

Consistent Hashing - 1 Hour Session

Duration: 60 minutes **Level:** Intermediate

Session Agenda

- ☐ Introduction to Consistent Hashing (10 min)
 - ☐ Hash Ring Fundamentals (15 min)
 - ☐ Virtual Nodes (10 min)
 - ☐ Rebalancing & Data Migration (10 min)
 - ☐ Implementation & Real-World Applications (15 min)
-

Learning Objectives

By the end of this session, you will understand: - Why traditional hashing fails in distributed systems - How consistent hashing solves the redistribution problem - The hash ring concept and key placement - Virtual nodes and their benefits - How to handle node additions and removals - Real-world applications in distributed databases and caches

1. Introduction to Consistent Hashing (10 min)

The Problem with Traditional Hashing

Simple Modulo Hashing:

```
server_index = hash(key) % number_of_servers
```

Example with 4 servers:

```
hash("user:123") = 12345
```

```
server = 12345 % 4 = 1 → Server 1
```

What happens when we add/remove a server?

flowchart LR

```
subgraph Before["Before: 4 servers"]
    K1["hash('user:123') % 4 = 1"] --> S1["Server 1"]
    K2["hash('user:456') % 4 = 0"] --> S0["Server 0"]
    K3["hash('user:789') % 4 = 3"] --> S3["Server 3"]
end

subgraph After["After: 5 servers"]
    K1a["hash('user:123') % 5 = 0"] --> S0a["Server 0 MOVED!"]
    K2a["hash('user:456') % 5 = 0"] --> S0b["Server 0 "]
    K3a["hash('user:789') % 5 = 4"] --> S4["Server 4 MOVED!"]
end

Before --> After
```

Result: ~80% of keys need to be remapped!

[!warning] The Redistribution Problem With N servers, adding or removing one server causes (N-1)/N keys to be remapped. For 100 servers, that's 99% of all data!

Why This Matters

Impact on Distributed Systems: - **Cache Invalidation:** Massive cache misses during scaling - **Database Sharding:** Expensive data migration - **Downtime:** System unavailable during rebalancing - **Cost:** Network bandwidth and compute for data movement

The Solution: Consistent Hashing

Key Insight: Instead of mapping keys to servers directly, map both keys AND servers to a fixed hash space (ring).

```
flowchart LR
    subgraph Traditional
        T1[key] --> T2[hash] --> T3[server_index]
    end

    subgraph Consistent
        C1[key] --> C2[hash] --> C3[position_on_ring] --> C4[nearest_server]
    end
```

Benefits: - Only K/N keys remapped when adding/removing nodes (K = total keys, N = nodes) - Minimal data movement during scaling - Predictable load distribution

2. Hash Ring Fundamentals (15 min)

The Hash Ring Concept

Creating the Ring:

```
flowchart TB
    subgraph Ring["Hash Ring (0 to 2^32 - 1)"]
        direction TB
        P0["0°"] --- P90["90°"]
        P90 --- P180["180°"]
        P180 --- P270["270°"]
        P270 --- P0
    end

    Formula["Position = hash(identifier) % ring_size"]
```

Placing Servers on the Ring

```
import hashlib

def hash_to_ring(key, ring_size=2**32):
    """Hash a key to a position on the ring"""
    hash_value = int(hashlib.md5(key.encode()).hexdigest(), 16)
    return hash_value % ring_size

# Place servers on the ring
servers = ["server-A", "server-B", "server-C", "server-D"]
server_positions = {s: hash_to_ring(s) for s in servers}

# Example positions (simplified to 0-360 for visualization)
# server-A: 45°
```

```
# server-B: 120°
# server-C: 200°
# server-D: 300°
```

Visual Representation:

```
flowchart TB
    subgraph HashRing["Hash Ring"]
        direction TB
        P0["0°"]
        A["server-A (45°)"]
        B["server-B (120°)"]
        C["server-C (200°)"]
        D["server-D (300°)"]

        P0 --> A --> B --> C --> D --> P0
    end
```

Key Placement: Finding the Right Server

Rule: A key is assigned to the first server encountered when moving clockwise from the key's position.

```
def find_server(key, server_positions):
    """Find the server responsible for a key"""
    key_position = hash_to_ring(key)

    # Sort servers by position
    sorted_servers = sorted(server_positions.items(), key=lambda x: x[1])

    # Find first server clockwise from key position
    for server, position in sorted_servers:
        if position >= key_position:
            return server

    # Wrap around to first server
    return sorted_servers[0][0]
```

Example:

Key "user:123" hashes to position 80°

Ring positions:

- server-A: 45°
- server-B: 120° ← First server clockwise from 80°
- server-C: 200°
- server-D: 300°

Result: "user:123" → server-B

Adding a New Server

```
flowchart TB
    subgraph Before["Before: 4 servers"]
        direction TB
        B_0["0°"] --> B_A["A (45°)"] --> B_B["B (120°)"] --> B_C["C (200°)"] --> B_D["D (300°)"] --> B_0
    end
```

```

subgraph After["After: Add server-E at 150°"]
    direction TB
    A_0["0°"] --> A_A["A (45°)"] --> A_B["B (120°)"] --> A_E["E (150°)"] --> A_C["C (200°)"] --> A_0
end

Before --> After

```

Only keys between 120° and 150° move from C to E!

