Categories, Algorithms, Programming

2024.11-02

17 November 2024

Sebastian Gutsche

Sebastian Posur

Øystein Skartsæterhagen

Fabian Zickgraf

Sebastian Gutsche

Email: gutsche@mathematik.uni-siegen.de Homepage: https://sebasguts.github.io/

Address: Department Mathematik Universität Siegen Walter-Flex-Straße 3

57068 Siegen Germany

Sebastian Posur

Email: sebastian.posur@uni-siegen.de

 $Homepage: \verb|https://sebastianpos.github.io||$

Address: Department Mathematik Universität Siegen Walter-Flex-Straße 3 57068 Siegen

Germany

Øystein Skartsæterhagen

Email: oysteini@math.ntnu.no

Homepage: http://www.math.ntnu.no/~oysteini/

Address: NTNU

Institutt for matematiske fag

7491 Trondheim

Norway

Fabian Zickgraf

Email: fabian.zickgraf@uni-siegen.de Homepage: https://github.com/zickgraf/

Address: Walter-Flex-Str. 3 57068 Siegen Germany

Contents

1	CAP	P Categories
	1.1	Categories
	1.2	Categorical properties
	1.3	Constructor
	1.4	Internal Attributes
	1.5	Logic switcher
	1.6	Tool functions
	1.7	Well-Definedness of Cells
	1.8	Unpacking data structures
	1.9	Caching
	1.10	Sanity checks
	1.11	Timing statistics
	1.12	Enable automatic calls of Add
	1.13	Performance tweaks
	1.14	LaTeX
2	Obje	
	2.1	Attributes for the Type of Objects
	2.2	Adding Objects to a Category
	2.3	Equalities for Objects
	2.4	Categorical Properties of Objects
	2.5	Random Objects
	2.6	Tool functions for caches
	2.7	Object constructors
	2.8	Well-Definedness of Objects
	2.9	Projectives
	2.10	Injectives
	2.11	r
	2.12	Dimensions
3	M	
		rphisms
	3.1	Attributes for the Type of Morphisms
	3.2	Adding Morphisms to a Category
	3.3	Morphism constructors
	3.4	Categorical Properties of Morphisms
	3.5	Random Morphisms

	3.6	Non-Categorical Properties of Morphisms
	3.7	Equality and Congruence for Morphisms
	3.8	Basic Operations for Morphisms in Ab-Categories
	3.9	Subobject and Factorobject Operations
	3.10	Identity Morphism and Composition of Morphisms
		Well-Definedness of Morphisms
	3.12	Lift/Colift
		Inverses
		Tool functions for caches
		IsHomSetInhabited
		Homomorphism structures
		Simplified Morphisms
		Reduction by split epi summands
		,
4	Cate	gory 2-Cells 52
	4.1	Attributes for the Type of 2-Cells
	4.2	Adding 2-Cells to a Category
	4.3	Identity 2-Cell and Composition of 2-Cells
	4.4	Well-Definedness for 2-Cells
5	Cate	gory of Categories 55
	5.1	The Category Cat
	5.2	Categories
	5.3	Constructors
	5.4	Functors
	5.5	Natural transformations
6		ersal Objects 61
	6.1	Kernel
	6.2	Cokernel
	6.3	Zero Object
	6.4	Terminal Object
	6.5	Initial Object
	6.6	Direct Sum
	6.7	Coproduct
	6.8	Direct Product
	6.9	Equalizer
		Coequalizer
	6.11	Fiber Product
	6.12	Pushout
	6.13	Image
	6.14	Coimage
	6.15	Homology objects
	6.16	Projective covers and injective envelopes

7	Add	Functions 10					
	7.1	Functions Installed by Add					
	7.2	Add Method					
	7.3	Method name record entries					
	7.4	Enhancing the method name record					
	7.5	Prepare functions					
	7.6	Available Add functions					
8	Managing Derived Methods 17						
	8.1	Info Class					
	8.2	Derivation Objects					
	8.3	Derivation Graphs					
	8.4	Managing Derivations in a Category					
9	Tech	nical Details 180					
	9.1	The Category Cat					
	9.2	Tools					
10	Limi	its and Colimits					
		Specification of Limits and Colimits					
		Enhancing Limit Specifications					
		Functions					
11	The Category Constructor						
		Info class					
		Constructors					
12	Reinterpretations of categories 197						
		Introduction					
		Tutorial					
		Implementation details					
		Relation to CompilerForCAP					
		Attributes					
		Constructors					
13	Create wrapper hulls of a category 202						
		GAP categories					
		Attributes					
		Constructors					
14	Dun	amy implementations 20:					
		Dummy rings					
		Dummy categories					
		Dummy homalg rings					

15	Exar	mples and Tests	209		
	15.1	Dummy implementations	209		
	15.2	Functors	210		
	15.3	HandlePrecompiledTowers	211		
	15.4	Terminal category	212		
16 Terminal category					
	16.1	GAP Categories	217		
	16.2	Constructors	218		
	16.3	Attributes	218		
Inc	lex		220		

Chapter 1

CAP Categories

Categories are the main GAP objects in CAP. They are used to associate GAP objects which represent objects and morphisms with their category. By associating a GAP object to the category, one of two filters belonging to the category (ObjectFilter/MorphismFilter) are set to true. Via Add methods, functions for specific existential quantifiers can be associated to the category and after that can be applied to GAP objects in the category. A GAP category object also knows which constructions are currently possible in this category.

Classically, a category consists of a class of objects, a set of morphisms, identity morphisms, and a composition function satisfying some simple axioms. In CAP, we use a slightly different notion of a category.

A CAP category C consists of the following data:

- A set Obj_C of objects.
- For every pair $a, b \in \mathrm{Obj}_{\mathbb{C}}$, a set $\mathrm{Hom}_{\mathbb{C}}(a, b)$ of *morphisms*.
- For every pair $a,b \in \mathrm{Obj}_{\mathbb{C}}$, an equivalence relation $\sim_{a,b}$ on $\mathrm{Hom}_{\mathbb{C}}(a,b)$ called *congruence for morphisms*.
- For every $a \in \text{Obj}_{\mathbb{C}}$, an *identity morphism* $\text{id}_a \in \text{Hom}_{\mathbb{C}}(a, a)$.
- For every triple $a, b, c \in \text{Obj}_{\mathbb{C}}$, a composition function

$$\circ$$
: $\operatorname{Hom}_{\mathbf{C}}(b,c) \times \operatorname{Hom}_{\mathbf{C}}(a,b) \to \operatorname{Hom}_{\mathbf{C}}(a,c)$

compatible with the congruence, i.e., if $\alpha, \alpha' \in \operatorname{Hom}_{\mathbf{C}}(a,b)$, $\beta, \beta' \in \operatorname{Hom}_{\mathbf{C}}(b,c)$, $\alpha \sim_{a,b} \alpha'$ and $\beta \sim_{b,c} \beta'$, then $\beta \circ \alpha \sim_{a,c} \beta' \circ \alpha'$.

• For all $a,b\in \mathrm{Obj}_{\mathbb{C}},\, \alpha\in \mathrm{Hom}_{\mathbb{C}}(a,b),$ we have

$$(\mathrm{id}_b \circ \alpha) \sim_{a,b} \alpha$$

and

$$\alpha \sim_{ab} (\alpha \circ id_a)$$
.

• For all $a,b,c,d \in \mathrm{Obj}_{\mathbb{C}}$, $\alpha \in \mathrm{Hom}_{\mathbb{C}}(a,b)$, $\beta \in \mathrm{Hom}_{\mathbb{C}}(b,c)$, $\gamma \in \mathrm{Hom}_{\mathbb{C}}(c,d)$, we have

$$((\gamma \circ \beta) \circ \alpha) \sim_{a,d} (\gamma \circ (\beta \circ \alpha))$$

1.1 Categories

1.1.1 IsCapCategory (for IsAttributeStoringRep)

▷ IsCapCategory(object)

(filter)

Returns: true or false

The GAP category of CAP categories. Objects of this type handle the CAP category information, the caching, and filters for objects in the CAP category. Please note that the object itself is not related to methods, you only need it as a handler and a presentation of the CAP category.

1.1.2 IsCapCategoryCell (for IsAttributeStoringRep)

▷ IsCapCategoryCell(object)

(filter)

Returns: true or false

The GAP category of CAP category cells. Every object, morphism, and 2-cell of a CAP category lies in this GAP category.

1.1.3 IsCapCategoryObject (for IsCapCategoryCell)

▷ IsCapCategoryObject(object)

(filter)

Returns: true or false

The GAP category of CAP category objects. Every object of a CAP category lies in this GAP category.

1.1.4 IsCapCategoryMorphism (for IsCapCategoryCell)

▷ IsCapCategoryMorphism(object)

(filter)

Returns: true or false

The GAP category of CAP category morphisms. Every morphism of a CAP category lies in this GAP category.

1.1.5 IsCapCategoryTwoCell (for IsCapCategoryCell)

▷ IsCapCategoryTwoCell(object)

(filter)

Returns: true or false

The GAP category of CAP category 2-cells. Every 2-cell of a CAP category lies in this GAP category.

1.2 Categorical properties

1.2.1 AddCategoricalProperty

▷ AddCategoricalProperty(list)

(function)

Adds a categorical property to the list of CAP categorical properties. *list* must be a list containing one entry, if the property is self dual, or two, if the dual property has a different name. If the first entry of the list is empty and the second is a property name, the property is assumed to have no dual.

1.2.2 IsEquippedWithHomomorphismStructure (for IsCapCategory)

▷ IsEquippedWithHomomorphismStructure(C)

(property)

Returns: true or false

The property of the category C being equipped with a homomorphism structure.

1.2.3 IsCategoryWithDecidableLifts (for IsCapCategory)

▷ IsCategoryWithDecidableLifts(C)

(property)

Returns: true or false

The property of the category C having decidable lifts.

1.2.4 IsCategoryWithDecidableColifts (for IsCapCategory)

 ${\scriptstyle \rhd} \ \, {\tt IsCategoryWithDecidableColifts(\it C)} \\$

(property)

Returns: true or false

The property of the category C having decidable colifts.

1.2.5 IsCategoryWithInitialObject (for IsCapCategory)

▷ IsCategoryWithInitialObject(C)

(property)

Returns: true or false

The property of the category C having an initial object.

1.2.6 IsCategoryWithTerminalObject (for IsCapCategory)

 ${\scriptstyle \rhd} \ \, {\tt IsCategoryWithTerminalObject} \, ({\it C}) \\$

(property)

Returns: true or false

The property of the category C having a terminal object.

1.2.7 IsCategoryWithZeroObject (for IsCapCategory)

▷ IsCategoryWithZeroObject(C)

(property)

Returns: true or false

The property of the category C having a zero object.

1.2.8 IsEnrichedOverCommutativeRegularSemigroup (for IsCapCategory)

▷ IsEnrichedOverCommutativeRegularSemigroup(C)

(property)

Returns: true or false

The property of the category C being enriched over a commutative regular semigroup.

1.2.9 IsSkeletalCategory (for IsCapCategory)

 \triangleright IsSkeletalCategory(C)

(property)

Returns: true or false

The property of the category $\mathcal C$ being skeletal, that is, whether IsEqualForObjects and IsIsomorphicForObjects coincide.

1.2.10 IsAbCategory (for IsCapCategory)

▷ IsAbCategory(C)

(property)

Returns: true or false

The property of the category C being preadditive.

1.2.11 IsLinearCategoryOverCommutativeRing (for IsCapCategory)

▷ IsLinearCategoryOverCommutativeRing(C)

(property)

Returns: true or false

The property of the category C being linear over a commutative ring.

1.2.12 IsLinearCategoryOverCommutativeRingWithFinitelyGeneratedFreeExternalHoms (for IsCapCategory)

▷ IsLinearCategoryOverCommutativeRingWithFinitelyGeneratedFreeExternalHoms(C)

(property)

Returns: true or false

The property of the category C being linear over a commutative ring k such that all external homs are finitely generated free k-modules.

1.2.13 IsAdditiveCategory (for IsCapCategory)

▷ IsAdditiveCategory(C)

(property)

Returns: true or false

The property of the category C being additive.

1.2.14 IsPreAbelianCategory (for IsCapCategory)

▷ IsPreAbelianCategory(C)

(property)

Returns: true or false

The property of the category C being preabelian.

1.2.15 IsAbelianCategory (for IsCapCategory)

▷ IsAbelianCategory(C)

(property)

Returns: true or false

The property of the category C being abelian.

1.2.16 IsAbelianCategoryWithEnoughProjectives (for IsCapCategory)

▷ IsAbelianCategoryWithEnoughProjectives(C)

(property)

Returns: true or false

The property of the category C being abelian with enough projectives.

1.2.17 IsAbelianCategoryWithEnoughInjectives (for IsCapCategory)

▷ IsAbelianCategoryWithEnoughInjectives(C)

(property)

Returns: true or false

The property of the category C being abelian with enough injectives.

1.2.18 IsLocallyOfFiniteProjectiveDimension (for IsCapCategory)

▷ IsLocallyOfFiniteProjectiveDimension(C)

(property)

Returns: true or false

The property of the category C being locally of finite projective dimension.

1.2.19 IsLocallyOfFiniteInjectiveDimension (for IsCapCategory)

▷ IsLocallyOfFiniteInjectiveDimension(C)

(property)

Returns: true or false

The property of the category C being locally of finite injective dimension.

1.3 Constructor

1.3.1 CreateCapCategory

▷ CreateCapCategory()

(operation)

Returns: a category

Creates a new CAP category from scratch. It gets a generic name.

1.3.2 CreateCapCategory (for IsString)

▷ CreateCapCategory(s)

(operation)

(operation)

Returns: a category

The argument is a string s. This o

The argument is a string s. This operation creates a new CAP category from scratch. Its name is set to s.

1.3.3 CreateCapCategory (for IsString, IsFunction, IsFunction, IsFunction)

 ${\tt \coloredge Category}(s,\ category_filter,\ object_filter,\ morphism_filter,\ two_cell_filter)$

Returns: a category

The argument is a string s. This operation creates a new CAP category from scratch. Its name is set to s. The category, its objects, its morphisms, and its two cells will lie in the corresponding given filters.

1.3.4 CreateCapCategoryWithDataTypes

 $\verb| CreateCapCategoryWithDataTypes| (s, category_filter, object_filter, morphism_filter, two_cell_filter, object_datum_type, morphism_datum_type, \\$

two_cell_datum_type)

(function)

Returns: a category

The argument is a string s. This operation creates a new CAP category from scratch. Its name is set to s. The category, its objects, its morphisms, and its two cells will lie in the corresponding given filters. The data types of the object/morphism/two cell datum can be given as described in CapJitInferredDataTypes (CompilerForCAP: CapJitInferredDataTypes). As a convenience, simply a filter can be given if this suffices to fully determine the data type. If a data type is not specified, pass fail instead.

1.4 Internal Attributes

1.4.1 Name (for IsCapCategory)

 \triangleright Name (C) (attribute)

Returns: a string

The argument is a category *C*. The output is its name.

Each category C stores various filters. They are used to apply the right functions in the method selection.

1.4.2 CategoryFilter (for IsCapCategory)

▷ CategoryFilter(C)

(attribute)

Returns: a filter

The argument is a category C. The output is a filter in which C lies.

1.4.3 ObjectFilter (for IsCapCategory)

▷ ObjectFilter(C)

(attribute)

Returns: a filter

The argument is a category C. The output is a filter in which all objects of C shall lie.

1.4.4 MorphismFilter (for IsCapCategory)

▷ MorphismFilter(C)

(attribute)

Returns: a filter

The argument is a category C. The output is a filter in which all morphisms of C shall lie.

1.4.5 TwoCellFilter (for IsCapCategory)

▷ TwoCellFilter(C)

(attribute)

Returns: a filter

The argument is a category C. The output is a filter in which all 2-cells of C shall lie.

1.4.6 ObjectDatumType (for IsCapCategory)

▷ ObjectDatumType(C)

(attribute)

Returns: a data type or fail

The argument is a category C. The output is the data type (see CapJitInferredDataTypes (**CompilerForCAP: CapJitInferredDataTypes**)) of object data of C (or fail if this data type is not specified).

1.4.7 MorphismDatumType (for IsCapCategory)

▷ MorphismDatumType(C)

(attribute)

Returns: a data type or fail

The argument is a category C. The output is the data type (see CapJitInferredDataTypes (**CompilerForCAP: CapJitInferredDataTypes**)) of morphism data of C (or fail if this data type is not specified).

1.4.8 TwoCellDatumType (for IsCapCategory)

▷ TwoCellDatumType(C)

(attribute)

Returns: a data type or fail

The argument is a category C. The output is the data type (see CapJitInferredDataTypes (**CompilerForCAP: CapJitInferredDataTypes**)) of two cell data of C (or fail if this data type is not specified).

1.4.9 CommutativeRingOfLinearCategory (for IsCapCategory)

□ CommutativeRingOfLinearCategory(C)

(attribute)

Returns: a ring

The argument is a category C which is expected to lie in the filter IsLinearCategoryOverCommutativeRing. The output is a commutative ring over which the category is linear.

1.4.10 RangeCategoryOfHomomorphismStructure (for IsCapCategory)

▷ RangeCategoryOfHomomorphismStructure(C)

(attribute)

Returns: a category

The argument is a category C which is expected to lie in the filter IsEquippedWithHomomorphismStructure. The output is the range category D of the defining functor $H: C^{\mathrm{op}} \times C \to D$ of the homomorphism structure.

1.4.11 AdditiveGenerators (for IsCapCategory)

▷ AdditiveGenerators(C)

(attribute)

Returns: a list of objects

The argument is an additive category C. The output is a list L of objects in C such that every object in C is a finite direct sum of objects in L.

1.4.12 IndecomposableProjectiveObjects (for IsCapCategory)

▷ IndecomposableProjectiveObjects(C)

(attribute)

Returns: a list of objects

The argument is an Abelian category C with enough projectives. The output is the set of indecomposable projective objects in C up to isomorphism. That is every projective object in C is isomorphic to a finite direct sum over these objects.

1.4.13 IndecomposableInjectiveObjects (for IsCapCategory)

▷ IndecomposableInjectiveObjects(C)

(attribute)

Returns: a list of objects

The argument is an Abelian category C with enough injectives. The output is the set of indecomposable injective objects in C up to isomorphism. That is every injective object in C is isomorphic to a finite direct sum over these objects.

1.5 Logic switcher

1.5.1 CapCategorySwitchLogicPropagationForObjectsOn

▷ CapCategorySwitchLogicPropagationForObjectsOn(C)

(function)

Activates the predicate logic propagation between equal objects for the category C.

1.5.2 CapCategorySwitchLogicPropagationForObjectsOff

▷ CapCategorySwitchLogicPropagationForObjectsOff(C)

(function)

Deactivates the predicate logic propagation between equal objects for the category C.

1.5.3 CapCategorySwitchLogicPropagationForMorphismsOn

▷ CapCategorySwitchLogicPropagationForMorphismsOn(C)

(function)

Activates the predicate logic propagation between equal morphisms for the category C.

1.5.4 CapCategorySwitchLogicPropagationForMorphismsOff

▷ CapCategorySwitchLogicPropagationForMorphismsOff(C)

(function)

Deactivates the predicate logic propagation between equal morphisms for the category C.

1.5.5 CapCategorySwitchLogicPropagationOn

▷ CapCategorySwitchLogicPropagationOn(C)

(function)

Activates the predicate logic propagation between equal cells for the category C.

1.5.6 CapCategorySwitchLogicPropagationOff

▷ CapCategorySwitchLogicPropagationOff(C)

(function)

Deactivates the predicate logic propagation between equal cells for the category C.

1.5.7 CapCategorySwitchLogicOn

▷ CapCategorySwitchLogicOn(C)

(function)

Activates the predicate implication logic for the category C.

1.5.8 CapCategorySwitchLogicOff

▷ CapCategorySwitchLogicOff(C)

(function)

Deactivates the predicate implication logic for the category C.

1.6 Tool functions

1.6.1 CanCompute (for IsCapCategory, IsString)

▷ CanCompute(C, string)

(operation)

▷ CanCompute(C, operation)

(operation)

Returns: true or false

The argument is a category C and a string string, which should be the name of a CAP operation, e.g., PreCompose. If applying this method is possible in C, the method returns true, false otherwise. If the string is not the name of a CAP operation, an error is raised. For debugging purposes one can also pass the CAP operation instead of its name.

1.6.2 OperationWeight (for IsCapCategory, IsString)

▷ OperationWeight(cat, op_name)

(operation)

Returns: an integer

Returns the weight of the operation currently installed as op_name in cat.

1.6.3 MissingOperationsForConstructivenessOfCategory (for IsCapCategory, IsString)

▷ MissingOperationsForConstructivenessOfCategory(C, s)

(operation)

Returns: a list

The arguments are a category C and a string s. If s is a categorical property (e.g. "IsAbelianCategory"), the output is a list of strings with CAP operations which are missing in C to have the categorical property constructively. If s is not a categorical property, an error is raised.

1.7 Well-Definedness of Cells

1.7.1 IsWellDefined (for IsCapCategoryCell)

 \triangleright IsWellDefined(c) (property)

Returns: a boolean

The argument is a cell c. The output is true if c is well-defined, otherwise the output is false.

1.8 Unpacking data structures

1.8.1 Down (for IsObject)

 \triangleright Down(x) (attribute)

Returns: a GAP object

The argument is a GAP object x. If x is an object in a CAP category, the output consists of data which are needed to reconstruct x (e.g., by passing them to an appropriate constructor). If x is a morphism in a CAP category, the output consists of a triple whose first entry is the source of x, the third entry is the range of x, and the second entry consists of data which are needed to reconstruct x (e.g., by passing them to an appropriate constructor, possibly together with the source and range of x).

1.8.2 DownOnlyMorphismData (for IsCapCategoryMorphism)

▷ DownOnlyMorphismData(x)

(attribute)

Returns: a GAP object

The argument is a morphism in a CAP category, the output consists of data which are needed to reconstruct x (e.g., by passing it to an appropriate constructor, possibly together with its source and range).

1.8.3 DownToBottom (for IsObject)

DownToBottom(x)

(attribute)

Returns: a GAP object

The argument is a GAP object x. This function iteratively calls Down until it becomes stable.

1.9 Caching

1.9.1 SetCachingOfCategory

▷ SetCachingOfCategory(category, type)

(function)

Sets the caching of category to type.

1.9.2 SetCachingOfCategoryWeak

▷ SetCachingOfCategoryWeak(category)

(function)

▷ SetCachingOfCategoryCrisp(category)

(function)

```
▷ DeactivateCachingOfCategory(category)
```

(function)

Sets the caching of category to weak, crisp or none, respectively.

1.9.3 SetDefaultCaching

```
▷ SetDefaultCaching(type) (function)

▷ SetDefaultCachingWeak() (function)

▷ SetDefaultCachingCrisp() (function)

▷ DeactivateDefaultCaching() (function)
```

Sets the default caching behaviour, all new categories will have their caching set to either weak, crisp, or none. The default at startup is weak.

1.10 Sanity checks

1.10.1 DisableInputSanityChecks

```
▷ DisableInputSanityChecks(category)
                                                             (function)
▷ DisableOutputSanityChecks(category)
                                                             (function)
(function)
(function)

    ▷ EnableFullInputSanityChecks(category)

                                                             (function)
(function)
▷ DisableSanityChecks(category)
                                                             (function)
▷ EnablePartialSanityChecks(category)
                                                             (function)

        ▷ EnableFullSanityChecks(category)

                                                             (function)
```

Most operations can perform optional sanity checks on their arguments and results. The checks can either be partial (set by default), full, or disabled. With the following commands you can either enable the full checks, the partial checks or, for performance, disable the checks altogether. You can do this for input checks, output checks or for both at once.

1.11 Timing statistics

1.11.1 EnableTimingStatistics

\triangleright	EnableTimingStatistics(category)	(function)
\triangleright	<pre>DisableTimingStatistics(category)</pre>	(function)
\triangleright	ResetTimingStatistics(category)	(function)
\triangleright	<pre>DisplayTimingStatistics(category)</pre>	(function)
\triangleright	BrowseTimingStatistics(category)	(function)

Enable, disable, reset, display, or browse timing statistics of the primitive operations of *category*. Caution: If a primitive operation calls another primitive operation, the runtime of the later (including sanity checks etc.) is also included in the runtime of the former.

1.12 Enable automatic calls of Add

1.12.1 EnableAddForCategoricalOperations

ightharpoonup EnableAddForCategoricalOperations(C) (function) ightharpoonup (function) ho (function)

Enables/disables the automatic call of Add for the output of primitively added functions for the category *C*. If the automatic call of Add is disabled (default), the output of primitively added functions must belong to the correct category. If the automatic call of Add is enabled, the output of primitively added functions only has to be a GAP object lying in IsAttributeStoringRep (with suitable attributes Source and Range if the output should be a morphism or a twocell).

1.13 Performance tweaks

For finding performance issues in primitive operations, you can collect timing statistics, see 1.11. You can use the package CompilerForCAP to compile your code. Additionally, CAP has several settings which can improve the performance. In the following some of these are listed.

- DeactivateCachingOfCategory or DeactivateDefaultCaching: see 1.9. This can either improve or degrade the performance depending on the concrete example.
- CapCategorySwitchLogicOff (on by default) or CapCategorySwitchLogicPropagationOff (off by default): see 1.5. This can either improve or degrade the performance depending on the concrete example.
- DisableSanityChecks: see 1.10.
- DisableAddForCategoricalOperations: see 1.12.
- DeactivateToDoList: see the package ToolsForHomalg.
- Use CreateCapCategoryObjectWithAttributes (2.2) instead of AddObject and CreateCapCategoryMorphismWithAttributes (3.2) instead of AddMorphism.
- Pass the option overhead := false to CreateCapCategory. Note: this may have unintended effects. Use with care!

1.14 LaTeX

1.14.1 LaTeXOutput (for IsCapCategoryCell)

▷ LaTeXOutput(c)

Returns: a string

The argument is a cell c. The output is a LaTeX string s (without enclosing dollar signs) that may be used to print out c nicely.

(operation)

1.14.2 LaTeXOutput (for IsCapCategory)

▷ LaTeXOutput(C) (operation)

Returns: a string

The argument is a category C. The output is a LaTeX string s (without enclosing dollar signs) that may be used to print out C nicely.

Chapter 2

Objects

Any GAP object which is IsCapCategoryObject can be added to a category and then becomes an object in this category. Any object can belong to one or no category. After a GAP object is added to the category, it knows which things can be computed in its category and to which category it belongs. It knows categorial properties and attributes, and the functions for existential quantifiers can be applied to the object.

2.1 Attributes for the Type of Objects

2.1.1 CapCategory (for IsCapCategoryObject)

▷ CapCategory(a)
Returns: a category

The argument is an object a. The output is the category \mathbb{C} to which a was added.

2.2 Adding Objects to a Category

2.2.1 Add (for IsCapCategory, IsCapCategoryObject)

▷ Add(category, object)

(operation)

(attribute)

Adds object as an object to category.

2.2.2 AddObject (for IsCapCategory, IsAttributeStoringRep)

▷ AddObject(category, object)

(operation)

Adds *object* as an object to *category*. If *object* already lies in the filter IsCapCategoryObject, the operation Add (2.2.1) can be used instead.

2.2.3 CreateCapCategoryObjectWithAttributes

▷ CreateCapCategoryObjectWithAttributes(category[, attribute1, value1, ...])

(function)

Returns: an object

Creates an object in category with the given attributes.

2.2.4 AsCapCategoryObject

▷ AsCapCategoryObject(category, value)

(function)

Returns: an object

EXPERIMENTAL: This specification might change any time without prior notice. Views value as an object in category.

2.2.5 AsPrimitiveValue (for IsCapCategoryObject)

▷ AsPrimitiveValue(object)

(attribute)

▷ AsInteger(object)

(attribute)

▷ AsHomalgMatrix(object)

(attribute)

Returns: a value

EXPERIMENTAL: This specification might change any time without prior notice. Views an object obtained via AsCapCategoryObject (2.2.4) as a primitive value again. Here, the word *primitive* means *primitive from the perspective of the category*. For example, from the perspective of an opposite category, objects of the underlying category are primitive values. The attribute is chosen according to the object datum type:

- For IsInt, the attribute AsInteger is used.
- For IsHomalgMatrix, the attribute AsHomalgMatrix is used.

In all other cases or if no object datum type is given, the attribute AsPrimitiveValue is used.

2.3 Equalities for Objects

2.3.1 IsEqualForObjects (for IsCapCategoryObject, IsCapCategoryObject)

▷ IsEqualForObjects(a, b)

(operation)

Returns: a boolean

The arguments are two objects a and b. The output is true if a = b, otherwise the output is false.

2.3.2 IsIsomorphicForObjects (for IsCapCategoryObject, IsCapCategoryObject)

 \triangleright IsIsomorphicForObjects(a, b)

(operation)

Returns: a boolean

The arguments are two objects a and b. The output is true if a and b are isomorphic, that is, if there exists an isomorphism $a \to b$, otherwise the output is false.

2.3.3 SomeIsomorphismBetweenObjects (for IsCapCategoryObject, IsCapCategory-Object)

 \triangleright SomeIsomorphismBetweenObjects(a, b)

(operation)

Returns: an isomorphism in Hom(a,b)

The arguments are two isomorphic objects a and b. The output is an isomorphism $a \to b$.

2.4 Categorical Properties of Objects

2.4.1 IsBijectiveObject (for IsCapCategoryObject)

▷ IsBijectiveObject(a)

(property)

Returns: a boolean

The argument is an object a. The output is true if a is a bijective object, otherwise the output is false.

2.4.2 IsProjective (for IsCapCategoryObject)

▷ IsProjective(a)

(property)

Returns: a boolean

The argument is an object a. The output is true if a is a projective object, otherwise the output is false.

2.4.3 IsInjective (for IsCapCategoryObject)

▷ IsInjective(a)

(property)

Returns: a boolean

The argument is an object a. The output is true if a is an injective object, otherwise the output is false.

2.4.4 IsTerminal (for IsCapCategoryObject)

▷ IsTerminal(a)

(property)

Returns: a boolean

The argument is an object a of a category C. The output is true if a is isomorphic to the terminal object of C, otherwise the output is false.

2.4.5 IsInitial (for IsCapCategoryObject)

▷ IsInitial(a)

(property)

Returns: a boolean

The argument is an object a of a category C. The output is true if a is isomorphic to the initial object of C, otherwise the output is false.

2.4.6 IsZeroForObjects (for IsCapCategoryObject)

▷ IsZeroForObjects(a)

(property)

Returns: a boolean

The argument is an object a of a category C. The output is true if a is isomorphic to the zero object of C, otherwise the output is false.

2.4.7 IsZero (for IsCapCategoryObject)

▷ IsZero(a)

(property)

Returns: a boolean

The argument is an object a of a category C. The output is true if a is isomorphic to the zero object of C, otherwise the output is false.

2.5 Random Objects

CAP provides two principal methods to generate random objects:

- By integers: The integer is simply a parameter that can be used to create a random object.
- By lists: The list is used when creating a random object would need more than one parameter. Lists offer more flexibility at the expense of the genericity of the methods. This happens because lists that are valid as input in some category may be not valid for other categories. Hence, these operations are not thought to be used in generic categorical algorithms.

2.5.1 RandomObjectByInteger (for IsCapCategory, IsInt)

▷ RandomObjectByInteger(C, n)

(operation)

Returns: an object in C

The arguments are a category C and an integer n. The output is a random object in C.

2.5.2 RandomObjectByList (for IsCapCategory, IsList)

 \triangleright RandomObjectByList(C, L)

(operation)

Returns: an object in C

The arguments are a category C and a list L. The output is a random object in C.

2.5.3 RandomObject (for IsCapCategory, IsInt)

▷ RandomObject(C, n)

(operation)

These are convenient methods and they, depending on the input, delegate to one of the above methods.

2.5.4 RandomObject (for IsCapCategory, IsList)

▷ RandomObject(C, L)

(operation)

2.6 Tool functions for caches

2.6.1 IsEqualForCacheForObjects (for IsCapCategoryObject, IsCapCategoryObject)

▷ IsEqualForCacheForObjects(phi, psi)

(operation)

Returns: true or false

By default, CAP uses caches to store the values of Categorical operations. To get a value out of the cache, one needs to compare the input of a basic operation with its previous input. To compare objects in the category, IsEqualForCacheForObjects is used. By default, IsEqualForCacheForObjects falls back to IsEqualForCache (see ToolsForHomalg), which in turn defaults to

recursive comparison for lists and IsIdenticalObj in all other cases. If you add a function via AddIsEqualForCacheForObjects, that function is used instead. A function $F: a, b \mapsto bool$ is expected there. The output has to be true or false. Fail is not allowed in this context.

