

(a) My parallel algorithm has `parSort` call a helper function, `parallelQuickSort`, that uses the already provided sequential implementation of `partition`, but recursively calls both sides of the pivot in parallel using an `async` wrapped around each recursive call.

(b) My solution is correct because the use of `async` does not change the original implementation outside of having the recursive work being done in parallel with each other. No data races are expected because the recursive calls are split in half from the pivot value, so no data accessed by the first recursive call will be accessed by the second recursive call due to the structure of the Quicksort algorithm.

(c)  $CPL = O(n)$

$WORK = O(n \log n)$

Explanation: My solution keeps the partition aspect of Quicksort sequential, while calling the function recursively in parallel.

The expected total  $WORK$  is  $O(n \log n)$  because 1) assuming each call to `partition` is 1 unit of  $WORK$ , and I call `partition` each time there is a recursive call of `parallelQuickSort`,  $n$  units of work are done for the partition part of this solution; 2) assuming each call to `parallelQuickSort` is 1 unit of work, `parallelQuickSort` is called on average  $\log n$  times due to me recursively calling the function for both the left and right side of the pivot at each call of `parallelQuickSort`. Multiplying these two parts together, we get a total  $WORK$  time of  $O(n \log n)$ .

The  $CPL$  is expected to be  $O(n)$  because each call of `parallelQuickSort` divides the amount of work by 2, so if we were to sum up the times of all the calls, we would get something like:

$CPL(n) = O(n) + O(n/2) + O(n/4) + O(n/8) + \dots \approx O(n)$ .

Test Output:

✓ Tests passed: 14 of 14 tests – 1 sec 437 ms

"C:\Program Files\Amazon Corretto\jdk11.0.12\_7\bin\java.exe" ...

Homework3CorrectnessTest.testRandomDataInput1K() starts...

Input array length = 1024

QuickSort Sequential metrics:  $WORK = 10335$ ,  $CPL = 10335$

QuickSort Parallel metrics:  $WORK = 10335$ ,  $CPL = 3554$

Speed-Up = 2.9079909960607764

Homework3CorrectnessTest.testRandomDataInput1K() ends.

