# Parallelzing an All-Pairs Shortest Path Algorithm

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#### Introduction

In this report we describe the implementation and tuning of a parallel all-pairs shortest path algorithm.

### Profiling the given code

#### VTune Amplifier

Given a working implementation of parallelized Floyd-Warshall algorithm, we can further increase the performance by profiling the computation. This will identify areas in the code that run much slower than the rest, giving opportunities to implement speedups. We used the VTune Amplifier to profile our code, calling our executable through the profiler with

amplxe-cl -collect hotspots ./path.x

Function	Module	CPU Time
square	path.x	42.751s
kmp barrier	libiomp5.so	9.623s
kmpc reduce nowait	libiomp5.so	3.498s
kmp fork barrier	libiomp5.so	2.738s
genrand	path.x	0.030s
fletcher16	path.x	0.020s
intel ssse3 rep memcpy	path.x	0.020s
kmp join call	libiomp5.so	0.010s
kmp launch thread	libiomp5.so	0.010s
kmp fork call	libiomp5.so	0.010s

The hotspots analysis results tell us that the most expensive compute-time occurs in square(). This is expected because square() is the only method with nested loops carrying out the algorithm  $(write\_matrix())$  only prints values before and after our algorithm has run).

There are two other methods in our top CPU time list from path.c however any effort put towards optimizing those would not be well spent because they are orders of magnitude faster than square().

We can dig deeper into square()'s performance by running the command amplxe-cl -report hotspots -source-object function="square"

Source Line	Source	CPU Time
47	for (int j = 0; j < n; ++j) {	
48	for (int $i = 0$ ; $i < n$ ; $++i$ ) {	0.020s
49	<pre>int lij = lnew[j*n+i];</pre>	0.020s
50	for (int $k = 0$ ; $k < n$ ; ++k) {	8.699s
51	int lik = $l[k*n+i]$ ;	25.457s
52	int $lkj = l[j*n+k];$	
53	if (lik + lkj < lij) {	3.759s
54	lij = lik+lkj;	
55	done = 0;	4.796s

This tells us the CPU time spent at many points within the method. We can see the majority of the time is spent retrieving a value from the array in the innermost loop. Observe that the matrix accesses are not optimized because we fetch non-contiguous memory each iteration and it is taking a long time. We can re-order the loops to better access our desired values and improve the runtime.

#### Vectorization Report

If we analyze the given code's vectorization report, we can try to adjust some code to take advantage of the compiler's vectorization capabilites. Compiling the code with flags

```
-qopt-report=5 -qopt-report-phase=vec
```

will produce a report summarizing the compiler's ability to vectorize our code. In summary, the given code path is reported to be mostly vectorized. Most estimated potential speedup values were greater than 5, yielding a large factor of speedup. Some loops were not vectorizeable because they contained print statements. Another non-vectorizeable loop was in fletcher16(), but our profiling results show this method to be insignificant in runtime comparison to square() so we will focus our efforts towards square().

# OpenMP Scaling Study

We did both strong scaling and weak scaling study using the provided OpenMP code.

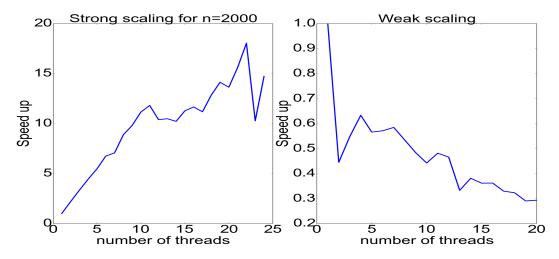
#### **Strong Scaling**

In the strong scaling, we compare parallel to serial time for a fixed size problem. Since the graph is randomly generated, for each experiment, we did 10 simulation and use the average time as their running time. Here we choose the problem size n=2000 and the speedup is summarized in left plot of Figure 1. As can be seen from the left plot of Figure 1, when we increase the number of threads from 1 to 12, the speed up grows linearly with respect to the number of threads. After 12 threads, the speedup doesn't grow linearly due to the excess amount of overheading and synchronization.

#### Weak Scaling

In weak scaling, you need to increase both the number of processors and the amount of jobs such that each processor has the same amount of jobs. In this problem, the time complexity is  $O(n^3 \log n)$ 

Figure 1: scaling study



and we let each processor has approximately  $O(2000^3 \log(2000))$  amount of work. The results are summarized in the right figure of Figure 1. As can be seen from the right figure of Figure 1, the speedup is actually decreasing when you increase the amount of work and the number of processors. This could due to the overheading and synchronization when the number of processors is large.

## MPI Implementation

We implemented a parallel version of the shortest path algorithm using the Message Passing Interface (MPI). In our implementation, each processor is responsible for updating a portion of the shortest path matrix l. Specifically, we partition by column, so that the processor labelled k (for k = 1, ..., p), updates  $l_{ij}$  for  $j \in J_k$ , where the  $(J_k)_{1 \le k \le p}$  define a partion of  $\{1, 2, ..., n\}$ . With this strategy the computation pattern for updating the shortest path matrix remains the same, we are simply looping over a smaller sets of columns.

After each processor has finished updating it's corresponding columns in the update  $l_{ij}^{s+1} = \min_k \{l_{ik}^s + l_{jk}^s\}$ , we call  $MPI\_Allgather$  so that each processor gets the fully updated  $l^{s+1}$  for the next step. Each processor also keeps a local "done" flag that will be true if nothing was updated. In order to determine whether to terminate or not, we call  $MPI\_Allreduce$  with a logical AND operator on the local done flags.

#### **Scaling Study**

We plan to include a scaling study of the MPI implementation. However, at this time the code is performing very poorly, so we will wait until it has been tuned further to show the results.

#### **Future Work**

For the final report, we plan to focus on tuning our paralell implementation.