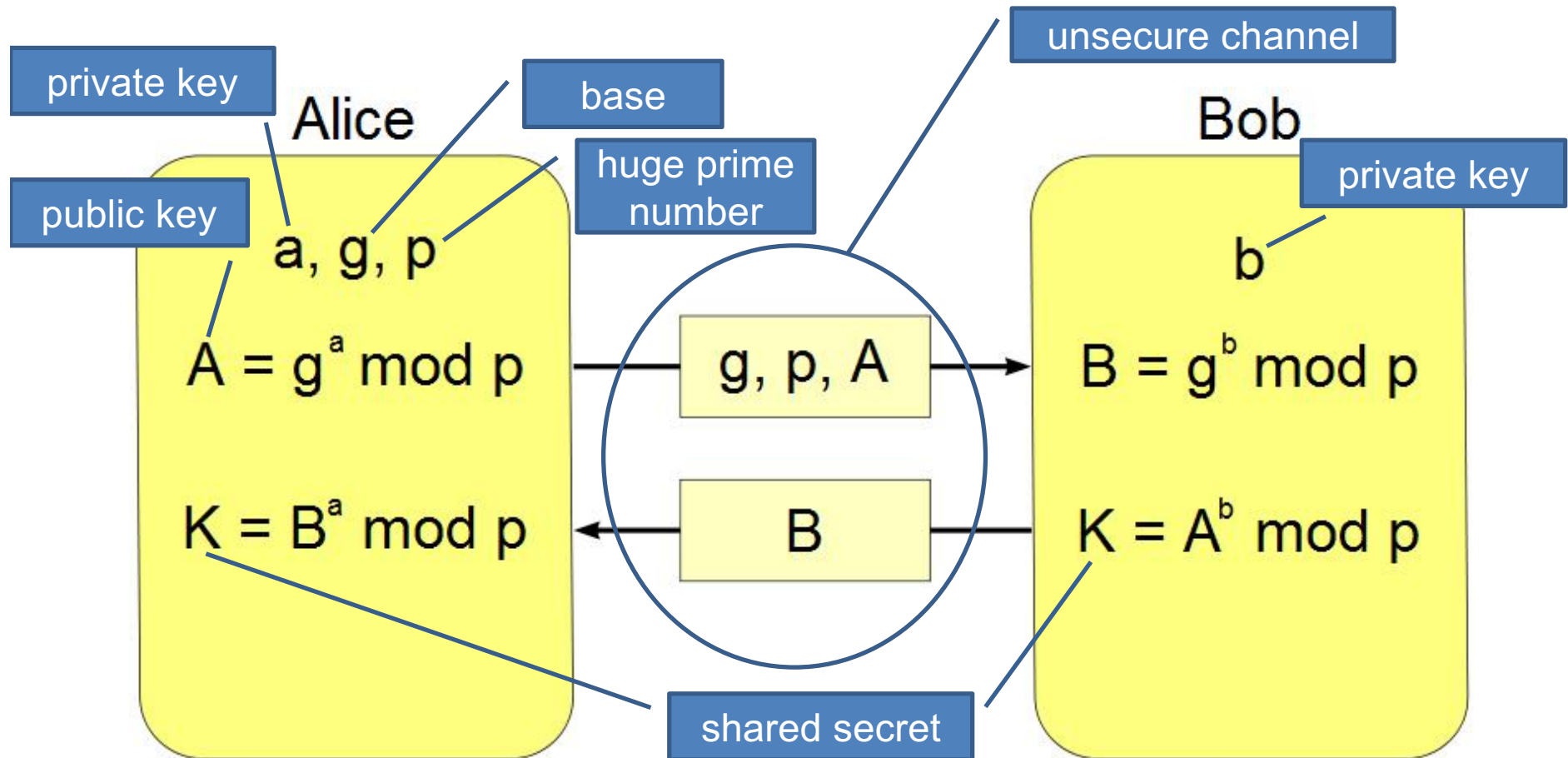
$$\underbrace{K_B^-(K_B^+(m))}_{\text{use public key first, followed by private key}} = m = \underbrace{K_B^+(K_B^-(m))}_{\text{use private key first, followed by public key}}$$

use public key  
first, followed by  
private key

use private key  
first, followed by  
public key

*Result is the same!*

# Diffie-Hellman key exchange



$$K = A^b \text{ mod } p = (g^a \text{ mod } p)^b \text{ mod } p = g^{ab} \text{ mod } p = (g^b \text{ mod } p)^a \text{ mod } p = B^a \text{ mod } p$$

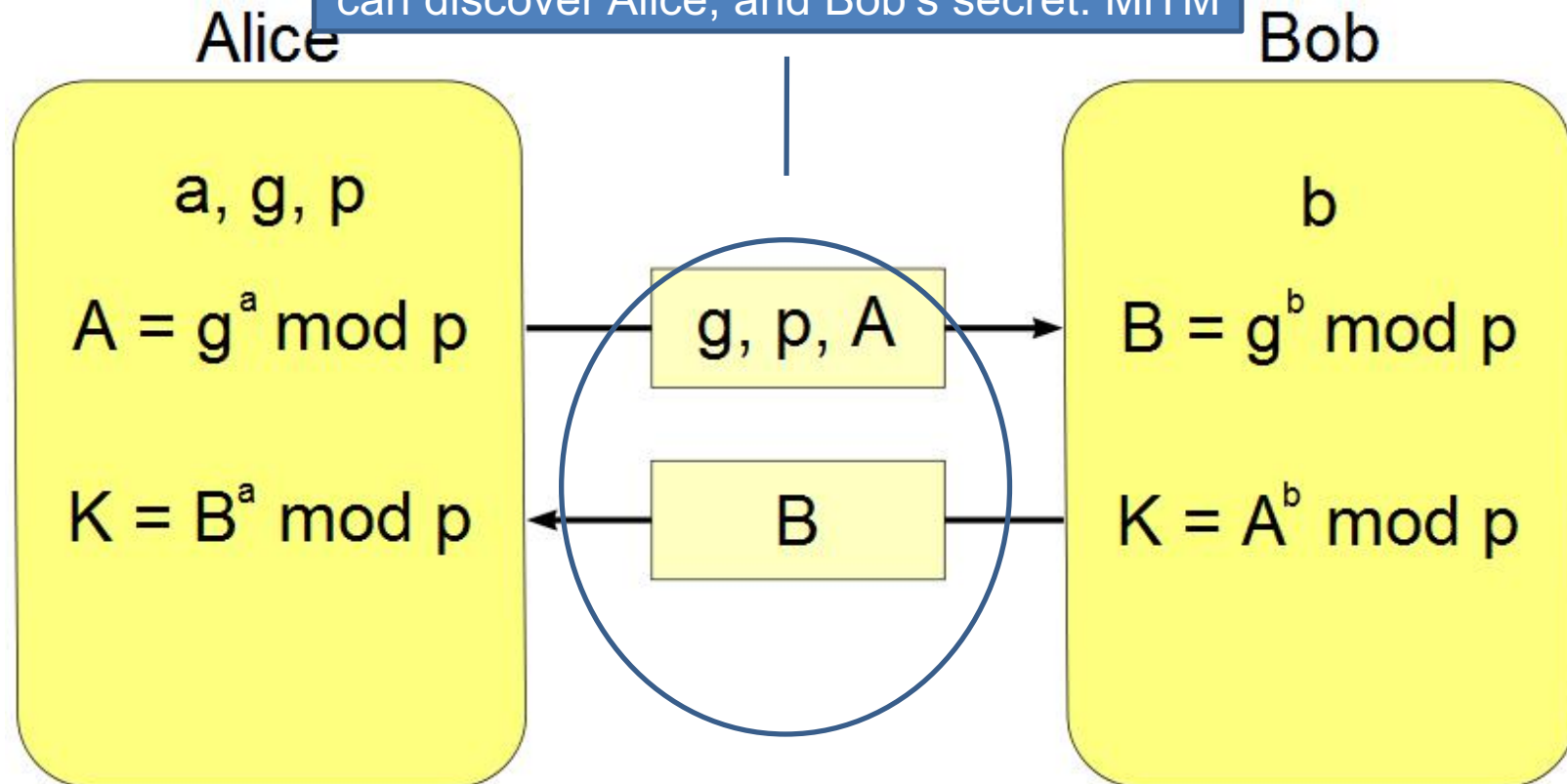
Alice's private key = 5, Bob's private key = 4,  $g=3$ ,  $p=7$

Alice's public key =  $3^5 \text{ mod } 7 = 5$ , Bob's public key =  $3^4 \text{ mod } 7 = 4$

Alice's shared key =  $4^5 \text{ mod } 7 = 2$ , Bob's shared key =  $5^4 \text{ mod } 7 = 2$

# Diffie-Hellman key exchange

If Eve can tamper with the channel, she can discover Alice, and Bob's secret: MiTM



$$K = A^b \bmod p = (g^a \bmod p)^b \bmod p = g^{ab} \bmod p = (g^b \bmod p)^a \bmod p = B^a \bmod p$$

