## **Stellar Evolution**

# **Calvin Sykes**

In [60]:

```
# Import statements
import numpy as np
import matplotlib.pyplot as plt
import scipy.stats
import scipy.interpolate
```

In [61]:

```
# Matplotlib settings
plt.rcParams['figure.figsize'] = [8, 6]
plt.rcParams['font.size'] = 14
plt.rcParams['lines.linewidth'] = 2
```

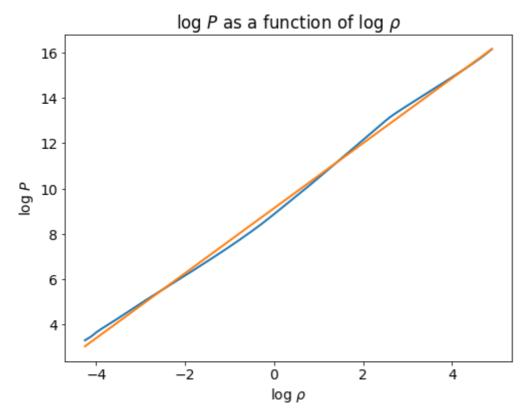
```
In [62]:
```

```
# Convenience function to return a specific column from the data file
def getcol(data, idx):
    return data[:,idx]
```

Plot a line graph of  $\log P$  as a function of  $\log \rho$ . Estimate the gradient of the curve, and from that calculate an approximate polytropic index for the star.

#### In [63]:

```
data = np.loadtxt('structure_00000.txt')
# numbers of columns in data file
col pressure = 3
col density = 4
log density = np.log10(getcol(data, col density))
log pressure = np.log10(getcol(data, col pressure))
# use linear fit to get gradient
m, c, _, _ = scipy.stats.linregress(log_density, log_pressure)
plt.figure()
ax = plt.gca()
ax.set_xlabel(r'$\log\ \rho$')
ax.set_ylabel(r'$\log\ P$')
ax.set title(r'$\log\ P$ as a function of $\log\ \rho$')
plt.plot(log_density, log_pressure)
plt.plot(log density, [m * x + c \text{ for } x \text{ in } log density])
plt.show()
```



The polytropic index n is given by  $n = 1/(\gamma - 1)$ , where  $P = K\rho^{\gamma}$ .

We have  $\log(P) = m \log(\rho) + c$ . Hence the gradient m is equal to  $\gamma$ .

## In [64]:

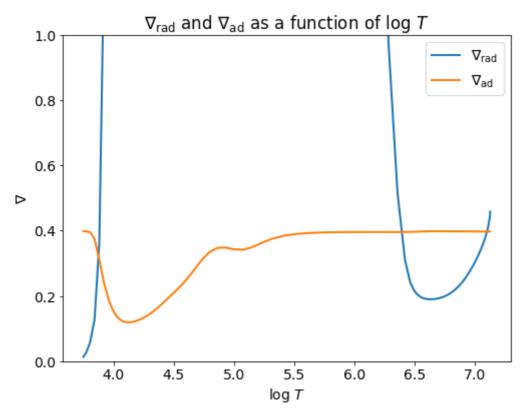
```
polytropic_index = 1 / (m - 1)
print('Polytropic index is {:.3f}'.format(polytropic_index))
```

Polytropic index is 2.307

Make a line plot of the radiative temperature gradient  $\nabla_{\rm rad}$  and adiabatic temperature gradient  $\nabla_{\rm ad}$  (where  $\nabla={\rm d}\log T/{\rm d}\log P$ ) as a function of  $\log T$ . Hence identify the size of the outer convection zone expressed as a fraction of the total radius of the star.

## In [65]:

```
# numbers of columns in data file
col rad temp grad = 15
col_adb_temp_grad = 10
col temp = 5
rad temp grad = getcol(data, col rad temp grad)
adb_temp_grad = getcol(data, col_adb_temp_grad)
log temp = np.log10(getcol(data, col temp))
plt.figure()
ax = plt.gca()
ax.set xlabel(r'$\log\ T$')
ax.set ylabel(r'$\nabla$')
ax.set_ylim(0, 1)
ax.set\_title(r'\$\nabla_\mathbb{s} and \nabla_\mathbb{s} as a function of
 $\log\ T$')
plt.plot(log temp, rad temp grad, label='$\\nabla \\mathrm{rad}$')
plt.plot(log temp, adb temp grad, label='$\\nabla \\mathrm{ad}$')
plt.legend()
plt.show()
```



#### In [66]:

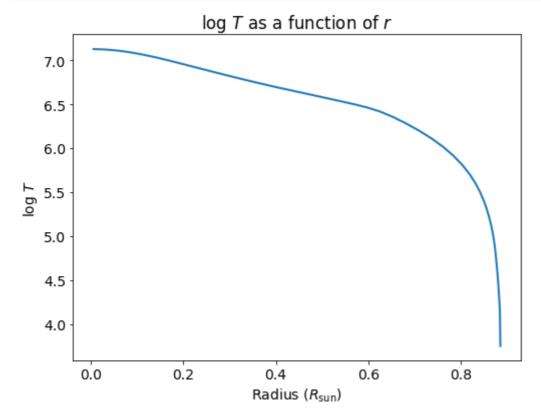
The convective region extends between log T values of 3.88 and 6.36

To find the corresponding radius coordinates, we plot  $\log T$  against r.