2.7 Object constructors

2.7.1 ObjectConstructor (for IsCapCategory, IsObject)

▷ ObjectConstructor(C, a)

(operation)

Returns: an object

The arguments are a category C and an object datum a (type and semantics of the object datum depend on the category). The output is an object of C defined by a. Note that by default this CAP operation is not cached. You can change this behaviour by calling SetCachingToWeak(C, "ObjectConstructor") resp. SetCachingToCrisp(C, "ObjectConstructor").

2.7.2 / (for IsObject, IsCapCategory)

 \triangleright /(a, C) (operation)

Returns: an object

Shorthand for ObjectConstructor(C, a).

2.7.3 ObjectDatum (for IsCapCategoryObject)

 \triangleright ObjectDatum(obj)

(attribute)

Returns: depends on the category

The argument is a CAP category object obj. The output is a datum which can be used to construct obj, that is, IsEqualForObjects(obj, ObjectConstructor(CapCategory(obj), ObjectDatum(obj)). Note that by default this CAP operation is not cached. You can change this behaviour by calling SetCachingToWeak(C, "ObjectDatum") resp. SetCachingToCrisp(C, "ObjectDatum").

2.8 Well-Definedness of Objects

2.8.1 IsWellDefinedForObjects (for IsCapCategoryObject)

▷ IsWellDefinedForObjects(a)

(operation)

Returns: a boolean

The argument is an object a. The output is true if a is well-defined, otherwise the output is false.

2.9 Projectives

For a given object A in an abelian category having enough projectives, the following commands allow us to compute some projective object P together with an epimorphism $\pi: P \to A$.

2.9.1 SomeProjectiveObject (for IsCapCategoryObject)

▷ SomeProjectiveObject(A)

(attribute)

Returns: an object

The argument is an object A. The output is some projective object P for which there exists an epimorphism $\pi: P \to A$.

2.9.2 EpimorphismFromSomeProjectiveObject (for IsCapCategoryObject)

(attribute)

Returns: a morphism in Hom(P,A)

The argument is an object A. The output is an epimorphism $\pi: P \to A$ with P a projective object that equals the output of SomeProjectiveObject(A).

2.9.3 EpimorphismFromSomeProjectiveObjectWithGivenSomeProjectiveObject (for IsCapCategoryObject, IsCapCategoryObject)

 \triangleright EpimorphismFromSomeProjectiveObjectWithGivenSomeProjectiveObject(A, P) (operation)

Returns: a morphism in Hom(P,A)

The arguments are an object A and a projective object P that equals the output of SomeProjectiveObject(A). The output is an epimorphism $\pi: P \to A$.

2.9.4 ProjectiveLift (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ ProjectiveLift(pi, epsilon)

(operation)

Returns: a morphism in Hom(P, B)

The arguments are a morphism $\pi: P \to A$ with P a projective, and an epimorphism $\varepsilon: B \to A$. The output is a morphism $\lambda: P \to B$ such that $\varepsilon \circ \lambda = \pi$.

2.10 Injectives

For a given object A in an abelian category having enough injectives, the following commands allow us to compute some injective object I together with a monomorphism $t: A \to I$.

2.10.1 SomeInjectiveObject (for IsCapCategoryObject)

▷ SomeInjectiveObject(A)

(attribute)

Returns: an object

The argument is an object A. The output is some injective object I for which there exists a monomorphism $\iota: A \to I$.

2.10.2 MonomorphismIntoSomeInjectiveObject (for IsCapCategoryObject)

(attribute)

Returns: a morphism in Hom(I,A)

The argument is an object A. The output is a monomorphism $\iota : A \to I$ with I an injective object that equals the output of SomeInjectiveObject(A).

2.10.3 MonomorphismIntoSomeInjectiveObjectWithGivenSomeInjectiveObject (for IsCapCategoryObject, IsCapCategoryObject)

ightharpoonup MonomorphismIntoSomeInjectiveObjectWithGivenSomeInjectiveObject(A, I) (operation) Returns: a morphism in Hom(I,A)

The arguments are an object A and an injective object I that equals the output of SomeInjectiveObject(A). The output is a monomorphism $\iota : A \to I$.

2.10.4 InjectiveColift (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ InjectiveColift(iota, beta)

(operation)

Returns: a morphism in Hom(A, I)

The arguments are a monomorphism $\iota : B \to A$ and a morphism $\beta : B \to I$ where I is an injective object. The output is a morphism $\lambda : A \to I$ such that $\lambda \circ \iota = \beta$.

2.11 Simplified Objects

Let i be a positive integer or ∞ . For a given object A, an i-th simplified object of A consists of

- an object A_i ,
- an isomorphism $\iota_A^i:A\to A_i$.

The idea is that the greater the i, the "simpler" the A_i (but this could mean the harder the computation) with ∞ as a possible value.

2.11.1 Simplify (for IsCapCategoryObject)

▷ Simplify(A)

(attribute)

Returns: an object

The argument is an object A. The output is a simplified object A_{∞} .

2.11.2 SimplifyObject (for IsCapCategoryObject, IsObject)

▷ SimplifyObject(A, i)

(operation)

Returns: an object

The arguments are an object A and a positive integer i or infinity. The output is a simplified object A_i .

2.11.3 SimplifyObject IsoFromInputObject (for IsCapCategoryObject, IsObject)

▷ SimplifyObject_IsoFromInputObject(A, i)

(operation)

Returns: a morphism in $Hom(A, A_i)$

The arguments are an object A and a positive integer i or infinity. The output is an isomorphism to a simplified object $t_A^i: A \to A_i$.

2.11.4 SimplifyObject_IsoToInputObject (for IsCapCategoryObject, IsObject)

▷ SimplifyObject_IsoToInputObject(A, i)

(operation)

Returns: a morphism in $Hom(A_i, A)$

The arguments are an object A and a positive integer i or infinity. The output is an isomorphism from a simplified object $(\iota_A^i)^{-1}:A_i\to A$ which is the inverse of the output of SimplifyObject_IsoFromInputObject.

2.12 Dimensions

2.12.1 ProjectiveDimension (for IsCapCategoryObject)

▷ ProjectiveDimension(A)

(attribute)

Returns: a nonnegative integer or infinity

The argument is an object A. The output is a the projective dimension of A.

2.12.2 InjectiveDimension (for IsCapCategoryObject)

▷ InjectiveDimension(A)

(attribute)

Returns: a nonnegative integer or infinity

The argument is an object A. The output is a the injective dimension of A.

Chapter 3

Morphisms

Any GAP object satisfying IsCapCategoryMorphism can be added to a category and then becomes a morphism in this category. Any morphism can belong to one or no category. After a GAP object is added to the category, it knows which things can be computed in its category and to which category it belongs. It knows categorical properties and attributes, and the functions for existential quantifiers can be applied to the morphism.

3.1 Attributes for the Type of Morphisms

3.1.1 CapCategory (for IsCapCategoryMorphism)

▷ CapCategory(alpha)
Returns: a category

The argument is a morphism α . The output is the category \mathbf{C} to which α was added.

(attribute)

3.1.2 Source (for IsCapCategoryMorphism)

Source(alpha) (attribute)

Returns: an object

The argument is a morphism $\alpha : a \to b$. The output is its source a.

3.1.3 Range (for IsCapCategoryMorphism)

▶ Range(alpha) (attribute)

Returns: an object

The argument is a morphism $\alpha : a \to b$. The output is its range b.

3.1.4 Target (for IsCapCategoryMorphism)

Returns: an object

The argument is a morphism $\alpha : a \to b$. The output is its target b.

3.2 Adding Morphisms to a Category

3.2.1 Add (for IsCapCategory, IsCapCategoryMorphism)

```
▷ Add(category, morphism)
```

(operation)

Adds morphism as a morphism to category.

3.2.2 AddMorphism (for IsCapCategory, IsAttributeStoringRep)

```
▷ AddMorphism(category, morphism)
```

(operation)

Adds morphism as a morphism to category. If morphism already lies in the filter IsCapCategoryMorphism, the operation Add (3.2.1) can be used instead.

3.2.3 CreateCapCategoryMorphismWithAttributes

```
\verb| > CreateCapCategoryMorphismWithAttributes(category, source, range[, attr1, val1, attr2, val2, ...]) \\ \\ (function)
```

Returns: a morphism

Creates a morphism in category with the given attributes.

3.2.4 AsCapCategoryMorphism

```
\qquad \qquad \triangleright \  \, \text{AsCapCategoryMorphism}(\textit{category}, \ \textit{source}, \ \textit{value}, \ \textit{range}) \qquad \qquad (\text{function})
```

Returns: a morphism

EXPERIMENTAL: This specification might change any time without prior notice. Views value as a morphism from source to range in category.

3.2.5 AsPrimitiveValue (for IsCapCategoryMorphism)

```
▷ AsPrimitiveValue(morphism)

▷ AsInteger(morphism)

▷ AsHomalgMatrix(morphism)

(attribute)

(attribute)
```

Returns: a value

EXPERIMENTAL: This specification might change any time without prior notice. Views a morphism obtained via AsCapCategoryMorphism (3.2.4) as a primitive value again. Here, the word primitive means primitive from the perspective of the category. For example, from the perspective of an opposite category, morphisms of the underlying category are primitive values. The attribute is chosen according to the morphism datum type:

- For IsInt, the attribute AsInteger is used.
- For IsHomalgMatrix, the attribute AsHomalgMatrix is used.

In all other cases or if no morphism datum type is given, the attribute AsPrimitiveValue is used.

3.3 Morphism constructors

3.3.1 MorphismConstructor (for IsCapCategoryObject, IsObject, IsCapCategoryObject)

 \triangleright MorphismConstructor(S, a, T)

(operation)

Returns: a morphism in Hom(S, T)

The arguments are two objects S and T in a category, and a morphism datum a (type and semantics of the morphism datum depend on the category). The output is a morphism in $\mathrm{Hom}(S,T)$ defined by a. Note that by default this CAP operation is not cached. You can change this behaviour by calling SetCachingToWeak(C, "MorphismConstructor") resp. SetCachingToCrisp(C, "MorphismConstructor").

3.3.2 MorphismDatum (for IsCapCategoryMorphism)

▷ MorphismDatum(mor)

(attribute)

Returns: depends on the category

The argument is a CAP category morphism mor. The output is a datum which can be used to construct mor, that is, IsEqualForMorphisms(mor, MorphismConstructor(Source(mor), MorphismDatum(mor), Range(mor)). Note that by default this CAP operation is not cached. You can change this behaviour by calling SetCachingToWeak(C, "MorphismDatum") resp. SetCachingToCrisp(C, "MorphismDatum").

3.4 Categorical Properties of Morphisms

3.4.1 IsMonomorphism (for IsCapCategoryMorphism)

▷ IsMonomorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is a monomorphism, otherwise the output is false.

3.4.2 IsEpimorphism (for IsCapCategoryMorphism)

▷ IsEpimorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is an epimorphism, otherwise the output is false.

3.4.3 IsIsomorphism (for IsCapCategoryMorphism)

▷ IsIsomorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is an isomorphism, otherwise the output is false.

3.4.4 IsSplitMonomorphism (for IsCapCategoryMorphism)

▷ IsSplitMonomorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is a split monomorphism, otherwise the output is false.

3.4.5 IsSplitEpimorphism (for IsCapCategoryMorphism)

▷ IsSplitEpimorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is a split epimorphism, otherwise the output is false.

3.4.6 IsOne (for IsCapCategoryMorphism)

▷ IsOne(alpha)

(property)

Returns: a boolean

The argument is a morphism $\alpha : a \to a$. The output is true if α is congruent to the identity of a, otherwise the output is false.

3.4.7 IsIdempotent (for IsCapCategoryMorphism)

▷ IsIdempotent(alpha)

(property)

Returns: a boolean

The argument is a morphism $\alpha: a \to a$. The output is true if $\alpha^2 \sim_{a,a} \alpha$, otherwise the output is false.

3.5 Random Morphisms

CAP provides two principal methods to generate random morphisms with or without fixed source and range:

- By integers: The integer is simply a parameter that can be used to create a random morphism.
- By lists: The list is used when creating a random morphism would need more than one parameter. Lists offer more flexibility at the expense of the genericity of the methods. This happens because lists that are valid as input in some category may be not valid for other categories. Hence, these operations are not thought to be used in generic categorical algorithms.

3.5.1 RandomMorphismWithFixedSourceByInteger (for IsCapCategoryObject, IsInt)

▷ RandomMorphismWithFixedSourceByInteger(a, n)

(operation)

Returns: a morphism in Hom(a, b)

The arguments are an object a in a category C and an integer n. The output is a random morphism $\alpha: a \to b$ for some object b in C. If C is equipped with the methods RandomObjectByInteger and RandomMorphismWithFixedSourceAndRangeByInteger and C is

an Ab-category, then RandomMorphismWithFixedSourceByInteger(C,a,n) can be derived as RandomMorphismWithFixedSourceAndRangeByInteger(C,a,b,1+Log2Int(n)) where b is computed via RandomObjectByInteger(C,n).

3.5.2 RandomMorphismWithFixedSourceByList (for IsCapCategoryObject, IsList)

▷ RandomMorphismWithFixedSourceByList(a, L)

(operation)

Returns: a morphism in Hom(a,b)

The arguments are an object a in a category C and a list L. The output is a random morphism $\alpha:a\to b$ for some object b in C. If C is equipped with the methods RandomObjectByList and RandomMorphismWithFixedSourceAndRangeByList and C is an Ab-category, then RandomMorphismWithFixedSourceByList(C,a,L) can be derived as RandomMorphismWithFixedSourceAndRangeByList(C,a,b,L[2]) where b is computed via RandomObjectByList(C,L[1]).

3.5.3 RandomMorphismWithFixedRangeByInteger (for IsCapCategoryObject, IsInt)

(operation)

Returns: a morphism in Hom(a,b)

The arguments are an object b in a category C and an integer n. The output is a random morphism $\alpha: a \to b$ for some object a in C. If C is equipped with the methods RandomObjectByInteger and RandomMorphismWithFixedSourceAndRangeByInteger and C is an Ab-category, then RandomMorphismWithFixedRangeByInteger(C,b,n) can be derived as RandomMorphismWithFixedSourceAndRangeByInteger(C,a,b,1+Log2Int(n)) where a is computed via RandomObjectByInteger(C,n).

3.5.4 RandomMorphismWithFixedRangeByList (for IsCapCategoryObject, IsList)

▷ RandomMorphismWithFixedRangeByList(b, L)

(operation)

Returns: a morphism in Hom(a,b)

The arguments are an object b in a category C and a list L. The output is a random morphism $\alpha: a \to b$ for some object a in C. If C is equipped with the methods RandomObjectByList and RandomMorphismWithFixedSourceAndRangeByList and C is an Ab-category, then RandomMorphismWithFixedRangeByList(C,b,L) can be derived as RandomMorphismWithFixedSourceAndRangeByList(C,a,b,L[2]) where a is computed via RandomObjectByList(C,L[1]).

3.5.5 RandomMorphismWithFixedSourceAndRangeByInteger (for IsCapCategory-Object, IsCapCategoryObject, IsInt)

▷ RandomMorphismWithFixedSourceAndRangeByInteger(a, b, n)

(operation)

Returns: a morphism in Hom(a,b)

The arguments are two objects a and b in a category C and an integer n. The output is a random morphism $\alpha: a \to b$ in C.

3.5.6 RandomMorphismWithFixedSourceAndRangeByList (for IsCapCategoryObject, IsCapCategoryObject, IsList)

▷ RandomMorphismWithFixedSourceAndRangeByList(a, b, L)

(operation)

Returns: a morphism in Hom(a,b)

This operation is not a CAP basic operation The arguments are two objects a and b in a category C and a list L. The output is a random morphism $\alpha : a \to b$ in C.

3.5.7 RandomMorphismByInteger (for IsCapCategory, IsInt)

▷ RandomMorphismByInteger(C, n)

(operation)

Returns: a morphism in *C*

The arguments are a category C and an integer n. The output is a random morphism in C. The operation can be derived in three different ways:

- If Cis methods RandomObjectByInteger equipped with the and ${\tt RandomMorphismWithFixedSourceAndRangeByInteger}$ and \boldsymbol{C} is Ab-category, then RandomMorphism(C, n)can be derived as RandomMorphismWithFixedSourceAndRangeByInteger(C, a, b, 1 + Log2Int(n)) where a and b are computed via RandomObjectByInteger(C, n).
- If C is equipped with the methods RandomObjectByInteger and RandomMorphismWithFixedSourceByInteger, then RandomMorphism(C,n) can be derived as RandomMorphismWithFixedSourceByInteger(C,a,1+Log2Int(n)) where a is computed via RandomObjectByInteger(C,n).
- If C is equipped with the methods RandomObjectByInteger and RandomMorphismWithFixedRangeByInteger, then RandomMorphism(C,n) can be derived as RandomMorphismWithFixedRangeByInteger(C,b,1+Log2Int(n)) where b is computed via RandomObjectByInteger(C,n).

3.5.8 RandomMorphismByList (for IsCapCategory, IsList)

⊳ RandomMorphismByList(C, L)

(operation)

Returns: a morphism in *C*

The arguments are a category C and a list L. The output is a random morphism in C. The operation can be derived in three different ways:

- If Cis equipped with the methods RandomObjectByList and ${\tt RandomMorphismWithFixedSourceAndRangeByList}$ and \boldsymbol{C} is an RandomMorphism(C, L)Ab-category, then can be derived as RandomMorphismWithFixedSourceAndRangeByList(C, a, b, L[3])) where a and b are computed via RandomObjectByList(C, L[i]) for i = 1, 2 respectively.
- If C is equipped with the methods RandomObjectByList and RandomMorphismWithFixedSourceByList, then RandomMorphism(C,L) can be derived as RandomMorphismWithFixedSourceByList(C,a,L[2]) where a is computed via RandomObjectByList(C,L[1]).

• If C is equipped with the methods RandomObjectByList and RandomMorphismWithFixedRangeByList, then RandomMorphism(C,L) can be derived as RandomMorphismWithFixedRangeByList(C,b,L[2]) where b is computed via RandomObjectByList(C,L[1]).

3.5.9 RandomMorphismWithFixedSource (for IsCapCategoryObject, IsInt)

▷ RandomMorphismWithFixedSource(a, n)	(operation)
▷ RandomMorphismWithFixedSource(a, L)	(operation)
▷ RandomMorphismWithFixedRange(b, n)	(operation)
▷ RandomMorphismWithFixedRange(b, L)	(operation)
▷ RandomMorphismWithFixedSourceAndRange(a, b, n)	(operation)
▷ RandomMorphismWithFixedSourceAndRange(a, b, L)	(operation)
<pre> RandomMorphism(a, b, n) </pre>	(operation)
<pre> RandomMorphism(a, b, L) </pre>	(operation)
<pre> RandomMorphism(C, n)</pre>	(operation)
⊳ RandomMorphism(C, L)	(operation)

These are convenient methods and they, depending on the input, delegate to one of the above methods.

3.6 Non-Categorical Properties of Morphisms

Non-categorical properties are not stable under equivalences of categories.

3.6.1 IsEqualToIdentityMorphism (for IsCapCategoryMorphism)

▷ IsEqualToIdentityMorphism(alpha)

Returns: a boolean

The argument is a morphism $\alpha: a \to b$. The output is true if $\alpha = \mathrm{id}_a$, otherwise the output is false.

3.6.2 IsEqualToZeroMorphism (for IsCapCategoryMorphism)

▷ IsEqualToZeroMorphism(alpha)

(property)

(property)

Returns: a boolean

The argument is a morphism $\alpha:a\to b$. The output is true if $\alpha=0$, otherwise the output is false.

3.6.3 IsEndomorphism (for IsCapCategoryMorphism)

▷ IsEndomorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is an endomorphism, otherwise the output is false.

3.6.4 IsAutomorphism (for IsCapCategoryMorphism)

▷ IsAutomorphism(alpha)

(property)

Returns: a boolean

The argument is a morphism α . The output is true if α is an automorphism, otherwise the output is false.

3.7 Equality and Congruence for Morphisms

3.7.1 IsCongruentForMorphisms (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsCongruentForMorphisms(alpha, beta)

(operation)

Returns: a boolean

The arguments are two morphisms $\alpha, \beta : a \to b$. The output is true if $\alpha \sim_{a,b} \beta$, otherwise the output is false.

3.7.2 IsEqualForMorphisms (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsEqualForMorphisms(alpha, beta)

(operation)

Returns: a boolean

The arguments are two morphisms $\alpha, \beta : a \to b$. The output is true if $\alpha = \beta$, otherwise the output is false.

3.7.3 IsEqualForMorphismsOnMor (for IsCapCategoryMorphism, IsCapCategory-Morphism)

▷ IsEqualForMorphismsOnMor(alpha, beta)

(operation)

Returns: a boolean

The arguments are two morphisms $\alpha: a \to b, \beta: c \to d$. The output is true if $\alpha = \beta$, otherwise the output is false.

3.8 Basic Operations for Morphisms in Ab-Categories

3.8.1 IsZeroForMorphisms (for IsCapCategoryMorphism)

▷ IsZeroForMorphisms(alpha)

(property)

Returns: a boolean

The argument is a morphism $\alpha: a \to b$. The output is true if $\alpha \sim_{a,b} 0$, otherwise the output is false.

${\bf 3.8.2} \quad Addition For Morphisms \quad (for \quad Is Cap Category Morphism, \quad Is Cap Category Morphism)$

ightharpoonup AdditionForMorphisms(alpha, beta)

(operation)

Returns: a morphism in Hom(a, b)

The arguments are two morphisms $\alpha, \beta : a \to b$. The output is the addition $\alpha + \beta$. Note: The addition has to be compatible with the congruence of morphisms.

3.8.3 SubtractionForMorphisms (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ SubtractionForMorphisms(alpha, beta)

(operation)

Returns: a morphism in Hom(a,b)

The arguments are two morphisms $\alpha, \beta : a \to b$. The output is the addition $\alpha - \beta$. Note: The addition has to be compatible with the congruence of morphisms.

3.8.4 AdditiveInverseForMorphisms (for IsCapCategoryMorphism)

▷ AdditiveInverseForMorphisms(alpha)

(attribute)

Returns: a morphism in Hom(a,b)

The argument is a morphism $\alpha : a \to b$. The output is its additive inverse $-\alpha$. Note: The addition has to be compatible with the congruence of morphisms.

3.8.5 MultiplyWithElementOfCommutativeRingForMorphisms (for IsRingElement, IsCapCategoryMorphism)

▷ MultiplyWithElementOfCommutativeRingForMorphisms(r, alpha)

(operation)

Returns: a morphism in Hom(a, b)

The arguments are an element r of a commutative ring and a morphism $\alpha: a \to b$. The output is the multiplication with the ring element $r \cdot \alpha$. Note: The multiplication has to be compatible with the congruence of morphisms.

3.8.6 * (for IsRingElement, IsCapCategoryMorphism)

ho *(r, alpha) **Returns:** a morphism in Hom(a,b)

(operation)

This is a convenience method. It has two arguments. The first argument is either a rational number q or an element r of a commutative ring R. The second argument is a morphism $\alpha: a \to b$ in a linear category over the commutative ring R. In the case where the first element is a rational number, this method tries to interpret q as an element r of R via $R!.interpret_rationals_func$. If no such interpretation exists, this method throws an error. The output is the multiplication with the ring element $r \cdot \alpha$.

3.8.7 ZeroMorphism (for IsCapCategoryObject, IsCapCategoryObject)

 \triangleright ZeroMorphism(a, b)

(operation)

Returns: a morphism in Hom(a, b)

The arguments are two objects a and b. The output is the zero morphism $0: a \to b$.

3.9 Subobject and Factorobject Operations

Subobjects of an object c are monomorphisms with range c and a special function for comparision. Similarly, factorobjects of an object c are epimorphisms with source c and a special function for comparision.

3.9.1 IsEqualAsSubobjects (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsEqualAsSubobjects(alpha, beta)

(operation)

Returns: a boolean

The arguments are two subobjects $\alpha: a \to c$, $\beta: b \to c$. The output is true if there exists an isomorphism $\iota: a \to b$ such that $\beta \circ \iota \sim_{a,c} \alpha$, otherwise the output is false.

3.9.2 IsEqualAsFactorobjects (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsEqualAsFactorobjects(alpha, beta)

(operation)

Returns: a boolean

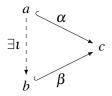
The arguments are two factorobjects $\alpha: c \to a$, $\beta: c \to b$. The output is true if there exists an isomorphism $\iota: b \to a$ such that $\iota \circ \beta \sim_{c,a} \alpha$, otherwise the output is false.

3.9.3 IsDominating (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsDominating(alpha, beta)

(operation)

Returns: a boolean



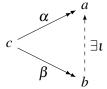
In short: Returns true iff α is smaller than β . Full description: The arguments are two subobjects $\alpha: a \to c$, $\beta: b \to c$. The output is true if there exists a morphism $\iota: a \to b$ such that $\beta \circ \iota \sim_{a,c} \alpha$, otherwise the output is false.

3.9.4 IsCodominating (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsCodominating(alpha, beta)

(operation)

Returns: a boolean



In short: Returns true iff α is smaller than β . Full description: The arguments are two factorobjects $\alpha: c \to a$, $\beta: c \to b$. The output is true if there exists a morphism $\iota: b \to a$ such that $\iota \circ \beta \sim_{c,a} \alpha$, otherwise the output is false.

3.10 Identity Morphism and Composition of Morphisms

3.10.1 IdentityMorphism (for IsCapCategoryObject)

▷ IdentityMorphism(a)

(attribute)

Returns: a morphism in Hom(a, a)

The argument is an object a. The output is its identity morphism id_a .

3.10.2 PreCompose (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ PreCompose(alpha, beta)

(operation)

Returns: a morphism in Hom(a, c)

The arguments are two morphisms $\alpha: a \to b$, $\beta: b \to c$. The output is the composition $\beta \circ \alpha: a \to c$.

3.10.3 PreCompose (for IsList)

▷ PreCompose(L)

(operation)

Returns: a morphism in $Hom(a_1, a_{n+1})$

This is a convenience method. The argument is a list of morphisms $L = (\alpha_1 : a_1 \to a_2, \alpha_2 : a_2 \to a_3, \dots, \alpha_n : a_n \to a_{n+1})$. The output is the composition $\alpha_n \circ (\alpha_{n-1} \circ (\dots (\alpha_2 \circ \alpha_1)))$.

3.10.4 PreComposeList (for IsCapCategoryObject, IsList, IsCapCategoryObject)

▷ PreComposeList(s, L, r)

(operation)

Returns: a morphism in Hom(s, r)

The arguments are two objects $s = a_1$, $r = a_{n+1}$, and a list of morphisms $L = (\alpha_1 : a_1 \to a_2, \alpha_2 : a_2 \to a_3, \dots, \alpha_n : a_n \to a_{n+1})$ in C. The output is the composition $\alpha_n \circ (\alpha_{n-1} \circ (\dots (\alpha_2 \circ \alpha_1)))$. If L is empty, then s must be equal to r and the output is congruent to the identity morphism of s.

3.10.5 PostCompose (for IsCapCategoryMorphism, IsCapCategoryMorphism)

 \triangleright PostCompose(beta, alpha)

(operation)

Returns: a morphism in Hom(a, c)

The arguments are two morphisms $\beta: b \to c, \ \alpha: a \to b$. The output is the composition $\beta \circ \alpha: a \to c$.

3.10.6 PostCompose (for IsList)

▷ PostCompose(L)

(operation)

Returns: a morphism in $Hom(a_1, a_{n+1})$

This is a convenience method. The argument is a list of morphisms $L = (\alpha_n : a_n \to a_{n+1}, \alpha_{n-1} : a_{n-1} \to a_n, \dots, \alpha_1 : a_1 \to a_2)$. The output is the composition $((\alpha_n \circ \alpha_{n-1}) \circ \dots \circ \alpha_2) \circ \alpha_1$.

3.10.7 PostComposeList (for IsCapCategoryObject, IsList, IsCapCategoryObject)

 \triangleright PostComposeList(s, L, r)

(operation)

Returns: a morphism in Hom(s, r)

The arguments are two objects $s = a_1$, $r = a_{n+1}$, and a list of morphisms $L = (\alpha_n : a_n \to a_{n+1}, \alpha_{n-1} : a_{n-1} \to a_n, \dots, \alpha_1 : a_1 \to a_2)$. The output is the composition $((\alpha_n \circ \alpha_{n-1}) \circ \dots \circ \alpha_2) \circ \alpha_1$. If L is empty, then s must be equal to r and the output is congruent to the identity morphism of s.

3.10.8 SumOfMorphisms (for IsCapCategoryObject, IsList, IsCapCategoryObject)

 \triangleright SumOfMorphisms(s, morphisms, r)

(operation)

Returns: a morphism in Hom(s, r)

The arguments are two objects s, r and a list morphisms of morphisms from s to r. The output is the sum of all elements in morphisms, or the zero-morphism from s to r if morphisms is empty.

3.10.9 LinearCombinationOfMorphisms (for IsCapCategoryObject, IsList, IsList, IsCapCategoryObject)

▷ LinearCombinationOfMorphisms(s, coeffs, mors, r)

(operation)

Returns: a morphism in Hom(s, r)

The arguments are two objects s, r in some linear category over a ring R, a list coeffs of ring elements in R and a list mors of morphisms from s to r. The output is the linear combination of the morphisms in mors with respect to the coefficients list coeffs, or the zero morphism from s to r if coeffs and mors are the empty lists.

3.11 Well-Definedness of Morphisms

3.11.1 IsWellDefinedForMorphisms (for IsCapCategoryMorphism)

▷ IsWellDefinedForMorphisms(alpha)

(operation)

Returns: a boolean

The argument is a morphism α . The output is true if α is well-defined, otherwise the output is false.

3.11.2 IsWellDefinedForMorphismsWithGivenSourceAndRange (for IsCapCategory-Object, IsCapCategoryMorphism, IsCapCategoryObject)

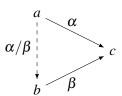
▷ IsWellDefinedForMorphismsWithGivenSourceAndRange(source, alpha, range) (operation)

Returns: a boolean

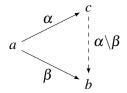
The arguments are two well-defined objects S and T and a morphism α . The output is true if α is a well-defined morphism from S to T, otherwise the output is false.

3.12 Lift/Colift

• For any pair of morphisms $\alpha: a \to c$, $\beta: b \to c$, we call each morphism $\alpha/\beta: a \to b$ such that $\beta \circ (\alpha/\beta) \sim_{a,c} \alpha$ a *lift of* α *along* β .



• For any pair of morphisms $\alpha : a \to c$, $\beta : a \to b$, we call each morphism $\alpha \setminus \beta : c \to b$ such that $(\alpha \setminus \beta) \circ \alpha \sim_{a,b} \beta$ a *colift of* β *along* α .



Note that such lifts (or colifts) do not have to be unique. So in general, we do not expect that algorithms computing lifts (or colifts) do this in a functorial way. Thus the operations Lift and Colift are not regarded as categorical operations, but only as set-theoretic operations.

3.12.1 LiftAlongMonomorphism (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ LiftAlongMonomorphism(iota, tau)

(operation)

Returns: a morphism in Hom(t, k)

The arguments are a monomorphism $t: k \hookrightarrow a$ and a morphism $\tau: t \to a$ such that there is a morphism $u: t \to k$ with $t \circ u \sim_{t,a} \tau$. The output is such a u.

3.12.2 ColiftAlongEpimorphism (for IsCapCategoryMorphism, IsCapCategoryMorphism)

 ${\scriptstyle \rhd\ Colift Along Epimorphism (\it epsilon,\ tau)}$

(operation)

Returns: a morphism in Hom(c,t)

The arguments are an epimorphism $\varepsilon: a \to c$ and a morphism $\tau: a \to t$ such that there is a morphism $u: c \to t$ with $u \circ \varepsilon \sim_{a,t} \tau$. The output is such a u.

${\bf 3.12.3} \quad Is Liftable Along Monomorphism \ (for \ Is Cap Category Morphism, \ Is Cap Category Morphism)$

 ${\tt \triangleright} \ \, {\tt IsLiftableAlongMonomorphism}(iota,\ tau)\\$

(operation)

Returns: a boolean

The arguments are a monomorphism $t: k \hookrightarrow a$ and a morphism $\tau: t \to a$. The output is true if there exists a morphism $u: t \to k$ with $t \circ u \sim_{t,a} \tau$. Otherwise, the output is false.

3.12.4 IsColiftableAlongEpimorphism (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsColiftableAlongEpimorphism(epsilon, tau)

(operation)

Returns: a boolean

The arguments are an epimorphism $\varepsilon: a \to c$ and a morphism $\tau: a \to t$. The output is true if there exists a morphism $u: c \to t$ with $u \circ \varepsilon \sim_{a,t} \tau$. Otherwise, the output is false.

3.12.5 Lift (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ Lift(alpha, beta)

(operation)

Returns: a morphism in Hom(a, b)

The arguments are two morphisms $\alpha: a \to c$, $\beta: b \to c$ such that a lift $\alpha/\beta: a \to b$ of α along β exists. The output is such a lift $\alpha/\beta: a \to b$. Recall that a lift $\alpha/\beta: a \to b$ of α along β is a morphism such that $\beta \circ (\alpha/\beta) \sim_{a,c} \alpha$.