Alice's private key = 5, Bob's private key = 4,  $g=3$ ,  $p=7$

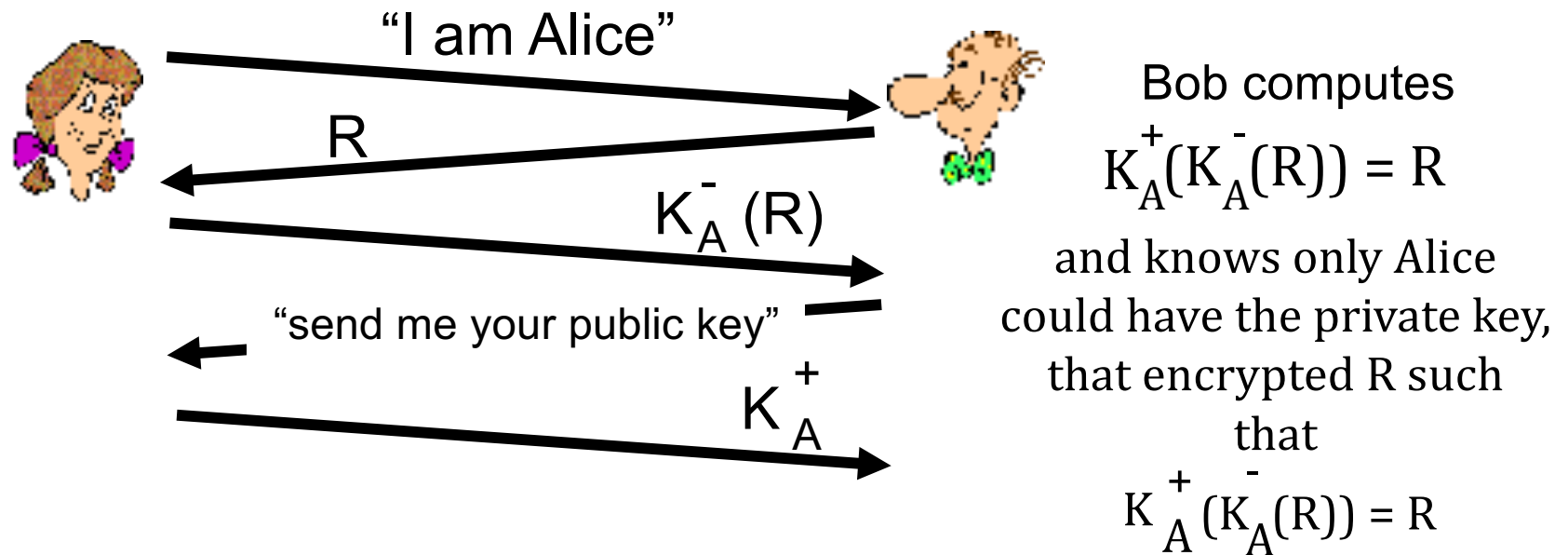
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Alice's shared key =  $4^5 \bmod 7 = 2$ , Bob's shared key =  $5^4 \bmod 7 = 2$

# Public-key certification

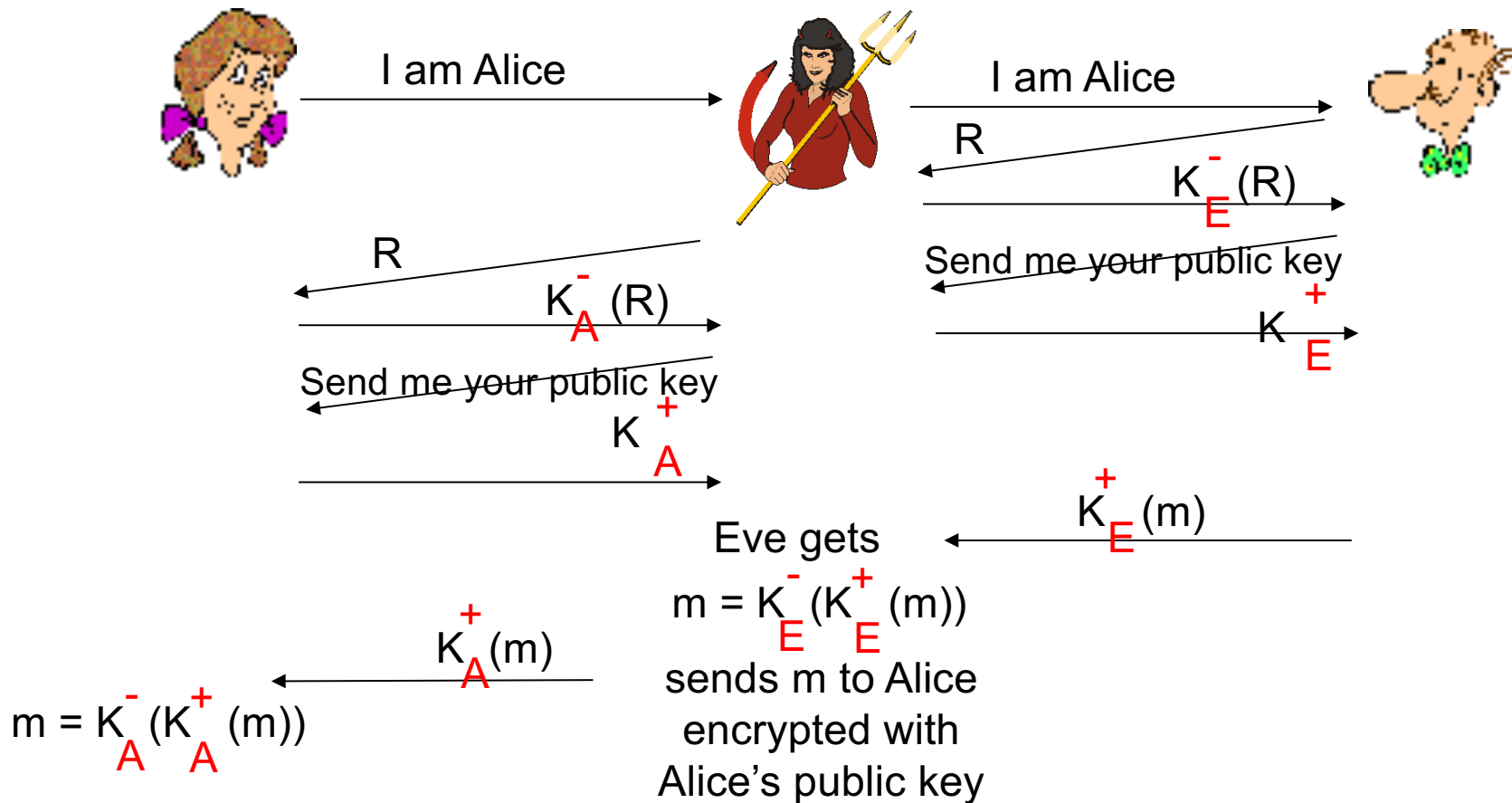
- motivation: Trudy plays pizza prank on Bob
  - Trudy creates e-mail order:  
*Dear Pizza Store, Please deliver to me four pepperoni pizzas. Thank you, Bob*
  - Trudy signs order with her private key
  - Trudy sends order to Pizza Store
  - Trudy sends to Pizza Store her public key, but says it's Bob's public key
  - Pizza Store verifies signature; then delivers four pepperoni pizzas to Bob
  - Bob doesn't even like pepperoni

# Kurose/Ross Authentication: ap5.0



# MiTM: Man in the Middle

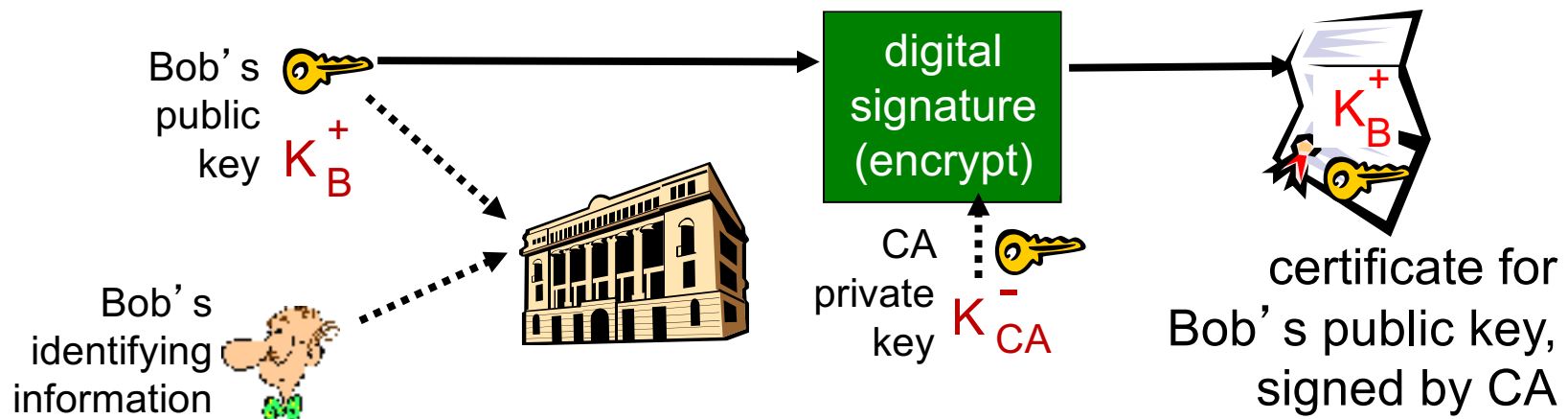
*man (or woman) in the middle attack:* Eve poses as Alice (to Bob) and as Bob (to Alice)



# Certification authorities

*certification authority (CA)*: binds public key to particular entity, E.