## In [67]:

```
col_radius = 1
radius = getcol(data, col_radius)

plt.figure()
ax = plt.gca()
ax.set_xlabel(r'Radius $(R_\mathrm{sun})$')
ax.set_ylabel(r'$\log\ T$')
ax.set_title(r'$\log\ T$ as a function of $r$')
plt.plot(radius, log_temp)
plt.show()
```



Linear interpolation of the curve above can be used to find the radial coordinates corresponding to the start and end of the convective region.

```
In [68]:
```

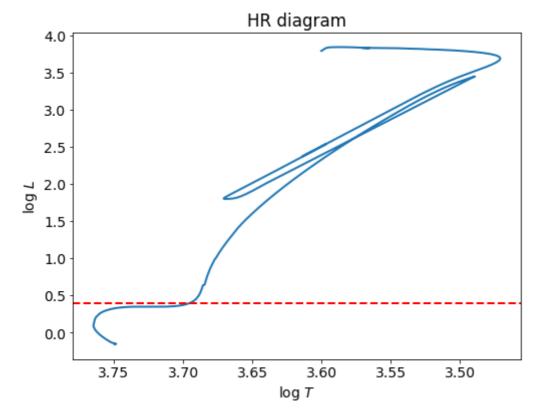
Outer convective zone extends between 0.652 and 0.886 R\_sun

Estimate the age of the star and the mass of the helium core at the point where the star begins its first ascent of the red giant branch.

To find this point, need to draw HR diagram.

#### In [69]:

```
summary = np.loadtxt('summary.txt')
# numbers of columns in data file
col temperature = 5
col luminosity = 3
# these quantities are already reported as logs
log temp = (getcol(summary, col temperature))
log_luminosity = (getcol(summary, col_luminosity))
plt.figure()
ax = plt.qca()
ax.set_xlabel(r'$\log\ T$')
ax.set_ylabel(r'$\log\ L$')
ax.set title('HR diagram')
ax.invert xaxis()
plt.plot(log temp, log luminosity)
plt.axhline(0.4, color='r', linestyle='--')
plt.show()
```



From HR diagram above, start of first RGB ascent is at  $log(L/L_{sun}) \sim 0.4$ .

```
In [70]:
```

```
rgb_log_l = 0.4
```

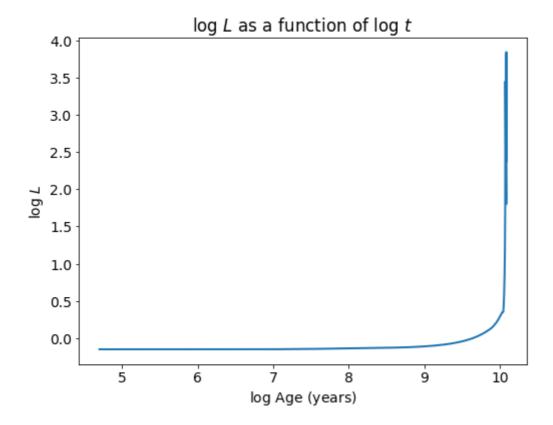
Plot  $\log L$  against  $\log t$  to find corresponding age.

#### In [71]:

```
col_age = 1
log_age = np.log10(getcol(summary, col_age))

plt.figure()
ax = plt.gca()
ax.set_xlabel(r'$\log\ \mathrm{Age}$ (years)')
ax.set_ylabel(r'$\log\ L$')
ax.set_title(r'$\log\ L$ as a function of $\log\ t$')
plt.plot(log_age, log_luminosity)
plt.show()
```

/usr/local/lib/python3.5/dist-packages/ipykernel\_launcher.py:2: Run timeWarning: divide by zero encountered in log10



## In [72]:

```
log_age_func_log_l = scipy.interpolate.interp1d(log_luminosity, log_age)
rgb_log_age = float(log_age_func_log_l(rgb_log_l))
print('Age at start of RGB ascent is {:.3g} yrs'.format(10**rgb_log_age))
```

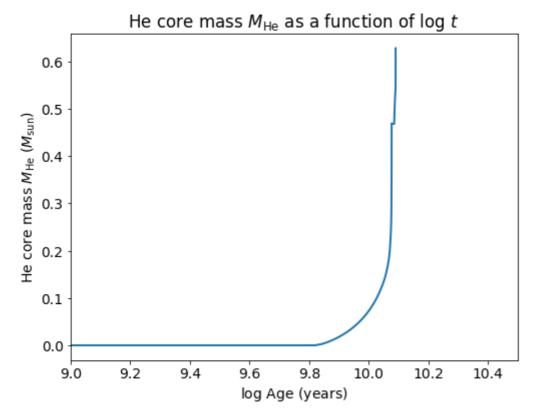
Age at start of RGB ascent is 1.13e+10 yrs

Finally, plot age against helium core mass.

#### In [73]:

```
col_he_core_mass = 23
he_core_mass = getcol(summary, col_he_core_mass)

plt.figure()
ax = plt.gca()
ax.set_xlabel(r'$\log\ \mathrm{Age}$ (years)')
ax.set_xlim(9, 10.5)
ax.set_ylabel(r'He core mass $M_\mathrm{He}\ (M_\mathrm{sun})$')
ax.set_title(r'He core mass $M_\mathrm{He}$ as a function of $\log\ t$')
plt.plot(log_age, he_core_mass)
plt.show()
```



## In [74]:

```
he_core_mass_func_log_age = scipy.interpolate.interpld(log_age, he_core_mass)
rgb_he_core_mass = float(he_core_mass_func_log_age(rgb_log_age))
print('He core mass at start of RGB ascent is {:.3g} M_sun'.format(rgb_he_core_mass))
```

He core mass at start of RGB ascent is 0.14 M\_sun