Impact Analysis:

```

# Keys affected when adding server-E at 150°
# Only keys in range (120°, 150°] move from server-C to server-E

# Before: Keys 121°-200° → server-C
# After:  Keys 121°-150° → server-E
#         Keys 151°-200° → server-C

# Percentage moved: (150-120)/(360)  8.3% of total keys
# Much better than 80% with modulo hashing!

```

Removing a Server

Remove server-B (120°):

Before:

- Keys 46°-120° → server-B

After:

- Keys 46°-120° → server-E (next clockwise server)

Only server-B's keys need to move!

3. Virtual Nodes (10 min)

The Load Imbalance Problem

With few physical nodes, distribution can be uneven:

4 servers, random positions:

- server-A: 10° (covers 10° of ring = 2.8%)
- server-B: 50° (covers 40° of ring = 11.1%)
- server-C: 300° (covers 250° of ring = 69.4%)
- server-D: 350° (covers 50° of ring = 13.9%)

server-C handles 69% of all keys!

Solution: Virtual Nodes (VNodes)

Idea: Each physical server gets multiple positions on the ring.

```

def create_virtual_nodes(server, num_vnodes=150):
    """Create multiple positions for a single server"""
    vnodes = {}
    for i in range(num_vnodes):

```

```

    vnode_key = f"{server}#vnode{i}"
    position = hash_to_ring(vnode_key)
    vnodes[position] = server
return vnodes

# Example: server-A with 3 virtual nodes
# server-A#vnode0 → position 45°
# server-A#vnode1 → position 180°
# server-A#vnode2 → position 290°

```

Visual with Virtual Nodes:

```

flowchart TB
    subgraph VNodeRing["Ring with Virtual Nodes (Physical: A, B)"]
        direction TB
        P0["0°"]
        A0["A#0 (45°)"]
        B0["B#0 (90°)"]
        A1["A#1 (150°)"]
        B1["B#1 (200°)"]
        B2["B#2 (250°)"]
        A2["A#2 (320°)"]

        P0 --> A0 --> B0 --> A1 --> B1 --> B2 --> A2 --> P0
    end

    style A0 fill:#4CAF50
    style A1 fill:#4CAF50
    style A2 fill:#4CAF50
    style B0 fill:#2196F3
    style B1 fill:#2196F3
    style B2 fill:#2196F3

```

Now load is distributed more evenly!

Benefits of Virtual Nodes

Aspect	Without VNodes	With VNodes
Load Distribution	Uneven	Even
Adding Node	Affects 1 range	Affects many small ranges
Heterogeneous	Not supported	Supported (more vnodes for powerful servers)
Failure Impact	Large chunk unavailable	Small chunks distributed

Handling Heterogeneous Hardware

```

# More powerful servers get more virtual nodes
server_vnodes = {
    "server-A": 100, # Standard server
    "server-B": 100, # Standard server
    "server-C": 200, # 2x capacity server
    "server-D": 50,  # Half capacity server
}

```

```
# server-C handles ~2x the load of A or B
# server-D handles ~0.5x the load of A or B
```

Choosing the Number of Virtual Nodes

Factors to consider:

- More vnodes = better distribution, but more memory for ring
- Typical range: 100-200 vnodes per physical node
- Amazon DynamoDB uses 256 vnodes per node

Memory calculation:

- 100 physical nodes × 150 vnodes = 15,000 ring entries
 - Each entry: ~100 bytes (position + server reference)
 - Total: ~1.5 MB (negligible)
-

4. Rebalancing & Data Migration (10 min)

When Rebalancing Occurs

1. **Node Addition:** New server joins the cluster
2. **Node Removal:** Server leaves (planned or failure)
3. **Capacity Change:** Adjusting virtual node count

Rebalancing Strategy

Adding a Node:

```
def add_node(ring, new_server, num_vnodes=150):
    """Add a new server to the ring"""
    keys_to_migrate = {}

    for i in range(num_vnodes):
        vnode_key = f"{new_server}#vnode{i}"
        new_position = hash_to_ring(vnode_key)

        # Find the server that currently owns this position
        current_owner = find_server_at_position(ring, new_position)

        # Keys between previous position and new position move to new server
        prev_position = find_previous_position(ring, new_position)
        keys_to_migrate[new_position] = {
            'from': current_owner,
            'range': (prev_position, new_position)
        }

        # Add new vnode to ring
        ring[new_position] = new_server

    return keys_to_migrate
```