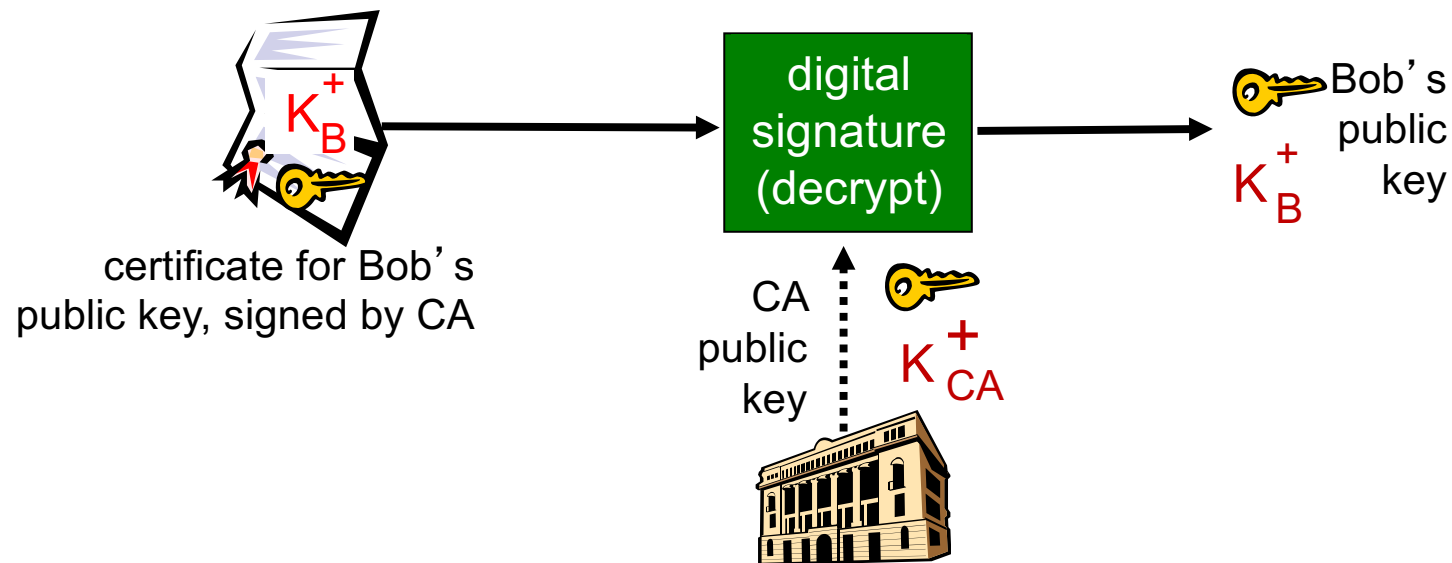
- E (person, router) registers its public key with CA.
  - E provides “proof of identity” to CA.
  - CA creates certificate binding E to its public key.
  - certificate containing E’s public key digitally signed by CA – CA says “this is E’s public key”





# Certification authorities

- when Alice wants Bob's public key:
  - gets Bob's certificate (Bob or elsewhere).
  - apply CA's public key to Bob's certificate, get Bob's public key



# Public Key Distribution of Secret Key

- Prepare a message
- Encrypt that message using conventional encryption using one time session key
- Encrypt the session key using public-key encryption with Alice's **public key**
- Attach the encrypted session key to the message and send it to Alice
- Only Alice can decrypt the session key
- Bob has obtained Alice's public key by means of Alice's **public-key certificate**, must be a valid key

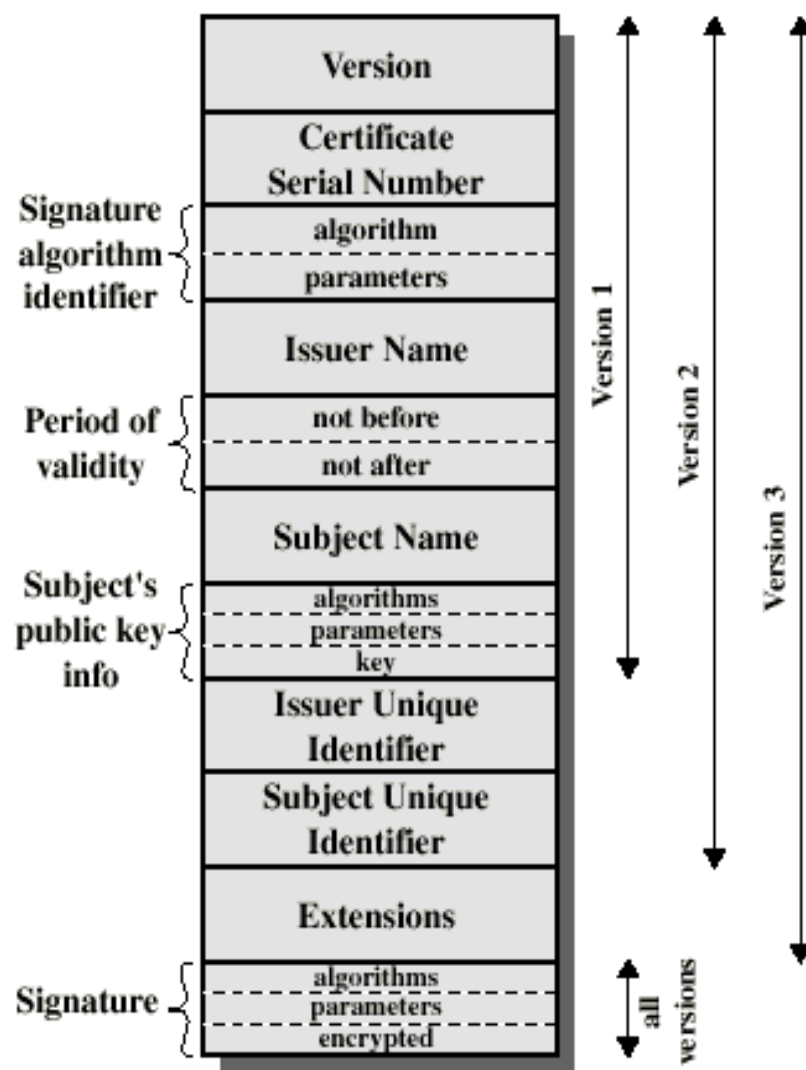
# X.509 Authentication Service

- Distributed set of servers that maintains a database about users.
- Each certificate contains the public key of a user and is signed with the private key of a CA.
- Is used in S/MIME, IP Security, SSL/TLS and SET.
- RSA is recommended to use but not mandatory.
- Digital Signature is assumed to use Hash algorithm
- Digital Certificate: user's id, public-key and CA information as input to hash function. Hash is then encrypted with CA's private key to produce **Digital Certificate**

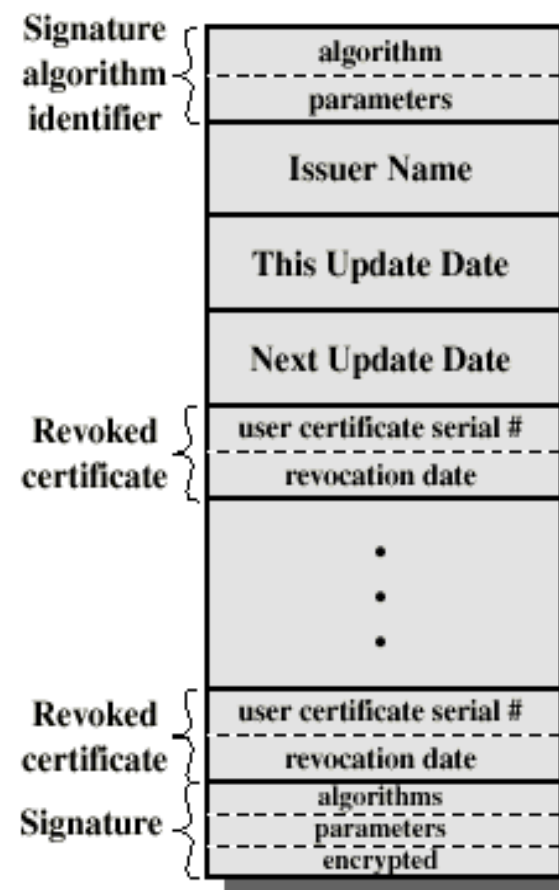
No need to memorise

Read: Stallings ch4 for a quick overview

# X.509 Formats



(a) X.509 Certificate



(b) Certificate Revocation List

# Obtaining a User's Certificate

- Characteristics of certificates generated by CA:
  - Any user with access to the public key of the CA can recover the user public key that was certified.
    - User can independently calculate hash, decrypt digital certificate using CA's public key, extract hash and compare if hashes match.
  - No part other than the CA can modify the certificate without this being detected.
- Certificates stored in a Directory server – not part of standard.

