

Possibility statistics assignment

Zihang Wang - zihang.wang@epita.fr

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PartI

We have several features X, Y and Z that help us describe 3 people A, B, C the following way, What is the correlation matrix of X, Y and Z?:

	X	Y	Z
A	1	2	1
B	2	-1	1
C	3	3	1

Solution:

$$E(X) = (1 + 2 + 3)/3 = 2$$

$$E(Y) = (2 - 1 + 3)/3 = \frac{4}{3}$$

$$E(Z) = (1 + 1 + 1)/3 = 1$$

$$E(XY) = (1 \times 2 + 2 \times -1 + 3 \times 3)/3 = 3$$

$$E(XZ) = (1 \times 1 + 2 \times 1 + 3 \times 1)/3 = 2$$

$$E(YZ) = (2 \times 1 + -1 \times 1 + 3 \times 1)/3 = \frac{4}{3}$$

$$Var(X) = \frac{1^2 + 2^2 + 3^2 - 3 \times 2^2}{3} = \frac{2}{3}$$

$$Var(Y) = \frac{2^2 + (-1)^2 + 3^2 - 3 \times (4/3)^2}{3} = \frac{26}{9}$$

$$Var(Z) = 0$$

$$Cov(X, Y) = 3 - 2 \times \frac{4}{3} = \frac{1}{3}$$

$$Cov(X, Z) = 2 - 2 \times 1 = 0$$

$$Cov(Y, Z) = \frac{4}{3} - \frac{4}{3} \times 1 = 0$$

According to the results, the correlation matrix is:

$$\begin{bmatrix} 2/3 & 1/3 & 0 \\ 1/3 & 26/9 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Check in Python:

```
import numpy as np
data = np.array([[1, 2, 3],
                 [2, -1, 3],
                 [1, 1, 1]])
np.cov(data, bias = True)
```