3.12.6 LiftOrFail (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ LiftOrFail(alpha, beta)

(operation)

Returns: a morphism in $Hom(a,b) + \{fail\}$

This is a convenience operation. The arguments are two morphisms $\alpha: a \to c$, $\beta: b \to c$. The output is a lift $\alpha/\beta: a \to b$ of α along β if such a lift exists or fail if it doesn't. Recall that a lift $\alpha/\beta: a \to b$ of α along β is a morphism such that $\beta \circ (\alpha/\beta) \sim_{a,c} \alpha$.

3.12.7 IsLiftable (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsLiftable(alpha, beta)

(operation)

Returns: a boolean

The arguments are two morphisms $\alpha: a \to c$, $\beta: b \to c$. The output is true if there exists a lift $\alpha/\beta: a \to b$ of α along β , i.e., a morphism such that $\beta \circ (\alpha/\beta) \sim_{a,c} \alpha$. Otherwise, the output is false.

3.12.8 Colift (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ Colift(alpha, beta)

(operation)

Returns: a morphism in Hom(c,b)

The arguments are two morphisms $\alpha: a \to c$, $\beta: a \to b$ such that a colift $\alpha \setminus \beta: c \to b$ of β along α exists. The output is such a colift $\alpha \setminus \beta: c \to b$. Recall that a colift $\alpha \setminus \beta: c \to b$ of β along α is a morphism such that $(\alpha \setminus \beta) \circ \alpha \sim_{a,b} \beta$.

3.12.9 ColiftOrFail (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ ColiftOrFail(alpha, beta)

(operation)

Returns: a morphism in $Hom(c,b) + \{fail\}$

This is a convenience operation. The arguments are two morphisms $\alpha: a \to c$, $\beta: a \to b$. The output is a colift $\alpha \setminus \beta: c \to b$ of β along α if such a colift exists or fail if it doesn't. Recall that a colift $\alpha \setminus \beta: c \to b$ of β along α is a morphism such that $(\alpha \setminus \beta) \circ \alpha \sim_{a,b} \beta$.

3.12.10 IsColiftable (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsColiftable(alpha, beta)

(operation)

Returns: a boolean

The arguments are two morphisms $\alpha: a \to c$, $\beta: a \to b$. The output is true if there exists a colift $\alpha \setminus \beta: c \to b$ of β along α ., i.e., a morphism such that $(\alpha \setminus \beta) \circ \alpha \sim_{a,b} \beta$. Otherwise, the output is false.

3.13 Inverses

Let $\alpha: a \to b$ be a morphism. An inverse of α is a morphism $\alpha^{-1}: b \to a$ such that $\alpha \circ \alpha^{-1} \sim_{b,b} \mathrm{id}_b$ and $\alpha^{-1} \circ \alpha \sim_{a,a} \mathrm{id}_a$.

$$id_a \underbrace{a \xrightarrow{\alpha} b}_{\alpha^{-1}} b id_b$$

3.13.1 InverseForMorphisms (for IsCapCategoryMorphism)

▷ InverseForMorphisms(alpha)

(operation)

Returns: a morphism in Hom(b, a)

The argument is an isomorphism $\alpha: a \to b$. The output is its inverse $\alpha^{-1}: b \to a$.

3.13.2 PreInverseForMorphisms (for IsCapCategoryMorphism)

 \triangleright PreInverseForMorphisms(alpha)

(operation)

Returns: a morphism in Hom(b, a)

The argument is a split-epimorphism $\alpha: a \to b$. The output is a pre-inverse $\iota: b \to a$ of α , i.e., ι satisfies $\alpha \circ \iota \sim_{b,b} \mathrm{id}_b$. The morphism ι is also known as a section or a right-inverse of α .

3.13.3 PostInverseForMorphisms (for IsCapCategoryMorphism)

▷ PostInverseForMorphisms(alpha)

(operation)

Returns: a morphism in Hom(b, a)

The argument is a split-monomorphism $\alpha: a \to b$. The output is a post-inverse $\pi: b \to a$ of α , i.e., π satisfies $\pi \circ \alpha \sim_{a,a} \mathrm{id}_a$. The morphism π is also known as a contraction or a left-inverse of α .

3.14 Tool functions for caches

3.14.1 IsEqualForCacheForMorphisms (for IsCapCategoryMorphism, IsCapCategoryMorphism)

 \triangleright IsEqualForCacheForMorphisms(phi, psi)

(operation)

Returns: true or false

By default, CAP uses caches to store the values of Categorical operations. To get a value out of the cache, one needs to compare the input of a basic operation with its previous input. To compare morphisms in the category, IsEqualForCacheForMorphisms is used. By default, IsEqualForCacheForMorphisms falls back to IsEqualForCache (see ToolsForHomalg), which in turn defaults to recursive comparison for lists and IsIdenticalObj in all other cases. If you add a function via AddIsEqualForCacheForMorphisms, that function is used instead. A function $F: a, b \mapsto bool$ is expected there. The output has to be true or false. Fail is not allowed in this context.

3.15 IsHomSetInhabited

3.15.1 IsHomSetInhabited (for IsCapCategoryObject, IsCapCategoryObject)

▷ IsHomSetInhabited(A, B)

(operation)

Returns: a boolean

The arguments are two objects A and B. The output is true if there exists a morphism from A to B, otherwise the output is false.

3.16 Homomorphism structures

Homomorphism structures are way to "oversee" the homomorphisms between two given objects. Let C, D be categories. A D-homomorphism structure for C consists of the following data:

- a functor $H: C^{op} \times C \to D$ (when C and D are Ab-categories, H is assumed to be bilinear).
- an object $1 \in D$, called the distinguished object,
- a bijection $v : \operatorname{Hom}_{C}(a,b) \simeq \operatorname{Hom}_{D}(1,H(a,b))$ natural in $a,b \in C$.

3.16.1 HomomorphismStructureOnObjects (for IsCapCategoryObject, IsCapCategoryObject)

⊳ HomomorphismStructureOnObjects(a, b)

(operation)

Returns: an object in D

The arguments are two objects a,b in C. The output is the value of the homomorphism structure on objects H(a,b).

3.16.2 HomomorphismStructureOnMorphisms (for IsCapCategoryMorphism, Is-CapCategoryMorphism)

 ${\tt > HomomorphismStructureOnMorphisms(alpha, beta)}\\$

(operation)

Returns: a morphism in $\text{Hom}_D(H(a',b),H(a,b'))$

The arguments are two morphisms $\alpha: a \to a', \beta: b \to b'$ in C. The output is the value of the homomorphism structure on morphisms $H(\alpha, \beta)$.

3.16.3 HomomorphismStructureOnMorphismsWithGivenObjects (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

 $\verb| HomomorphismStructureOnMorphismsWithGivenObjects(s, alpha, beta, r) | (operation) \\ \textbf{Returns:} \ a \ morphism \ in \ Hom_D(H(a',b),H(a,b')) \\ | (operation) | (oper$

The arguments are an object s = H(a',b) in D, two morphisms $\alpha : a \to a', \beta : b \to b'$ in C, and an object r = H(a,b') in D. The output is the value of the homomorphism structure on morphisms $H(\alpha,\beta)$.

3.16.4 DistinguishedObjectOfHomomorphismStructure (for IsCapCategory)

 ${\tt \triangleright \ DistinguishedObjectOfHomomorphismStructure(\it C)}\\$

(attribute)

Returns: an object in D

The argument is a category C. The output is the distinguished object 1 in D of the homomorphism structure.

3.16.5 InterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructure (for IsCapCategoryMorphism)

 ${\tt \triangleright} \ \, InterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructure(alpha)}$

(attribute)

Returns: a morphism in $\text{Hom}_D(1, H(a, a'))$

The argument is a morphism $\alpha: a \to a'$ in C. The output is the corresponding morphism $v(\alpha): 1 \to H(a,a')$ in D of the homomorphism structure.

3.16.6 InterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructureWithC (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

 ${\tt \triangleright InterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructureWithGivenObjects(alpha, r)} \\ (operation)$

Returns: a morphism in $Hom_D(1,r)$

The arguments are the distinguished object 1, a morphism $\alpha : a \to a'$, and the object r = H(a, a'). The output is the corresponding morphism $v(\alpha) : 1 \to r$ in D of the homomorphism structure.

3.16.7 InterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism (for IsCapCategoryObject, IsCapCategoryObject, IsCapCategoryMorphism)

▷ InterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism(a, a', iota) (operation)

Returns: a morphism in $\text{Hom}_C(a, a')$

The arguments are objects a, a' in C and a morphism $\iota : 1 \to H(a, a')$ in D. The output is the corresponding morphism $v^{-1}(\iota) : a \to a'$ in C of the homomorphism structure.

3.16.8 SolveLinearSystemInAbCategory (for IsList, IsList, IsList)

▷ SolveLinearSystemInAbCategory(alpha, beta, gamma)

(operation)

Returns: a list of morphisms $[X_1, ..., X_n]$

The arguments are three lists α , β , and γ . The first list α (the left coefficients) is a list of list of morphisms $\alpha_{ij}: A_i \to B_j$, where $i=1\dots m$ and $j=1\dots n$ for integers $m,n\geq 1$. The second list β (the right coefficients) is a list of list of morphisms $\beta_{ij}: C_j \to D_i$, where $i=1\dots m$ and $j=1\dots n$. The third list γ (the right side) is a list of morphisms $\gamma_i: A_i \to D_i$, where $i=1,\dots,m$. Assumes that a solution to the linear system defined by α , β , γ exists, i.e., there exist morphisms $X_j: B_j \to C_j$ for $j=1\dots n$ such that $\sum_{j=1}^n \alpha_{ij} \cdot X_j \cdot \beta_{ij} = \gamma_i$ for all $i=1\dots m$. The output is list of such morphisms $X_j: B_j \to C_j$ for $j=1\dots n$.

3.16.9 SolveLinearSystemInAbCategoryOrFail (for IsList, IsList, IsList)

▷ SolveLinearSystemInAbCategoryOrFail(alpha, beta, gamma)

(operation)

Returns: a list of morphisms $[X_1, ..., X_n]$ or fail

This is a convenience operation. Like SolveLinearSystemInAbCategory, but without the assumption that a solution exists. If no solution exists, fail is returned.

3.16.10 MereExistenceOfSolutionOfLinearSystemInAbCategory (for IsList, IsList, IsList)

▷ MereExistenceOfSolutionOfLinearSystemInAbCategory(alpha, beta, gamma) (operation)
Returns: a boolean

Like SolveLinearSystemInAbCategory, but the output is simply true if a solution exists, false otherwise.

3.16.11 HomStructure (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ HomStructure(alpha, beta)

(operation)

Returns: a morphism in $\text{Hom}_D(H(a',b),H(a,b'))$

This is a convenience method. The arguments are two morphisms $\alpha: a \to a', \beta: b \to b'$ in C. The output is HomomorphismStructureOnMorphisms called on α , β .

3.16.12 HomStructure (for IsCapCategoryMorphism, IsCapCategoryObject)

▷ HomStructure(alpha, b)

(operation)

Returns: a morphism in $\text{Hom}_D(H(a',b),H(a,b))$

This is a convenience method. The arguments are a morphism $\alpha: a \to a'$ and an object b in C. The output is HomomorphismStructureOnMorphisms called on α , id_b .

3.16.13 HomStructure (for IsCapCategoryObject, IsCapCategoryMorphism)

▷ HomStructure(a, beta)

(operation)

Returns: a morphism in $\text{Hom}_D(H(a,b),H(a,b'))$

This is a convenience method. The arguments are an object a and a morphism $\beta: b \to b'$ in C. The output is HomomorphismStructureOnMorphisms called on id_a , β .

3.16.14 HomStructure (for IsCapCategoryObject, IsCapCategoryObject)

▷ HomStructure(a, b)

(operation)

Returns: an object

This is a convenience method. The arguments are two objects a and b in C. The output is HomomorphismStructureOnObjects called on a,b.

3.16.15 HomStructure (for IsCapCategoryMorphism)

(operation)

This is a convenience method for InterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphism

3.16.16 HomStructure (for IsCapCategoryObject, IsCapCategoryObject, IsCapCategoryMorphism)

⊳ HomStructure(arg1, arg2, arg3)

(operation)

 $This is a convenience method for {\tt InterpretMorphismFromDistinguishedObjectToHomomorphismStructure} \textit{And the properties of the propert$

3.16.17 HomStructure (for IsCapCategory)

(operation)

This is a convenience method for DistinguishedObjectOfHomomorphismStructure.

3.16.18 ExtendRangeOfHomomorphismStructureByFullEmbedding (for IsCapCategory, IsCapCategory, IsFunction, IsFunction, IsFunction)

- \triangleright DistinguishedObjectOfHomomorphismStructureExtendedByFullEmbedding(C, E) (operation)
- E, distinguished_object, alpha, r) (operation)

Returns: nothing

If $i:D \to E$ is a full embedding of categories, every D-homomorphism structure for a category C extends to a E-homomorphism structure for C. This operations accepts four functions and installs operations DistinguishedObjectOfHomomorphismStructureExtendedByFullEmbedding, HomomorphismStructureOnObjectsExtendedByFullEmbedding etc. which correspond to the <math>E-homomorphism structure for C. Note: To distinguish embeddings in different categories, in addition to C also E is passed to the operations. When using this with different embeddings with the range category E, only the last embedding will be used. The arguments are:

- object_function gets the categories C and E and an object in D.
- morphism_function gets the categories C and E, an object in E, a morphism in D and another object in E. The objects are the results of object_function applied to the source and range of the morphism.
- object_function_inverse gets the categories C and E and an object in E.

• morphism_function_inverse gets the categories C and E, an object in D, a morphism in E and another object in D. The objects are the results of object_function_inverse applied to the source and range of the morphism.

object_function and morphism_function define the embedding. object_function_inverse and morphism_function_inverse define the inverse of the embedding on its image.

3.16.19 ExtendRangeOfHomomorphismStructureByIdentityAsFullEmbedding (for IsCapCategory)

Chooses the identity on D as the full embedding in ExtendRangeOfHomomorphismStructureByFullEmbedding (3.16.18). This is useful to handle this case as a degenerate case of ExtendRangeOfHomomorphismStructureByFullEmbedding (3.16.18).

3.16.20 MorphismsOfExternalHom (for IsCapCategoryObject, IsCapCategoryObject)

▷ MorphismsOfExternalHom(a, b)

(operation)

Returns: a list of morphisms in Hom(a,b)

The argument are two objects a, b. The output is a list of all morphisms from a to b.

3.16.21 BasisOfExternalHom (for IsCapCategoryObject, IsCapCategoryObject)

▷ BasisOfExternalHom(a, b)

(operation)

Returns: a list of morphisms in $Hom_C(a,b)$

The arguments are objects a, b in a k-linear category C. The output is a list L of morphisms which is a basis of $\operatorname{Hom}_C(a,b)$ in the sense that any given morphism $\alpha: a \to b$ can uniquely be written as a linear combination of L with the coefficients in CoefficientsOfMorphism(α).

3.16.22 CoefficientsOfMorphism (for IsCapCategoryMorphism)

▷ CoefficientsOfMorphism(alpha)

(attribute)

Returns: a list of elements in k

This is a convenience method. The argument is a morphism $\alpha : a \to b$ in a k-linear category C. The output is a list of coefficients of α with respect to the list BasisOfExternalHom(a,b).

3.17 Simplified Morphisms

Let $\phi: A \to B$ be a morphism. There are several different natural ways to look at ϕ as an object in an ambient category:

- $\operatorname{Hom}(A,B)$, the set of homomorphisms with the equivalence relation $\operatorname{IsCongruentForMorphisms}$ regarded as a category,
- $\sum_{A} \text{Hom}(A, B)$, the category of morphisms where the range is fixed,

- $\sum_{B} \text{Hom}(A, B)$, the category of morphisms where the source is fixed,
- $\sum_{A,B} \text{Hom}(A,B)$, the category of morphisms where neither source nor range is fixed,

and furthermore, if ϕ happens to be an endomorphism $A \to A$, we also have

• $\sum_{A} \text{Hom}(A, A)$, the category of endomorphisms.

Let \mathbb{C} be one of the categories above in which ϕ may reside as an object, and let i be a non-negative integer or ∞ . CAP provides commands for passing from ϕ to ϕ_i , where ϕ_i is isomorphic to ϕ in \mathbb{C} , but "simpler". The idea is that the greater the i, the "simpler" the ϕ_i (but this could mean the harder the computation), with ∞ as a possible value. The case i=0 defaults to the identity operator for all simplifications. For the Add-operatations, only the cases $i\geq 1$ have to be given as functions.

If we regard ϕ as an object in the category $\operatorname{Hom}(A,B)$, ϕ_i is again in $\operatorname{Hom}(A,B)$ such that $\phi \sim_{A,B} \phi_i$. This case is handled by the following commands:

3.17.1 SimplifyMorphism (for IsCapCategoryMorphism, IsObject)

▷ SimplifyMorphism(phi, i)

(operation)

Returns: a morphism in Hom(A, B)

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is a simplified morphism ϕ_i .

If we regard ϕ as an object in the category $\sum_A \operatorname{Hom}(A,B)$, then ϕ_i is a morphism of type $A_i \to B$ and there is an isomorphism $\sigma_i : A \to A_i$ such that $\phi_i \circ \sigma_i \sim_{A,B} \phi$. This case is handled by the following commands:

3.17.2 SimplifySource (for IsCapCategoryMorphism, IsObject)

▷ SimplifySource(phi, i)

(operation)

Returns: a morphism in $Hom(A_i, B)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is a simplified morphism with simplified source $\phi_i: A_i \to B$.

3.17.3 SimplifySource_IsoToInputObject (for IsCapCategoryMorphism, IsObject)

▷ SimplifySource_IsoToInputObject(phi, i)

(operation)

Returns: a morphism in $Hom(A_i, A)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $(\sigma_i)^{-1}: A_i \to A$.

3.17.4 SimplifySource_IsoFromInputObject (for IsCapCategoryMorphism, IsObject)

▷ SimplifySource_IsoFromInputObject(phi, i)

(operation)

Returns: a morphism in $Hom(A, A_i)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $\sigma_i: A \to A_i$.

If we regard ϕ as an object in the category $\sum_B \operatorname{Hom}(A,B)$, then ϕ_i is a morphism of type $A \to B_i$ and there is an isomorphism $\rho_i : B \to B_i$ such that $\rho_i^{-1} \circ \phi_i \sim_{A,B} \phi$. This case is handled by the following commands:

3.17.5 SimplifyRange (for IsCapCategoryMorphism, IsObject)

▷ SimplifyRange(phi, i)

(operation)

Returns: a morphism in $Hom(A, B_i)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is a simplified morphism with simplified range $\phi_i: A \to B_i$.

3.17.6 SimplifyRange_IsoToInputObject (for IsCapCategoryMorphism, IsObject)

▷ SimplifyRange_IsoToInputObject(phi, i)

(operation)

Returns: a morphism in $Hom(B_i, B)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $(\rho_i)^{-1}: B_i \to B$.

3.17.7 SimplifyRange_IsoFromInputObject (for IsCapCategoryMorphism, IsObject)

▷ SimplifyRange_IsoFromInputObject(phi, i)

(operation)

Returns: a morphism in $Hom(B, B_i)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $\rho_i: B \to B_i$.

If we regard ϕ as an object in the category $\sum_{A,B} \operatorname{Hom}(A,B)$, then ϕ_i is a morphism of type $A_i \to B_i$ and there is are isomorphisms $\sigma_i : A \to A_i$ and $\rho_i : B \to B_i$ such that $\rho_i^{-1} \circ \phi_i \circ \sigma_i \sim_{A,B} \phi$. This case is handled by the following commands:

3.17.8 SimplifySourceAndRange (for IsCapCategoryMorphism, IsObject)

▷ SimplifySourceAndRange(phi, i)

(operation)

Returns: a morphism in $Hom(A_i, B_i)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is a simplified morphism with simplified source and range $\phi_i: A_i \to B_i$.

3.17.9 SimplifySourceAndRange_IsoToInputRange (for IsCapCategoryMorphism, IsObject)

 $\quad \qquad \triangleright \ \, {\tt SimplifySourceAndRange_IsoToInputRange}(\textit{phi}\,,\,\,i)$

(operation)

Returns: a morphism in $Hom(B_i, B)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $(\rho_i)^{-1}: B_i \to B$.

3.17.10 SimplifySourceAndRange_IsoFromInputRange (for IsCapCategoryMorphism, IsObject)

▷ SimplifySourceAndRange_IsoFromInputRange(phi, i)

(operation)

Returns: a morphism in $Hom(B, B_i)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $\rho_i: B \to B_i$.

3.17.11 SimplifySourceAndRange_IsoToInputSource (for IsCapCategoryMorphism, IsObject)

▷ SimplifySourceAndRange_IsoToInputSource(phi, i)

(operation)

Returns: a morphism in $Hom(A_i, A)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $(\sigma_i)^{-1}: A_i \to A$.

3.17.12 SimplifySourceAndRange_IsoFromInputSource (for IsCapCategoryMorphism, IsObject)

▷ SimplifySourceAndRange_IsoFromInputSource(phi, i)

(operation)

Returns: a morphism in $Hom(A, A_i)$

The arguments are a morphism $\phi: A \to B$ and a non-negative integer i or infinity. The output is the isomorphism $\sigma_i: A \to A_i$.

If $\phi:A\to A$ is an endomorphism, we may regard it as an object in the category $\sum_A \operatorname{Hom}(A,A)$. In this case ϕ_i is a morphism of type $A_i\to A_i$ and there is an isomorphism $\sigma_i:A\to A_i$ such that $\sigma_i^{-1}\circ\phi_i\circ\sigma_i\sim_{A,A}\phi$. This case is handled by the following commands:

3.17.13 SimplifyEndo (for IsCapCategoryMorphism, IsObject)

▷ SimplifyEndo(phi, i)

(operation)

Returns: a morphism in $\text{Hom}(A_i, A_i)$

The arguments are an endomorphism $\phi: A \to A$ and a non-negative integer i or infinity. The output is a simplified endomorphism $\phi_i: A_i \to A_i$.

3.17.14 SimplifyEndo_IsoToInputObject (for IsCapCategoryMorphism, IsObject)

▷ SimplifyEndo_IsoToInputObject(phi, i)

(operation)

Returns: a morphism in $Hom(A_i, A)$

The arguments are an endomorphism $\phi: A \to A$ and a non-negative integer i or infinity. The output is the isomorphism $(\sigma_i)^{-1}: A_i \to A$.

3.17.15 SimplifyEndo_IsoFromInputObject (for IsCapCategoryMorphism, IsObject)

▷ SimplifyEndo_IsoFromInputObject(phi, i)

(operation)

Returns: a morphism in $Hom(A, A_i)$

The arguments are an endomorphism $\phi: A \to A$ and a non-negative integer i or infinity. The output is the isomorphism $\sigma_i: A \to A_i$.

3.17.16 Simplify (for IsCapCategoryMorphism)

Simplify(phi) (attribute)

Returns: a morphism in $\text{Hom}(A_{\infty}, B_{\infty})$

This is a convenient method. The argument is a morphism $\phi: A \to B$. The output is a "simplified" version of ϕ that may change the source and range of ϕ (up to isomorphism). To be precise, the output is an ∞ -th simplified morphism of $(\iota_A^{\infty})^{-1} \circ \phi \circ \iota_A^{\infty}$.

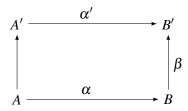
3.18 Reduction by split epi summands

Let $\alpha: A \to B$ be a morphism in an additive category. Suppose we are given direct sum decompositions of $A \simeq A' \oplus A''$ and $B \simeq B' \oplus B''$ such that

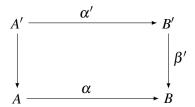
$$A' \oplus A'' \xrightarrow{\alpha' \oplus \alpha''} B' \oplus B''$$

$$A \xrightarrow{\alpha} B$$

If α'' is a split epimorphism, then we call $\alpha': A' \to B'$ some reduction of α by split epi summands. The inclusions/projections of the decompositions into direct sums induce commutative diagrams



and



3.18.1 SomeReductionBySplitEpiSummand (for IsCapCategoryMorphism)

 ${\scriptstyle \rhd} \ {\tt SomeReductionBySplitEpiSummand(alpha)}$

(attribute)

Returns: a morphism in Hom(A', B')

The argument is a morphism $\alpha : A \to B$. The output is some reduction of α by split epi summands $\alpha' : A' \to B'$.

${\bf 3.18.2} \quad Some Reduction By Split Epi Summand_Morphism To Input Range \ (for\ Is Cap Category Morphism)$

The argument is a morphism $\alpha : A \to B$. The output is the morphism $\beta' : B' \to B$ linking α with some reduction by split epi summands.

3.18.3 SomeReductionBySplitEpiSummand_MorphismFromInputRange (for IsCap-CategoryMorphism)

The argument is a morphism $\alpha: A \to B$. The output is the morphism $\beta: B \to B'$ linking α with some reduction by split epi summands.

Chapter 4

Category 2-Cells

4.1 Attributes for the Type of 2-Cells

4.1.1 Source (for IsCapCategoryTwoCell)

 \triangleright Source(c) (attribute)

Returns: a morphism

The argument is a 2-cell $c: \alpha \to \beta$. The output is its source α .

4.1.2 Range (for IsCapCategoryTwoCell)

 \triangleright Range(c) (attribute)

Returns: a morphism

The argument is a 2-cell $c: \alpha \to \beta$. The output is its range β .

4.1.3 Target (for IsCapCategoryTwoCell)

 $\triangleright \mathsf{Target}(c)$ (attribute)

Returns: a morphism

The argument is a 2-cell $c: \alpha \to \beta$. The output is its target β .

4.2 Adding 2-Cells to a Category

4.2.1 Add (for IsCapCategory, IsCapCategoryTwoCell)

▷ Add(category, twocell)

Adds twocell as a 2-cell to category.

4.2.2 AddTwoCell (for IsCapCategory, IsAttributeStoringRep)

▷ AddTwoCell(category, twocell) (operation)

Adds twocell as a 2-cell to category. If twocell already lies in the filter IsCapCategoryTwoCell, the operation Add (4.2.1) can be used instead.

(operation)

4.2.3 CreateCapCategoryTwoCellWithAttributes

 $\verb| CreateCapCategoryTwoCellWithAttributes(category, source, range[, attr1, val1, attr2, val2, ...])| (function) \\$

Returns: a twocell

Creates a 2-cell in category with the given attributes.

4.3 Identity 2-Cell and Composition of 2-Cells

4.3.1 IdentityTwoCell (for IsCapCategoryMorphism)

▷ IdentityTwoCell(alpha)

(attribute)

Returns: a 2-cell

The argument is a morphism α . The output is its identity 2-cell $id_{\alpha} : \alpha \to \alpha$.

4.3.2 HorizontalPreCompose (for IsCapCategoryTwoCell, IsCapCategoryTwoCell)

 \triangleright HorizontalPreCompose(c, d)

(operation)

Returns: a 2-cell

The arguments are two 2-cells $c: \alpha \to \beta$, $d: \gamma \to \delta$ between morphisms $\alpha, \beta: a \to b$ and $\gamma, \delta: b \to c$. The output is their horizontal composition $d*c: (\gamma \circ \alpha) \to (\delta \circ \beta)$.

4.3.3 HorizontalPostCompose (for IsCapCategoryTwoCell, IsCapCategoryTwoCell)

 \triangleright HorizontalPostCompose(d, c)

(operation)

Returns: a 2-cell

The arguments are two 2-cells $d: \gamma \to \delta$, $c: \alpha \to \beta$ between morphisms $\alpha, \beta: a \to b$ and $\gamma, \delta: b \to c$. The output is their horizontal composition $d*c: (\gamma \circ \alpha) \to (\delta \circ \beta)$.

4.3.4 VerticalPreCompose (for IsCapCategoryTwoCell, IsCapCategoryTwoCell)

 \triangleright VerticalPreCompose(c, d)

(operation)

Returns: a 2-cell

The arguments are two 2-cells $c: \alpha \to \beta$, $d: \beta \to \gamma$ between morphisms $\alpha, \beta, \gamma: a \to b$. The output is their vertical composition $d \circ c: \alpha \to \gamma$.

4.3.5 VerticalPostCompose (for IsCapCategoryTwoCell, IsCapCategoryTwoCell)

▷ VerticalPostCompose(d, c)

(operation)

Returns: a 2-cell

The arguments are two 2-cells $d: \beta \to \gamma$, $c: \alpha \to \beta$ between morphisms $\alpha, \beta, \gamma: a \to b$. The output is their vertical composition $d \circ c: \alpha \to \gamma$.

4.4 Well-Definedness for 2-Cells

4.4.1 IsWellDefinedForTwoCells (for IsCapCategoryTwoCell)

▷ IsWellDefinedForTwoCells(c)

(operation)

Returns: a boolean

The argument is a 2-cell c. The output is true if c is well-defined, otherwise the output is false.

Chapter 5

Category of Categories

Categories itself with functors as morphisms form a category Cat. So the data structure of CapCategorys is designed to be objects in a category. This category is implemented in CapCat. For every category, the corresponding object in Cat can be obtained via AsCatObject. The implementation of the category of categories offers a data structure for functors. Those are implemented as morphisms in this category, so functors can be handled like morphisms in a category. Also convenience functions to install functors as methods are implemented (in order to avoid ApplyFunctor).

5.1 The Category Cat

5.1.1 CapCat

This variable stores the category of categories. Every category object is constructed as an object in this category, so Cat is constructed when loading the package.

5.2 Categories

5.2.1 IsCapCategoryAsCatObject (for IsCapCategoryObject)

▷ IsCapCategoryAsCatObject(object)

(filter)

Returns: true or false

The GAP category of CAP categories seen as object in Cat.

5.2.2 IsCapFunctor (for IsCapCategoryMorphism)

▷ IsCapFunctor(object)

(filter)

Returns: true or false The GAP category of functors.

5.2.3 IsCapNaturalTransformation (for IsCapCategoryTwoCell)

▷ IsCapNaturalTransformation(object)

(filter)

Returns: true or false

The GAP category of natural transformations.

5.3 Constructors

5.3.1 AsCatObject (for IsCapCategory)

```
\triangleright AsCatObject(C) (attribute)
```

Given a CAP category C, this method returns the corresponding object in Cat. For technical reasons, the filter IsCapCategory must not imply the filter IsCapCategoryObject. For example, if InitialObject is applied to an object, it returns the initial object of its category. If it is applied to a category, it returns the initial object of the category. If a CAP category would be a category object itself, this would be ambiguous. So categories must be wrapped in a CatObject to be an object in Cat. This method returns the wrapper object. The category can be reobtained by AsCapCategory.

5.3.2 AsCapCategory (for IsCapCategoryAsCatObject)

For an object C in Cat, this method returns the underlying CAP category. This method is inverse to AsCatObject, i.e. AsCapCategory(AsCatObject(A)) = A.

5.4 Functors

Functors are morphisms in Cat, thus they have source and target which are categories. A multivariate functor can be constructed via a product category as source, a presheaf is constructed via the opposite category as source. However, the user can explicitly decide the arity of a functor (which will only have technical implications). Thus, it is for example possible to consider a functor $A \times B \to C$ either as a unary functor with source category $A \times B$ or as a binary functor. Moreover, an object and a morphism function can be added to a functor, to apply it to objects or morphisms in the source category.

5.4.1 CapFunctor (for IsString, IsCapCategory, IsCapCategory)

```
▷ CapFunctor(name, A, B) (operation)
```

These methods construct a unary CAP functor. The first argument is a string for the functor's name. A and B are the source and target of the functor, and they can be given as objects in CapCat or as a CAP-category.

5.4.2 CapFunctor (for IsString, IsList, IsCapCategory)

```
▷ CapFunctor(name, list, B) (operation)
▷ CapFunctor(name, list, B) (operation)
```

These methods construct a possible multivariate CAP functor. The first argument is a string for the functor's name. The second argument is a list encoding the input signature of the functor. It can be given as a list of pairs $[[A_1,b_1],\ldots,[A_n,b_n]]$ where a pair consists of a category A_i (given as an object in CapCat or as a CAP-category) and a boolean b_i for $i=1,\ldots,n$. Instead of a pair $[A_i,b_i]$, you can also give simply A_i , which will be interpreted as the pair $[A_i, \mathtt{false}]$. The third argument is the target B of the functor, and it can be given as an object in CapCat or as a CAP-category. The output is a functor with source given by the product category $D_1 \times \ldots \times D_n$, where $D_i = A_i$ if $b_i = \mathtt{false}$, and $D_i = A_i^{\mathrm{op}}$ otherwise.

5.4.3 SourceOfFunctor (for IsCapFunctor)

▷ SourceOfFunctor(F)

The argument is a functor *F*. The output is its source as CAP category.