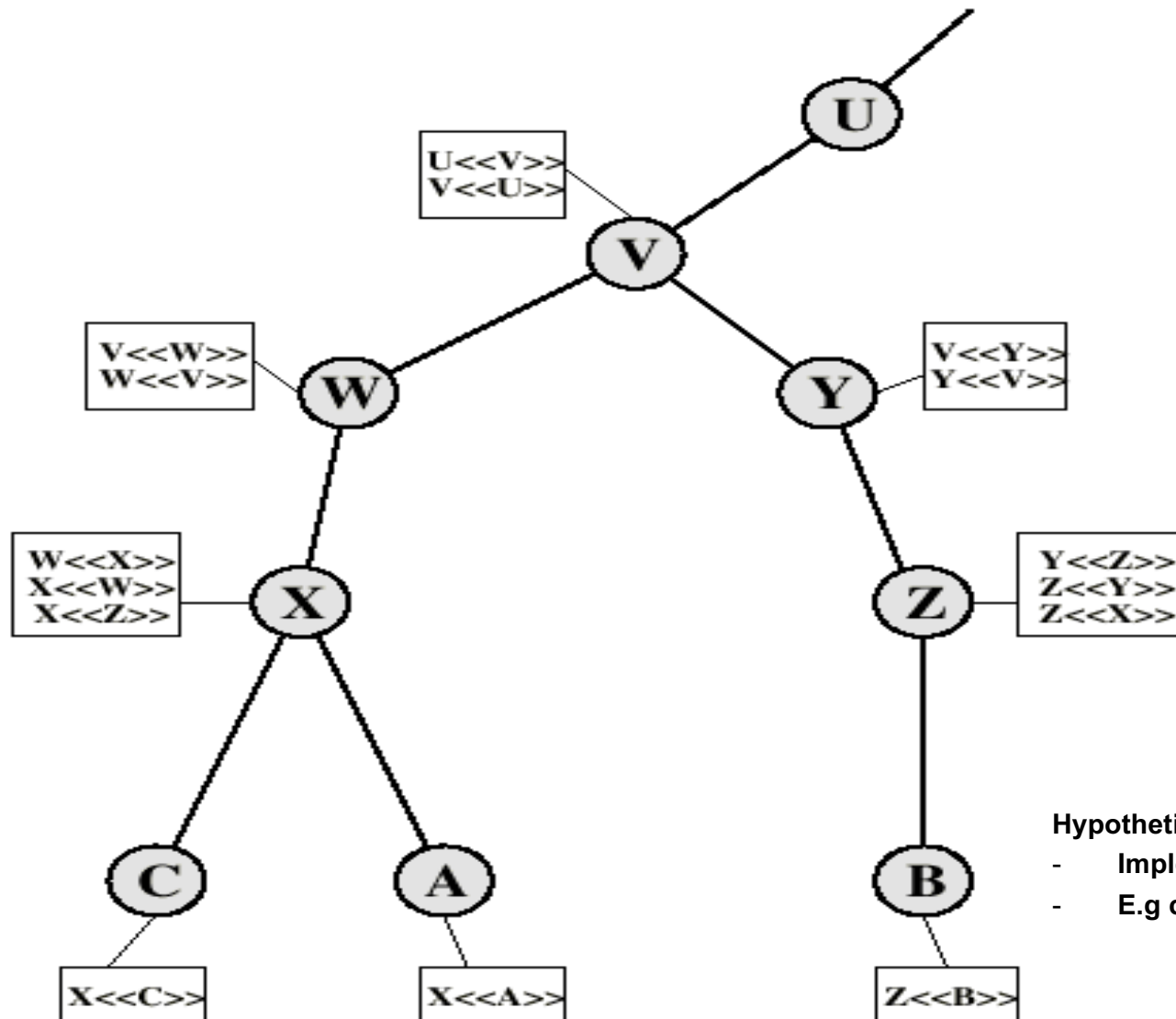
# Distributed Directory

- Users can be registered with a CA and would know its public Key
- Now if A got its certificate from CA X1 and B got it from CA X2.
- If A doesn't know CA X2's public key, it can't trust B's certificate issued by CA X2.
- However, if the two CA's have securely exchanged their public keys, then it can work.
  - A obtains the certificate of X2 signed by X1
  - A knows securely X1's public key
  - A obtains X2's public key from certificate and can verify using X1's signature on certificate
  - A can now get B's certificate from CA X2.
  - Since it has trusted public key for CA X2, things work as usual.

# Distributed Directory: Certificate Chain

- Notation  $Y \ll X \gg$  Certificate of user  $X$  issued by authority  $Y$
- A obtains B's public key using the following X.509 notation  
 $X_1 \ll X_2 \gg X_2 \ll B \gg$
- B obtains A's public key using the following X.509 notation  
 $X_2 \ll X_1 \gg X_1 \ll A \gg$ 
  - *Arbitrary chain is possible as long as consecutive pair  $(X_n, X_{n+1})$  of CAs have exchanged certificates securely*

# X.509 CA Hierarchy



Hypothetical Example

- Implementations may vary
- E.g cache entries



# Hierarchy of CAs

- Previous figure: Connected Circles hierarchical relationship, boxes shows certificates maintained in each CA's directory
  - Forward Certs: Certs of X generated by other CAs (e.g at circle X,  $W \ll X \gg$ ) – PARENT
  - Reverse Certs: Certs generated by X for others. (e.g. at circle X,  $X \ll C \gg$   $X \ll A \gg$ ) - CHILD
- A can acquire the following Certs from the directory to establish as certification to B
$$X \ll W \gg W \ll V \gg V \ll Y \gg Y \ll Z \gg Z \ll B \gg$$

(Try to get A's certificate)

# Revocation of Certificates

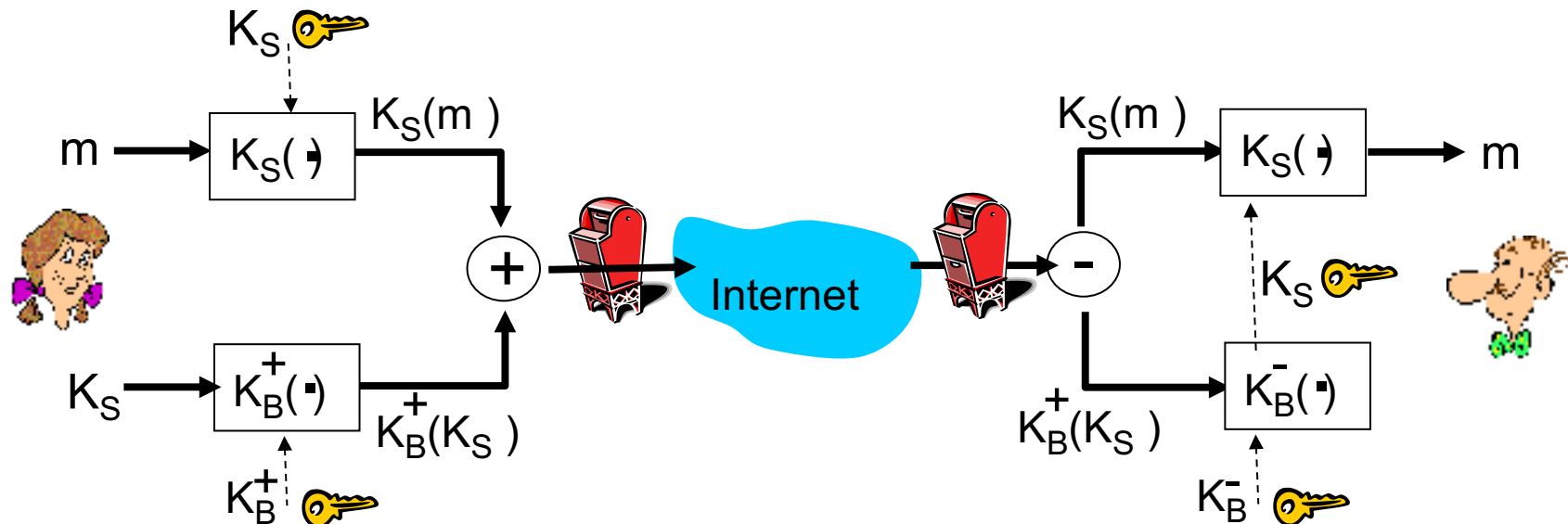
- Reasons for revocation:
  - The users secret key is assumed to be compromised.
  - The user is no longer certified by this CA.
  - The CA's certificate is assumed to be compromised.
- X.509 has a new version 3 with some recommendations for improvement
  - read in your own time if interested

# Application Layer Security

- Security can be implemented at various layers
- Application Layer Security
  - *A quick glimpse at secure email (PGP)*
- Secure Socket Layer (SSL) / Transport Layer Security (TLS)
  - Part 2 this week
- Network Layer Security
  - IPSec next week
- Link Layer Security
  - WLAN covered earlier, more on Enterprise later

# Secure e-mail: Alice

- ❖ Alice wants to send confidential e-mail,  $m$ , to Bob.

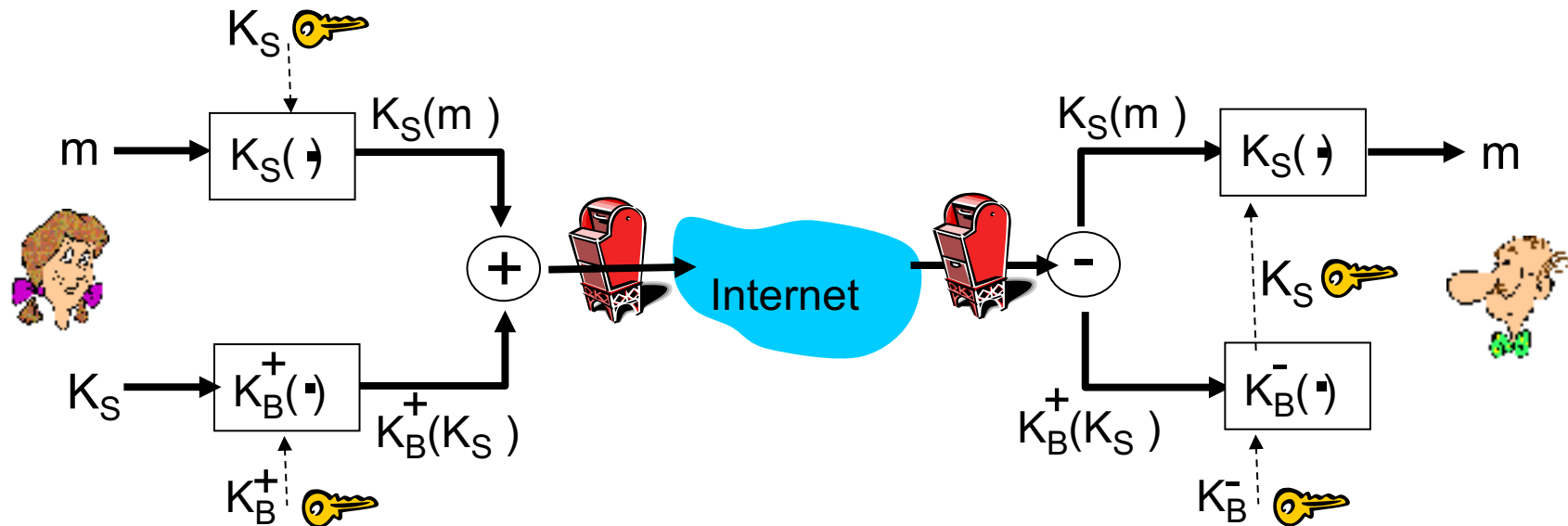


## Alice:

- ❖ generates random *symmetric* private key,  $K_S$
- ❖ encrypts message with  $K_S$  (for efficiency)
- ❖ also encrypts  $K_S$  with Bob's public key
- ❖ sends both  $K_S(m)$  and  $K_B(K_S)$  to Bob

# Secure e-mail: Bob

- ❖ Alice wants to send confidential e-mail,  $m$ , to Bob.

