

(1)

(1.1) Return true if the list contains any zero else return false

(1.2) $T(n) = O(1) + O(1) + T(n/3)$

(1.3) $O(n/3 + 2)$

(1.4)

```
function f(x: List[Integer]) {  
  var n: Integer = Length(x) {  
    for int i = 0; i < n ; i++) {  
      if x[i] == 0 {  
        return true  
      }  
    }  
  }  
  return false  
}
```

(1.5)

They are different. The complexity of iterative is $O(n)$ while the complexity of recursive is $O(n/3 + 2)$. Recursive is more efficient.

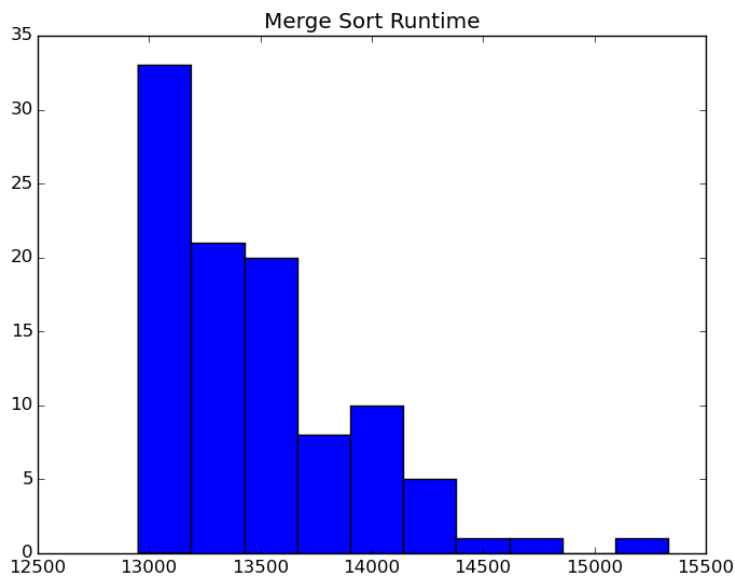
(2)

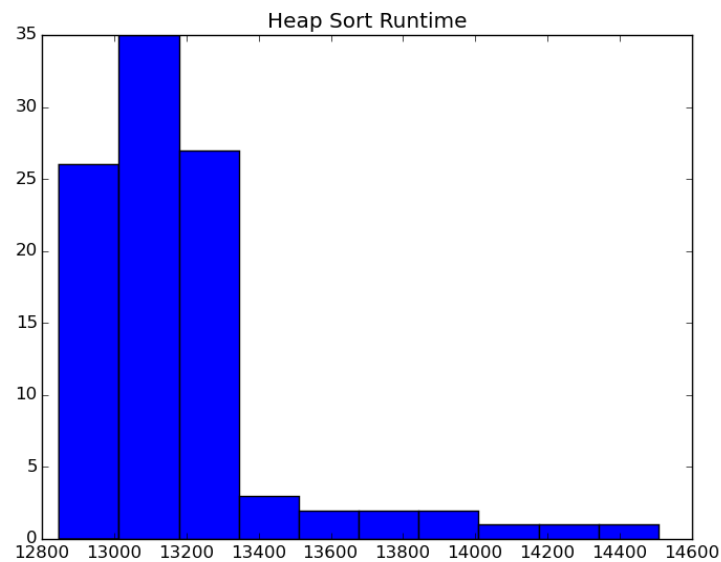
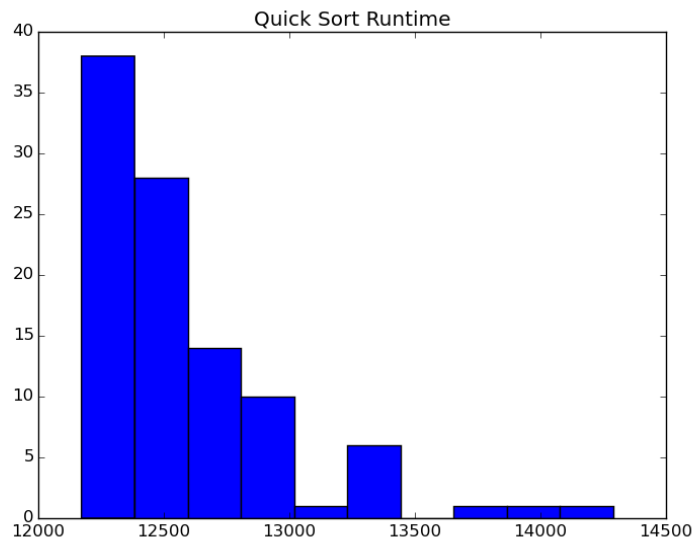
(2.1)

Assume each char is 6 bits and each string is 75 bytes. The object head is 12 bytes. So, the total memory usage is $12 + (75 * 1 \text{ million}) = 75 \text{ mb}$

(2.2) See Attachment.

(2.3)





(3)

(3.1)

Assume each char is 6 bits and each string is 75 bytes. The object head is 12 bytes. So, the total memory usage is $12 + (75 \times 100 \text{ million}) = 7500000012 \text{ Byte} = 7.5 \text{ GB}$.

(3.2) See Attachment.

(3.3)

```
function sort(File file)
```

```
    ArrayList<File> files
```

```
    int chunk_size = 1024*1024*1024
```

```
    Reader reader = new Reader(file)
```

```
    // create a String arrayList
```

```
    ArrayList<String> StringArrayList = new ArrayList<String>();
```

```
    // Fill the arrayList
```

```
    String line = ""
```

```
    while (line not empty)
```

```
        int current_chunk_size = 0
```

```
        // Fill in the ArrayList from file
```

```
        while ((line = reader.readLine() not NULL) &&( current_chunk_size < chunk_size))
```

```
            StringArrayList.add(line)
```

```
            currentchunksize + line.length()
```

```
    // Sorting
```

```
    quickSort(StringArrayList)
```

```
    // Store in temp file
```

```
    File tmp = new tempfile
```

```
    PrintWriter writer = new PrintWriter(tmp)
```

```
    for (String s in StringArrayList)
```

```
        PrintWrriter.write(s)
```

```
    files.add(tmap)
```

```
    clear StringArrayList
```

```
    // use N-way merge to merge every chunk file
```

```
    ArrayList<String> sorted = merge(files)
```

```
    // Write sorted to file
```

```
    PrintWriter writer = new PrintWriter("sorted.txt")
```

```
    for (String s in sorted)
```

```
        writer.write(s)
```

```
    // merge
```

```
    function: ArrayList<String> merge (List<File> files)
```

```
    ArrayList<String> sorted = new ArrayList<String>
```

```
    Comparator<String> cmp: compare string_1 and string 2
```

```
    Comparator<CusFileBuffer> cmp: compare the first string of each file
```

```
    PriorityQueue<CusFileBuffer> pq
```

```
    Add the files as file buffer to the PriorityQueue
```

```

while (pq.size() greater than zero)
    poll the first buffer
    pop the string from the buffer
    add the string the sorted ArrayList

```

```

close all buffer reader
return sorted

```

```

// Customize buffer class
class cusFileBuffer
    BufferedReader reaer
    File ofile
    String line
    boolean empty

```

```

Constructor(File file):
    set the ofile variable
    set the reader
    read()
boolean empty:
    return empty
void read:
    readL() from the file
void close:
    close the reader
String peek:
    return line
String pop:
    String temp = peek()
    read()
    return temp

```

(3.4) $O(n \log n + nk^2)$ while is chunk_size. $n \log n$ = complexity of quick sort for n chunk. nk^2 = complexity of n way merge

(3.5)

see Attachment.