5.4.4 RangeOfFunctor (for IsCapFunctor)

▷ RangeOfFunctor(F) (attribute)

The argument is a functor F. The output is its range as CAP category.

5.4.5 AddObjectFunction (for IsCapFunctor, IsFunction)

▷ AddObjectFunction(F, f)

This operation adds a function f to the functor F which can then be applied to objects in the source. The given function f has to take arguments according to the InputSignature of F, i.e., if the input signature is given by $[[A_1,b_1],\ldots,[A_n,b_n]]$, then f must take n arguments, where the i-th argument is an object in the category A_i (the boolean b_i is ignored). The function should return an object in the range of the functor, except when the automatic call of AddObject was enabled via EnableAddForCategoricalOperations. In this case the output only has to be a GAP object in IsAttributeStoringRep, which will be automatically added as an object to the range of the functor.

5.4.6 FunctorObjectOperation (for IsCapFunctor)

▷ FunctorObjectOperation(F)

(attribute)

(attribute)

(operation)

Returns: a GAP operation

The argument is a functor F. The output is the GAP operation realizing the action of F on objects.

5.4.7 AddMorphismFunction (for IsCapFunctor, IsFunction)

▷ AddMorphismFunction(F, f)

(operation)

This operation adds a function f to the functor F which can then be applied to morphisms in the source. The given function f has to take as its first argument an object f that is equal (via IsEqualForObjects) to the source of the result of applying f to the input morphisms. The next arguments of f have to morphisms according to the InputSignature of f, i.e., if the input signature

is given by $[[A_1,b_1],\ldots,[A_n,b_n]]$, then f must take n arguments, where the i-th argument is a morphism in the category A_i (the boolean b_i is ignored). The last argument of f must be an object f that is equal (via IsEqualForObjects) to the range of the result of applying f to the input morphisms. The function should return a morphism in the range of the functor, except when the automatic call of AddMorphism was enabled via EnableAddForCategoricalOperations. In this case the output only has to be a GAP object in IsAttributeStoringRep (with attributes Source and Range containing also GAP objects in IsAttributeStoringRep), which will be automatically added as a morphism to the range of the functor.

5.4.8 FunctorMorphismOperation (for IsCapFunctor)

(attribute)

Returns: a GAP operation

The argument is a functor F. The output is the GAP operation realizing the action of F on morphisms.

5.4.9 ApplyFunctor

▷ ApplyFunctor(func, A[, B, ...])

(function)

Returns: IsCapCategoryCell Applies the functor *func* either to

- an object or morphism A in the source of func or
- to objects or morphisms belonging to the categories in the input signature of func.

5.4.10 InputSignature (for IsCapFunctor)

▷ InputSignature(F)

(attribute)

Returns: IsList

The argument is a functor F. The output is a list of pairs $[[A_1, b_1], \dots, [A_n, b_n]]$ where a pair consists of a CAP-category A_i and a boolean b_i for $i = 1, \dots, n$. The source of F is given by the product category $D_1 \times \dots \times D_n$, where $D_i = A_i$ if $b_i = false$, and $D_i = A_i^{op}$ otherwise.

5.4.11 InstallFunctor (for IsCapFunctor, IsString)

 \triangleright InstallFunctor(F, s)

(operation)

Returns: nothing

The arguments are a functor F and a string s. To simplify the description of this operation, we let $[[A_1,b_1],\ldots,[A_n,b_n]]$ denote the input signature of F. This method tries to install 3 operations: an operation ω_1 with the name s0n0bjects, and an operation ω_3 with the name s0nMorphisms. The operation ω_1 takes as input either n- objects/morphisms in A_i or a single object/morphism in the source of F, and outputs the result of applying F to this input. ω_2 and ω_3 are the corresponding variants for objects or morphisms only. This function can only be called once for each functor, every further call will be ignored.

5.4.12 IdentityFunctor (for IsCapCategory)

▷ IdentityFunctor(cat)

(attribute)

Returns: a functor

Returns the identity functor of the category cat viewed as an object in the category of categories.

5.4.13 FunctorCanonicalizeZeroObjects (for IsCapCategory)

▷ FunctorCanonicalizeZeroObjects(cat)

(attribute)

Returns: a functor

Returns the endofunctor of the category cat with zero which maps each (object isomorphic to the) zero object to ZeroObject(cat) and to itself otherwise. This functor is equivalent to the identity functor.

5.4.14 NaturalIsomorphismFromIdentityToCanonicalizeZeroObjects (for IsCapCategory)

▷ NaturalIsomorphismFromIdentityToCanonicalizeZeroObjects(cat)

(attribute)

Returns: a natural transformation

Returns the natural isomorphism from the identity functor to FunctorCanonicalizeZeroObjects(cat).

5.4.15 FunctorCanonicalizeZeroMorphisms (for IsCapCategory)

(attribute)

Returns: a functor

Returns the endofunctor of the category cat with zero which maps each object to itself, each morphism ϕ to itself, unless it is congruent to the zero morphism; in this case it is mapped to $ZeroMorphism(Source(\phi), Range(\phi))$. This functor is equivalent to the identity functor.

5.4.16 NaturalIsomorphismFromIdentityToCanonicalizeZeroMorphisms (for IsCap-Category)

 ${\tt \triangleright} \ {\tt NaturalIsomorphismFromIdentityToCanonicalizeZeroMorphisms}({\it cat})$

(attribute)

Returns: a natural transformation

Returns the natural isomorphism from the identity functor to FunctorCanonicalizeZeroMorphisms(cat).

5.5 Natural transformations

Natural transformations form the 2-cells of Cat. As such, it is possible to compose them vertically and horizontally, see Section 4.3.

5.5.1 Name (for IsCapNaturalTransformation)

Name(arg) (attribute)

Returns: a string

As every functor, every natural transformation has a name attribute. It has to be a string and will be set by the Constructor.

5.5.2 NaturalTransformation (for IsCapFunctor, IsCapFunctor)

NaturalTransformation([name,]F, G)

(operation)

Returns: a natural transformation

Constructs a natural transformation between the functors $F: A \to B$ and $G: A \to B$. The string name is optional, and, if not given, set automatically from the names of the functors

5.5.3 AddNaturalTransformationFunction (for IsCapNaturalTransformation, IsFunction)

▷ AddNaturalTransformationFunction(N, func)

(operation)

Adds the function func to the natural transformation N. The function should take three arguments. If $N: F \to G$, the arguments should be F(A), A, G(A). The output should be a morphism, $F(A) \to G(A)$.

5.5.4 ApplyNaturalTransformation

▷ ApplyNaturalTransformation(N, A)

(function)

Returns: a morphism

Given a natural transformation $\mathbb{N}: F \to G$ and an object A, this function should return the morphism $F(A) \to G(A)$, corresponding to \mathbb{N} .

5.5.5 InstallNaturalTransformation (for IsCapNaturalTransformation, IsString)

▷ InstallNaturalTransformation(N, name)

(operation)

Installs the natural transformation N as operation with the name name. Argument for this operation is an object, output is a morphism.

5.5.6 HorizontalPreComposeNaturalTransformationWithFunctor (for IsCapNaturalTransformation, IsCapFunctor)

(operation)

Returns: a natural transformation

Computes the horizontal composition of the natural transformation N and the functor F.

5.5.7 HorizontalPreComposeFunctorWithNaturalTransformation (for IsCapFunctor, IsCapNaturalTransformation)

(operation)

Returns: a natural transformation

Computes the horizontal composition of the functor *F* and the natural transformation *N*.

Chapter 6

Universal Objects

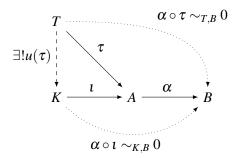
6.1 Kernel

For a given morphism $\alpha: A \to B$, a kernel of α consists of three parts:

- an object K,
- a morphism $\iota: K \to A$ such that $\alpha \circ \iota \sim_{K,B} 0$,
- a dependent function u mapping each morphism $\tau: T \to A$ satisfying $\alpha \circ \tau \sim_{T,B} 0$ to a morphism $u(\tau): T \to K$ such that $\iota \circ u(\tau) \sim_{T,A} \tau$.

The triple (K, ι, u) is called a *kernel* of α if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object K of such a triple by KernelObject (α) . We say that the morphism $u(\tau)$ is induced by the *universal property of the kernel*.

KernelObject is a functorial operation. This means: for $\mu : A \to A'$, $\nu : B \to B'$, $\alpha : A \to B$, $\alpha' : A' \to B'$ such that $\nu \circ \alpha \sim_{A,B'} \alpha' \circ \mu$, we obtain a morphism KernelObject(α) \to KernelObject(α').



6.1.1 KernelObject (for IsCapCategoryMorphism)

▷ KernelObject(alpha)

(attribute)

Returns: an object

The argument is a morphism α . The output is the kernel K of α .

6.1.2 KernelEmbedding (for IsCapCategoryMorphism)

(attribute)

Returns: a morphism in Hom(KernelObject(α),A)

The argument is a morphism $\alpha : A \to B$. The output is the kernel embedding $\iota : \text{KernelObject}(\alpha) \to A$.

6.1.3 KernelEmbeddingWithGivenKernelObject (for IsCapCategoryMorphism, IsCapCategoryObject)

▷ KernelEmbeddingWithGivenKernelObject(alpha, K)

(operation)

Returns: a morphism in Hom(K,A)

The arguments are a morphism $\alpha : A \to B$ and an object $K = \text{KernelObject}(\alpha)$. The output is the kernel embedding $\iota : K \to A$.

6.1.4 MorphismFromKernelObjectToSink (for IsCapCategoryMorphism)

(operation)

Returns: the zero morphism in Hom(KernelObject(α), B)

The argument is a morphism $\alpha : A \to B$. The output is the zero morphism $0 : \text{KernelObject}(\alpha) \to B$.

6.1.5 MorphismFromKernelObjectToSinkWithGivenKernelObject (for IsCapCategoryMorphism, IsCapCategoryObject)

 ${\tt \,\, \,\, \,\, \,\, Morphism From Kernel Object To Sink With Given Kernel Object (\it alpha, \,\, \it K) \,\, \, \, }$

(operation)

Returns: the zero morphism in Hom(K, B)

The arguments are a morphism $\alpha : A \to B$ and an object $K = \text{KernelObject}(\alpha)$. The output is the zero morphism $0 : K \to B$.

6.1.6 KernelLift (for IsCapCategoryMorphism, IsCapCategoryObject, IsCapCategoryMorphism)

▷ KernelLift(alpha, T, tau)

(operation)

Returns: a morphism in $Hom(T, KernelObject(\alpha))$

The arguments are a morphism $\alpha: A \to B$, a test object T, and a test morphism $\tau: T \to A$ satisfying $\alpha \circ \tau \sim_{T,B} 0$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau): T \to \text{KernelObject}(\alpha)$ given by the universal property of the kernel.

6.1.7 KernelLiftWithGivenKernelObject (for IsCapCategoryMorphism, IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

▷ KernelLiftWithGivenKernelObject(alpha, T, tau, K)

(operation)

Returns: a morphism in Hom(T, K)

The arguments are a morphism $\alpha: A \to B$, a test object T, a test morphism $\tau: T \to A$ satisfying $\alpha \circ \tau \sim_{T,B} 0$, and an object $K = \text{KernelObject}(\alpha)$. For convenience, the test object T can be omitted

and is automatically derived from tau in that case. The output is the morphism $u(\tau): T \to K$ given by the universal property of the kernel.

6.1.8 KernelObjectFunctorial (for IsList)

▷ KernelObjectFunctorial(L)

(operation)

Returns: a morphism in Hom(KernelObject(α), KernelObject(α'))

The argument is a list $L = [\alpha : A \to B, [\mu : A \to A', \nu : B \to B'], \alpha' : A' \to B']$ of morphisms. The output is the morphism KernelObject(α) \to KernelObject(α') given by the functoriality of the kernel.

6.1.9 KernelObjectFunctorial (for IsCapCategoryMorphism, IsCapCategoryMorphism) IsCapCategoryMorphism)

▷ KernelObjectFunctorial(alpha, mu, alpha_prime)

(operation)

Returns: a morphism in Hom(KernelObject(α), KernelObject(α'))

The arguments are three morphisms $\alpha: A \to B$, $\mu: A \to A'$, $\alpha': A' \to B'$. The output is the morphism KernelObject(α) \to KernelObject(α') given by the functoriality of the kernel.

6.1.10 KernelObjectFunctorialWithGivenKernelObjects (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

▷ KernelObjectFunctorialWithGivenKernelObjects(s, alpha, mu, alpha_prime, r)

(operation)

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \text{KernelObject}(\alpha)$, three morphisms $\alpha : A \to B$, $\mu : A \to A'$, $\alpha' : A' \to B'$, and an object $r = \text{KernelObject}(\alpha')$. The output is the morphism $\text{KernelObject}(\alpha) \to \text{KernelObject}(\alpha')$ given by the functoriality of the kernel.

6.1.11 KernelObjectFunctorialWithGivenKernelObjects (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

▷ KernelObjectFunctorialWithGivenKernelObjects(s, alpha, mu, nu, alpha_prime,
r)
(operation)

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \text{KernelObject}(\alpha)$, four morphisms $\alpha : A \to B$, $\mu : A \to A'$, $\nu : B \to B'$, $\alpha' : A' \to B'$, and an object $r = \text{KernelObject}(\alpha')$. The output is the morphism $\text{KernelObject}(\alpha) \to \text{KernelObject}(\alpha')$ given by the functoriality of the kernel.

6.2 Cokernel

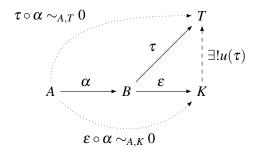
For a given morphism $\alpha: A \to B$, a cokernel of α consists of three parts:

- an object K,
- a morphism $\varepsilon: B \to K$ such that $\varepsilon \circ \alpha \sim_{A,K} 0$,

• a dependent function u mapping each $\tau: B \to T$ satisfying $\tau \circ \alpha \sim_{A,T} 0$ to a morphism $u(\tau): K \to T$ such that $u(\tau) \circ \varepsilon \sim_{B,T} \tau$.

The triple (K, ε, u) is called a *cokernel* of α if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object K of such a triple by CokernelObject (α) . We say that the morphism $u(\tau)$ is induced by the *universal property of the cokernel*.

CokernelObject is a functorial operation. This means: for $\mu : A \to A'$, $\nu : B \to B'$, $\alpha : A \to B$, $\alpha' : A' \to B'$ such that $\nu \circ \alpha \sim_{A,B'} \alpha' \circ \mu$, we obtain a morphism CokernelObject(α) \to CokernelObject(α').



6.2.1 CokernelObject (for IsCapCategoryMorphism)

▷ CokernelObject(alpha)

(attribute)

Returns: an object

The argument is a morphism $\alpha : A \to B$. The output is the cokernel K of α .

6.2.2 CokernelProjection (for IsCapCategoryMorphism)

▷ CokernelProjection(alpha)

(attribute)

Returns: a morphism in $Hom(B, CokernelObject(\alpha))$

The argument is a morphism $\alpha: A \to B$. The output is the cokernel projection $\varepsilon: B \to \operatorname{CokernelObject}(\alpha)$.

6.2.3 CokernelProjectionWithGivenCokernelObject (for IsCapCategoryMorphism, IsCapCategoryObject)

▷ CokernelProjectionWithGivenCokernelObject(alpha, K)

(operation)

Returns: a morphism in Hom(B, K)

The arguments are a morphism $\alpha : A \to B$ and an object $K = \text{CokernelObject}(\alpha)$. The output is the cokernel projection $\varepsilon : B \to \text{CokernelObject}(\alpha)$.

6.2.4 MorphismFromSourceToCokernelObject (for IsCapCategoryMorphism)

 ${\tt \, \, \, \, \, \, MorphismFrom Source To Cokernel Object (\it alpha) }$

(operation)

Returns: the zero morphism in $Hom(A, CokernelObject(\alpha))$.

The argument is a morphism $\alpha: A \to B$. The output is the zero morphism $0: A \to \text{CokernelObject}(\alpha)$.

6.2.5 MorphismFromSourceToCokernelObjectWithGivenCokernelObject (for Is-CapCategoryMorphism, IsCapCategoryObject)

 \triangleright MorphismFromSourceToCokernelObjectWithGivenCokernelObject(alpha, K) (operation) **Returns:** the zero morphism in Hom(A, K).

The argument is a morphism $\alpha : A \to B$ and an object $K = \text{CokernelObject}(\alpha)$. The output is the zero morphism $0 : A \to K$.

6.2.6 CokernelColift (for IsCapCategoryMorphism, IsCapCategoryObject, IsCapCategoryMorphism)

▷ CokernelColift(alpha, T, tau)

(operation)

Returns: a morphism in Hom(CokernelObject(α), T)

The arguments are a morphism $\alpha: A \to B$, a test object T, and a test morphism $\tau: B \to T$ satisfying $\tau \circ \alpha \sim_{A,T} 0$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau)$: CokernelObject $(\alpha) \to T$ given by the universal property of the cokernel.

6.2.7 CokernelColiftWithGivenCokernelObject (for IsCapCategoryMorphism, IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

ightharpoonup CokernelColiftWithGivenCokernelObject(alpha, T, tau, K) (operation)

Returns: a morphism in Hom(K,T)

The arguments are a morphism $\alpha: A \to B$, a test object T, a test morphism $\tau: B \to T$ satisfying $\tau \circ \alpha \sim_{A,T} 0$, and an object $K = \text{CokernelObject}(\alpha)$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau): K \to T$ given by the universal property of the cokernel.

6.2.8 CokernelObjectFunctorial (for IsList)

▷ CokernelObjectFunctorial(L)

(operation)

Returns: a morphism in Hom(CokernelObject(α), CokernelObject(α'))

The argument is a list $L = [\alpha : A \to B, [\mu : A \to A', \nu : B \to B'], \alpha' : A' \to B']$. The output is the morphism CokernelObject(α) \to CokernelObject(α') given by the functoriality of the cokernel.

6.2.9 CokernelObjectFunctorial (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ CokernelObjectFunctorial(alpha, nu, alpha_prime)

(operation)

Returns: a morphism in Hom(CokernelObject(α), CokernelObject(α'))

The arguments are three morphisms $\alpha: A \to B, v: B \to B', \alpha': A' \to B'$. The output is the morphism CokernelObject(α) \to CokernelObject(α) given by the functoriality of the cokernel.

(attribute)

6.2.10 CokernelObjectFunctorialWithGivenCokernelObjects (for IsCap-CategoryObject, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

▷ CokernelObjectFunctorialWithGivenCokernelObjects(s, alpha, nu, alpha_prime,
r)
(operation)

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \text{CokernelObject}(\alpha)$, three morphisms $\alpha : A \to B, v : B \to B', \alpha' : A' \to B'$, and an object $r = \text{CokernelObject}(\alpha')$. The output is the morphism $\text{CokernelObject}(\alpha) \to \text{CokernelObject}(\alpha')$ given by the functoriality of the cokernel.

6.2.11 CokernelObjectFunctorialWithGivenCokernelObjects (for IsCap-CategoryObject, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

 $\verb|> CokernelObjectFunctorialWithGivenCokernelObjects(s, alpha, mu, nu, alpha_prime, r) | (operation) | (operati$

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \text{CokernelObject}(\alpha)$, four morphisms $\alpha : A \to B, \mu : A \to A', \nu : B \to B', \alpha' : A' \to B'$, and an object $r = \text{CokernelObject}(\alpha')$. The output is the morphism $\text{CokernelObject}(\alpha) \to \text{CokernelObject}(\alpha')$ given by the functoriality of the cokernel.

6.3 Zero Object

A zero object consists of three parts:

- an object Z,
- a function u_{in} mapping each object A to a morphism $u_{in}(A): A \to Z$,
- a function u_{out} mapping each object A to a morphism $u_{\text{out}}(A): Z \to A$.

The triple $(Z, u_{\rm in}, u_{\rm out})$ is called a zero object if the morphisms $u_{\rm in}(A)$, $u_{\rm out}(A)$ are uniquely determined up to congruence of morphisms. We denote the object Z of such a triple by ZeroObject. We say that the morphisms $u_{\rm in}(A)$ and $u_{\rm out}(A)$ are induced by the universal property of the zero object.

6.3.1 ZeroObject (for IsCapCategory)

▷ ZeroObject(C)

Returns: an object

The argument is a category C. The output is a zero object Z of C.

6.3.2 ZeroObject (for IsCapCategoryCell)

 \triangleright ZeroObject(c) (attribute)

Returns: an object

This is a convenience method. The argument is a cell c. The output is a zero object Z of the category C for which $c \in C$.

6.3.3 UniversalMorphismFromZeroObject (for IsCapCategoryObject)

▷ UniversalMorphismFromZeroObject(A)

(attribute)

Returns: a morphism in Hom(ZeroObject, A)

The argument is an object A. The output is the universal morphism u_{out} : ZeroObject $\to A$.

6.3.4 UniversalMorphismFromZeroObjectWithGivenZeroObject (for IsCapCategoryObject, IsCapCategoryObject)

(operation)

Returns: a morphism in Hom(Z,A)

The arguments are an object A, and a zero object Z = ZeroObject. The output is the universal morphism $u_{\text{out}}: Z \to A$.

6.3.5 UniversalMorphismIntoZeroObject (for IsCapCategoryObject)

□ UniversalMorphismIntoZeroObject(A)

(attribute)

Returns: a morphism in Hom(A, ZeroObject)

The argument is an object A. The output is the universal morphism $u_{in}: A \to ZeroObject$.

6.3.6 UniversalMorphismIntoZeroObjectWithGivenZeroObject (for IsCapCategory-Object, IsCapCategoryObject)

ightharpoonup UniversalMorphismIntoZeroObjectWithGivenZeroObject(A, Z)

(operation)

Returns: a morphism in Hom(A, Z)

The arguments are an object A, and a zero object Z = ZeroObject. The output is the universal morphism $u_{\text{in}} : A \to Z$.

6.3.7 MorphismFromZeroObject (for IsCapCategoryObject)

(attribute)

Returns: a morphism in Hom(ZeroObject, A)

This is a synonym for UniversalMorphismFromZeroObject.

6.3.8 MorphismIntoZeroObject (for IsCapCategoryObject)

▷ MorphismIntoZeroObject(A)

(attribute)

Returns: a morphism in Hom(A, ZeroObject)

This is a synonym for UniversalMorphismIntoZeroObject.

6.3.9 IsomorphismFromZeroObjectToInitialObject (for IsCapCategory)

 ${\tt \triangleright} \ \, {\tt IsomorphismFromZeroObjectToInitialObject(\it C)}\\$

(attribute)

Returns: a morphism in Hom(ZeroObject, InitialObject)

The argument is a category C. The output is the unique isomorphism ZeroObject \rightarrow InitialObject.

6.3.10 IsomorphismFromInitialObjectToZeroObject (for IsCapCategory)

▷ IsomorphismFromInitialObjectToZeroObject(C)

(attribute)

Returns: a morphism in Hom(InitialObject, ZeroObject)

The argument is a category C. The output is the unique isomorphism InitialObject \rightarrow ZeroObject.

6.3.11 IsomorphismFromZeroObjectToTerminalObject (for IsCapCategory)

▷ IsomorphismFromZeroObjectToTerminalObject(C)

(attribute)

Returns: a morphism in Hom(ZeroObject, TerminalObject)

The argument is a category C. The output is the unique isomorphism ZeroObject \rightarrow TerminalObject.

6.3.12 IsomorphismFromTerminalObjectToZeroObject (for IsCapCategory)

▷ IsomorphismFromTerminalObjectToZeroObject(C)

(attribute)

Returns: a morphism in Hom(TerminalObject, ZeroObject)

The argument is a category C. The output is the unique isomorphism TerminalObject \rightarrow ZeroObject.

6.3.13 ZeroObjectFunctorial (for IsCapCategory)

▷ ZeroObjectFunctorial(C)

(attribute)

Returns: a morphism in Hom(ZeroObject, ZeroObject)

The argument is a category C. The output is the unique morphism ZeroObject \rightarrow ZeroObject.

6.3.14 ZeroObjectFunctorialWithGivenZeroObjects (for IsCapCategoryObject, Is-CapCategoryObject)

Returns: a morphism in $Hom(zero_object1, zero_object2)$

The argument is a category C and a zero object ZeroObject(C) twice (for compatibility with other functorials). The output is the unique morphism $zero_object1 \rightarrow zero_object2$.

6.4 Terminal Object

A terminal object consists of two parts:

- an object T,
- a function u mapping each object A to a morphism $u(A): A \to T$.

The pair (T, u) is called a *terminal object* if the morphisms u(A) are uniquely determined up to congruence of morphisms. We denote the object T of such a pair by TerminalObject. We say that the morphism u(A) is induced by the *universal property of the terminal object*.

TerminalObject is a functorial operation. This just means: There exists a unique morphism $T \to T$.

6.4.1 TerminalObject (for IsCapCategory)

▷ TerminalObject(C)

(attribute)

Returns: an object

The argument is a category C. The output is a terminal object T of C.

6.4.2 TerminalObject (for IsCapCategoryCell)

▷ TerminalObject(c)

(attribute)

Returns: an object

This is a convenience method. The argument is a cell c. The output is a terminal object T of the category C for which $c \in C$.

6.4.3 UniversalMorphismIntoTerminalObject (for IsCapCategoryObject)

▷ UniversalMorphismIntoTerminalObject(A)

(attribute)

Returns: a morphism in Hom(A, TerminalObject)

The argument is an object A. The output is the universal morphism $u(A): A \to \text{TerminalObject}$.

6.4.4 UniversalMorphismIntoTerminalObjectWithGivenTerminalObject (for IsCap-CategoryObject, IsCapCategoryObject)

ightharpoonup UniversalMorphismIntoTerminalObjectWithGivenTerminalObject(A, T) (operation)

Returns: a morphism in Hom(A,T)

The argument are an object A, and an object T = TerminalObject. The output is the universal morphism $u(A): A \to T$.

6.4.5 TerminalObjectFunctorial (for IsCapCategory)

▷ TerminalObjectFunctorial(C)

(attribute)

Returns: a morphism in Hom(TerminalObject, TerminalObject)

The argument is a category C. The output is the unique morphism TerminalObject \rightarrow TerminalObject.

6.4.6 TerminalObjectFunctorialWithGivenTerminalObjects (for IsCapCategoryObject, IsCapCategoryObject)

 ${\tt \begin{tabular}{l} $ \beg$

Returns: a morphism in Hom(terminal_ob ject 1, terminal_ob ject 2)

The argument is a category C and a terminal object TerminalObject(C) twice (for compatibility with other functorials). The output is the unique morphism $terminal_ob$ $ject 1 \rightarrow terminal_ob$ ject 2.

6.5 Initial Object

An initial object consists of two parts:

• an object I,

• a function u mapping each object A to a morphism $u(A): I \to A$.

The pair (I, u) is called a *initial object* if the morphisms u(A) are uniquely determined up to congruence of morphisms. We denote the object I of such a triple by InitialObject. We say that the morphism u(A) is induced by the *universal property of the initial object*.

InitialObject is a functorial operation. This just means: There exists a unique morphisms $I \to I$.

6.5.1 InitialObject (for IsCapCategory)

▷ InitialObject(C) (attribute)

Returns: an object

The argument is a category C. The output is an initial object I of C.

6.5.2 InitialObject (for IsCapCategoryCell)

 \triangleright InitialObject(c) (attribute)

Returns: an object

This is a convenience method. The argument is a cell c. The output is an initial object I of the category C for which $c \in C$.

6.5.3 UniversalMorphismFromInitialObject (for IsCapCategoryObject)

▷ UniversalMorphismFromInitialObject(A)

(attribute)

Returns: a morphism in Hom(InitialObject, *A*).

The argument is an object A. The output is the universal morphism u(A): InitialObject $\to A$.

6.5.4 UniversalMorphismFromInitialObjectWithGivenInitialObject (for IsCapCategoryObject, IsCapCategoryObject)

 \triangleright UniversalMorphismFromInitialObjectWithGivenInitialObject(A, I) (operation) **Returns:** a morphism in Hom(I,A).

The arguments are an object A, and an object I = InitialObject. The output is the universal morphism u(A): InitialObject $\to A$.

6.5.5 InitialObjectFunctorial (for IsCapCategory)

▷ InitialObjectFunctorial(C)

(attribute)

Returns: a morphism in Hom(InitialObject, InitialObject)

The argument is a category C. The output is the unique morphism InitialObject \rightarrow InitialObject.

6.5.6 InitialObjectFunctorialWithGivenInitialObjects (for IsCapCategoryObject, IsCapCategoryObject)

▷ InitialObjectFunctorialWithGivenInitialObjects(C, initial_object1, initial_object2)

(operation)

Returns: a morphism in Hom(*initial*₀*b ject*1, *initial*₀*b ject*2)

The argument is a category C and an initial object InitialObject(C) twice (for compatibility with other functorials). The output is the unique morphism $initial_ob$ $ject1 \rightarrow initial_ob$ ject2.

6.6 Direct Sum

For an integer $n \ge 1$ and a given list $D = (S_1, \dots, S_n)$ in an Ab-category, a direct sum consists of five parts:

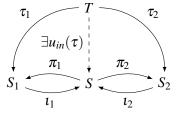
- an object S,
- a list of morphisms $\pi = (\pi_i : S \to S_i)_{i=1...n}$,
- a list of morphisms $\iota = (\iota_i : S_i \to S)_{i=1...n}$,
- a dependent function u_{in} mapping every list $\tau = (\tau_i : T \to S_i)_{i=1...n}$ to a morphism $u_{in}(\tau) : T \to S$ such that $\pi_i \circ u_{in}(\tau) \sim_{T,S_i} \tau_i$ for all i = 1, ..., n.
- a dependent function u_{out} mapping every list $\tau = (\tau_i : S_i \to T)_{i=1...n}$ to a morphism $u_{\text{out}}(\tau) : S \to T$ such that $u_{\text{out}}(\tau) \circ \iota_i \sim_{S_i,T} \tau_i$ for all i = 1, ..., n,

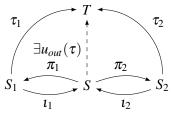
such that

- $\sum_{i=1}^n \iota_i \circ \pi_i \sim_{S,S} \mathrm{id}_S$,
- $\pi_i \circ \iota_i \sim_{S_i,S_i} \delta_{i,j}$,

where $\delta_{i,j} \in \text{Hom}(S_i, S_j)$ is the identity if i = j, and 0 otherwise. The 5-tuple $(S, \pi, \iota, u_{\text{in}}, u_{\text{out}})$ is called a *direct sum* of D. We denote the object S of such a 5-tuple by $\bigoplus_{i=1}^n S_i$. We say that the morphisms $u_{\text{in}}(\tau), u_{\text{out}}(\tau)$ are induced by the *universal property of the direct sum*.

DirectSum is a functorial operation. This means: For $(\mu_i : S_i \to S_i')_{i=1...n}$, we obtain a morphism $\bigoplus_{i=1}^n S_i \to \bigoplus_{i=1}^n S_i'$.





6.6.1 DirectSum

▷ DirectSum(arg)

(function)

Returns: an object

This is a convenience method. There are two different ways to use this method:

- The argument is a list of objects $D = (S_1, \dots, S_n)$.
- The arguments are objects S_1, \ldots, S_n .

The output is the direct sum $\bigoplus_{i=1}^{n} S_i$.

6.6.2 DirectSumOp (for IsList)

▷ DirectSumOp(D) (operation)

Returns: an object

The argument is a list of objects $D = (S_1, \dots, S_n)$. The output is the direct sum $\bigoplus_{i=1}^n S_i$.

6.6.3 ProjectionInFactorOfDirectSum (for IsList, IsInt)

▷ ProjectionInFactorOfDirectSum(D, k)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^n S_i, S_k)$

The arguments are a list of objects $D = (S_1, ..., S_n)$ and an integer k. The output is the k-th projection $\pi_k : \bigoplus_{i=1}^n S_i \to S_k$.

6.6.4 ProjectionInFactorOfDirectSumWithGivenDirectSum (for IsList, IsInt, IsCap-CategoryObject)

 ${\color{blue} \triangleright} \ \, \texttt{ProjectionInFactorOfDirectSumWithGivenDirectSum}(\textit{D, k, S}) \qquad \qquad (\textit{operation})$

Returns: a morphism in $Hom(S, S_k)$

The arguments are a list of objects $D = (S_1, \dots, S_n)$, an integer k, and an object $S = \bigoplus_{i=1}^n S_i$. The output is the k-th projection $\pi_k : S \to S_k$.

6.6.5 InjectionOfCofactorOfDirectSum (for IsList, IsInt)

 \triangleright InjectionOfCofactorOfDirectSum(D, k)

(operation)

Returns: a morphism in $\text{Hom}(S_k, \bigoplus_{i=1}^n S_i)$

The arguments are a list of objects $D = (S_1, ..., S_n)$ and an integer k. The output is the k-th injection $\iota_k : S_k \to \bigoplus_{i=1}^n S_i$.

