

1. Data Probability Table

| | Yes | | | | No | | | |
|-------|-------|-------|--------|-------|-------|-------|--------|-------|
| | Round | | Square | | Round | | Square | |
| | Large | Small | Large | Small | Large | Small | Large | Small |
| Blue | 0.000 | 0.000 | 0.000 | 0.000 | 0.067 | 0.067 | 0.000 | 0.067 |
| Green | 0.067 | 0.000 | 0.200 | 0.000 | 0.000 | 0.067 | 0.000 | 0.067 |
| Red | 0.133 | 0.067 | 0.000 | 0.000 | 0.000 | 0.000 | 0.067 | 0.133 |

We can use this data to construct the Bayesian Probability Table:

| | |
|---------------|------------|
| P(Yes) | 0.467 |
| P(No) | 0.533 |
| P(Round Yes) | 0.571 |
| P(Round No) | 0.375 |
| P(Square Yes) | 0.429 |
| P(Square No) | 0.625 |
| P(Large Yes) | 0.85714286 |
| P(Large No) | 0.25 |
| P(Small Yes) | 0.14285714 |
| P(Small No) | 0.75 |
| P(Blue Yes) | 0 |
| P(Blue No) | 0.375 |
| P(Green Yes) | 0.57142857 |
| P(Green No) | 0.25 |
| P(Red Yes) | 0.42857143 |
| P(Red No) | 0.375 |

- Assuming that the features are all mutually exclusive, we can calculate the normalize probability distribution of Square Large Red. We have the following formula:

$$P(\text{YES, Square, Large, Red}) = P(\text{YES} \mid \text{Square, Large, Red}) * P(\text{Square} \mid \text{Large, Red}) * P(\text{Large} \mid \text{Red}) * P(\text{Red})$$

Expanding, and then simplifying it using Bayes' Formula, we are left with:

$$P(\text{YES, Square, Large, Red}) = P(\text{YES} \mid \text{Square, Large, Red}) * P(\text{Square, Large, Red})$$

Rearranging the terms, we then have:

$$P(\text{YES} \mid \text{Square, Large, Red}) = P(\text{YES, Square, Large, Red}) / P(\text{Square, Large, Red})$$

and its counterpart:

$$P(\text{No} \mid \text{Square, Large, Red}) = P(\text{No, Square, Large, Red}) / P(\text{Square, Large, Red})$$

From the above data:

$$P(\text{YES, Square, Large, Red}): 0$$

$$P(\text{NO, Square, Large, Red}): 0.067$$

$$P(\text{Square, Large, Red}): 0.067$$

Normalizing the probability

$$P(\text{YES} \mid \text{Square, Large, Red}): 0 / 0.067 = 0$$

$$P(\text{NO} \mid \text{Square, Large, Red}) : 0.067 / 0.067 = 1$$

Given the provided data, the model would predict that Square Large Red would NOT be safe.