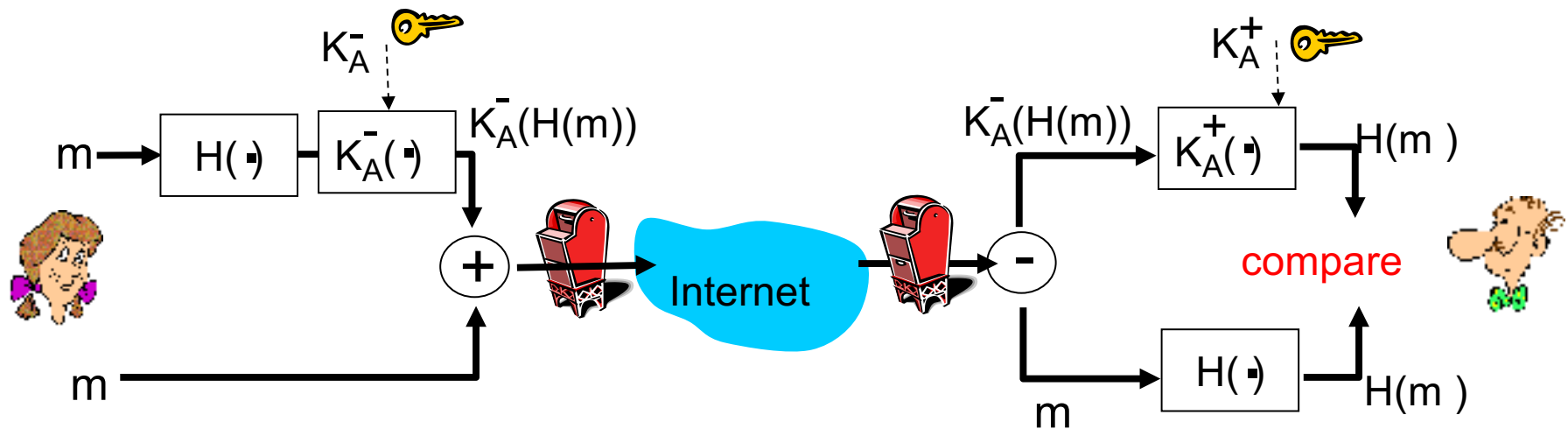


**Bob:**

- ❖ uses his private key to decrypt and recover  $K_S$
- ❖ uses  $K_S$  to decrypt  $K_S(m)$  to recover  $m$

# Secure e-mail (continued)

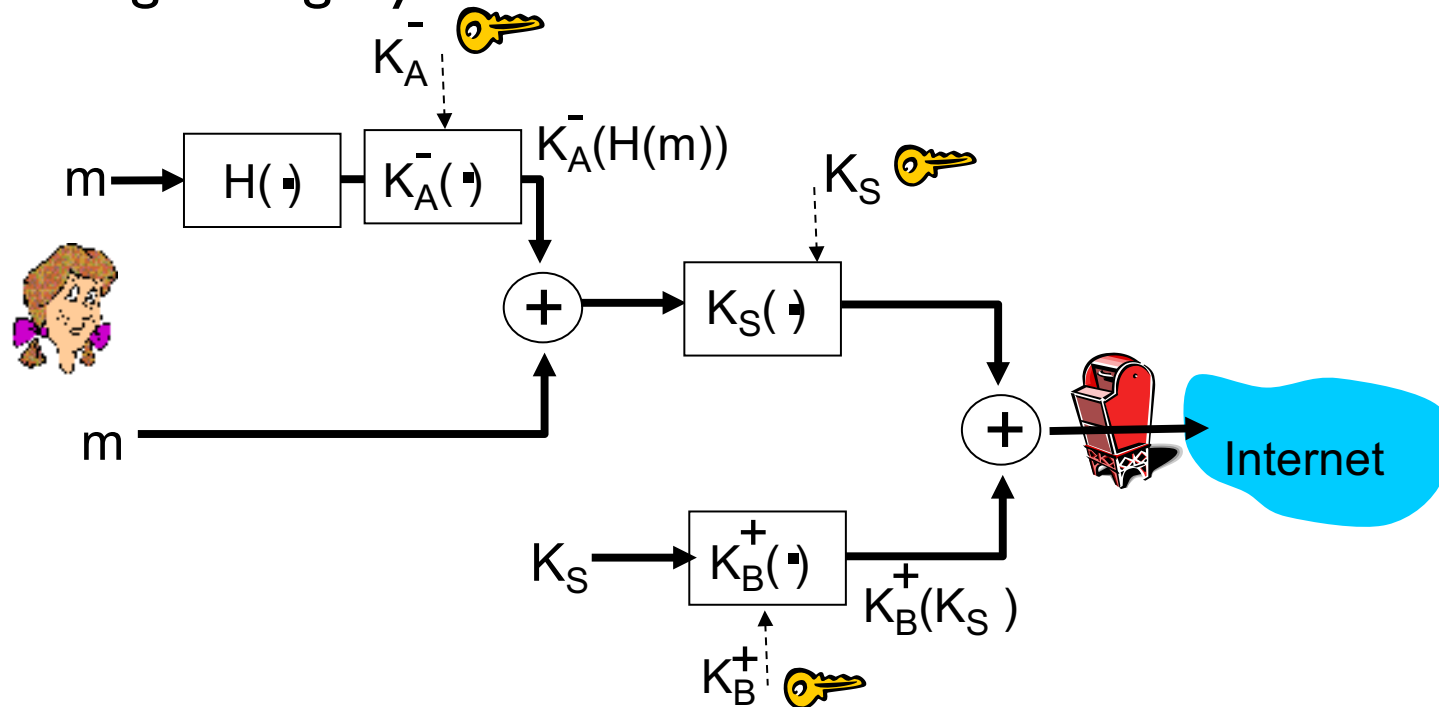
- ❖ Alice wants to provide sender authentication message integrity



- ❖ Alice digitally signs message
- ❖ sends both message (in the clear) and digital signature

# Secure e-mail (continued)

- ❖ Alice wants to provide secrecy, sender authentication, message integrity.



*Alice uses three keys:* her private key, Bob's public key, newly created symmetric key (Exercise: see how Bob's side works)

# Acknowledgements

- Network Security Essentials: Stallings, Chapter 4 provided by Henric Johnson, Blekinge Institute of Technology, Sweden ( Please refer to Section 4.3 and 4.4 from Staillings)
- Computer Networking A top-Down Approach: Jim Kurose and Keith Ross, chapter 8 (several lecture foils provided by authors)



# Revise Authentication Basics

- Next set of foils are for self study you have already done in 3331/9331 (Kurose-Ross Ch8)
- These are basic building blocks and please revise them as they will help understand material covered in this subject.

# Authentication

*Goal:* Bob wants Alice to “prove” her identity to him

*Protocol ap1.0:* Alice says “I am Alice”



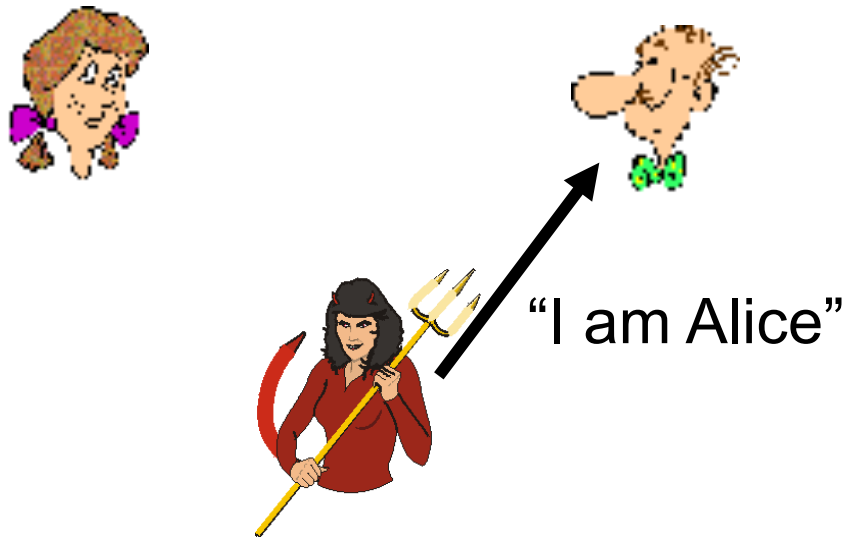
Failure scenario??