6.6.6 InjectionOfCofactorOfDirectSumWithGivenDirectSum (for IsList, IsInt, IsCap-CategoryObject)

 ${\tt \triangleright InjectionOfCofactorOfDirectSumWithGivenDirectSum}(\textit{D, k, S}) \qquad \qquad (operation)$

Returns: a morphism in $Hom(S_k, S)$

The arguments are a list of objects $D = (S_1, \dots, S_n)$, an integer k, and an object $S = \bigoplus_{i=1}^n S_i$. The output is the k-th injection $\iota_k : S_k \to S$.

6.6.7 UniversalMorphismIntoDirectSum (for IsList, IsCapCategoryObject, IsList)

▷ UniversalMorphismIntoDirectSum(D, T, tau)

(operation)

Returns: a morphism in $\text{Hom}(T, \bigoplus_{i=1}^n S_i)$

The arguments are a list of objects $D = (S_1, \ldots, S_n)$, a test object T, and a list of morphisms $\tau = (\tau_i : T \to S_i)_{i=1...n}$. For convenience, the diagram D and/or the test object T can be omitted and are automatically derived from tau in that case. The output is the morphism $u_{\text{in}}(\tau) : T \to \bigoplus_{i=1}^n S_i$ given by the universal property of the direct sum.

6.6.8 UniversalMorphismIntoDirectSumWithGivenDirectSum (for IsList, IsCapCategoryObject, IsList, IsCapCategoryObject)

 \triangleright UniversalMorphismIntoDirectSumWithGivenDirectSum(D, T, tau, S) (operation) **Returns:** a morphism in Hom(T,S)

The arguments are a list of objects $D = (S_1, \ldots, S_n)$, a test object T, a list of morphisms $\tau = (\tau_i : T \to S_i)_{i=1...n}$, and an object $S = \bigoplus_{i=1}^n S_i$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u_{in}(\tau) : T \to S$ given by the universal property of the direct sum.

6.6.9 UniversalMorphismFromDirectSum (for IsList, IsCapCategoryObject, IsList)

 \triangleright UniversalMorphismFromDirectSum(D, T, tau)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^n S_i, T)$

The arguments are a list of objects $D = (S_1, \ldots, S_n)$, a test object T, and a list of morphisms $\tau = (\tau_i : S_i \to T)_{i=1...n}$. For convenience, the diagram D and/or the test object T can be omitted and are automatically derived from tau in that case. The output is the morphism $u_{\text{out}}(\tau) : \bigoplus_{i=1}^n S_i \to T$ given by the universal property of the direct sum.

6.6.10 UniversalMorphismFromDirectSumWithGivenDirectSum (for IsList, IsCap-CategoryObject, IsList, IsCapCategoryObject)

 \triangleright UniversalMorphismFromDirectSumWithGivenDirectSum(D, T, tau, S) (operation)

Returns: a morphism in Hom(S,T)

The arguments are a list of objects $D = (S_1, \ldots, S_n)$, a test object T, a list of morphisms $\tau = (\tau_i : S_i \to T)_{i=1...n}$, and an object $S = \bigoplus_{i=1}^n S_i$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u_{\text{out}}(\tau) : S \to T$ given by the universal property of the direct sum.

6.6.11 IsomorphismFromDirectSumToDirectProduct (for IsList)

▷ IsomorphismFromDirectSumToDirectProduct(D)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^n S_i, \prod_{i=1}^n S_i)$

The argument is a list of objects $D = (S_1, ..., S_n)$. The output is the canonical isomorphism $\bigoplus_{i=1}^n S_i \to \prod_{i=1}^n S_i$.

6.6.12 IsomorphismFromDirectProductToDirectSum (for IsList)

▷ IsomorphismFromDirectProductToDirectSum(D)

(operation)

Returns: a morphism in $\text{Hom}(\prod_{i=1}^n S_i, \bigoplus_{i=1}^n S_i)$

The argument is a list of objects $D = (S_1, ..., S_n)$. The output is the canonical isomorphism $\prod_{i=1}^n S_i \to \bigoplus_{i=1}^n S_i$.

6.6.13 IsomorphismFromDirectSumToCoproduct (for IsList)

▷ IsomorphismFromDirectSumToCoproduct(D)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^n S_i, \bigsqcup_{i=1}^n S_i)$

The argument is a list of objects $D = (S_1, ..., S_n)$. The output is the canonical isomorphism $\bigoplus_{i=1}^n S_i \to \bigsqcup_{i=1}^n S_i$.

6.6.14 IsomorphismFromCoproductToDirectSum (for IsList)

▷ IsomorphismFromCoproductToDirectSum(D)

(operation)

Returns: a morphism in $\text{Hom}(\bigsqcup_{i=1}^n S_i, \bigoplus_{i=1}^n S_i)$

The argument is a list of objects $D = (S_1, ..., S_n)$. The output is the canonical isomorphism $\bigcup_{i=1}^n S_i \to \bigoplus_{i=1}^n S_i$.

6.6.15 MorphismBetweenDirectSums (for IsList, IsList, IsList)

 \triangleright MorphismBetweenDirectSums(diagram_S, M, diagram_T)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^m A_i, \bigoplus_{j=1}^n B_j)$

The arguments are given as follows:

- diagram_S is a list of objects $(A_i)_{i=1...m}$,
- diagram_T is a list of objects $(B_j)_{j=1...n}$,
- M is a list of lists of morphisms $((\phi_{i,j}:A_i \to B_j)_{j=1...n})_{i=1...m}$

The output is the morphism $\bigoplus_{i=1}^m A_i \to \bigoplus_{j=1}^n B_j$ defined by the matrix M.

6.6.16 MorphismBetweenDirectSums (for IsList)

▷ MorphismBetweenDirectSums(M)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^m A_i, \bigoplus_{j=1}^n B_j)$

This is a convenience method. The argument $M = ((\phi_{i,j} : A_i \to B_j)_{j=1...n})_{i=1...m}$ is a (non-empty) list of (non-empty) lists of morphisms. The output is the morphism $\bigoplus_{i=1}^m A_i \to \bigoplus_{j=1}^n B_j$ defined by the matrix M.

6.6.17 MorphismBetweenDirectSumsWithGivenDirectSums (for IsCapCategoryObject, IsList, IsList, IsList, IsCapCategoryObject)

ightharpoonup MorphismBetweenDirectSumsWithGivenDirectSums(S, $diagram_S$, M, $diagram_T$, T)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^m A_i, \bigoplus_{j=1}^n B_j)$

The arguments are given as follows:

- diagram_S is a list of objects $(A_i)_{i=1...m}$,
- diagram_T is a list of objects $(B_i)_{i=1...n}$,
- S is the direct sum $\bigoplus_{i=1}^m A_i$,
- T is the direct sum $\bigoplus_{i=1}^n B_i$,
- M is a list of lists of morphisms $((\phi_{i,j}: A_i \to B_j)_{j=1...n})_{i=1...m}$

The output is the morphism $\bigoplus_{i=1}^m A_i \to \bigoplus_{i=1}^n B_i$ defined by the matrix M.

6.6.18 ComponentOfMorphismIntoDirectSum (for IsCapCategoryMorphism, IsList, IsInt)

▷ ComponentOfMorphismIntoDirectSum(alpha, D, k)

(operation)

Returns: a morphism in $Hom(A, S_k)$

The arguments are a morphism $\alpha: A \to S$, a list $D = (S_1, \dots, S_n)$ of objects with $S = \bigoplus_{j=1}^n S_j$, and an integer k. The output is the component morphism $A \to S_k$.

6.6.19 ComponentOfMorphismFromDirectSum (for IsCapCategoryMorphism, Is-List, IsInt)

▷ ComponentOfMorphismFromDirectSum(alpha, D, k)

(operation)

Returns: a morphism in $Hom(S_k, A)$

The arguments are a morphism $\alpha: S \to A$, a list $D = (S_1, \dots, S_n)$ of objects with $S = \bigoplus_{j=1}^n S_j$, and an integer k. The output is the component morphism $S_k \to A$.

6.6.20 DirectSumFunctorial (for IsList, IsList, IsList)

 $\quad \qquad \text{DirectSumFunctorial}(source_diagram, \ L, \ range_diagram)\\$

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^n S_i, \bigoplus_{i=1}^n S_i')$

The arguments are a list of objects $(S_i)_{i=1...n}$, a list of morphisms $L=(\mu_1:S_1\to S_1',\ldots,\mu_n:S_n\to S_n')$, and a list of objects $(S_i')_{i=1...n}$. For convenience, source_diagram and range_diagram can be omitted and are automatically derived from L in that case. The output is a morphism $\bigoplus_{i=1}^n S_i \to \bigoplus_{i=1}^n S_i'$ given by the functoriality of the direct sum.

6.6.21 DirectSumFunctorialWithGivenDirectSums (for IsCapCategoryObject, IsList, IsList, IsCapCategoryObject)

▷ DirectSumFunctorialWithGivenDirectSums(d_1, source_diagram, L, range_diagram, d_2)

(operation)

Returns: a morphism in $Hom(d_1, d_2)$

The arguments are an object $d_1 = \bigoplus_{i=1}^n S_i$, a list of objects $(S_i)_{i=1...n}$, a list of morphisms $L = (\mu_1 : S_1 \to S'_1, \dots, \mu_n : S_n \to S'_n)$, a list of objects $(S'_i)_{i=1...n}$, and an object $d_2 = \bigoplus_{i=1}^n S'_i$. For convenience, source_diagram and range_diagram can be omitted and are automatically derived from L in that case. The output is a morphism $d_1 \to d_2$ given by the functoriality of the direct sum.

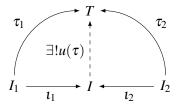
6.7 Coproduct

For an integer $n \ge 1$ and a given list of objects $D = (I_1, \dots, I_n)$, a coproduct of D consists of three parts:

- an object I,
- a list of morphisms $\iota = (\iota_i : I_i \to I)_{i=1...n}$
- a dependent function u mapping each list of morphisms $\tau = (\tau_i : I_i \to T)$ to a morphism $u(\tau) : I \to T$ such that $u(\tau) \circ \iota_i \sim_{I_i,T} \tau_i$ for all i = 1, ..., n.

The triple (I, ι, u) is called a *coproduct* of D if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object I of such a triple by $\bigsqcup_{i=1}^{n} I_i$. We say that the morphism $u(\tau)$ is induced by the *universal property of the coproduct*.

Coproduct is a functorial operation. This means: For $(\mu_i : I_i \to I'_i)_{i=1...n}$, we obtain a morphism $\bigsqcup_{i=1}^n I_i \to \bigsqcup_{i=1}^n I'_i$.



6.7.1 Coproduct (for IsList)

 \triangleright Coproduct(D) (operation)

Returns: an object

The argument is a list of objects $D = (I_1, \dots, I_n)$. The output is the coproduct $\bigsqcup_{i=1}^n I_i$.

6.7.2 Coproduct (for IsCapCategoryObject, IsCapCategoryObject)

▷ Coproduct(I1, I2)

Returns: an object

This is a convenience method. The arguments are two objects I_1, I_2 . The output is the coproduct $I_1 \bigsqcup I_2$.

6.7.3 Coproduct (for IsCapCategoryObject, IsCapCategoryObject, IsCapCategoryObject)

Coproduct(I1, I2) (operation)

Returns: an object

This is a convenience method. The arguments are three objects I_1, I_2, I_3 . The output is the coproduct $I_1 \bigsqcup I_2 \bigsqcup I_3$.

6.7.4 InjectionOfCofactorOfCoproduct (for IsList, IsInt)

▷ InjectionOfCofactorOfCoproduct(D, k)

(operation)

(operation)

Returns: a morphism in $\text{Hom}(I_k, \bigsqcup_{i=1}^n I_i)$

The arguments are a list of objects $D = (I_1, \dots, I_n)$ and an integer k. The output is the k-th injection $\iota_k : I_k \to \bigsqcup_{i=1}^n I_i$.

6.7.5 InjectionOfCofactorOfCoproductWithGivenCoproduct (for IsList, IsInt, IsCap-CategoryObject)

 \triangleright InjectionOfCofactorOfCoproductWithGivenCoproduct(D, k, I) (operation)

Returns: a morphism in $Hom(I_k, I)$

The arguments are a list of objects $D = (I_1, \dots, I_n)$, an integer k, and an object $I = \bigsqcup_{i=1}^n I_i$. The output is the k-th injection $\iota_k : I_k \to I$.

6.7.6 UniversalMorphismFromCoproduct (for IsList, IsCapCategoryObject, IsList)

▷ UniversalMorphismFromCoproduct(D, T, tau)

(operation)

Returns: a morphism in $\text{Hom}(\bigsqcup_{i=1}^n I_i, T)$

The arguments are a list of objects $D = (I_1, \ldots, I_n)$, a test object T, and a list of morphisms $\tau = (\tau_i : I_i \to T)$. For convenience, the diagram D and/or the test object T can be omitted and are automatically derived from tau in that case. The output is the morphism $u(\tau) : \bigsqcup_{i=1}^n I_i \to T$ given by the universal property of the coproduct.

6.7.7 UniversalMorphismFromCoproductWithGivenCoproduct (for IsList, IsCap-CategoryObject, IsList, IsCapCategoryObject)

 \triangleright UniversalMorphismFromCoproductWithGivenCoproduct(D, T, tau, I) (operation)

Returns: a morphism in Hom(I,T)

The arguments are a list of objects $D = (I_1, \dots, I_n)$, a test object T, a list of morphisms $\tau = (\tau_i : I_i \to T)$, and an object $I = \bigsqcup_{i=1}^n I_i$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau) : I \to T$ given by the universal property of the coproduct.

6.7.8 CoproductFunctorial (for IsList, IsList, IsList)

 $ightharpoonup ext{CoproductFunctorial}(source_diagram, L, range_diagram) ext{ (operation)}$ $ext{Returns: a morphism in } ext{Hom}(\bigsqcup_{i=1}^{n} I_i, \bigsqcup_{i=1}^{n} I_i')$

The arguments are a list of objects $(I_i)_{i=1...n}$, a list $L=(\mu_1:I_1\to I'_1,\ldots,\mu_n:I_n\to I'_n)$, and a list of objects $(I'_i)_{i=1...n}$. For convenience, $source_diagram$ and $range_diagram$ can be omitted and are automatically derived from L in that case. The output is a morphism $\bigsqcup_{i=1}^n I_i \to \bigsqcup_{i=1}^n I'_i$ given by the functoriality of the coproduct.

6.7.9 CoproductFunctorialWithGivenCoproducts (for IsCapCategoryObject, IsList, IsList, IsCapCategoryObject)

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \bigsqcup_{i=1}^n I_i$, a list of objects $(I_i)_{i=1...n}$, a list $L = (\mu_1 : I_1 \to I'_1, \ldots, \mu_n : I_n \to I'_n)$, a list of objects $(I'_i)_{i=1...n}$, and an object $r = \bigsqcup_{i=1}^n I'_i$. For convenience, source_diagram and range_diagram can be omitted and are automatically derived from L in that case. The output is a morphism $\bigsqcup_{i=1}^n I_i \to \bigsqcup_{i=1}^n I'_i$ given by the functoriality of the coproduct.

6.7.10 ComponentOfMorphismFromCoproduct (for IsCapCategoryMorphism, Is-List, IsInt)

▷ ComponentOfMorphismFromCoproduct(alpha, D, k)

(operation)

Returns: a morphism in $Hom(I_k, A)$

The arguments are a morphism $\alpha: I \to A$, a list $D = (I_1, \dots, I_n)$ of objects with $I = \bigsqcup_{j=1}^n I_j$, and an integer k. The output is the component morphism $I_k \to A$.

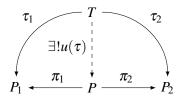
6.8 Direct Product

For an integer $n \ge 1$ and a given list of objects $D = (P_1, \dots, P_n)$, a direct product of D consists of three parts:

- an object P,
- a list of morphisms $\pi = (\pi_i : P \to P_i)_{i=1...n}$
- a dependent function u mapping each list of morphisms $\tau = (\tau_i : T \to P_i)_{i=1,\dots,n}$ to a morphism $u(\tau) : T \to P$ such that $\pi_i \circ u(\tau) \sim_{T,P_i} \tau_i$ for all $i = 1,\dots,n$.

The triple (P, π, u) is called a *direct product* of D if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object P of such a triple by $\prod_{i=1}^{n} P_i$. We say that the morphism $u(\tau)$ is induced by the *universal property of the direct product*.

DirectProduct is a functorial operation. This means: For $(\mu_i : P_i \to P_i')_{i=1...n}$, we obtain a morphism $\prod_{i=1}^n P_i \to \prod_{i=1}^n P_i'$.



6.8.1 DirectProduct

▷ DirectProduct(arg)

(function)

Returns: an object

This is a convenience method. There are two different ways to use this method:

- The argument is a list of objects $D = (P_1, \dots, P_n)$.
- The arguments are objects P_1, \ldots, P_n .

The output is the direct product $\prod_{i=1}^{n} P_i$.

6.8.2 DirectProductOp (for IsList)

▷ DirectProductOp(D)

(operation)

Returns: an object

The argument is a list of objects $D = (P_1, \dots, P_n)$. The output is the direct product $\prod_{i=1}^n P_i$.

6.8.3 ProjectionInFactorOfDirectProduct (for IsList, IsInt)

 \triangleright ProjectionInFactorOfDirectProduct(D, k)

(operation)

Returns: a morphism in $\text{Hom}(\prod_{i=1}^n P_i, P_k)$

The arguments are a list of objects $D=(P_1,\ldots,P_n)$ and an integer k. The output is the k-th projection $\pi_k:\prod_{i=1}^n P_i\to P_k$.

6.8.4 ProjectionInFactorOfDirectProductWithGivenDirectProduct (for IsList, IsInt, IsCapCategoryObject)

 \triangleright ProjectionInFactorOfDirectProductWithGivenDirectProduct(D, k, P) (operation)

Returns: a morphism in Hom(P, P_k)

The arguments are a list of objects $D = (P_1, \dots, P_n)$, an integer k, and an object $P = \prod_{i=1}^n P_i$. The output is the k-th projection $\pi_k : P \to P_k$.

6.8.5 UniversalMorphismIntoDirectProduct (for IsList, IsCapCategoryObject, IsList)

▷ UniversalMorphismIntoDirectProduct(D, T, tau)

(operation)

Returns: a morphism in $\text{Hom}(T, \prod_{i=1}^n P_i)$

The arguments are a list of objects $D = (P_1, \dots, P_n)$, a test object T, and a list of morphisms $\tau = (\tau_i : T \to P_i)_{i=1,\dots,n}$. For convenience, the diagram D and/or the test object T can be omitted and are automatically derived from tau in that case. The output is the morphism $u(\tau) : T \to \prod_{i=1}^n P_i$ given by the universal property of the direct product.

6.8.6 UniversalMorphismIntoDirectProductWithGivenDirectProduct (for IsList, Is-CapCategoryObject, IsList, IsCapCategoryObject)

 \triangleright UniversalMorphismIntoDirectProductWithGivenDirectProduct(D, T, tau, P) (operation)

Returns: a morphism in $\text{Hom}(T, \prod_{i=1}^n P_i)$

The arguments are a list of objects $D=(P_1,\ldots,P_n)$, a test object T, a list of morphisms $\tau=(\tau_i:T\to P_i)_{i=1,\ldots,n}$, and an object $P=\prod_{i=1}^n P_i$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau):T\to\prod_{i=1}^n P_i$ given by the universal property of the direct product.

6.8.7 DirectProductFunctorial (for IsList, IsList, IsList)

 \triangleright DirectProductFunctorial(source_diagram, L, range_diagram) (operation) **Returns:** a morphism in Hom($\prod_{i=1}^{n} P_i, \prod_{i=1}^{n} P_i'$)

The arguments are a list of objects $(P_i)_{i=1...n}$, a list of morphisms $L=(\mu_i:P_i\to P_i')_{i=1...n}$, and a list of objects $(P_i')_{i=1...n}$. For convenience, $source_diagram$ and $range_diagram$ can be omitted and are automatically derived from L in that case. The output is a morphism $\prod_{i=1}^n P_i \to \prod_{i=1}^n P_i'$ given by the functoriality of the direct product.

6.8.8 DirectProductFunctorialWithGivenDirectProducts (for IsCapCategoryObject, IsList, IsList, IsCapCategoryObject)

 $\label{eq:continuous} $$ $$ $$ DirectProductFunctorialWithGivenDirectProducts(s, source_diagram, L, range_diagram, r) $$ $$ $$ $$ $$ (operation) $$$

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \prod_{i=1}^n P_i$, a list of objects $(P_i)_{i=1...n}$, a list of morphisms $L = (\mu_i : P_i \to P_i')_{i=1...n}$, a list of objects $(P_i')_{i=1...n}$, and an object $r = \prod_{i=1}^n P_i'$. For convenience, source_diagram and range_diagram can be omitted and are automatically derived from L in that case. The output is a morphism $\prod_{i=1}^n P_i \to \prod_{i=1}^n P_i'$ given by the functoriality of the direct product.

6.8.9 ComponentOfMorphismIntoDirectProduct (for IsCapCategoryMorphism, IsList, IsInt)

▷ ComponentOfMorphismIntoDirectProduct(alpha, D, k)

(operation)

Returns: a morphism in $Hom(A, P_k)$

The arguments are a morphism $\alpha: A \to P$, a list $D = (P_1, \dots, P_n)$ of objects with $P = \prod_{j=1}^n P_j$, and an integer k. The output is the component morphism $A \to P_k$.

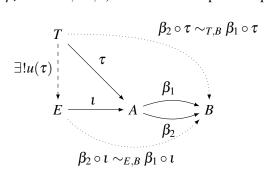
6.9 Equalizer

For an integer $n \ge 1$ and a given list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$, an equalizer of D consists of three parts:

- an object E,
- a morphism $\iota : E \to A$ such that $\beta_i \circ \iota \sim_{E,B} \beta_i \circ \iota$ for all pairs i, j.
- a dependent function u mapping each morphism $\tau = (\tau : T \to A)$ such that $\beta_i \circ \tau \sim_{T,B} \beta_j \circ \tau$ for all pairs i, j to a morphism $u(\tau) : T \to E$ such that $\iota \circ u(\tau) \sim_{T,A} \tau$.

The triple (E, ι, u) is called an *equalizer* of D if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object E of such a triple by Equalizer(D). We say that the morphism $u(\tau)$ is induced by the *universal property of the equalizer*.

Equalizer is a functorial operation. This means: For a second diagram $D' = (\beta_i' : A' \to B')_{i=1...n}$ and a natural morphism between equalizer diagrams (i.e., a collection of morphisms $\mu : A \to A'$ and $\beta : B \to B'$ such that $\beta_i' \circ \mu \sim_{A,B'} \beta \circ \beta_i$ for i = 1,...,n) we obtain a morphism Equalizer(D) \to Equalizer(D').



6.9.1 Equalizer

Returns: an object

This is a convenience method. There are three different ways to use this method:

- The arguments are an object A and a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$.
- The argument is a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$.
- The arguments are morphisms $\beta_1: A \to B, \dots, \beta_n: A \to B$.

The output is the equalizer Equalizer (D).

6.9.2 EqualizerOp (for IsCapCategoryObject, IsList)

▷ EqualizerOp(A, D)

(operation)

Returns: an object

The arguments are an object A and list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$. For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the equalizer Equalizer (D).

6.9.3 EmbeddingOfEqualizer (for IsCapCategoryObject, IsList)

▷ EmbeddingOfEqualizer(A, D)

(operation)

Returns: a morphism in Hom(Equalizer(D), A)

The arguments are an object A and a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$. For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the equalizer embedding ι : Equalizer(D) $\to A$.

6.9.4 EmbeddingOfEqualizerWithGivenEqualizer (for IsCapCategoryObject, IsList, IsCapCategoryObject)

▷ EmbeddingOfEqualizerWithGivenEqualizer(A, D, E)

(operation)

Returns: a morphism in Hom(E,A)

The arguments are an object A, a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$, and an object E = Equalizer(D). For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the equalizer embedding $\iota : E \to A$.

6.9.5 MorphismFromEqualizerToSink (for IsCapCategoryObject, IsList)

▷ MorphismFromEqualizerToSink(A, D)

(operation)

Returns: a morphism in Hom(Equalizer(D), B)

The arguments are an object A and a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$. For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the composition μ : Equalizer(D) $\to B$ of the embedding ι : Equalizer(D) $\to A$ and β_1 .

6.9.6 MorphismFromEqualizerToSinkWithGivenEqualizer (for IsCapCategoryObject, IsList, IsCapCategoryObject)

▷ MorphismFromEqualizerToSinkWithGivenEqualizer(A, D, E)

(operation)

Returns: a morphism in Hom(E, B)

The arguments are an object A, a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$ and an object E = Equalizer(D). For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the composition $\mu : E \to B$ of the embedding $\iota : E \to A$ and β_1 .

6.9.7 UniversalMorphismIntoEqualizer (for IsCapCategoryObject, IsList, IsCapCategoryObject, IsCapCategoryMorphism)

▷ UniversalMorphismIntoEqualizer(A, D, T, tau)

(operation)

Returns: a morphism in Hom(T, Equalizer(D))

The arguments are an object A, a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$, a test object T, and a morphism $\tau : T \to A$ such that $\beta_i \circ \tau \sim_{T,B} \beta_j \circ \tau$ for all pairs i,j. For convenience, the object A can be omitted and is automatically derived from D in that case. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau) : T \to \text{Equalizer}(D)$ given by the universal property of the equalizer.

6.9.8 UniversalMorphismIntoEqualizerWithGivenEqualizer (for IsCapCategoryObject, IsList, IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

 \triangleright UniversalMorphismIntoEqualizerWithGivenEqualizer(A, D, T, tau, E) (operation) **Returns:** a morphism in Hom(T,E)

The arguments are an object A, a list of morphisms $D=(\beta_i:A\to B)_{i=1...n}$, a test object T, a morphism $\tau:T\to A)$ such that $\beta_i\circ\tau\sim_{T,B}\beta_j\circ\tau$ for all pairs i,j, and an object E=Equalizer(D). For convenience, the object A can be omitted and is automatically derived from D in that case. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau):T\to E$ given by the universal property of the equalizer.

6.9.9 EqualizerFunctorial (for IsList, IsCapCategoryMorphism, IsList)

▷ EqualizerFunctorial(Ls, mu, Lr)

(operation)

Returns: a morphism in Hom(Equalizer($(\beta_i)_{i=1...n}$), Equalizer($(\beta'_i)_{i=1...n}$))

The arguments are a list of morphisms $L_s = (\beta_i : A \to B)_{i=1...n}$, a morphism $\mu : A \to A'$, and a list of morphisms $L_r = (\beta_i' : A' \to B')_{i=1...n}$ such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \mu \sim_{A,B'} \beta \circ \beta_i$ for $i = 1, \ldots, n$. The output is the morphism Equalizer $((\beta_i)_{i=1...n}) \to \text{Equalizer}((\beta_i')_{i=1...n})$ given by the functorality of the equalizer.

6.9.10 EqualizerFunctorialWithGivenEqualizers (for IsCapCategoryObject, IsList, IsCapCategoryMorphism, IsList, IsCapCategoryObject)

 \triangleright EqualizerFunctorialWithGivenEqualizers(s, Ls, mu, Lr, r) (operation)

Returns: a morphism in Hom(s,r)

The arguments are an object $s = \text{Equalizer}((\beta_i)_{i=1...n})$, a list of morphisms $L_s = (\beta_i : A \to B)_{i=1...n}$, a morphism $\mu : A \to A'$, and a list of morphisms $L_r = (\beta_i' : A' \to B')_{i=1...n}$ such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \mu \sim_{A,B'} \beta \circ \beta_i$ for $i = 1, \ldots, n$, and an object $r = \text{Equalizer}((\beta_i')_{i=1...n})$. The output is the morphism $s \to r$ given by the functorality of the equalizer.

6.9.11 JointPairwiseDifferencesOfMorphismsIntoDirectProduct (for IsCapCategory-Object, IsList)

 $\verb| DointPairwiseDifferencesOfMorphismsIntoDirectProduct(A, D) \\ \textbf{Returns:} \ \ a \ morphism \ in \ Hom(A, \prod_{i=1}^{n-1} B)$

The arguments are an object A and a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$. The output is a morphism $A \to \prod_{i=1}^{n-1} B$ such that its kernel equalizes the β_i .

6.9.12 IsomorphismFromEqualizerToKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectPro (for IsCapCategoryObject, IsList)

Returns: a morphism in Hom(Equalizer(D), Δ)

The arguments are an object A and a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$. The output is a morphism Equalizer(D) $\to \Delta$, where Δ denotes the kernel object equalizing the morphisms β_i .

6.9.13 IsomorphismFromKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProductToEqua (for IsCapCategoryObject, IsList)

▷ IsomorphismFromKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProductToEqualizer(A, D)
(operation)

Returns: a morphism in $Hom(\Delta, Equalizer(D))$

The arguments are an object A and a list of morphisms $D = (\beta_i : A \to B)_{i=1...n}$. The output is a morphism $\Delta \to \text{Equalizer}(D)$, where Δ denotes the kernel object equalizing the morphisms β_i .

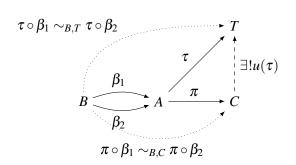
6.10 Coequalizer

For an integer $n \ge 1$ and a given list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$, a coequalizer of D consists of three parts:

- an object C,
- a morphism $\pi: A \to C$ such that $\pi \circ \beta_i \sim_{B,C} \pi \circ \beta_j$ for all pairs i, j,
- a dependent function u mapping the morphism $\tau: A \to T$ such that $\tau \circ \beta_i \sim_{B,T} \tau \circ \beta_j$ to a morphism $u(\tau): C \to T$ such that $u(\tau) \circ \pi \sim_{A,T} \tau$.

The triple (C, π, u) is called a *coequalizer* of D if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object C of such a triple by Coequalizer(D). We say that the morphism $u(\tau)$ is induced by the *universal property of the coequalizer*.

Coequalizer is a functorial operation. This means: For a second diagram $D' = (\beta_i' : B' \to A')_{i=1...n}$ and a natural morphism between coequalizer diagrams (i.e., a collection of morphisms $\mu : A \to A'$ and $\beta : B \to B'$ such that $\beta_i' \circ \beta \sim_{B,A'} \mu \circ \beta_i$ for i = 1,...n) we obtain a morphism Coequalizer(D) \to Coequalizer(D').



6.10.1 Coequalizer

▷ Coequalizer(arg) (function)

Returns: an object

This is a convenience method. There are three different ways to use this method:

- The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$.
- The argument is a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$.
- The arguments are morphisms $\beta_1: B \to A, \dots, \beta_n: B \to A$.

The output is the coequalizer Coequalizer (D).

6.10.2 CoequalizerOp (for IsCapCategoryObject, IsList)

▷ CoequalizerOp(A, D)

Returns: an object

The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$. For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the coequalizer Coequalizer (D).

6.10.3 ProjectionOntoCoequalizer (for IsCapCategoryObject, IsList)

▷ ProjectionOntoCoequalizer(A, D)

(operation)

(operation)

Returns: a morphism in Hom(A, Coequalizer(D)).

The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$. For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the projection $\pi : A \to \text{Coequalizer}(D)$.

6.10.4 ProjectionOntoCoequalizerWithGivenCoequalizer (for IsCapCategoryObject, IsList, IsCapCategoryObject)

▷ ProjectionOntoCoequalizerWithGivenCoequalizer(A, D, C)

(operation)

Returns: a morphism in Hom(A, C).

The arguments are an object A, a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$, and an object C = Coequalizer(D). For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the projection $\pi : A \to C$.

6.10.5 MorphismFromSourceToCoequalizer (for IsCapCategoryObject, IsList)

▷ MorphismFromSourceToCoequalizer(A, D)

(operation)

Returns: a morphism in Hom(B, Coequalizer(D)).

The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$. For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the composition $\mu : B \to \text{Coequalizer}(D)$ of β_1 and the projection $\pi : A \to \text{Coequalizer}(D)$.

6.10.6 MorphismFromSourceToCoequalizerWithGivenCoequalizer (for IsCapCategoryObject, IsList, IsCapCategoryObject)

 \triangleright MorphismFromSourceToCoequalizerWithGivenCoequalizer(A, D, C) (operation) **Returns:** a morphism in Hom(B,C).

The arguments are an object A, a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$ and an object C = Coequalizer(D). For convenience, the object A can be omitted and is automatically derived from D in that case. The output is the composition $\mu : B \to C$ of β_1 and the projection $\pi : A \to C$.

