

A. Designing a topdown parser: Consider the following grammar.

```

prog      : stmt-list
stmt-list : stmt-list stmt | stmt
stmt     : PRINT expr | PRINT string
string    : BEGINQUOTE charlist ENDQUOTE
charlist : charlist LETTER |  $\epsilon$ 
expr     : expr + term | expr - term | term
term     : term * factor | term / factor | factor
factor    : ( expr ) | NUM

```

The nonterminal symbols are:

prog, stmt-list, stmt, string, charlist, expr, term, factor

The terminal symbols are:

PRINT, BEGINQUOTE, ENDQUOTE, LETTER, +, -, *, /, (,), NUM

(A1) The grammar is left-recursive. Transform it into a non-left recursive grammar using the following ranking of the nonterminals.

prog, stmt-list, stmt, string, charlist, expr, term, factor

```

prog      : stmt-list
stmt-list : stmt stmt-list'
stmt-list' : stmt stmt-list' |  $\epsilon$ 
stmt     : PRINT expr | PRINT string
string    : BEGINQUOTE charlist ENDQUOTE
charlist  : charlist'
charlist' : LETTER charlist' |  $\epsilon$ 
expr     : term expr'
expr'    : + term expr' | - term expr' |  $\epsilon$ 
term     : factor term'
term'    : * factor term' | / factor term' |  $\epsilon$ 
factor    : ( expr ) | NUM

```

(A2) Further modify the grammar so it is left factored.

```
prog      : stmt-list
stmt-list : stmt stmt-list'
stmt-list' : stmt stmt-list' | ε
stmt      : PRINT word
word      : expr | string
string    : BEGINQUOTE charlist ENDQUOTE
charlist  : charlist'
charlist' : LETTER charlist' | ε
expr      : term expr'
expr'     : + term expr' | - term expr' | ε
term      : factor term'
term'     : * factor term' | / factor term' | ε
factor    : ( expr ) | NUM
```

(A3) Compute the FIRST sets of each nonterminal symbols.

```
prog      : { PRINT }
stmt-list : { PRINT }
stmt-list' : { PRINT }
stmt      : { PRINT }
word      : { (, NUM, BEGINQUOTE }
string    : { BEGINQUOTE }
charlist  : { LETTER }
charlist' : { LETTER }
expr      : { (, NUM }
expr'     : { +, - }
term      : { (, NUM }
term'     : { *, / }
factor    : { (, NUM }
```

(A4) Compute the FOLLOW sets of each nonterminal symbols

prog : { }
stmt-list : { }
stmt-list' : { }
stmt : { PRINT }
word : { PRINT }
string : { PRINT }
charlist : { ENDQUOTE }
charlist' : { ENDQUOTE }
expr : { PRINT,) }
expr' : { PRINT,) }
term : { +, -, PRINT,) }
term' : { +, -, PRINT,) }
factor : { *, /, +, -, PRINT,) }