# Authentication

*Goal:* Bob wants Alice to “prove” her identity to him

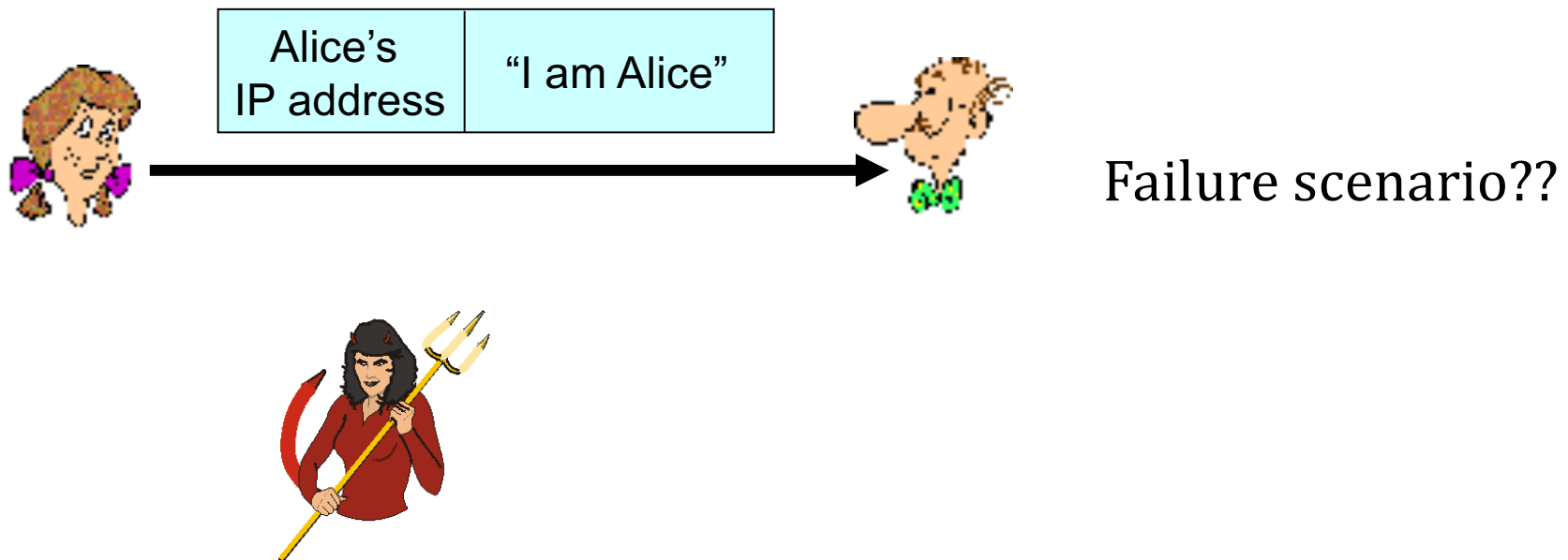
*Protocol ap1.0:* Alice says “I am Alice”



In a network,  
Bob can not “see” Alice, so  
Eve simply declares  
herself to be Alice

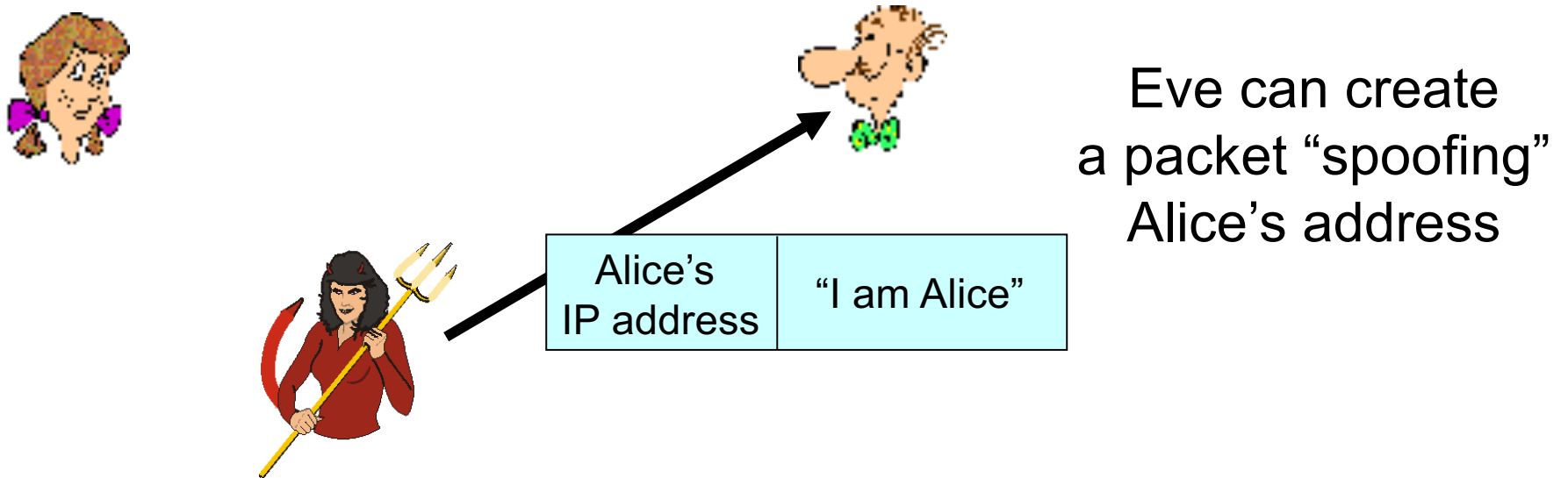
# Authentication: another try

*Protocol ap2.0:* Alice says “I am Alice” in an IP packet containing her source IP address



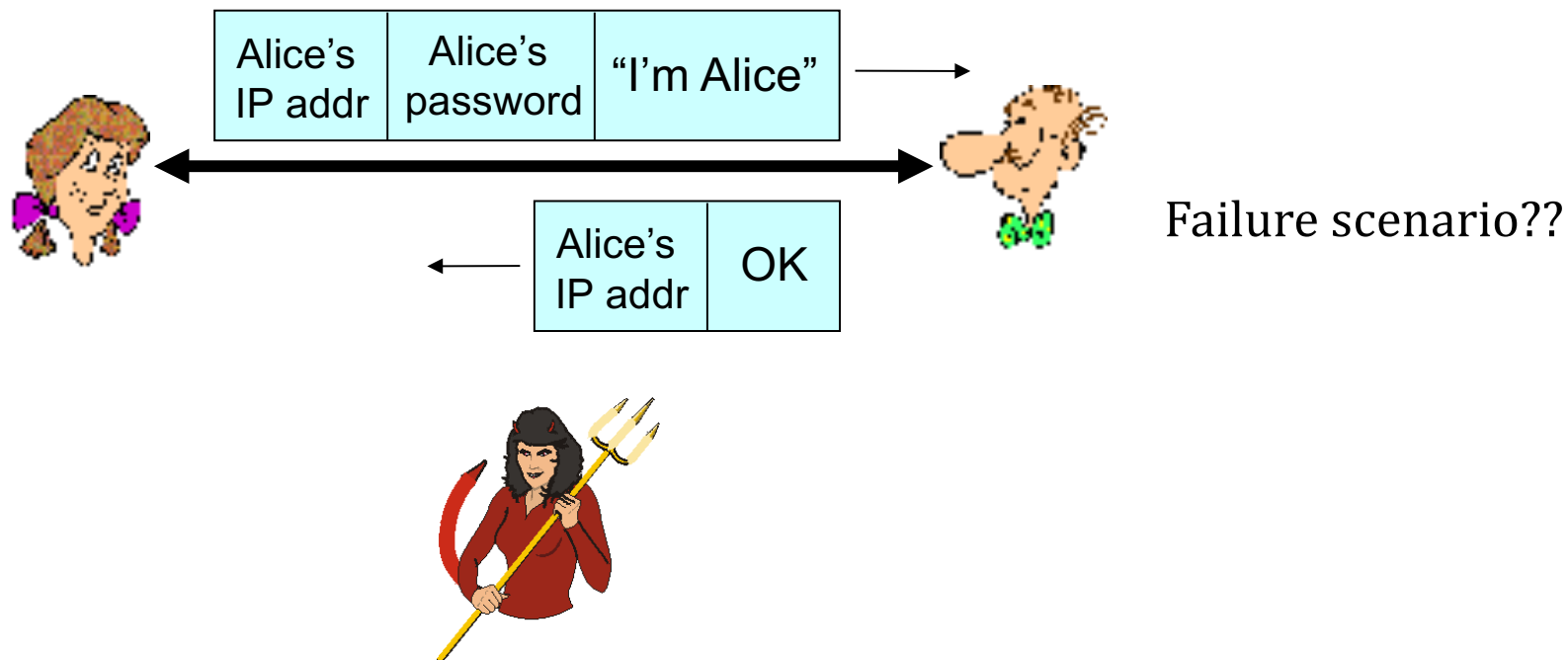
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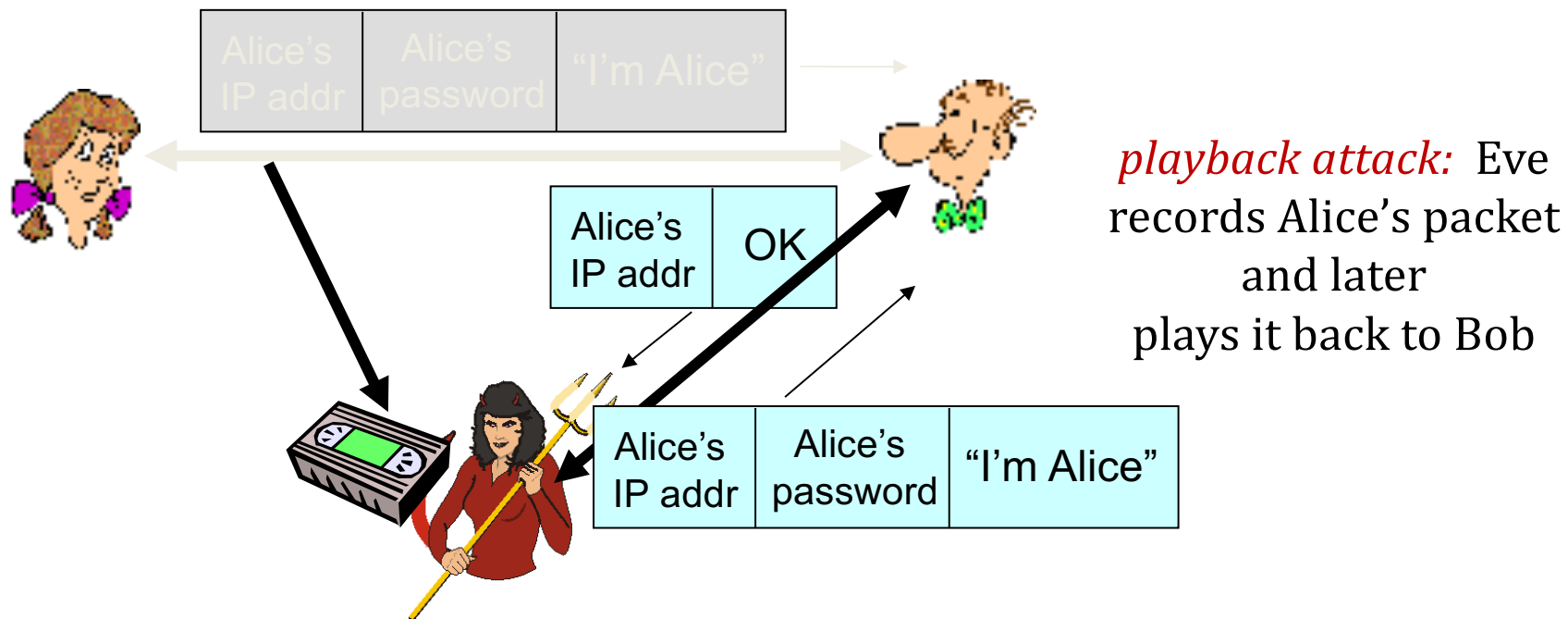
# Authentication: another try

*Protocol ap3.0:* Alice says “I am Alice” and sends her secret password to “prove” it.