6.10.7 UniversalMorphismFromCoequalizer (for IsCapCategoryObject, IsList, Is-CapCategoryObject, IsCapCategoryMorphism)

 \triangleright UniversalMorphismFromCoequalizer(A, D, T, tau)

(operation)

Returns: a morphism in Hom(Coequalizer(D), T)

The arguments are an object A, a list of morphisms $D=(\beta_i:B\to A)_{i=1...n}$, a test object T, and a morphism $\tau:A\to T$ such that $\tau\circ\beta_i\sim_{B,T}\tau\circ\beta_j$ for all pairs i,j. For convenience, the object A can be omitted and is automatically derived from D in that case. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau)$: Coequalizer(D) $\to T$ given by the universal property of the coequalizer.

ightharpoonup UniversalMorphismFromCoequalizerWithGivenCoequalizer(A, D, T, tau, C) (operation) Returns: a morphism in $\operatorname{Hom}(C,T)$

The arguments are an object A, a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$, a test object T, a morphism $\tau : A \to T$ such that $\tau \circ \beta_i \sim_{B,T} \tau \circ \beta_j$, and an object C = Coequalizer(D). For convenience, the object A can be omitted and is automatically derived from D in that case. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau) : C \to T$ given by the universal property of the coequalizer.

6.10.9 CoequalizerFunctorial (for IsList, IsCapCategoryMorphism, IsList)

▷ CoequalizerFunctorial(Ls, mu, Lr)

(operation)

Returns: a morphism in Hom(Coequalizer($(\beta_i)_{i=1...n}$), Coequalizer($(\beta'_i)_{i=1...n}$))

The arguments are a list of morphisms $L_s = (\beta_i : B \to A)_{i=1...n}$, a morphism $\mu : A \to A'$, and a list of morphisms $L_r = (\beta_i' : B' \to A')_{i=1...n}$ such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \beta \sim_{B,A'} \mu \circ \beta_i$ for i = 1, ... n. The output is the morphism Coequalizer $((\beta_i)_{i=1}^n) \to \text{Coequalizer}((\beta_i')_{i=1}^n)$ given by the functorality of the coequalizer.

6.10.10 CoequalizerFunctorialWithGivenCoequalizers (for IsCapCategoryObject, IsList, IsCapCategoryMorphism, IsList, IsCapCategoryObject)

 \triangleright CoequalizerFunctorialWithGivenCoequalizers(s, Ls, mu, Lr, r) (operation)

Returns: a morphism in Hom(s,r)

The arguments are an object $s = \text{Coequalizer}((\beta_i)_{i=1}^n)$, a list of morphisms $L_s = (\beta_i : B \to A)_{i=1...n}$, a morphism $\mu : A \to A'$, and a list of morphisms $L_r = (\beta_i' : B' \to A')_{i=1...n}$ such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \beta \sim_{B,A'} \mu \circ \beta_i$ for i = 1,...n, and an object $r = \text{Coequalizer}((\beta_i')_{i=1}^n)$. The output is the morphism $s \to r$ given by the functorality of the coequalizer.

6.10.11 JointPairwiseDifferencesOfMorphismsFromCoproduct (for IsCapCategory-Object, IsList)

ightharpoonup JointPairwiseDifferencesOfMorphismsFromCoproduct(A, D) (operation)

Returns: a morphism in $\operatorname{Hom}(\bigsqcup_{i=1}^{n-1} B, A)$

The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$. The output is a morphism $\bigcup_{i=1}^{n-1} B \to A$ such that its cokernel coequalizes the β_i .

6.10.12 IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCo (for IsCapCategoryObject, IsList)

 $\verb|> IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproduct(A, D)| (operation)$

Returns: a morphism in Hom(Coequalizer(D), Δ)

The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$. The output is a morphism Coequalizer(D) $\to \Delta$, where Δ denotes the cokernel object coequalizing the morphisms β_i .

6.10.13 IsomorphismFromCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproductToCoe (for IsCapCategoryObject, IsList)

 $\verb|> IsomorphismFromCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproductToCoequalizer(A,D)| (operation)$

Returns: a morphism in $Hom(\Delta, Coequalizer(D))$

The arguments are an object A and a list of morphisms $D = (\beta_i : B \to A)_{i=1...n}$. The output is a morphism $\Delta \to \text{Coequalizer}(D)$, where Δ denotes the cokernel object coequalizing the morphisms β_i .

6.11 Fiber Product

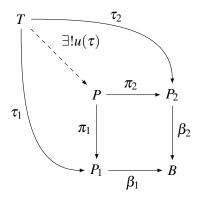
For an integer $n \ge 1$ and a given list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$, a fiber product of D consists of three parts:

- an object P,
- a list of morphisms $\pi = (\pi_i : P \to P_i)_{i=1...n}$ such that $\beta_i \circ \pi_i \sim_{P,B} \beta_j \circ \pi_j$ for all pairs i, j.
- a dependent function u mapping each list of morphisms $\tau = (\tau_i : T \to P_i)$ such that $\beta_i \circ \tau_i \sim_{T,B} \beta_i \circ \tau_j$ for all pairs i, j to a morphism $u(\tau) : T \to P$ such that $\pi_i \circ u(\tau) \sim_{T,P_i} \tau_i$ for all $i = 1, \dots, n$.

The triple (P, π, u) is called a *fiber product* of D if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object P of such a triple by FiberProduct(D). We say that the morphism $u(\tau)$ is induced by the *universal property of the fiber product*.

FiberProduct is a functorial operation. This means: For a second diagram $D' = (\beta_i' : P_i' \to B')_{i=1...n}$ and a natural morphism between pullback diagrams (i.e., a collection of morphisms $(\mu_i : P_i \to P_i')_{i=1...n}$

and $\beta: B \to B'$ such that $\beta'_i \circ \mu_i \sim_{P_i, B'} \beta \circ \beta_i$ for i = 1, ..., n) we obtain a morphism FiberProduct(D').



6.11.1 IsomorphismFromFiberProductToEqualizerOfDirectProductDiagram (for Is-List)

 $\verb| IsomorphismFromFiberProductToEqualizerOfDirectProductDiagram({\it D}) \\ \textbf{Returns:} \ \ a \ morphism \ in \ Hom(FiberProduct({\it D}), \Delta) \\ | \\$

The argument is a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$. The output is a morphism FiberProduct $(D) \to \Delta$, where Δ denotes the equalizer of the product diagram of the morphisms β_i .

6.11.2 IsomorphismFromEqualizerOfDirectProductDiagramToFiberProduct (for Is-List)

 $\verb| Discrete From Equalizer Of Direct Product Diagram To Fiber Product (\textit{D}) \\ \textbf{Returns:} \ \ a \ morphism \ in \ Hom(\Delta, Fiber Product(D)) \\ \end{aligned}$

The argument is a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$. The output is a morphism $\Delta \to \text{FiberProduct}(D)$, where Δ denotes the equalizer of the product diagram of the morphisms β_i .

6.11.3 FiberProductEmbeddingInDirectProduct (for IsList)

▷ FiberProductEmbeddingInDirectProduct(D)

(operation)

Returns: a morphism in Hom(FiberProduct(D), $\prod_{i=1}^{n} P_i$)

This is a convenience method. The argument is a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$. The output is the natural embedding FiberProduct $(D) \to \prod_{i=1}^n P_i$.

6.11.4 FiberProductEmbeddingInDirectSum (for IsList)

FiberProductEmbeddingInDirectSum(D)

(operation)

Returns: a morphism in Hom(FiberProduct(D), $\bigoplus_{i=1}^{n} P_i$)

This is a convenience method. The argument is a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$. The output is the natural embedding FiberProduct $(D) \to \bigoplus_{i=1}^n P_i$.

6.11.5 FiberProduct

▶ FiberProduct(arg)
Returns: an object

(function)

This is a convenience method. There are two different ways to use this method:

- The argument is a list of morphisms $D = (\beta_i : P_i \rightarrow B)_{i=1...n}$.
- The arguments are morphisms $\beta_1: P_1 \to B, \dots, \beta_n: P_n \to B$.

The output is the fiber product FiberProduct(D).

6.11.6 FiberProductOp (for IsList)

▷ FiberProductOp(D)

(operation)

Returns: an object

The argument is a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$. The output is the fiber product FiberProduct(D).

6.11.7 ProjectionInFactorOfFiberProduct (for IsList, IsInt)

▷ ProjectionInFactorOfFiberProduct(D, k)

(operation)

Returns: a morphism in Hom(FiberProduct(D), P_k)

The arguments are a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$ and an integer k. The output is the k-th projection π_k : FiberProduct $(D) \to P_k$.

6.11.8 ProjectionInFactorOfFiberProductWithGivenFiberProduct (for IsList, IsInt, IsCapCategoryObject)

ightharpoonup ProjectionInFactorOfFiberProductWithGivenFiberProduct(D, k, P) (operation)

Returns: a morphism in Hom(P, P_k)

The arguments are a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$, an integer k, and an object P = FiberProduct(D). The output is the k-th projection $\pi_k : P \to P_k$.

6.11.9 MorphismFromFiberProductToSink (for IsList)

(operation)

Returns: a morphism in Hom(FiberProduct(D), B)

The arguments are a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$. The output is the composition μ : FiberProduct $(D) \to B$ of the 1-st projection π_1 : FiberProduct $(D) \to P_1$ and β_1 .

6.11.10 MorphismFromFiberProductToSinkWithGivenFiberProduct (for IsList, Is-CapCategoryObject)

→ MorphismFromFiberProductToSinkWithGivenFiberProduct(D, P)

(operation)

Returns: a morphism in Hom(P, B)

The arguments are a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$ and an object P = FiberProduct(D). The output is the composition $\mu : P \to B$ of the 1-st projection $\pi_1 : P \to P_1$ and β_1 .

6.11.11 UniversalMorphismIntoFiberProduct (for IsList, IsCapCategoryObject, Is-List)

 \triangleright UniversalMorphismIntoFiberProduct(D, T, tau)

(operation)

Returns: a morphism in Hom(T, FiberProduct(D))

The arguments are a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$, a test object T, and a list of morphisms $\tau = (\tau_i : T \to P_i)$ such that $\beta_i \circ \tau_i \sim_{T,B} \beta_j \circ \tau_j$ for all pairs i, j. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau) : T \to \text{FiberProduct}(D)$ given by the universal property of the fiber product.

6.11.12 UniversalMorphismIntoFiberProductWithGivenFiberProduct (for IsList, Is-CapCategoryObject, IsList, IsCapCategoryObject)

 \triangleright UniversalMorphismIntoFiberProductWithGivenFiberProduct(D, T, tau, P) (operation) **Returns:** a morphism in Hom(T,P)

The arguments are a list of morphisms $D = (\beta_i : P_i \to B)_{i=1...n}$, a test object T, a list of morphisms $\tau = (\tau_i : T \to P_i)$ such that $\beta_i \circ \tau_i \sim_{T,B} \beta_j \circ \tau_j$ for all pairs i, j, and an object P = FiberProduct(D). For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau) : T \to P$ given by the universal property of the fiber product.

6.11.13 FiberProductFunctorial (for IsList, IsList, IsList)

▷ FiberProductFunctorial(Ls, Lm, Lr)

(operation)

Returns: a morphism in Hom(FiberProduct($(\beta_i)_{i=1...n}$), FiberProduct($(\beta_i')_{i=1...n}$))

The arguments are three lists of morphisms $L_s = (\beta_i : P_i \to B)_{i=1...n}$, $L_m = (\mu_i : P_i \to P_i')_{i=1...n}$, $L_r = (\beta_i' : P_i' \to B')_{i=1...n}$ having the same length n such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \mu_i \sim_{P_i,B'} \beta \circ \beta_i$ for i = 1,...,n. The output is the morphism FiberProduct $((\beta_i')_{i=1...n})$ given by the functoriality of the fiber product.

6.11.14 FiberProductFunctorialWithGivenFiberProducts (for IsCapCategoryObject, IsList, IsList, IsList, IsCapCategoryObject)

 $\verb| FiberProductFunctorialWithGivenFiberProducts(s, Ls, Lm, Lr, r) \\ \textbf{Returns:} \ \ \text{a morphism in } \text{Hom}(s,r) \\ \end{aligned}$

The arguments are an object $s = \text{FiberProduct}((\beta_i)_{i=1...n})$, three lists of morphisms $L_s = (\beta_i : P_i \to B)_{i=1...n}$, $L_m = (\mu_i : P_i \to P_i')_{i=1...n}$, $L_r = (\beta_i' : P_i' \to B')_{i=1...n}$ having the same length n such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \mu_i \sim_{P_i,B'} \beta \circ \beta_i$ for $i = 1, \ldots, n$, and an object $r = \text{FiberProduct}((\beta_i')_{i=1...n})$. The output is the morphism $s \to r$ given by the functoriality of the fiber product.

6.12 Pushout

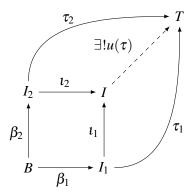
For an integer $n \ge 1$ and a given list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$, a pushout of D consists of three parts:

- an object *I*,
- a list of morphisms $\iota = (\iota_i : I_i \to I)_{i=1...n}$ such that $\iota_i \circ \beta_i \sim_{B,I} \iota_i \circ \beta_i$ for all pairs i, j, j

• a dependent function u mapping each list of morphisms $\tau = (\tau_i : I_i \to T)_{i=1...n}$ such that $\tau_i \circ \beta_i \sim_{B,T} \tau_i \circ \beta_i$ to a morphism $u(\tau) : I \to T$ such that $u(\tau) \circ \iota_i \sim_{I_i,T} \tau_i$ for all i = 1, ..., n.

The triple (I, ι, u) is called a *pushout* of D if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object I of such a triple by Pushout(D). We say that the morphism $u(\tau)$ is induced by the *universal property of the pushout*.

Pushout is a functorial operation. This means: For a second diagram $D' = (\beta_i' : B' \to I_i')_{i=1...n}$ and a natural morphism between pushout diagrams (i.e., a collection of morphisms $(\mu_i : I_i \to I_i')_{i=1...n}$ and $\beta : B \to B'$ such that $\beta_i' \circ \beta \sim_{B,I_i'} \mu_i \circ \beta_i$ for i = 1, ...n) we obtain a morphism Pushout $(D) \to \text{Pushout}(D')$.



6.12.1 IsomorphismFromPushoutToCoequalizerOfCoproductDiagram (for IsList)

□ IsomorphismFromPushoutToCoequalizerOfCoproductDiagram(D)

(operation)

Returns: a morphism in $Hom(Pushout(D), \Delta)$

The argument is a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$. The output is a morphism Pushout $(D) \to \Delta$, where Δ denotes the coequalizer of the coproduct diagram of the morphisms β_i .

6.12.2 IsomorphismFromCoequalizerOfCoproductDiagramToPushout (for IsList)

(operation)

Returns: a morphism in $Hom(\Delta, Pushout(D))$

The argument is a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$. The output is a morphism $\Delta \to \text{Pushout}(D)$, where Δ denotes the coequalizer of the coproduct diagram of the morphisms β_i .

6.12.3 PushoutProjectionFromCoproduct (for IsList)

PushoutProjectionFromCoproduct(D)

(operation)

Returns: a morphism in $\text{Hom}(\bigsqcup i = 1^n I_i, \text{Pushout}(D))$

This is a convenience method. The argument is a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$. The output is the natural projection $\bigsqcup_{i=1}^n I_i \to \text{Pushout}(D)$.

6.12.4 PushoutProjectionFromDirectSum (for IsList)

PushoutProjectionFromDirectSum(D)

(operation)

Returns: a morphism in $\text{Hom}(\bigoplus_{i=1}^n I_i, \text{Pushout}(D))$

This is a convenience method. The argument is a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$. The output is the natural projection $\bigoplus_{i=1}^n I_i \to \text{Pushout}(D)$.

Pushout (for IsList) 6.12.5

▷ Pushout(D) (operation)

Returns: an object

The argument is a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$. The output is the pushout Pushout (D).

6.12.6 Pushout (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ Pushout(D) (operation)

Returns: an object

This is a convenience method. The arguments are a morphism α and a morphism β . The output is the pushout Pushout (α, β) .

6.12.7 InjectionOfCofactorOfPushout (for IsList, IsInt)

▷ InjectionOfCofactorOfPushout(D, k)

(operation)

Returns: a morphism in $Hom(I_k, Pushout(D))$.

The arguments are a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$ and an integer k. The output is the k-th injection $\iota_k: I_k \to \operatorname{Pushout}(D)$.

InjectionOfCofactorOfPushoutWithGivenPushout (for IsList, IsInt, IsCapCat-6.12.8 egoryObject)

▷ InjectionOfCofactorOfPushoutWithGivenPushout(D, k, I)

(operation)

Returns: a morphism in $Hom(I_k, I)$.

The arguments are a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$, an integer k, and an object I =Pushout(*D*). The output is the *k*-th injection $\iota_k : I_k \to I$.

6.12.9 MorphismFromSourceToPushout (for IsList)

▷ MorphismFromSourceToPushout(D)

(operation)

Returns: a morphism in Hom(B, Pushout(D)).

The arguments are a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$. The output is the composition $\mu: B \to \operatorname{Pushout}(D)$ of β_1 and the 1-st injection $\iota_1: I_1 \to \operatorname{Pushout}(D)$.

6.12.10 MorphismFromSourceToPushoutWithGivenPushout (for IsList, IsCapCategoryObject)

▷ MorphismFromSourceToPushoutWithGivenPushout(D, I)

(operation)

Returns: a morphism in Hom(B, I).

The arguments are a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$ and an object I = Pushout(D). The output is the composition $\mu: B \to I$ of β_1 and the 1-st injection $\iota_1: I_1 \to I$.

6.12.11 UniversalMorphismFromPushout (for IsList, IsCapCategoryObject, IsList)

▷ UniversalMorphismFromPushout(D, T, tau)

(operation)

Returns: a morphism in Hom(Pushout(D), T)

The arguments are a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$, a test object T, and a list of morphisms $\tau = (\tau_i : I_i \to T)_{i=1...n}$ such that $\tau_i \circ \beta_i \sim_{B,T} \tau_j \circ \beta_j$. For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau)$: Pushout(D) $\to T$ given by the universal property of the pushout.

6.12.12 UniversalMorphismFromPushoutWithGivenPushout (for IsList, IsCapCategoryObject, IsList, IsCapCategoryObject)

ightharpoonup UniversalMorphismFromPushoutWithGivenPushout(D, T, tau, I) (operation)

Returns: a morphism in Hom(I,T)

The arguments are a list of morphisms $D = (\beta_i : B \to I_i)_{i=1...n}$, a test object T, a list of morphisms $\tau = (\tau_i : I_i \to T)_{i=1...n}$ such that $\tau_i \circ \beta_i \sim_{B,T} \tau_j \circ \beta_j$, and an object I = Pushout(D). For convenience, the test object T can be omitted and is automatically derived from tau in that case. The output is the morphism $u(\tau) : I \to T$ given by the universal property of the pushout.

6.12.13 PushoutFunctorial (for IsList, IsList, IsList)

▷ PushoutFunctorial(Ls, Lm, Lr)

(operation)

Returns: a morphism in Hom(Pushout($(\beta_i)_{i=1}^n$), Pushout($(\beta_i')_{i=1}^n$))

The arguments are three lists of morphisms $L_s = (\beta_i : B \to I_i)_{i=1...n}$, $L_m = (\mu_i : I_i \to I_i')_{i=1...n}$, $L_r = (\beta_i' : B' \to I_i')_{i=1...n}$ having the same length n such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \beta \sim_{B,I_i'} \mu_i \circ \beta_i$ for i=1,...n. The output is the morphism $Pushout((\beta_i)_{i=1}^n) \to Pushout((\beta_i')_{i=1}^n)$ given by the functoriality of the pushout.

6.12.14 PushoutFunctorialWithGivenPushouts (for IsCapCategoryObject, IsList, IsList, IsCapCategoryObject)

 \triangleright PushoutFunctorialWithGivenPushouts(s, Ls, Lm, Lr, r) (operation) **Returns:** a morphism in Hom(s,r)

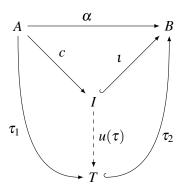
The arguments are an object $s = \operatorname{Pushout}((\beta_i)_{i=1}^n)$, three lists of morphisms $L_s = (\beta_i : B \to I_i)_{i=1...n}$, $L_m = (\mu_i : I_i \to I_i')_{i=1...n}$, $L_r = (\beta_i' : B' \to I_i')_{i=1...n}$ having the same length n such that there exists a morphism $\beta : B \to B'$ such that $\beta_i' \circ \beta \sim_{B,I_i'} \mu_i \circ \beta_i$ for $i=1,\ldots n$, and an object $r = \operatorname{Pushout}((\beta_i')_{i=1}^n)$. The output is the morphism $s \to r$ given by the functoriality of the pushout.

6.13 Image

For a given morphism $\alpha : A \to B$, an image of α consists of four parts:

- an object I,
- a morphism $c: A \to I$,
- a monomorphism $\iota: I \hookrightarrow B$ such that $\iota \circ c \sim_{A,B} \alpha$,
- a dependent function u mapping each pair of morphisms $\tau = (\tau_1 : A \to T, \tau_2 : T \hookrightarrow B)$ where τ_2 is a monomorphism such that $\tau_2 \circ \tau_1 \sim_{A,B} \alpha$ to a morphism $u(\tau) : I \to T$ such that $\tau_2 \circ u(\tau) \sim_{I,B} \iota$ and $u(\tau) \circ c \sim_{A,T} \tau_1$.

The 4-tuple (I, c, ι, u) is called an *image* of α if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object I of such a 4-tuple by $\operatorname{im}(\alpha)$. We say that the morphism $u(\tau)$ is induced by the *universal property of the image*.



6.13.1 IsomorphismFromImageObjectToKernelOfCokernel (for IsCapCategoryMorphism)

□ IsomorphismFromImageObjectToKernelOfCokernel(alpha)

(attribute)

Returns: a morphism in $Hom(im(\alpha), KernelObject(CokernelProjection(\alpha)))$

The argument is a morphism α . The output is the canonical morphism $\operatorname{im}(\alpha) \to \operatorname{KernelObject}(\operatorname{CokernelProjection}(\alpha))$.

6.13.2 IsomorphismFromKernelOfCokernelToImageObject (for IsCapCategoryMorphism)

▷ IsomorphismFromKernelOfCokernelToImageObject(alpha)

(attribute)

Returns: a morphism in Hom(KernelObject(CokernelProjection(α)), im(α))

The argument is a morphism α . The output is the canonical morphism KernelObject(CokernelProjection(α)) \rightarrow im(α).

6.13.3 ImageObject (for IsCapCategoryMorphism)

▷ ImageObject(alpha)

(attribute)

Returns: an object

The argument is a morphism α . The output is the image im(α).

6.13.4 ImageEmbedding (for IsCapCategoryMorphism)

▷ ImageEmbedding(alpha)

(attribute)

Returns: a morphism in $Hom(im(\alpha), B)$

The argument is a morphism $\alpha: A \to B$. The output is the image embedding $\iota: \operatorname{im}(\alpha) \hookrightarrow B$.

6.13.5 ImageEmbeddingWithGivenImageObject (for IsCapCategoryMorphism, IsCapCategoryObject)

 ${\tt \triangleright} \ {\tt ImageEmbeddingWithGivenImageObject(alpha,\ I)}$

(operation)

Returns: a morphism in Hom(I, B)

The argument is a morphism $\alpha : A \to B$ and an object $I = \operatorname{im}(\alpha)$. The output is the image embedding $\iota : I \hookrightarrow B$.

6.13.6 CoastrictionToImage (for IsCapCategoryMorphism)

▷ CoastrictionToImage(alpha)

(attribute)

Returns: a morphism in $Hom(A, im(\alpha))$

The argument is a morphism $\alpha: A \to B$. The output is the coastriction to image $c: A \to \operatorname{im}(\alpha)$.

6.13.7 CoastrictionToImageWithGivenImageObject (for IsCapCategoryMorphism, IsCapCategoryObject)

▷ CoastrictionToImageWithGivenImageObject(alpha, I)

(operation)

Returns: a morphism in Hom(A, I)

The argument is a morphism $\alpha : A \to B$ and an object $I = \operatorname{im}(\alpha)$. The output is the coastriction to image $c : A \to I$.

6.13.8 UniversalMorphismFromImage (for IsCapCategoryMorphism, IsList)

 ${\tt > UniversalMorphismFromImage(alpha,\ tau)}$

(operation)

Returns: a morphism in $Hom(im(\alpha), T)$

The arguments are a morphism $\alpha: A \to B$ and a pair of morphisms $\tau = (\tau_1: A \to T, \tau_2: T \hookrightarrow B)$ where τ_2 is a monomorphism such that $\tau_2 \circ \tau_1 \sim_{A,B} \alpha$. The output is the morphism $u(\tau): \operatorname{im}(\alpha) \to T$ given by the universal property of the image.

6.13.9 UniversalMorphismFromImageWithGivenImageObject (for IsCapCategory-Morphism, IsList, IsCapCategoryObject)

(operation)

Returns: a morphism in Hom(I, T)

The arguments are a morphism $\alpha: A \to B$, a pair of morphisms $\tau = (\tau_1: A \to T, \tau_2: T \hookrightarrow B)$ where τ_2 is a monomorphism such that $\tau_2 \circ \tau_1 \sim_{A,B} \alpha$, and an object $I = \operatorname{im}(\alpha)$. The output is the morphism $u(\tau): \operatorname{im}(\alpha) \to T$ given by the universal property of the image.

6.13.10 ImageObjectFunctorial (for IsCapCategoryMorphism, IsCapCategoryMorphism) IsCapCategoryMorphism)

▷ ImageObjectFunctorial(alpha, nu, alpha_prime)

(operation)

Returns: a morphism in Hom(ImageObject(α), ImageObject(α'))

The arguments are three morphisms $\alpha: A \to B$, $v: B \to B'$, $\alpha': A' \to B'$. The output is the morphism ImageObject(α) \to ImageObject(α') given by the functoriality of the image.

6.13.11 ImageObjectFunctorialWithGivenImageObjects (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

 \triangleright ImageObjectFunctorialWithGivenImageObjects(s, alpha, nu, alpha_prime, r) (operation)

Returns: a morphism in Hom(s, r)

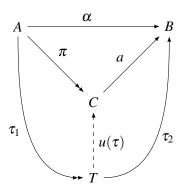
The arguments are an object $s = \text{ImageObject}(\alpha)$, three morphisms $\alpha : A \to B$, $v : B \to B'$, $\alpha' : A' \to B'$, and an object $r = \text{ImageObject}(\alpha')$. The output is the morphism $\text{ImageObject}(\alpha) \to \text{ImageObject}(\alpha')$ given by the functoriality of the image.

6.14 Coimage

For a given morphism $\alpha : A \to B$, a coimage of α consists of four parts:

- an object C,
- an epimorphism $\pi: A \rightarrow C$,
- a morphism $a: C \to B$ such that $a \circ \pi \sim_{AB} \alpha$,
- a dependent function u mapping each pair of morphisms $\tau = (\tau_1 : A \twoheadrightarrow T, \tau_2 : T \to B)$ where τ_1 is an epimorphism such that $\tau_2 \circ \tau_1 \sim_{A,B} \alpha$ to a morphism $u(\tau) : T \to C$ such that $u(\tau) \circ \tau_1 \sim_{A,C} \pi$ and $a \circ u(\tau) \sim_{T,B} \tau_2$.

The 4-tuple (C, π, a, u) is called a *coimage* of α if the morphisms $u(\tau)$ are uniquely determined up to congruence of morphisms. We denote the object C of such a 4-tuple by $\operatorname{coim}(\alpha)$. We say that the morphism $u(\tau)$ is induced by the *universal property of the coimage*.



6.14.1 MorphismFromCoimageToImage (for IsCapCategoryMorphism)

(attribute)

Returns: a morphism in $Hom(coim(\alpha), im(\alpha))$

The argument is a morphism $\alpha : A \to B$. The output is the canonical morphism (in a preabelian category) $coim(\alpha) \to im(\alpha)$.

6.14.2 MorphismFromCoimageToImageWithGivenObjects (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

 $\qquad \qquad \qquad \triangleright \ \, \texttt{MorphismFromCoimageToImageWithGivenObjects(\textit{C}, alpha, I)} \qquad \qquad (operation)$

Returns: a morphism in Hom(C, I)

The argument is an object $C = \text{coim}(\alpha)$, a morphism $\alpha : A \to B$, and an object $I = \text{im}(\alpha)$. The output is the canonical morphism (in a preabelian category) $C \to I$.

6.14.3 InverseOfMorphismFromCoimageToImage (for IsCapCategoryMorphism)

▷ InverseOfMorphismFromCoimageToImage(alpha)

(attribute)

Returns: a morphism in $Hom(im(\alpha), coim(\alpha))$

The argument is a morphism $\alpha : A \to B$. The output is the inverse of the canonical morphism (in an abelian category) $\operatorname{im}(\alpha) \to \operatorname{coim}(\alpha)$.

6.14.4 InverseOfMorphismFromCoimageToImageWithGivenObjects (for IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

 \triangleright InverseOfMorphismFromCoimageToImageWithGivenObjects(I, alpha, C) (operation) Returns: a morphism in Hom(I,C)

The argument is an object $C = \text{coim}(\alpha)$, a morphism $\alpha : A \to B$, and an object $I = \text{im}(\alpha)$. The output is the inverse of the canonical morphism (in an abelian category) $I \to C$.

6.14.5 IsomorphismFromCoimageToCokernelOfKernel (for IsCapCategoryMorphism)

 ${\tt \triangleright} \ \, {\tt IsomorphismFromCoimageToCokernelOfKernel(alpha)}$

(attribute)

Returns: a morphism in $Hom(coim(\alpha), CokernelObject(KernelEmbedding(\alpha))).$

The argument is a morphism $\alpha : A \to B$. The output is the canonical morphism $coim(\alpha) \to CokernelObject(KernelEmbedding(\alpha))$.

6.14.6 IsomorphismFromCokernelOfKernelToCoimage (for IsCapCategoryMorphism)

▷ IsomorphismFromCokernelOfKernelToCoimage(alpha)

(attribute)

Returns: a morphism in Hom(CokernelObject(KernelEmbedding(α)), coim(α)).

The argument is a morphism $\alpha : A \to B$. The output is the canonical morphism CokernelObject(KernelEmbedding(α)) \to coim(α).

6.14.7 CoimageObject (for IsCapCategoryMorphism)

▷ CoimageObject(alpha)

(attribute)

Returns: an object

The argument is a morphism α . The output is the coimage $coim(\alpha)$.

6.14.8 CoimageProjection (for IsCapCategoryMorphism)

ightharpoonup CoimageProjection(alpha)

(attribute)

Returns: a morphism in $Hom(A, coim(\alpha))$

The argument is a morphism $\alpha: A \to B$. The output is the coimage projection $\pi: A \to \operatorname{coim}(\alpha)$.

6.14.9 CoimageProjectionWithGivenCoimageObject (for IsCapCategoryMorphism, IsCapCategoryObject)

 ${\tt \vartriangleright} \ \, {\tt CoimageProjectionWithGivenCoimageObject(alpha, \ C)}$

(operation)

Returns: a morphism in Hom(A, C)

The arguments are a morphism $\alpha : A \to B$ and an object $C = \text{coim}(\alpha)$. The output is the coimage projection $\pi : A \twoheadrightarrow C$.

6.14.10 AstrictionToCoimage (for IsCapCategoryMorphism)

▷ AstrictionToCoimage(alpha)

(attribute)

Returns: a morphism in $Hom(coim(\alpha), B)$

The argument is a morphism $\alpha: A \to B$. The output is the astriction to coimage $a: \text{coim}(\alpha) \to B$.

6.14.11 AstrictionToCoimageWithGivenCoimageObject (for IsCapCategoryMorphism, IsCapCategoryObject)

▷ AstrictionToCoimageWithGivenCoimageObject(alpha, C)

(operation)

Returns: a morphism in Hom(C, B)

The argument are a morphism $\alpha : A \to B$ and an object $C = \text{coim}(\alpha)$. The output is the astriction to coimage $a : C \to B$.

6.14.12 UniversalMorphismIntoCoimage (for IsCapCategoryMorphism, IsList)

▷ UniversalMorphismIntoCoimage(alpha, tau)

(operation)

Returns: a morphism in $Hom(T, coim(\alpha))$

The arguments are a morphism $\alpha: A \to B$ and a pair of morphisms $\tau = (\tau_1: A \twoheadrightarrow T, \tau_2: T \to B)$ where τ_1 is an epimorphism such that $\tau_2 \circ \tau_1 \sim_{A,B} \alpha$. The output is the morphism $u(\tau): T \to \text{coim}(\alpha)$ given by the universal property of the coimage.