Migration Process:

- Step 1: Add new node to ring (metadata only)
- Step 2: New node starts accepting writes for its range

Step 3: Background migration of existing keys
Step 4: Old node stops serving migrated keys

Timeline:

t=0 [Add to ring]
t=1 [Accept new writes]
t=2-10 [Background migration]
t=11 [Complete]

Handling Node Failures

Graceful Removal:

```
def remove_node_graceful(ring, server):  
    """Gracefully remove a server"""  
    # 1. Stop accepting new writes  
    server.stop_writes()  
  
    # 2. Migrate data to successor nodes  
    for vnode_position in get_vnodes(ring, server):  
        successor = find_next_server(ring, vnode_position)  
        migrate_data(server, successor, vnode_position)  
  
    # 3. Remove from ring  
    remove_vnodes(ring, server)
```

Sudden Failure:

When a node fails unexpectedly:

1. Detect failure (heartbeat timeout)
2. Remove from ring immediately
3. Successor nodes now responsible for failed node's range
4. If replication exists, replicas serve requests
5. Re-replicate data to maintain replication factor

Data Replication with Consistent Hashing

```
flowchart TB  
    subgraph Replication["Replication Factor: 3"]  
        direction TB  
        Key["Key 'user:123' at 80°"]  
  
        subgraph Ring["Hash Ring"]  
            A["A (45°)"]  
            B["B (120°)<br/> Primary"]  
            E["E (150°)<br/> Replica 1"]  
            C["C (200°)<br/> Replica 2"]  
            D["D (300°)"]  
  
            A --> B --> E --> C --> D --> A  
        end  
  
        Key -.->|"clockwise"| B  
    end
```

```
style B fill:#2196F3
style E fill:#4CAF50
style C fill:#FFC107
```

Strategy: Replicate to N-1 successor nodes

5. Implementation & Real-World Applications (15 min)

Complete Implementation

```
import hashlib
from bisect import bisect_right

class ConsistentHashRing:
    def __init__(self, num_vnodes=150):
        self.num_vnodes = num_vnodes
        self.ring = {} # position -> server
        self.sorted_positions = []
        self.servers = set()

    def _hash(self, key):
        """Generate hash for a key"""
        return int(hashlib.md5(key.encode()).hexdigest(), 16)

    def add_server(self, server):
        """Add a server with virtual nodes"""
        self.servers.add(server)
        for i in range(self.num_vnodes):
            vnode_key = f"{server}#vnode{i}"
            position = self._hash(vnode_key)
            self.ring[position] = server

        self.sorted_positions = sorted(self.ring.keys())

    def remove_server(self, server):
        """Remove a server and its virtual nodes"""
        self.servers.discard(server)
        positions_to_remove = [
            pos for pos, srv in self.ring.items() if srv == server
        ]
        for pos in positions_to_remove:
            del self.ring[pos]

        self.sorted_positions = sorted(self.ring.keys())

    def get_server(self, key):
        """Find the server responsible for a key"""
        if not self.ring:
            return None

        key_hash = self._hash(key)
```



```

    # Find first position >= key_hash
    idx = bisect_right(self.sorted_positions, key_hash)

    # Wrap around if necessary
    if idx == len(self.sorted_positions):
        idx = 0

    position = self.sorted_positions[idx]
    return self.ring[position]

def get_servers_for_replication(self, key, replicas=3):
    """Get N servers for replication"""
    if not self.ring or replicas > len(self.servers):
        return list(self.servers)

    key_hash = self._hash(key)
    idx = bisect_right(self.sorted_positions, key_hash)

    servers = []
    seen = set()

    while len(servers) < replicas:
        if idx >= len(self.sorted_positions):
            idx = 0

        server = self.ring[self.sorted_positions[idx]]
        if server not in seen:
            servers.append(server)
            seen.add(server)

        idx += 1

    return servers

# Usage
ring = ConsistentHashRing(num_vnodes=150)
ring.add_server("server-A")
ring.add_server("server-B")
ring.add_server("server-C")

# Find server for a key
server = ring.get_server("user:12345")
print(f"user:12345 -> {server}")

# Get replicas
replicas = ring.get_servers_for_replication("user:12345", replicas=3)
print(f"Replicas: {replicas}")

```

Real-World Applications

1. Amazon DynamoDB

DynamoDB Partitioning:

- Uses consistent hashing for partition key distribution

- 256 virtual nodes per physical partition
- Automatic rebalancing during scaling

Partition Key → Hash → Partition

"user:123" → 0x7F... → Partition-B

2. Apache Cassandra

Cassandra Token Ring:

- Each node owns a range of tokens
- Virtual nodes (vnodes) enabled by default
- Configurable replication factor

```
CREATE KEYSPACE my_keyspace
WITH replication = {
    'class': 'NetworkTopologyStrategy',
    'datacenter1': 3
};
```

3. Redis Cluster

Redis Cluster:

- 16384 hash slots (not continuous ring)
- Each node owns a subset of slots
- Manual or automatic slot migration

```
CLUSTER ADDSLOTS 0 1 2 3 ... 5460 # Node A
CLUSTER ADDSLOTS 5461 ... 10922 # Node B
CLUSTER ADDSLOTS 10923 ... 16383 # Node C
```

4. Content Delivery Networks (CDNs)

CDN Edge Server Selection:

- Hash(content_url) → Edge server
- Ensures same content always served from same edge
- Maximizes cache hit rate

Request: GET /images/logo.png

Hash: 0x3F...

Edge: edge-server-tokyo-2

Load Balancing with Consistent Hashing

```
class ConsistentHashLoadBalancer:
    def __init__(self):
        self.ring = ConsistentHashRing(num_vnodes=100)
        self.server_health = {}

    def add_backend(self, server, weight=1):
        """Add backend server with optional weight"""
        # More vnodes for higher weight
        vnodes = 100 * weight
        self.ring.num_vnodes = vnodes
        self.ring.add_server(server)
        self.server_health[server] = True
```

```

def get_backend(self, request_key):
    """Get backend for a request"""
    # Use session ID or client IP as key for sticky sessions
    server = self.ring.get_server(request_key)

    # Health check
    if not self.server_health.get(server, False):
        # Fallback to next healthy server
        return self._get_next_healthy(request_key)

    return server

def _get_next_healthy(self, key):
    """Find next healthy server on the ring"""
    servers = self.ring.get_servers_for_replication(key,
                                                    replicas=len(self.ring.servers))

    for server in servers:
        if self.server_health.get(server, False):
            return server
    return None

```

Common Pitfalls & Solutions

1. Hot Spots

Problem: Some keys are accessed much more frequently.

Popular user "celebrity:123" → server-B

Server-B gets 100x more traffic than others

Solutions: - Add read replicas for hot keys - Cache hot keys at application layer - Split hot keys across multiple entries

2. Uneven Virtual Node Distribution

Problem: Random hashing can still create clusters.

Solution: Use deterministic placement or jump consistent hashing.

```

# Jump Consistent Hash (Google)
def jump_consistent_hash(key, num_buckets):
    b, j = -1, 0
    while j < num_buckets:
        b = j
        key = ((key * 286293355777941757) + 1) & 0xFFFFFFFFFFFFFFFF
        j = int((b + 1) * (float(1 << 31) / float((key >> 33) + 1)))
    return b

```

3. Ring Metadata Synchronization

Problem: All nodes need consistent view of the ring.

Solutions: - Gossip protocol (Cassandra) - Centralized coordinator (ZooKeeper) - Consensus algorithm (Raft)

4. Data Migration During Rebalancing

Problem: Large data movement affects performance.

Solutions: - Background migration with rate limiting - Dual-write during transition - Lazy migration (migrate on access)

Comparison with Alternatives

Approach	Redistribution	Complexity	Use Case
Modulo Hash	~100% on change	Low	Static clusters
Consistent Hash	~K/N on change	Medium	Dynamic clusters
Rendezvous Hash	~K/N on change	Medium	When order matters
Jump Hash	~K/N on change	Low	Memory-constrained

Key Takeaways

1. **Consistent hashing minimizes data movement** when scaling clusters
2. **Virtual nodes ensure even distribution** and support heterogeneous hardware
3. **The hash ring is a fundamental building block** for distributed databases and caches
4. **Replication integrates naturally** by using successor nodes
5. **Real systems like DynamoDB, Cassandra, and Redis** all use variants of consistent hashing

Practical Exercise

Scenario: Design a distributed cache for a social media platform.

Requirements: - 10 cache servers initially - Must scale to 50 servers - Session data must be sticky (same user → same server) - Handle server failures gracefully

Questions: 1. How many virtual nodes per server? 2. How to handle user session stickiness? 3. What happens when a server fails? 4. How to migrate data when adding servers?

Quick Reference

Hash Ring Operations

```
# Add server
ring.add_server("server-new")

# Remove server
ring.remove_server("server-old")

# Find server for key
server = ring.get_server("my-key")

# Get replicas
replicas = ring.get_servers_for_replication("my-key", n=3)
```

Key Formulas

Keys remapped (modulo): $(N-1)/N$ 100% for large N

Keys remapped (consistent): K/N where K=total keys, N=nodes

Virtual nodes memory: nodes \times vnodes \times ~100 bytes

Recommended vnodes: 100-256 per physical node

Session End - Thank You!

#consistent-hashing #distributed-systems #partitioning #architecture #session-notes