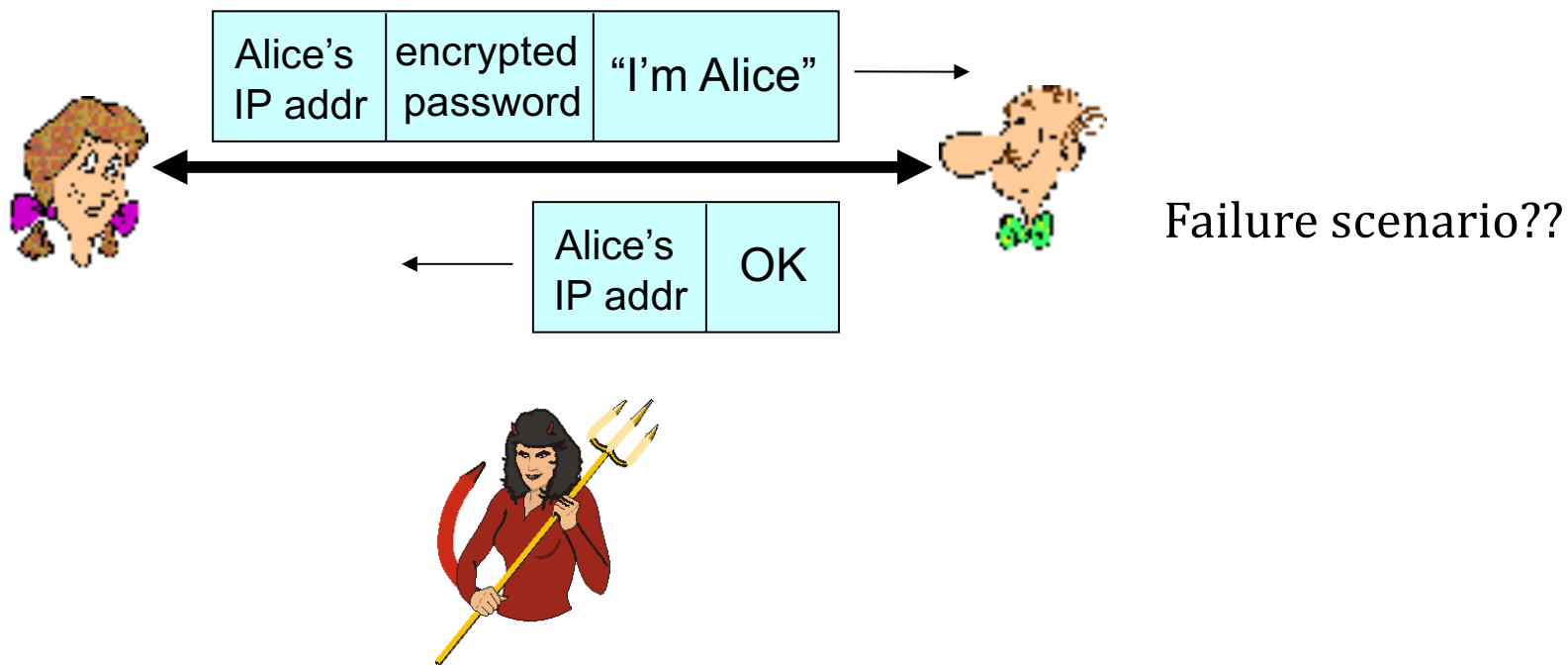
# Authentication: another try

*Protocol ap3.0:* Alice says “I am Alice” and sends her secret password to “prove” it.



# Authentication: yet another try

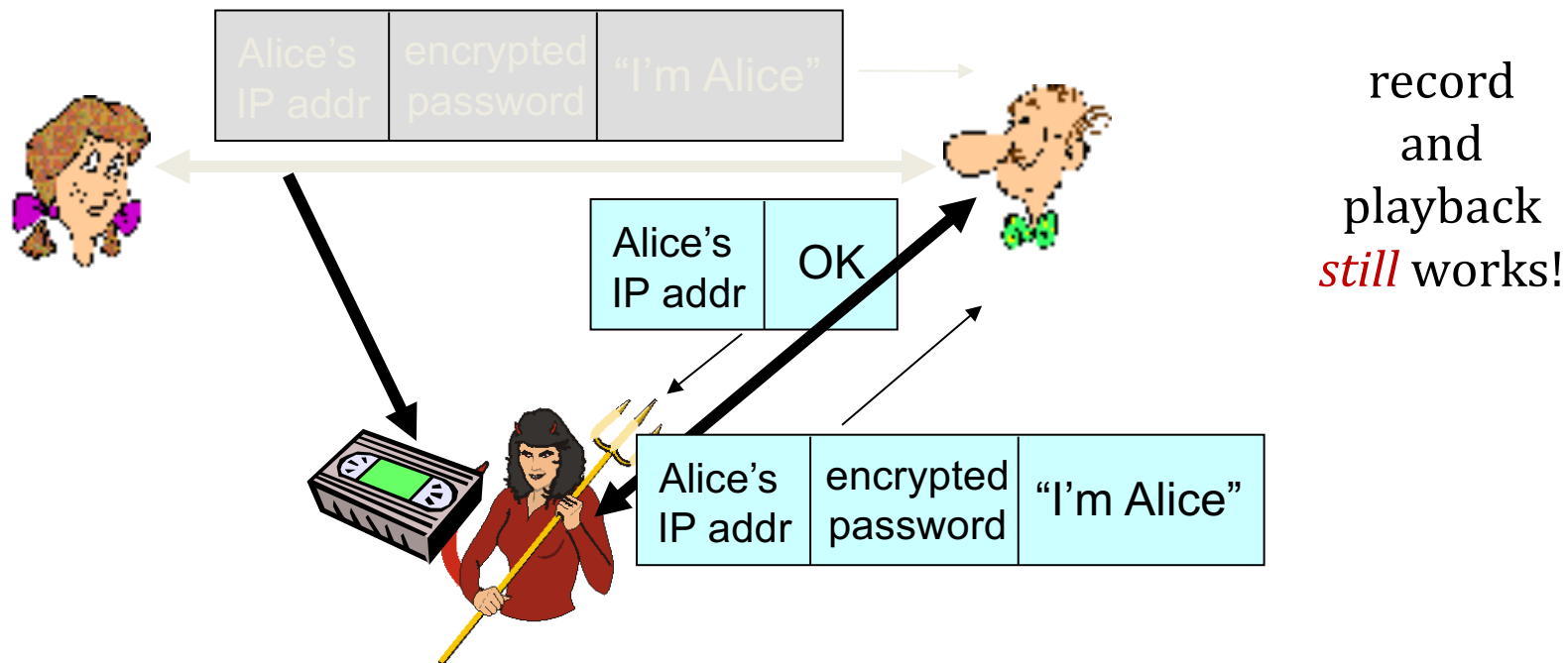
*Protocol ap3.1:* Alice says “I am Alice” and sends her *encrypted* secret password to “prove” it.





# Authentication: yet another try

*Protocol ap3.1:* Alice says “I am Alice” and sends her *encrypted* secret password to “prove” it.

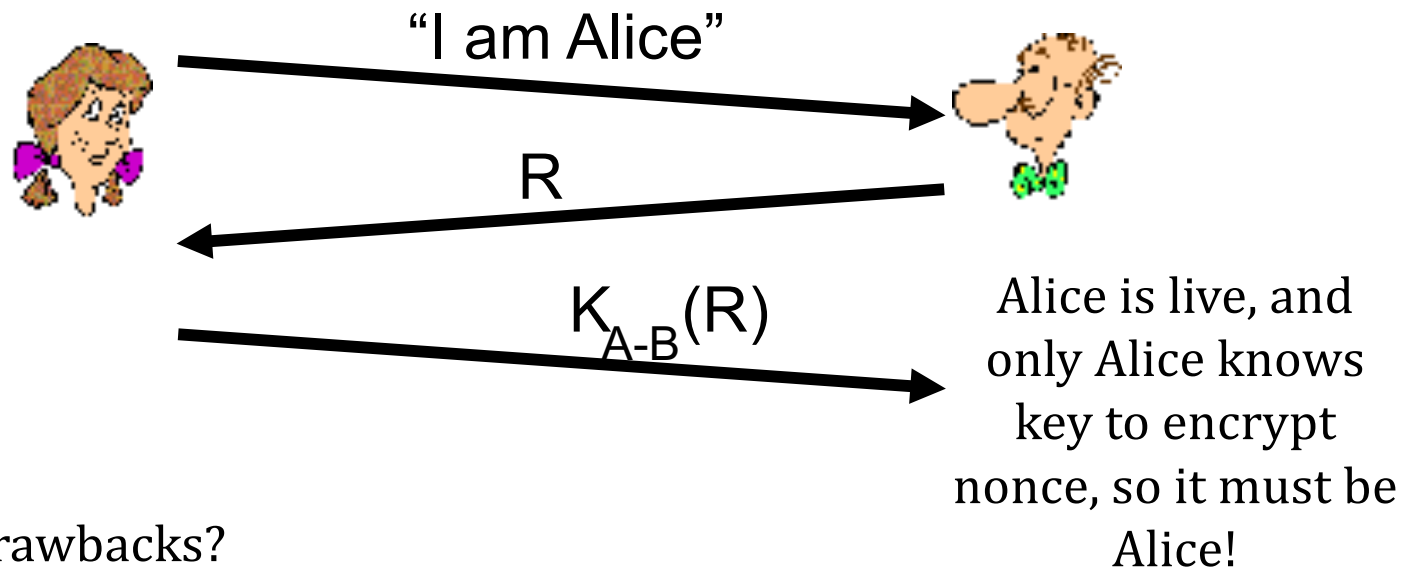


# Authentication: yet another try

*Goal:* avoid playback attack

*nonce:* number (R) used only *once-in-a-lifetime*

*ap4.0:* to prove Alice “live”, Bob sends Alice *nonce*, R. Alice must return R, encrypted with shared secret key