6.14.13 UniversalMorphismIntoCoimageWithGivenCoimageObject (for IsCapCategoryMorphism, IsList, IsCapCategoryObject)

 $\verb| DniversalMorphismIntoCoimageWithGivenCoimageObject(alpha, tau, C) \\ \textbf{Returns:} \ \ a \ morphism \ in \ Hom(T,C)$

The arguments are a morphism $\alpha: A \to B$, a pair of morphisms $\tau = (\tau_1: A \twoheadrightarrow T, \tau_2: T \to B)$ where τ_1 is an epimorphism such that $\tau_2 \circ \tau_1 \sim_{A,B} \alpha$, and an object $C = \text{coim}(\alpha)$. The output is the morphism $u(\tau): T \to C$ given by the universal property of the coimage.

Whenever the CoastrictionToImage is an epi, or the AstrictionToCoimage is a mono, there is a canonical morphism from the image to the coimage. If this canonical morphism is an isomorphism, we call it the *canonical identification* (between image and coimage).

6.14.14 CoimageObjectFunctorial (for IsCapCategoryMorphism, IsCapCategoryMorphism) Morphism, IsCapCategoryMorphism)

 ${\tt \vartriangleright} \ {\tt CoimageObjectFunctorial(alpha, mu, alpha_prime)}$

(operation)

Returns: a morphism in Hom(CoimageObject(α), CoimageObject(α'))

The arguments are three morphisms $\alpha: A \to B, \mu: A \to A', \alpha': A' \to B'$. The output is the morphism CoimageObject(α) \to CoimageObject(α') given by the functoriality of the coimage.

6.14.15 CoimageObjectFunctorialWithGivenCoimageObjects (for IsCapCategory-Object, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryObject)

Returns: a morphism in Hom(s, r)

The arguments are an object $s = \text{CoimageObject}(\alpha)$, three morphisms $\alpha : A \to B, \mu : A \to A', \alpha' : A' \to B'$, and an object $r = \text{CoimageObject}(\alpha')$. The output is the morphism $\text{CoimageObject}(\alpha) \to \text{CoimageObject}(\alpha')$ given by the functoriality of the coimage.

6.15 Homology objects

In an abelian category, we can define the operation that takes as an input a pair of morphisms $\alpha : A \to B$, $\beta : B \to C$ and outputs the subquotient of B given by

• $H := \text{KernelObject}(\beta) / (\text{KernelObject}(\beta) \cap \text{ImageObject}(\alpha)).$

This object is called a *homology object* of the pair α, β . Note that we do not need the precomposition of α and β to be zero in order to make sense of this notion. Moreover, given a second pair $\gamma: D \to E$, $\delta: E \to F$ of morphisms, and a morphism $\varepsilon: B \to E$ such that there exists $\omega_1: A \to D$, $\omega_2: C \to F$ with $\varepsilon \circ \alpha \sim_{A,E} \gamma \circ \omega_1$ and $\omega_2 \circ \beta \sim_{B,F} \delta \circ \varepsilon$ there is a functorial way to obtain from these data a morphism between the two corresponding homology objects.

6.15.1 HomologyObject (for IsCapCategoryMorphism, IsCapCategoryMorphism)

⊳ HomologyObject(alpha, beta)

(operation)

Returns: an object

The arguments are two morphisms $\alpha : A \to B, \beta : B \to C$. The output is the homology object H of this pair.

6.15.2 HomologyObjectFunctorial (for IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism, IsCapCategoryMorphism)

ightharpoonup HomologyObjectFunctorial(alpha, beta, epsilon, gamma, delta) (operation) Returns: a morphism in $\operatorname{Hom}(H_1, H_2)$

The argument are five morphisms $\alpha: A \to B$, $\beta: B \to C$, $\varepsilon: B \to E$, $\gamma: D \to E$, $\delta: E \to F$ such that there exists $\omega_1: A \to D$, $\omega_2: C \to F$ with $\varepsilon \circ \alpha \sim_{A,E} \gamma \circ \omega_1$ and $\omega_2 \circ \beta \sim_{B,F} \delta \circ \varepsilon$. The output is the functorial morphism induced by ε between the corresponding homology objects H_1 and H_2 , where H_1 denotes the homology object of the pair α, β , and H_2 denotes the homology object of the pair γ, δ .

6.15.3 HomologyObjectFunctorialWithGivenHomologyObjects (for IsCapCategory-Object, IsList, IsCapCategoryObject)

 \triangleright HomologyObjectFunctorialWithGivenHomologyObjects(H_1 , L, H_2) (operation)

Returns: a morphism in Hom(H_1 , H_2)

The arguments are an object H_1 , a list L consisting of five morphisms $\alpha: A \to B$, $\beta: B \to C$, $\varepsilon: B \to E$, $\gamma: D \to E$, $\delta: E \to F$, and an object H_2 , such that $H_1 = \text{HomologyObject}(\alpha, \beta)$ and $H_2 = \text{HomologyObject}(\gamma, \delta)$, and such that there exists $\omega_1: A \to D$, $\omega_2: C \to F$ with $\varepsilon \circ \alpha \sim_{A,E} \gamma \circ \omega_1$ and $\omega_2 \circ \beta \sim_{B,F} \delta \circ \varepsilon$. The output is the functorial morphism induced by ε between the corresponding homology objects H_1 and H_2 , where H_1 denotes the homology object of the pair α, β , and H_2 denotes the homology object of the pair γ, δ .

6.15.4 IsomorphismFromHomologyObjectToItsConstructionAsAnImageObject (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsomorphismFromHomologyObjectToItsConstructionAsAnImageObject(alpha, beta)

(operation)

Returns: a morphism in Hom(HomologyObject(α, β), I)

The arguments are two morphisms $\alpha: A \to B, \beta: B \to C$. The output is the natural isomorphism from the homology object H of α and β to the construction of the homology object as ImageObject(PreCompose(KernelEmbedding(β), CokernelProjection(α)), denoted by I.

6.15.5 IsomorphismFromItsConstructionAsAnImageObjectToHomologyObject (for IsCapCategoryMorphism, IsCapCategoryMorphism)

▷ IsomorphismFromItsConstructionAsAnImageObjectToHomologyObject(alpha, beta)

(operation)

Returns: a morphism in Hom(I, HomologyObject(α, β))

The arguments are two morphisms $\alpha:A\to B,\beta:B\to C$. The output is the natural isomorphism from the construction of the homology object as ImageObject(PreCompose(KernelEmbedding(β), CokernelProjection(α)), denoted by I, to the homology object H of α and β .

6.16 Projective covers and injective envelopes

6.16.1 ProjectiveCoverObject (for IsCapCategoryObject)

▷ ProjectiveCoverObject(A)

(attribute)

Returns: an object

The argument is an object A. The output is a projective cover of A.

6.16.2 EpimorphismFromProjectiveCoverObject (for IsCapCategoryObject)

 ${\scriptstyle \rhd} \ \, {\tt EpimorphismFromProjectiveCoverObject({\tt A})} \\$

(attribute)

Returns: an epimorphism

The argument is an object A. The output is an epimorphism from a projective cover of A.

6.16.3 EpimorphismFromProjectiveCoverObjectWithGivenProjectiveCoverObject (for IsCapCategoryObject, IsCapCategoryObject)

 \triangleright EpimorphismFromProjectiveCoverObjectWithGivenProjectiveCoverObject(A, P) (operation)

Returns: an epimorphism

The argument is an object A. The output is the epimorphism from the projective cover P of A.

6.16.4 InjectiveEnvelopeObject (for IsCapCategoryObject)

▷ InjectiveEnvelopeObject(A)

(attribute)

Returns: an object

The argument is an object A. The output is an injective envelope of A.

6.16.5 MonomorphismIntoInjectiveEnvelopeObject (for IsCapCategoryObject)

▷ MonomorphismIntoInjectiveEnvelopeObject(A)

(attribute)

Returns: a monomorphism

The argument is an object A. The output is a monomorphism into an injective envelope of A.

6.16.6 MonomorphismIntoInjectiveEnvelopeObjectWithGivenInjectiveEnvelopeObject (for IsCapCategoryObject, IsCapCategoryObject)

Returns: a monomorphism

The argument is an object A. The output is a monomorphism into an injective envelope I of A.

Chapter 7

Add Functions

This section describes the overall structure of Add-functions and the functions installed by them.

7.1 Functions Installed by Add

Add functions have the following syntax:

```
DeclareOperation( "AddSomeFunc",
[ IsCapCategory, IsList, IsInt ] );
```

The first argument is the category to which some function (e.g. KernelObject) is added, the second is a list containing pairs of functions and additional filters for the arguments, (e.g. if one argument is a morphism, an additional filter could be IsMomomorphism). The third is an optional weight which will then be the weight for SomeFunc (default value: 100). This is described later. If only one function is to be installed, the list can be replaced by the function. CAP installs the given function(s) as methods for SomeFunc (resp. SomeFuncOp if SomeFunc is not an operation).

All installed methods follow the following steps, described below:

- · Redirect function
- Prefunction
- Function
- Logic
- Postfunction
- Addfunction

Every other part, except from function, does only depend on the name SomeFunc. We now explain the steps in detail.

• Redirect function: The redirect is used to redirect the computation from the given functions to some other symbol. If there is for example a with given method for some universal property, and the universal object is already computed, the redirect function might detect such a thing, calls the with given operation with the universal object as additional argument and then returns the

value. In general, the redirect can be an arbitrary function. It is called with the same arguments as the operation SomeFunc itself and can return an array containing [true, something], which will cause the installed method to simply return the object something, or [false]. If the output is false, the computation will continue with the step Prefunction.

- Prefunction: The prefunction should be used for error handling and plausibility checks of the input to SomeFunc (e.g. for KernelLift it should check wether range and source of the morphims coincide). Generally, the prefunction is defined in the method record and only depends on the name SomeFunc. It is called with the same input as the function itself, and should return either [true], which continues the computation, or [false, "message"], which will cause an error with message "message" and some additional information.
- Full prefunction: The full prefuction has the same semantics as the prefunction, but can perform additional, very costly checks. They are disabled by default.
- Function: This will launch the function(s) given as arguments. The result should be as specified in the type of SomeFunc. The resulting object is now named the result.
- Logic: For every function, some logical todos can be implemented in a logic texfile for the category. If there is some logic written down in a file belonging to the category, or belonging to some type of category. Please see the description of logic for more details. If there is some logic and some predicate relations for the function SomeFunc, it is installed in this step for the result.
- Postfunction: The postfunction called with the arguments of the function and the result. It can be an arbitrary function doing some cosmetics. If for example SomeFunc is KernelEmbedding, it will set the KernelObject of the input morphism to result. The postfunction is also taken from the method record and does only depend on the name SomeFunc.
- Addfunction: If the result is a category cell, it is added to the category for which the function was installed. This is disabled by default and can be enabled via EnableAddForCategoricalOperations (1.12.1).

7.2 Add Method

Except from installing a new method for the name SomeFunc, an Add method does slightly more. Every Add method has the same structure. The steps in the Add method are as follows:

- Default weight: If the weight parameter is -1, the default weight is assumed, which is 100.
- Weight check: If the current weight of the operation is lower than the given weight of the new functions, then the add function returns and installs nothing.
- Installation: Next, the method to install the functions is created. It creates the correct filter list, by merging the standard filters for the operation with the particular filters for the given functions, then installs the method as described above.

After calling an add method, the corresponding operation is available in the category. Also, some derivations, which are triggered by the setting of the primitive value, might be available.

7.3 Method name record entries

The entries of method name records can have the following components:

```
_{-} Code
"filter_list",
    "input_arguments_names",
    "return_type",
    "output_source_getter_string",
    "output_source_getter_preconditions",
    "output_range_getter_string",
    "output_range_getter_preconditions",
    "with_given_object_position",
    "dual_operation",
    "dual_arguments_reversed",
    "dual_with_given_objects_reversed",
    "dual_preprocessor_func",
    "dual_preprocessor_func_string",
    "dual_postprocessor_func",
    "dual_postprocessor_func_string",
    "functorial",
    "compatible_with_congruence_of_morphisms",
    "redirect_function",
    "pre_function",
    "pre_function_full",
    "post_function",
]
```

- pre_function (optional): A function which is used as the prefunction of the installed methods, as described above. Can also be the name of another operation. In this case the pre function of the referenced operation is used.
- pre_function_full (optional): A function which is used as the full prefunction of the installed methods, as described above. Can also be the name of another operation. In this case the full pre function of the referenced operation is used.
- redirect_function (optional): A function which is used as the redirect function of the installed methods, as described above. Can also be the name of another operation. In this case the redirect function of the referenced operation is used.
- post_function (optional): A function which is used as the postfunction of the installed methods, as described above.
- filter_list: A list containing the basic filters for the methods installed by the add methods. Possible entries are filters, or the strings listed below, which will be replaced by appropriate filters at the time the add method is called. The first entry of filter_list must be the string category. If the category can be inferred from the remaining arguments, a convenience method without the category as the first argument is installed automatically.

```
- category,
```

```
- object,
- morphism,
- twocell,
- object_in_range_category_of_homomorphism_structure,
- morphism_in_range_category_of_homomorphism_structure,
- list_of_objects,
- list_of_morphisms,
- list_of_twocells.
```

• return_type: The return type can either be a filter or one of the strings in the list below. For objects, morphisms and 2-cells the correct Add function (see above) is used for the result of the computation. Otherwise, no Add function is used after all.

```
Code
Γ
    "object",
    "morphism",
    "twocell",
    "object_in_range_category_of_homomorphism_structure",
    "morphism_in_range_category_of_homomorphism_structure",
    "bool",
    "list_of_objects",
    "list_of_morphisms",
    "list_of_lists_of_morphisms",
    "object_datum",
    "morphism_datum",
    "nonneg_integer_or_infinity",
    "list_of_elements_of_commutative_ring_of_linear_structure",
7
```

- functorial (optional): If an object has a corresponding functorial function, e.g., KernelObject and KernelObjectFunctorial, the name of the functorial is stored as a string.
- dual_operation (optional): Name of the dual operation.
- dual_arguments_reversed (optional): Boolean, marks whether for the call of the dual operation all arguments have to be given in reversed order.
- dual_with_given_objects_reversed (optional): Boolean, marks whether for the call of the dual operation the source and range of a with given operation have to be given in reversed order.
- dual_preprocessor_func[_string] (optional): let f be an operation with dual operation g. For the automatic installation of g from f, the arguments given to g are preprocessed by this given function. The function can also be given as a string.
- dual_postprocessor_func[_string] (optional): let f be an operation with dual operation g. For the automatic installation of g from f, the computed value of f is postprocessed by the given function. The function can also be given as a string.

- input_arguments_names (optional): A duplicate free list (of the same length as filter_list) of strings. For example, these strings will be used as the names of the arguments when automatically generating functions for this operation, e.g. in the opposite category.
- output_source_getter_string (optional): Only valid if the operation returns a morphism: a piece of GAP code which computes the source of the returned morphism. The input arguments are available via the names given in input_arguments_names.
- output_source_getter_preconditions (optional): Only valid if output_source_getter_string is set: The preconditions of output_source_getter_string in the same form as preconditions of derivations but with the CAP operations given as strings.
- output_range_getter_string (optional): Only valid if the operation returns a morphism: a piece of GAP code which computes the range of the returned morphism. The input arguments are available via the names given in input_arguments_names.
- output_range_getter_preconditions (optional): Only valid if output_range_getter_string is set: The preconditions of output_range_getter_string in the same form as preconditions of derivations but with the CAP operations given as strings.
- with_given_object_position (optional): One of the following strings: "Source", "Range", or "both". Set for the without given operation in a with given pair. Describes whether the source resp. range are given (as the last argument of the with given operation) or both (as the second and the last argument of the with given operation).
- compatible_with_congruence_of_morphisms (optional): Indicates if the operation is compatible with the congruence of morphisms, that is, if the output does not change with regard to IsEqualForObjects and IsCongruentForMorphisms if the input changes with regard to IsEqualForObjects and IsCongruentForMorphisms.

7.4 Enhancing the method name record

The function CAP_INTERNAL_ENHANCE_NAME_RECORD can be applied to a method name record to make the following enhancements:

- Function name: Set the component function_name to the entry name.
- WithGiven special case: If the current entry belongs to a WithGiven operation or its without given pair, the with_given_without_given_name_pair is set. Additionally, the with given flag of the WithGiven operation is set to true.
- Redirect and post functions are created for all operations belonging to universal constructions (e.g. KernelLift) which are not a WithGiven operation.

7.5 Prepare functions

7.5.1 CAPOperationPrepareFunction

▷ CAPOperationPrepareFunction(prepare_function, category, func)
Returns: a function

Given a non-CAP-conform function for any of the categorical operations, i.e., a function that computes the direct sum of two objects instead of a list of objects, this function wraps the function with a wrapper function to fit in the CAP context. For the mentioned binary direct sum one can call this function with "BinaryDirectSumToDirectSum" as prepare_function, the category, and the binary direct sum function. The function then returns a function that can be used for the direct sum categorical operation.

Note that *func* is not handled by the CAP caching mechanism and that the use of prepare functions is incompatible with WithGiven operations. Thus, one has to ensure manually that the equality and typing specifications are fulfilled.

7.5.2 CAPAddPrepareFunction

```
▷ CAPAddPrepareFunction(prepare_function, name, doc_string[,
precondition_list]) (function)
```

Adds a prepare function to the list of CAP's prepare functions. The first argument is the prepare function itself. It should always be a function that takes a category and a function and returns a function. The argument <code>name</code> is the name of the prepare function, which is used in CAPOperationPrepareFunction. The argument <code>doc_string</code> should be a short string describing the functions. The optional argument <code>precondition_list</code> can describe preconditions for the prepare function to work, i.e., if the category does need to have PreCompose computable. This information is also recovered automatically from the prepare function itself, so the <code>precondition_list</code> is only necessary if the function needed is not explicitly used in the prepare function, e.g., if you use + instead of <code>AdditionForMorphisms</code>.

7.5.3 ListCAPPrepareFunctions

▷ ListCAPPrepareFunctions(arg)

(function)

Lists all prepare functions.

7.6 Available Add functions

7.6.1 AddAdditionForMorphisms (for IsCapCategory, IsFunction)

```
    AddAdditionForMorphisms(C, F) (operation)

    AddAdditionForMorphisms(C, F, weight) (operation)

    Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation AdditionForMorphisms. Optionally, a weight

(default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,beta) \mapsto$ AdditionForMorphisms(alpha, beta).

7.6.2 AddAdditiveGenerators (for IsCapCategory, IsFunction)

```
▷ AddAdditiveGenerators(C, F)
                                                                                     (operation)

▷ AddAdditiveGenerators(C, F, weight)
                                                                                     (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation AdditiveGenerators. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto AdditiveGenerators()$.

7.6.3 AddAdditiveInverseForMorphisms (for IsCapCategory, IsFunction)

```
▷ AddAdditiveInverseForMorphisms(C, F)
                                                                                  (operation)

▷ AddAdditiveInverseForMorphisms(C, F, weight)
                                                                                  (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation AdditiveInverseForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto$ AdditiveInverseForMorphisms(alpha).

7.6.4 AddAstrictionToCoimage (for IsCapCategory, IsFunction)

```
▷ AddAstrictionToCoimage(C, F)
                                                                                    (operation)

▷ AddAstrictionToCoimage(C, F, weight)
                                                                                    (operation)
   Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation AstrictionToCoimage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto AstrictionToCoimage(alpha)$.

AddAstrictionToCoimageWithGivenCoimageObject (for IsCapCategory, Is-7.6.5 **Function**)

```
(operation)

▷ AddAstrictionToCoimageWithGivenCoimageObject(C, F, weight)

                                                 (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function Fto the category for the basic operation AstrictionToCoimageWithGivenCoimageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,C) \mapsto$ AstrictionToCoimageWithGivenCoimageObject(alpha, C).

7.6.6 AddBasisOfExternalHom (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation BasisOfExternalHom. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{BasisOfExternalHom}(arg2, arg3)$.

7.6.7 AddCoastrictionToImage (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoastrictionToImage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto \texttt{CoastrictionToImage}(alpha)$.

7.6.8 AddCoastrictionToImageWithGivenImageObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoastrictionToImageWithGivenImageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,I) \mapsto$

7.6.9 AddCoefficientsOfMorphism (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoefficientsOfMorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{CoefficientsOfMorphism}(arg2)$.

7.6.10 AddCoequalizer (for IsCapCategory, IsFunction)

CoastrictionToImageWithGivenImageObject(alpha, I).

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation Coequalizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms) \mapsto \text{Coequalizer}(Y, morphisms)$.

7.6.11 AddCoequalizerFunctorial (for IsCapCategory, IsFunction)

```
▷ AddCoequalizerFunctorial(C, F) (operation)
▷ AddCoequalizerFunctorial(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoequalizerFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, mu, morphismsp) \mapsto CoequalizerFunctorial(morphisms, mu, morphismsp)$.

7.6.12 AddCoequalizerFunctorialWithGivenCoequalizers (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoequalizerFunctorialWithGivenCoequalizers. Optionally, weight (default: 100) can be specified which should roughly correspond the computational complexity of the function (lower weight = to faster execution). F: $(P, morphisms, mu, morphismsp, Pp) \mapsto$ complex CoequalizerFunctorialWithGivenCoequalizers(P, morphisms, mu, morphismsp, Pp).

7.6.13 AddCoimageObject (for IsCapCategory, IsFunction)

```
▷ AddCoimageObject(C, F) (operation)

▷ AddCoimageObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoimageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{CoimageObject}(arg2)$.

7.6.14 AddCoimageObjectFunctorial (for IsCapCategory, IsFunction)

```
▷ AddCoimageObjectFunctorial(C, F) (operation)
▷ AddCoimageObjectFunctorial(C, F, weight) (operation)

■ Potential (C, F, weight)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoimageObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity

of the function (lower weight = less complex = faster execution). $F:(alpha,mu,alphap) \mapsto \texttt{CoimageObjectFunctorial}(alpha,mu,alphap)$.

7.6.15 AddCoimageObjectFunctorialWithGivenCoimageObjects (for IsCapCategory, IsFunction)

Returns: nothing

The arguments Cfunction F. This are a category and operaadds the given function Fto the category for the basic operation CoimageObjectFunctorialWithGivenCoimageObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(C, alpha, mu, alphap, Cp) \mapsto$ CoimageObjectFunctorialWithGivenCoimageObjects(C, alpha, mu, alphap, Cp).

7.6.16 AddCoimageProjection (for IsCapCategory, IsFunction)

▷ AddCoimageProjection(C, F) (operation)
▷ AddCoimageProjection(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoimageProjection. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \texttt{CoimageProjection}(alpha)$.

7.6.17 AddCoimageProjectionWithGivenCoimageObject (for IsCapCategory, Is-Function)

▷ AddCoimageProjectionWithGivenCoimageObject(C, F) (operation)

▷ AddCoimageProjectionWithGivenCoimageObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoimageProjectionWithGivenCoimageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,C) \mapsto CoimageProjectionWithGivenCoimageObject(alpha,C)$.

7.6.18 AddCokernelColift (for IsCapCategory, IsFunction)

▷ AddCokernelColift(C, F) (operation)
▷ AddCokernelColift(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CokernelColift. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, T, tau) \mapsto \texttt{CokernelColift}(alpha, T, tau)$.

7.6.19 AddCokernelColiftWithGivenCokernelObject (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CokernelColiftWithGivenCokernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,T,tau,P)\mapsto CokernelColiftWithGivenCokernelObject(alpha,T,tau,P)$.

7.6.20 AddCokernelObject (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CokernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \texttt{CokernelObject}(alpha)$.

7.6.21 AddCokernelObjectFunctorial (for IsCapCategory, IsFunction)

▷ AddCokernelObjectFunctorial(C, F) (operation)
▷ AddCokernelObjectFunctorial(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CokernelObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,mu,alphap) \mapsto CokernelObjectFunctorial(alpha,mu,alphap)$.

7.6.22 AddCokernelObjectFunctorialWithGivenCokernelObjects (for IsCapCategory, IsFunction)

▷ AddCokernelObjectFunctorialWithGivenCokernelObjects(C, F) (operation)
▷ AddCokernelObjectFunctorialWithGivenCokernelObjects(C, F, weight) (operation)
Returns: nothing

The arguments are category Cand a function F. This operathe tion adds the given function Fto category for the basic operation CokernelObjectFunctorialWithGivenCokernelObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(P,alpha,mu,alphap,Pp) \mapsto$ CokernelObjectFunctorialWithGivenCokernelObjects(P, alpha, mu, alphap, Pp).

AddCokernelProjection (for IsCapCategory, IsFunction)

▷ AddCokernelProjection(C, F) (operation) ▷ AddCokernelProjection(C, F, weight) (operation) **Returns:** nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CokernelProjection. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto \texttt{CokernelProjection}(alpha)$.

7.6.24 AddCokernelProjectionWithGivenCokernelObject (for IsCapCategory, Is-**Function**)

▷ AddCokernelProjectionWithGivenCokernelObject(C, F) (operation) ▷ AddCokernelProjectionWithGivenCokernelObject(C, F, weight) (operation) **Returns:** nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CokernelProjectionWithGivenCokernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha, P) \mapsto$ CokernelProjectionWithGivenCokernelObject(alpha, P).

7.6.25 AddColift (for IsCapCategory, IsFunction)

```
▷ AddColift(C, F)
                                                                                         (operation)
▷ AddColift(C, F, weight)
                                                                                         (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation Colift. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,beta) \mapsto \texttt{Colift}(alpha,beta)$.

AddColiftAlongEpimorphism (for IsCapCategory, IsFunction)

```
(operation)

▷ AddColiftAlongEpimorphism(C, F, weight)
                                                           (operation)
  Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ColiftAlongEpimorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(epsilon, tau) \mapsto$ ColiftAlongEpimorphism(epsilon,tau).

AddComponentOfMorphismFromCoproduct (for IsCapCategory, IsFunction) 7.6.27

```
(operation)

▷ AddComponentOfMorphismFromCoproduct(C, F, weight)
                                                       (operation)
  Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ComponentOfMorphismFromCoproduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,I,i)\mapsto ComponentOfMorphismFromCoproduct(alpha,I,i)$.

7.6.28 AddComponentOfMorphismFromDirectSum (for IsCapCategory, IsFunction)

```
▷ AddComponentOfMorphismFromDirectSum(C, F) (operation)
▷ AddComponentOfMorphismFromDirectSum(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ComponentOfMorphismFromDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,S,i)\mapsto ComponentOfMorphismFromDirectSum(alpha,S,i)$.

7.6.29 AddComponentOfMorphismIntoDirectProduct (for IsCapCategory, IsFunction)

```
▷ AddComponentOfMorphismIntoDirectProduct(C, F) (operation)

▷ AddComponentOfMorphismIntoDirectProduct(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ComponentOfMorphismIntoDirectProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,P,i)\mapsto ComponentOfMorphismIntoDirectProduct(alpha,P,i)$.

7.6.30 AddComponentOfMorphismIntoDirectSum (for IsCapCategory, IsFunction)

```
▷ AddComponentOfMorphismIntoDirectSum(C, F) (operation)

▷ AddComponentOfMorphismIntoDirectSum(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ComponentOfMorphismIntoDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,S,i)\mapsto ComponentOfMorphismIntoDirectSum(alpha,S,i)$.

7.6.31 AddCoproduct (for IsCapCategory, IsFunction)

```
> AddCoproduct(C, F) (operation)

> AddCoproduct(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation Coproduct. Optionally, a weight (default: 100) can be specified

which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects) \mapsto \texttt{Coproduct}(objects)$.

7.6.32 AddCoproductFunctorial (for IsCapCategory, IsFunction)

```
▷ AddCoproductFunctorial(C, F) (operation)

▷ AddCoproductFunctorial(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoproductFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,L,objectsp) \mapsto CoproductFunctorial(objects,L,objectsp)$.

7.6.33 AddCoproductFunctorialWithGivenCoproducts (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation CoproductFunctorialWithGivenCoproducts. Optionally, weight (default: 100) can be specified which should roughly correspond function to the computational complexity the (lower less faster execution). F $(P, objects, L, objectsp, Pp) \mapsto$ complex ${\tt CoproductFunctorialWithGivenCoproducts}(P, objects, L, objectsp, Pp).$

7.6.34 AddDirectProduct (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DirectProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects) \mapsto \texttt{DirectProduct}(objects)$.

7.6.35 AddDirectProductFunctorial (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DirectProductFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,L,objectsp) \mapsto DirectProductFunctorial(objects,L,objectsp)$.

7.6.36 AddDirectProductFunctorialWithGivenDirectProducts (for IsCapCategory, IsFunction)

▷ AddDirectProductFunctorialWithGivenDirectProducts(C, F) (operation)
▷ AddDirectProductFunctorialWithGivenDirectProducts(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DirectProductFunctorialWithGivenDirectProducts. weight (default: 100) can be specified which should Optionally, correspond the computational complexity of the function (lower weight to less complex faster execution). F: $(P, ob jects, L, ob jectsp, Pp) \mapsto$ DirectProductFunctorialWithGivenDirectProducts(P, objects, L, objectsp, Pp).

7.6.37 AddDirectSum (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects) \mapsto \text{DirectSum}(objects)$.

7.6.38 AddDirectSumFunctorial (for IsCapCategory, IsFunction)

▷ AddDirectSumFunctorial(C, F) (operation)
▷ AddDirectSumFunctorial(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DirectSumFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,L,objectsp) \mapsto DirectSumFunctorial(objects,L,objectsp)$.

7.6.39 AddDirectSumFunctorialWithGivenDirectSums (for IsCapCategory, IsFunction)

▷ AddDirectSumFunctorialWithGivenDirectSums(C, F) (operation)
 ▷ AddDirectSumFunctorialWithGivenDirectSums(C, F, weight) (operation)
 Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DirectSumFunctorialWithGivenDirectSums. Optionally, weight (default: 100) can be specified which should roughly correspond the the function to computational complexity of (lower weight complex faster execution). $F: (P, objects, L, objectsp, Pp) \mapsto$ DirectSumFunctorialWithGivenDirectSums(P, objects, L, objectsp, Pp).

7.6.40 AddDistinguishedObjectOfHomomorphismStructure (for IsCapCategory, Is-Function)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation DistinguishedObjectOfHomomorphismStructure. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto DistinguishedObjectOfHomomorphismStructure()$.

7.6.41 AddEmbeddingOfEqualizer (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation EmbeddingOfEqualizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y,morphisms) \mapsto \text{EmbeddingOfEqualizer}(Y,morphisms)$.

7.6.42 AddEmbeddingOfEqualizerWithGivenEqualizer (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation EmbeddingOfEqualizerWithGivenEqualizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms, P) \mapsto \text{EmbeddingOfEqualizerWithGivenEqualizer}(Y, morphisms, P)$.

7.6.43 AddEpimorphismFromProjectiveCoverObject (for IsCapCategory, IsFunction)

▷ AddEpimorphismFromProjectiveCoverObject(C, F) (operation)

▷ AddEpimorphismFromProjectiveCoverObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation EpimorphismFromProjectiveCoverObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A) \mapsto \text{EpimorphismFromProjectiveCoverObject}(A)$.

7.6.44 AddEpimorphismFromProjectiveCoverObjectWithGivenProjectiveCoverObject (for IsCapCategory, IsFunction)

▷ AddEpimorphismFromProjectiveCoverObjectWithGivenProjectiveCoverObject(C, F)

(operation)

Returns: nothing

F. This The arguments category Cfunction operaare and the given function Fthe category for the operation tion adds to basic EpimorphismFromProjectiveCoverObjectWithGivenProjectiveCoverObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,P) \mapsto$ EpimorphismFromProjectiveCoverObjectWithGivenProjectiveCoverObject(A, P).

7.6.45 AddEpimorphismFromSomeProjectiveObject (for IsCapCategory, IsFunction)

(operation)

▷ AddEpimorphismFromSomeProjectiveObject(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation EpimorphismFromSomeProjectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A) \mapsto \text{EpimorphismFromSomeProjectiveObject}(A)$.

7.6.46 AddEpimorphismFromSomeProjectiveObjectWithGivenSomeProjectiveObject (for IsCapCategory, IsFunction)

▷ AddEpimorphismFromSomeProjectiveObjectWithGivenSomeProjectiveObject(C, F)

(operation)

Returns: nothing

This The arguments are category Cand function F. operathe given function to the category for the basic operation adds FEpimorphismFromSomeProjectiveObjectWithGivenSomeProjectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,P) \mapsto$ ${\tt EpimorphismFromSomeProjectiveObjectWithGivenSomeProjectiveObject}(A,P).$

7.6.47 AddEqualizer (for IsCapCategory, IsFunction)

▷ AddEqualizer(C, F)

(operation)

▷ AddEqualizer(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation Equalizer. Optionally, a weight (default: 100) can be specified

which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y,morphisms) \mapsto \text{Equalizer}(Y,morphisms)$.

7.6.48 AddEqualizerFunctorial (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation EqualizerFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, mu, morphismsp) \mapsto \text{EqualizerFunctorial}(morphisms, mu, morphismsp)$.