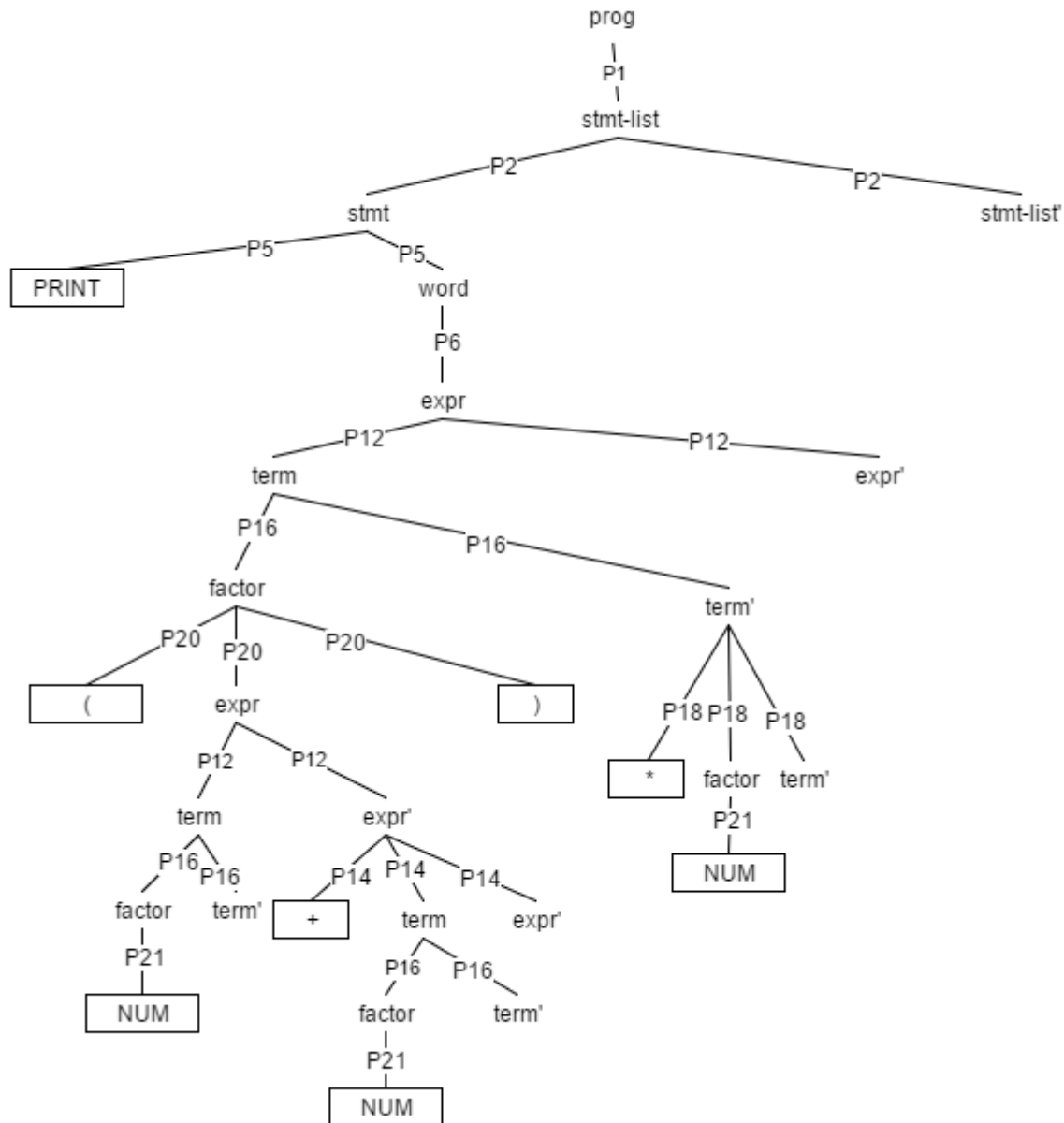
(A5) Compute the predictive parsing table of the grammar.

Non - Terminal	Input Symbol											
	PRINT	BEGINQUOTE	ENDQUOTE	LETTER	+	-	*	/	()	NUM	\$
prog	prog : stmt-list											
stmt-list	stmt-list : stmt stmt-list'											
stmt-list'	stmt-list' : stmt stmt-list'											stmt-list' : ϵ
stmt	stmt : PRINT word											
word		word : string							word : expr		word : expr	
string		string : BEGINQUOTE charlist ENDQUOTE										
charlist			charlist : charlist'	charlist : charlist'								
charlist'			charlist' : ϵ	charlist' : LETTER charlist'								
expr									expr : term expr'		expr : term expr'	
expr'	expr' : ϵ				expr' : + term expr'	expr' : - term expr'				expr' : ϵ		expr' : ϵ
term									term : factor term'		term : factor term'	
term'	term' : ϵ				term' : ϵ	term' : ϵ	term' : * factor term'	term' : / factor term'		term' : ϵ		term' : ϵ
factor									factor : (expr)		factor : NUM	

(A6) Consider the following program.

PRINT (NUM + NUM) * NUM

Use the predictive parsing table to construct the parse tree. At each step, show the production used to expand the nodes.



P1. **prog : stmt-list**

- P2. **stmt-list : stmt stmt-list'**
- P3. **stmt-list' : stmt stmt-list'**
- P4. **stmt-list' : ϵ**
- P5. **stmt : PRINT word**
- P6. **word : expr**
- P7. **word : string**
- P8. **string : BEGINQUOTE charlist ENDQUOTE**
- P9. **charlist : charlist'**
- P10. **charlist' : ϵ**
- P11. **charlist' : LETTER charlist'**
- P12. **expr : term expr'**
- P13. **expr' : ϵ**
- P14. **expr' : + term expr'**
- P15. **expr' : - term expr'**
- P16. **term : factor term'**
- P17. **term' : ϵ**
- P18. **term' : * factor term'**
- P19. **term' : / factor term'**
- P20. **factor : (expr)**
- P21. **factor : NUM**