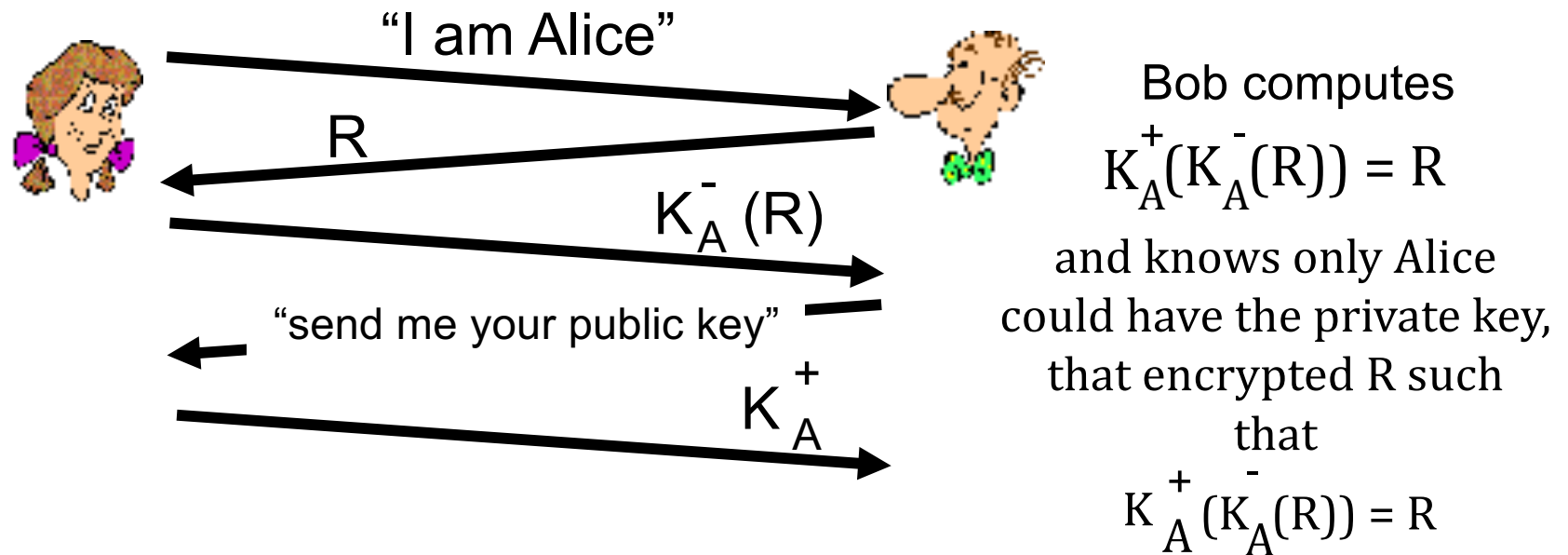


# Authentication: ap5.0

ap4.0 requires shared symmetric key

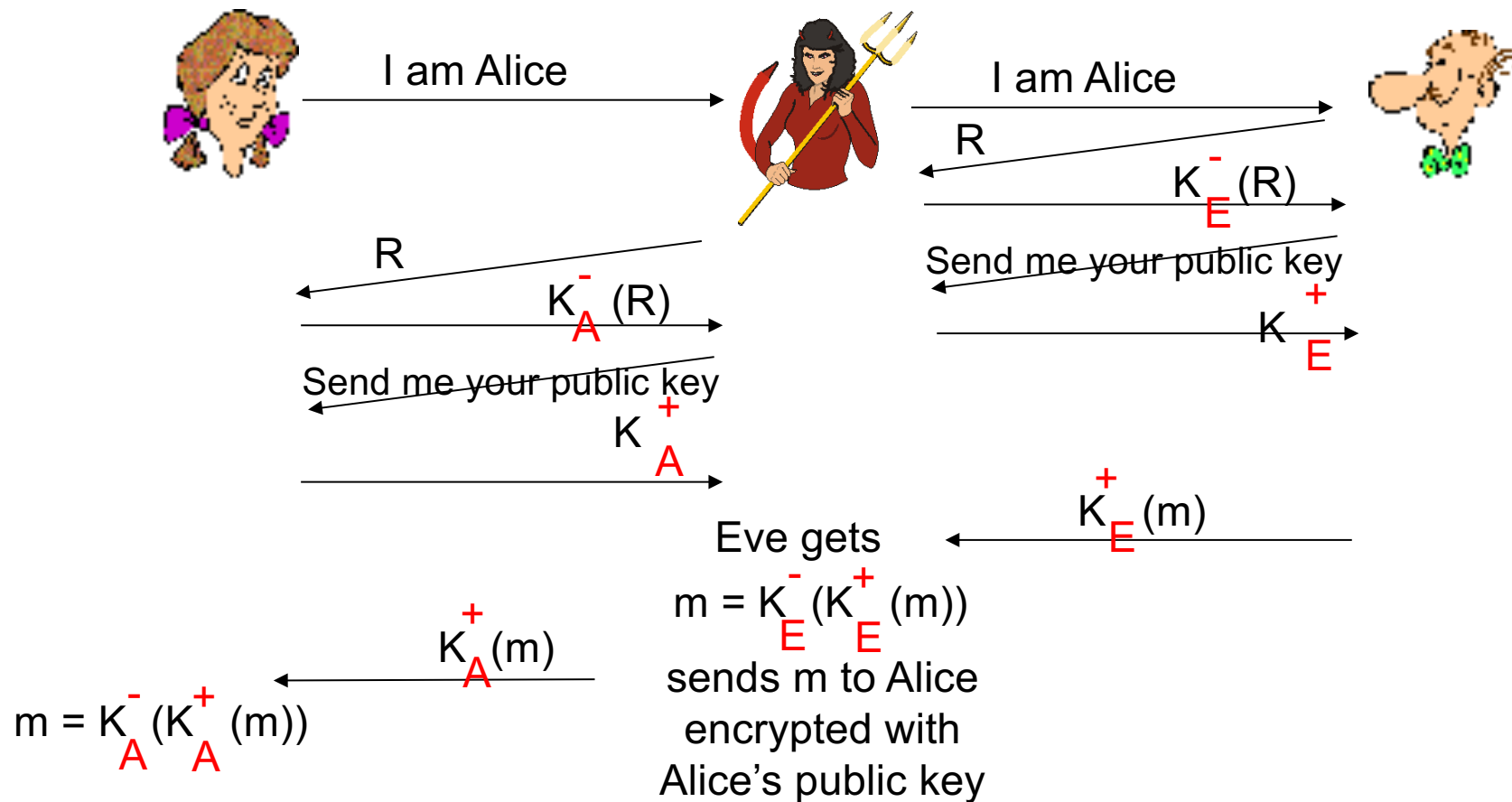
- can we authenticate using public key techniques?

*ap5.0*: use nonce, public key cryptography



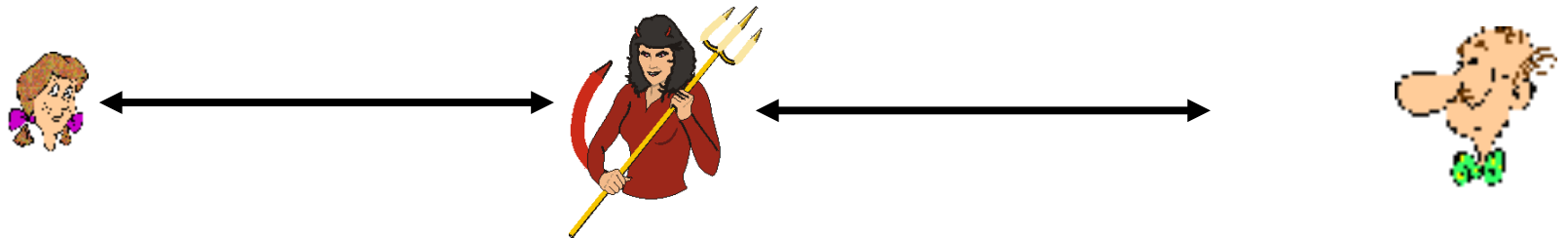
# ap5.0: security hole

*man (or woman) in the middle attack:* Eve poses as Alice (to Bob) and as Bob (to Alice)



# ap5.0: security hole

*man (or woman) in the middle attack:* Eve poses as Alice (to Bob) and as Bob (to Alice)



difficult to detect:

- ❖ Bob receives everything that Alice sends, and vice versa. (e.g., so Bob, Alice can meet one week later and recall conversation!)
- ❖ problem is that Eve receives all messages as well!