7.6.49 AddEqualizerFunctorialWithGivenEqualizers (for IsCapCategory, IsFunction)

```
    ▷ AddEqualizerFunctorialWithGivenEqualizers(C, F) (operation)
    ▷ AddEqualizerFunctorialWithGivenEqualizers(C, F, weight) (operation)
    Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation EqualizerFunctorialWithGivenEqualizers. Optionally, weight (default: 100) can be specified which should roughly correspond function to the computational complexity the (lower weight complex faster execution). F: $(P, morphisms, mu, morphismsp, Pp) \mapsto$ less EqualizerFunctorialWithGivenEqualizers(P, morphisms, mu, morphismsp, Pp).

7.6.50 AddFiberProduct (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation FiberProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms) \mapsto \texttt{FiberProduct}(morphisms)$.

7.6.51 AddFiberProductFunctorial (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation FiberProductFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, L, morphismsp) \mapsto FiberProductFunctorial(morphisms, L, morphismsp)$.

7.6.52 AddFiberProductFunctorialWithGivenFiberProducts (for IsCapCategory, Is-Function)

 $\begin{tabular}{ll} $ > $ AddFiberProductFunctorialWithGivenFiberProducts({\it C}, {\it F}) & (operation) \\ $ > $ AddFiberProductFunctorialWithGivenFiberProducts({\it C}, {\it F}, {\it weight}) & (operation) \\ \end{tabular}$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation FiberProductFunctorialWithGivenFiberProducts. (default: 100) can be specified which should Optionally, weight correspond the computational complexity of the function (lower weight to less complex faster execution). F: $(P, morphisms, L, morphismsp, Pp) \mapsto$ FiberProductFunctorialWithGivenFiberProducts(P, morphisms, L, morphisms, P).

7.6.53 AddHomologyObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation HomologyObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, beta) \mapsto \text{HomologyObject}(alpha, beta)$.

7.6.54 AddHomologyObjectFunctorialWithGivenHomologyObjects (for IsCapCategory, IsFunction)

▷ AddHomologyObjectFunctorialWithGivenHomologyObjects(C, F) (operation)
▷ AddHomologyObjectFunctorialWithGivenHomologyObjects(C, F, weight) (operation)
Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ${\tt Homology0bjectFunctorialWithGivenHomology0bjects}$. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (H_1, L, H_2) \mapsto {\tt Homology0bjectFunctorialWithGivenHomology0bjects}(H_1, L, H_2)$.

7.6.55 AddHomomorphismStructureOnMorphisms (for IsCapCategory, IsFunction)

▷ AddHomomorphismStructureOnMorphisms(C, F) (operation)
▷ AddHomomorphismStructureOnMorphisms(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation HomomorphismStructureOnMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,beta) \mapsto \text{HomomorphismStructureOnMorphisms}(alpha,beta)$.

7.6.56 AddHomomorphismStructureOnMorphismsWithGivenObjects (for IsCap-Category, IsFunction)

 ${\color{blue} \triangleright} \ \, \mathsf{AddHomomorphismStructureOnMorphismsWithGivenObjects} \, (\mathit{C}, \ \mathit{F}) \qquad \qquad (\mathsf{operation})$

 ${\tt \triangleright} \ \, {\tt AddHomomorphismStructureOnMorphismsWithGivenObjects(\textit{C},\textit{F},\textit{weight})} \qquad \quad ({\tt operation})$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation HomomorphismStructureOnMorphismsWithGivenObjects. 100) can be specified which should Optionally, weight (default: correspond the computational complexity of the function (lower weight to less complex faster execution). F: $(source, alpha, beta, range) \mapsto$ ${\tt HomomorphismStructureOnMorphismsWithGivenObjects}(source, alpha, beta, range).$

7.6.57 AddHomomorphismStructureOnObjects (for IsCapCategory, IsFunction)

▷ AddHomomorphismStructureOnObjects(C, F) (operation)
▷ AddHomomorphismStructureOnObjects(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation HomomorphismStructureOnObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{HomomorphismStructureOnObjects}(arg2, arg3)$.

7.6.58 AddHorizontalPostCompose (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation HorizontalPostCompose. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{HorizontalPostCompose}(arg2, arg3)$.

7.6.59 AddHorizontalPreCompose (for IsCapCategory, IsFunction)

AddHorizontalPreCompose(C, F) (operation)

 AddHorizontalPreCompose(C, F, weight) (operation)

 Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation HorizontalPreCompose. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{HorizontalPreCompose}(arg2, arg3)$.

7.6.60 AddIdentityMorphism (for IsCapCategory, IsFunction)

```
▷ AddIdentityMorphism(C, F) (operation)
▷ AddIdentityMorphism(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IdentityMorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(a) \mapsto \text{IdentityMorphism}(a)$.

7.6.61 AddIdentityTwoCell (for IsCapCategory, IsFunction)

```
▷ AddIdentityTwoCell(C, F) (operation)

▷ AddIdentityTwoCell(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IdentityTwoCell. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IdentityTwoCell}(arg2)$.

7.6.62 AddImageEmbedding (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ImageEmbedding. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \text{ImageEmbedding}(alpha)$.

7.6.63 AddImageEmbeddingWithGivenImageObject (for IsCapCategory, IsFunction)

```
▷ AddImageEmbeddingWithGivenImageObject(C, F) (operation)

▷ AddImageEmbeddingWithGivenImageObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ImageEmbeddingWithGivenImageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,I)\mapsto ImageEmbeddingWithGivenImageObject(alpha,I)$.

7.6.64 AddImageObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ImageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{ImageObject}(arg2)$.

7.6.65 AddImageObjectFunctorial (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ImageObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,nu,alphap) \mapsto$ ImageObjectFunctorial(alpha,nu,alphap).

7.6.66 AddImageObjectFunctorialWithGivenImageObjects (for IsCapCategory, IsFunction)

```
▷ AddImageObjectFunctorialWithGivenImageObjects(C, F) (operation)
▷ AddImageObjectFunctorialWithGivenImageObjects(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ImageObjectFunctorialWithGivenImageObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (I, alpha, nu, alphap, Ip) \mapsto$ ImageObjectFunctorialWithGivenImageObjects(I, alpha, nu, alphap, Ip).

7.6.67 AddIndecomposableInjectiveObjects (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IndecomposableInjectiveObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto IndecomposableInjectiveObjects()$.

7.6.68 AddIndecomposableProjectiveObjects (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IndecomposableProjectiveObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computa-

tional complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto IndecomposableProjectiveObjects()$.

7.6.69 AddInitialObject (for IsCapCategory, IsFunction)

```
▷ AddInitialObject(C, F) (operation)

▷ AddInitialObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InitialObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: () \mapsto \text{InitialObject}()$.

7.6.70 AddInitialObjectFunctorial (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InitialObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: () \mapsto \text{InitialObjectFunctorial}()$.

7.6.71 AddInitialObjectFunctorialWithGivenInitialObjects (for IsCapCategory, Is-Function)

```
▷ AddInitialObjectFunctorialWithGivenInitialObjects(C, F) (operation)
▷ AddInitialObjectFunctorialWithGivenInitialObjects(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InitialObjectFunctorialWithGivenInitialObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(P,Pp)\mapsto$ InitialObjectFunctorialWithGivenInitialObjects(P,Pp).

7.6.72 AddInjectionOfCofactorOfCoproduct (for IsCapCategory, IsFunction)

```
▷ AddInjectionOfCofactorOfCoproduct(C, F) (operation)
▷ AddInjectionOfCofactorOfCoproduct(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectionOfCofactorOfCoproduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,k) \mapsto InjectionOfCofactorOfCoproduct(objects,k)$.

7.6.73 AddInjectionOfCofactorOfCoproductWithGivenCoproduct (for IsCapCategory, IsFunction)

▷ AddInjectionOfCofactorOfCoproductWithGivenCoproduct(C, F) (operation)
▷ AddInjectionOfCofactorOfCoproductWithGivenCoproduct(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectionOfCofactorOfCoproductWithGivenCoproduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). F: $(objects, k, P) \mapsto \text{InjectionOfCofactorOfCoproductWithGivenCoproduct}(objects, k, P)$.

7.6.74 AddInjectionOfCofactorOfDirectSum (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectionOfCofactorOfDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,k) \mapsto InjectionOfCofactorOfDirectSum(objects,k)$.

7.6.75 AddInjectionOfCofactorOfDirectSumWithGivenDirectSum (for IsCapCategory, IsFunction)

▷ AddInjectionOfCofactorOfDirectSumWithGivenDirectSum(C, F) (operation)
▷ AddInjectionOfCofactorOfDirectSumWithGivenDirectSum(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectionOfCofactorOfDirectSumWithGivenDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). F: $(objects, k, P) \mapsto \text{InjectionOfCofactorOfDirectSumWithGivenDirectSum}(objects, k, P)$.

7.6.76 AddInjectionOfCofactorOfPushout (for IsCapCategory, IsFunction)

▷ AddInjectionOfCofactorOfPushout(C, F) (operation)
▷ AddInjectionOfCofactorOfPushout(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectionOfCofactorOfPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, k) \mapsto InjectionOfCofactorOfPushout(morphisms, k)$.

7.6.77 AddInjectionOfCofactorOfPushoutWithGivenPushout (for IsCapCategory, IsFunction)

▷ AddInjectionOfCofactorOfPushoutWithGivenPushout(C, F) (operation)
▷ AddInjectionOfCofactorOfPushoutWithGivenPushout(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectionOfCofactorOfPushoutWithGivenPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, k, P) \mapsto InjectionOfCofactorOfPushoutWithGivenPushout(morphisms, k, P)$.

7.6.78 AddInjectiveColift (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectiveColift. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, beta) \mapsto \text{InjectiveColift}(alpha, beta)$.

7.6.79 AddInjectiveDimension (for IsCapCategory, IsFunction)

▷ AddInjectiveDimension(C, F) (operation)
▷ AddInjectiveDimension(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectiveDimension. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{InjectiveDimension}(arg2)$.

7.6.80 AddInjectiveEnvelopeObject (for IsCapCategory, IsFunction)

```
▷ AddInjectiveEnvelopeObject(C, F) (operation)
▷ AddInjectiveEnvelopeObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InjectiveEnvelopeObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{InjectiveEnvelopeObject}(arg2)$.

7.6.81 AddInterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructure (for IsCapCategory, IsFunction)

- $\label{eq:continuous} $$ $$ $$ AddInterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructure(C, F) $$ (operation) $$$
- ▷ AddInterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructure(C,

F, weight) (operation)

Returns: nothing

F. arguments category Cand function This The are operathe given the category the function Fto for basic operation $Interpret {\tt Morphism As Morphism From Distinguished Object To Homomorphism Structure}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(al\,pha)\mapsto$ InterpretMorphism As Morphism From Distinguished Object To Homomorphism Structure (alpha).

7.6.82 AddInterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructureW (for IsCapCategory, IsFunction)

▷ AddInterpretMorphismAsMorphismFromDistinguishedObjectToHomomorphismStructureWithGivenObjec
F, weight)
(operation)

Returns: nothing

The and function F. This arguments are a category Coperafunction given Fto the category for the basic operation InterpretMorphism As Morphism From Distinguished Object To Homomorphism Structure With Given Objects.Optionally, weight (default: 100) specified which should can be roughly correspond computational of the function (lower to the complexity execution). $F : (source, alpha, range) \mapsto$ less complex = faster InterpretMorphism As Morphism From Distinguished Object To Homomorphism Structure With Given Objects (some property of the Morphism From Distinguished Object To Homomorphism Structure With Given Objects (some property of the Morphism From Distinguished Object To Homomorphism Structure With Given Objects (some property of the Morphism From Distinguished Object To Homomorphism Structure With Given Objects (some property of the Morphism From Distinguished Object To Homomorphism Structure With Given Objects (some property of the Morphism From Distinguished Object To Homomorphism From Distinguished Object To Homomorphism Structure With Given Objects (some property of the Morphism From Distinguished Object To Homomorphism From Distinguish

7.6.83 AddInterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism (for IsCapCategory, IsFunction)

 ${} \rhd \ \, \mathsf{AddInterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism}(\mathit{C}, F) \\ \qquad \qquad \qquad (operation)$

 ${\tt \triangleright AddInterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism(\it{C}, F, weight)} \\ (operation)$

Returns: nothing

The arguments category Cand function F. This operaare given function the the basic adds Fto category for operation InterpretMorphism From Distinguished Object To Homomorphism Structure As Morphism.specified Optionally, weight (default: 100) can be which should roughly the computational of the function correspond complexity (lower F: $(source, range, alpha) \mapsto$ less complex = faster execution). InterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism(source, range, alpha).

7.6.84 AddInverseForMorphisms (for IsCapCategory, IsFunction)

▷ AddInverseForMorphisms(C, F)
▷ AddInverseForMorphisms(C, F, weight)

(operation) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InverseForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \text{InverseForMorphisms}(alpha)$.

7.6.85 AddInverseOfMorphismFromCoimageToImage (for IsCapCategory, IsFunction)

```
▷ AddInverseOfMorphismFromCoimageToImage(C, F) (operation)
▷ AddInverseOfMorphismFromCoimageToImage(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InverseOfMorphismFromCoimageToImage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto InverseOfMorphismFromCoimageToImage(alpha)$.

7.6.86 AddInverseOfMorphismFromCoimageToImageWithGivenObjects (for IsCap-Category, IsFunction)

```
▷ AddInverseOfMorphismFromCoimageToImageWithGivenObjects(C, F) (operation)
▷ AddInverseOfMorphismFromCoimageToImageWithGivenObjects(C, F, weight) (operation)
Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation InverseOfMorphismFromCoimageToImageWithGivenObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(I,alpha,C)\mapsto$ InverseOfMorphismFromCoimageToImageWithGivenObjects(I,alpha,C).

7.6.87 AddIsAutomorphism (for IsCapCategory, IsFunction)

```
▷ AddIsAutomorphism(C, F) (operation)

▷ AddIsAutomorphism(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsAutomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsAutomorphism}(arg2)$.

7.6.88 AddIsBijectiveObject (for IsCapCategory, IsFunction)

```
▷ AddIsBijectiveObject(C, F) (operation)

▷ AddIsBijectiveObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsBijectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto$ IsBijectiveObject(arg2).

7.6.89 AddIsCodominating (for IsCapCategory, IsFunction)

```
ightharpoonup AddIsCodominating(C, F) (operation)

ightharpoonup AddIsCodominating(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsCodominating. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{IsCodominating}(arg2, arg3)$.

7.6.90 AddIsColiftable (for IsCapCategory, IsFunction)

```
ightharpoonup AddIsColiftable(C, F) (operation)

ightharpoonup AddIsColiftable(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsColiftable. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{IsColiftable}(arg2, arg3)$.

7.6.91 AddIsColiftableAlongEpimorphism (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsColiftableAlongEpimorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto IsColiftableAlongEpimorphism(arg2, arg3)$.

7.6.92 AddIsCongruentForMorphisms (for IsCapCategory, IsFunction)

```
▷ AddIsCongruentForMorphisms(C, F) (operation)

▷ AddIsCongruentForMorphisms(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsCongruentForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto$ IsCongruentForMorphisms(arg2, arg3).

7.6.93 AddIsDominating (for IsCapCategory, IsFunction)

```
> AddIsDominating(C, F) (operation)

> AddIsDominating(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsDominating. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{IsDominating}(arg2, arg3)$.

7.6.94 AddIsEndomorphism (for IsCapCategory, IsFunction)

```
ightharpoonup AddIsEndomorphism(C, F) (operation)

ightharpoonup AddIsEndomorphism(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEndomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsEndomorphism}(arg2)$.

7.6.95 AddIsEpimorphism (for IsCapCategory, IsFunction)

```
▷ AddIsEpimorphism(C, F) (operation)

▷ AddIsEpimorphism(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEpimorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsEpimorphism}(arg2)$.

7.6.96 AddIsEqualAsFactorobjects (for IsCapCategory, IsFunction)

```
▷ AddIsEqualAsFactorobjects(C, F) (operation)
▷ AddIsEqualAsFactorobjects(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualAsFactorobjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto IsEqualAsFactorobjects(arg2, arg3)$.

7.6.97 AddIsEqualAsSubobjects (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualAsSubobjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto$ IsEqualAsSubobjects(arg2, arg3).

7.6.98 AddIsEqualForCacheForMorphisms (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualForCacheForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto IsEqualForCacheForMorphisms(arg2, arg3)$.

7.6.99 AddIsEqualForCacheForObjects (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualForCacheForObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto$

IsEqualForCacheForObjects(arg2, arg3).

7.6.100 AddIsEqualForMorphisms (for IsCapCategory, IsFunction)

▷ AddIsEqualForMorphisms(C, F) (operation)

▷ AddIsEqualForMorphisms(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto$ IsEqualForMorphisms(arg2, arg3).

7.6.101 AddIsEqualForMorphismsOnMor (for IsCapCategory, IsFunction)

▷ AddIsEqualForMorphismsOnMor(C, F) (operation)
▷ AddIsEqualForMorphismsOnMor(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualForMorphismsOnMor. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto IsEqualForMorphismsOnMor(arg2, arg3)$.

7.6.102 AddIsEqualForObjects (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualForObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto$ IsEqualForObjects(arg2, arg3).

7.6.103 AddIsEqualToIdentityMorphism (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualToIdentityMorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsEqualToIdentityMorphism(arg2)$.

7.6.104 AddIsEqualToZeroMorphism (for IsCapCategory, IsFunction)

```
▷ AddIsEqualToZeroMorphism(C, F) (operation)

▷ AddIsEqualToZeroMorphism(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsEqualToZeroMorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsEqualToZeroMorphism}(arg2)$.

7.6.105 AddIsHomSetInhabited (for IsCapCategory, IsFunction)

```
▷ AddIsHomSetInhabited(C, F) (operation)

▷ AddIsHomSetInhabited(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsHomSetInhabited. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto$ IsHomSetInhabited(arg2, arg3).

7.6.106 AddIsIdempotent (for IsCapCategory, IsFunction)

```
ightharpoonup AddIsIdempotent(C, F) (operation)

ho AddIsIdempotent(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsIdempotent. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsIdempotent(arg2)$.

7.6.107 AddIsInitial (for IsCapCategory, IsFunction)

```
▷ AddIsInitial(C, F) (operation)

▷ AddIsInitial(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsInitial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsInitial}(arg2)$.

7.6.108 AddIsInjective (for IsCapCategory, IsFunction)

```
ightharpoonup AddIsInjective(C, F) (operation)

ho AddIsInjective(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsInjective. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsInjective(arg2)$.

7.6.109 AddIsIsomorphicForObjects (for IsCapCategory, IsFunction)

```
▷ AddIsIsomorphicForObjects(C, F) (operation)
▷ AddIsIsomorphicForObjects(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsIsomorphicForObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(object_1, object_2) \mapsto IsIsomorphicForObjects(object_1, object_2)$.

7.6.110 AddIsIsomorphism (for IsCapCategory, IsFunction)

```
▷ AddIsIsomorphism(C, F) (operation)

▷ AddIsIsomorphism(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsIsomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsIsomorphism}(arg2)$.

7.6.111 AddIsLiftable (for IsCapCategory, IsFunction)

```
ightharpoonup AddIsLiftable(C, F) (operation)

ightharpoonup AddIsLiftable(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsLiftable. Optionally, a weight (default: 100) can be specified

which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \mathtt{IsLiftable}(arg2, arg3)$.

7.6.112 AddIsLiftableAlongMonomorphism (for IsCapCategory, IsFunction)

```
▷ AddIsLiftableAlongMonomorphism(C, F) (operation)
▷ AddIsLiftableAlongMonomorphism(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsLiftableAlongMonomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto IsLiftableAlongMonomorphism(arg2, arg3)$.

7.6.113 AddIsMonomorphism (for IsCapCategory, IsFunction)

```
▷ AddIsMonomorphism(C, F) (operation)

▷ AddIsMonomorphism(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsMonomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsMonomorphism}(arg2)$.

7.6.114 AddIsOne (for IsCapCategory, IsFunction)

```
▷ AddIsOne(C, F) (operation)
▷ AddIsOne(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsOne. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsOne(arg2)$.

7.6.115 AddIsProjective (for IsCapCategory, IsFunction)

```
> AddIsProjective(C, F) (operation)

> AddIsProjective(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsProjective. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsProjective}(arg2)$.

7.6.116 AddIsSplitEpimorphism (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsSplitEpimorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsSplitEpimorphism(arg2)$.

7.6.117 AddIsSplitMonomorphism (for IsCapCategory, IsFunction)

```
    AddIsSplitMonomorphism(C, F) (operation)

    AddIsSplitMonomorphism(C, F, weight) (operation)

    Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsSplitMonomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsSplitMonomorphism(arg2)$.

7.6.118 AddIsTerminal (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsTerminal. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \texttt{IsTerminal}(arg2)$.

7.6.119 AddIsWellDefinedForMorphisms (for IsCapCategory, IsFunction)

```
▷ AddIsWellDefinedForMorphisms(C, F) (operation)

▷ AddIsWellDefinedForMorphisms(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsWellDefinedForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto IsWellDefinedForMorphisms(alpha)$.

7.6.120 AddIsWellDefinedForMorphismsWithGivenSourceAndRange (for IsCapCategory, IsFunction)

```
▷ AddIsWellDefinedForMorphismsWithGivenSourceAndRange(C, F) (operation)
▷ AddIsWellDefinedForMorphismsWithGivenSourceAndRange(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category Cand function F. This operaoperation the given function Fto the basic tion adds category for the IsWellDefinedForMorphismsWithGivenSourceAndRange. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of

the function (lower weight = less complex = faster execution). $F : (source, alpha, range) \mapsto IsWellDefinedForMorphismsWithGivenSourceAndRange(source, alpha, range).$

7.6.121 AddIsWellDefinedForObjects (for IsCapCategory, IsFunction)

```
▷ AddIsWellDefinedForObjects(C, F) (operation)
▷ AddIsWellDefinedForObjects(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsWellDefinedForObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower

weight = less complex = faster execution). $F: (arg2) \mapsto \texttt{IsWellDefinedForObjects}(arg2)$.

7.6.122 AddIsWellDefinedForTwoCells (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsWellDefinedForTwoCells. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{IsWellDefinedForTwoCells}(arg2)$.

7.6.123 AddIsZeroForMorphisms (for IsCapCategory, IsFunction)

```
▷ AddIsZeroForMorphisms(C, F) (operation)

▷ AddIsZeroForMorphisms(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsZeroForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsZeroForMorphisms(arg2)$.

7.6.124 AddIsZeroForObjects (for IsCapCategory, IsFunction)

```
▷ AddIsZeroForObjects(C, F) (operation)
▷ AddIsZeroForObjects(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsZeroForObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto IsZeroForObjects(arg2)$.

7.6.125 AddIsomorphismFromCoequalizerOfCoproductDiagramToPushout (for Is-CapCategory, IsFunction)

tion)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromCoequalizerOfCoproductDiagramToPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D) \mapsto IsomorphismFromCoequalizerOfCoproductDiagramToPushout(<math>D$).

7.6.126 AddIsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFrom (for IsCapCategory, IsFunction)

- ▷ AddIsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproduct(F, weight) (operation)

Returns: nothing

The arguments and function F. This are category Coperafunction tion adds given Fto the category for the basic operation Is omorphism From Coequalizer To Cokernel Of Joint Pairwise Differences Of Morphisms From Coproduct.Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,D)\mapsto$ ${\tt IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproduct} (A,D) and {\tt IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproduct} (A,D) and {\tt IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproduct} (A,D) and {\tt IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproduct} (A,D) and {\tt IsomorphismFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoequalizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfJointPairwiseDifferencesOfMorphismsFromCoepualizerToCokernelOfferencesOfMorphismsFromCoepualizerToCokernelOfferencesOfference$

7.6.127 AddIsomorphismFromCoimageToCokernelOfKernel (for IsCapCategory, Is-Function)

- - **Returns:** nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromCoimageToCokernelOfKernel. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto IsomorphismFromCoimageToCokernelOfKernel(alpha)$.

7.6.128 AddIsomorphismFromCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproductTo (for IsCapCategory, IsFunction)

- ${\tt > AddIsomorphismFromCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproductToCoequalizer(F, weight)} \\ (operation)$

Returns: nothing

arguments function F. This category Cand operaare the tion adds given function Fto category for the basic operation Is omorphism From Cokernel Of Joint Pairwise Differences Of Morphisms From Coproduct To Coequalizer.

Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,D) \mapsto IsomorphismFromCokernelOfJointPairwiseDifferencesOfMorphismsFromCoproductToCoequalizer(A,D)$

7.6.129 AddIsomorphismFromCokernelOfKernelToCoimage (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromCokernelOfKernelToCoimage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto IsomorphismFromCokernelOfKernelToCoimage(alpha)$.

7.6.130 AddIsomorphismFromCoproductToDirectSum (for IsCapCategory, IsFunction)

▷ AddIsomorphismFromCoproductToDirectSum(C, F) (operation)
▷ AddIsomorphismFromCoproductToDirectSum(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromCoproductToDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D) \mapsto \text{IsomorphismFromCoproductToDirectSum}(D)$.

$\textbf{7.6.131} \quad \textbf{AddIsomorphismFromDirectProductToDirectSum} \ \ (\textbf{for IsCapCategory, IsFunction})$

▷ AddIsomorphismFromDirectProductToDirectSum(C, F) (operation)

▷ AddIsomorphismFromDirectProductToDirectSum(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromDirectProductToDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D) \mapsto \text{IsomorphismFromDirectProductToDirectSum}(D)$.

7.6.132 AddIsomorphismFromDirectSumToCoproduct (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromDirectSumToCoproduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D) \mapsto IsomorphismFromDirectSumToCoproduct(D)$.

7.6.133 AddIsomorphismFromDirectSumToDirectProduct (for IsCapCategory, IsFunction)

 ${\hspace{0.2cm}} \hspace{0.2cm} \hspace{0.2cm}$

 $\qquad \qquad \qquad \triangleright \ \, \mathsf{AddIsomorphismFromDirectSumToDirectProduct}(\mathit{C},\ \mathit{F},\ \mathit{weight}) \\$

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromDirectSumToDirectProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D) \mapsto I$ somorphismFromDirectSumToDirectProduct(D).

7.6.134 AddIsomorphismFromEqualizerOfDirectProductDiagramToFiberProduct (for IsCapCategory, IsFunction)

▷ AddIsomorphismFromEqualizerOfDirectProductDiagramToFiberProduct(C, F) (operation)
▷ AddIsomorphismFromEqualizerOfDirectProductDiagramToFiberProduct(C, F,
weight) (operation)

Returns: nothing

The arguments are a category Cand a function F. This operafunction F the category for the operation tion the given to basic Isomorphism From Equalizer Of Direct Product Diagram To Fiber Product.Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D)\mapsto \mathtt{IsomorphismFromEqualizerOfDirectProductDiagramToFiberProduct}(D).$

7.6.135 AddIsomorphismFromEqualizerToKernelOfJointPairwiseDifferencesOfMorphismsIntoDire (for IsCapCategory, IsFunction)

- $> AddIsomorphismFromEqualizerToKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProduct (F) \\ (operation)$
- ▷ AddIsomorphismFromEqualizerToKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProduct(
 F, weight)
 (operation)

Returns: nothing

The arguments category Cand function This are a operation adds given function Fto the category for the basic Isomorphism From Equalizer To Kernel Of Joint Pairwise Differences Of Morphisms Into Direct Product.Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,D) \mapsto$ ${\tt IsomorphismFromEqualizerToKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProduct} (A,D) and {\tt IsomorphismFromEqualizerToKernelOfFormEqualizerToKernelOfToKernelOfFormEqualizerToKe$

7.6.136 AddIsomorphismFromFiberProductToEqualizerOfDirectProductDiagram (for IsCapCategory, IsFunction)

▷ AddIsomorphismFromFiberProductToEqualizerOfDirectProductDiagram(C, F) (operation)
▷ AddIsomorphismFromFiberProductToEqualizerOfDirectProductDiagram(C, F,
weight) (operation)

Returns: nothing

arguments The are category Cand function This operafunction operation tion adds the given to the category for the basic Isomorphism From Fiber Product To Equalizer Of Direct Product Diagram.Optionally, 100) can be specified which should roughly correspond to the coma weight (default: putational complexity of the function (lower weight = less complex = faster execution). $F:(D)\mapsto \mathtt{IsomorphismFromFiberProductToEqualizerOfDirectProductDiagram}(D).$

7.6.137 AddIsomorphismFromHomologyObjectToItsConstructionAsAnImageObject (for IsCapCategory, IsFunction)

 \triangleright AddIsomorphismFromHomologyObjectToItsConstructionAsAnImageObject(C, F) (operation)

Returns: nothing

arguments The are category Cand a function This operaa given function Fthe category the basic operation Isomorphism From Homology Object To Its Construction As An Image Object.Optionally, weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,beta) \mapsto$ IsomorphismFromHomologyObjectToItsConstructionAsAnImageObject(alpha, beta).

7.6.138 AddIsomorphismFromImageObjectToKernelOfCokernel (for IsCapCategory, IsFunction)

▷ AddIsomorphismFromImageObjectToKernelOfCokernel(C, F) (operation)
▷ AddIsomorphismFromImageObjectToKernelOfCokernel(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromImageObjectToKernelOfCokernel. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto IsomorphismFromImageObjectToKernelOfCokernel(alpha)$.

7.6.139 AddIsomorphismFromInitialObjectToZeroObject (for IsCapCategory, IsFunction)

▷ AddIsomorphismFromInitialObjectToZeroObject(C, F) (operation)
▷ AddIsomorphismFromInitialObjectToZeroObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromInitialObjectToZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto IsomorphismFromInitialObjectToZeroObject()$.

7.6.140 AddIsomorphismFromItsConstructionAsAnImageObjectToHomologyObject (for IsCapCategory, IsFunction)

- \triangleright AddIsomorphismFromItsConstructionAsAnImageObjectToHomologyObject(C, F) (operation)
- ${\tt > AddIsomorphismFromItsConstructionAsAnImageObjectToHomologyObject(\it{C}, \it{F}, \it{weight)}} \end{substructionAsAnImageObjectToHomologyObject(\it{C}, \it{F}, \it{weight)}}$

Returns: nothing

The arguments are a category Cand a function F. This operafunction Fthe adds the given to category for the basic operation Isomorphism From Its Construction As An Image Object To Homology Object.Optionally, weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,beta) \mapsto$ ${\tt IsomorphismFromItsConstructionAsAnImageObjectToHomologyObject} (alpha, beta).$

7.6.141 AddIsomorphismFromKernelOfCokernelToImageObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromKernelOfCokernelToImageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto IsomorphismFromKernelOfCokernelToImageObject(alpha)$.

7.6.142 AddIsomorphismFromKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProductTo (for IsCapCategory, IsFunction)

- ▷ AddIsomorphismFromKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProductToEqualizer(
 F)
 (operation)
- $\verb| > AddIsomorphismFromKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProductToEqualizer (F, weight) \\ (operation)$

Returns: nothing

arguments are category Cand function F. This a operagiven function Fthe category for the basic operation adds to Is omorphism From Kernel Of Joint Pairwise Differences Of Morphisms Into Direct Product To Equalizer.Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,D)\mapsto$ ${\tt IsomorphismFromKernelOfJointPairwiseDifferencesOfMorphismsIntoDirectProductToEqualizer} (A,D) \\$

7.6.143 AddIsomorphismFromPushoutToCoequalizerOfCoproductDiagram (for Is-CapCategory, IsFunction)

 $\begin{tabular}{l} \triangleright AddIsomorphismFromPushoutToCoequalizerOfCoproductDiagram(C, F) & (operation) \\ \triangleright AddIsomorphismFromPushoutToCoequalizerOfCoproductDiagram(C, F, $weight) & (operation) \\ \end{tabular}$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromPushoutToCoequalizerOfCoproductDiagram. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(D) \mapsto$ IsomorphismFromPushoutToCoequalizerOfCoproductDiagram(D).

7.6.144 AddIsomorphismFromTerminalObjectToZeroObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromTerminalObjectToZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto IsomorphismFromTerminalObjectToZeroObject()$.

7.6.145 AddIsomorphismFromZeroObjectToInitialObject (for IsCapCategory, IsFunction)

```
▷ AddIsomorphismFromZeroObjectToInitialObject(C, F) (operation)
▷ AddIsomorphismFromZeroObjectToInitialObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromZeroObjectToInitialObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto IsomorphismFromZeroObjectToInitialObject()$.

7.6.146 AddIsomorphismFromZeroObjectToTerminalObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation IsomorphismFromZeroObjectToTerminalObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto IsomorphismFromZeroObjectToTerminalObject()$.

7.6.147 AddJointPairwiseDifferencesOfMorphismsFromCoproduct (for IsCapCategory, IsFunction)

 $\begin{tabular}{ll} $ \rhd$ AddJointPairwiseDifferencesOfMorphismsFromCoproduct(C, F) & (operation) \\ $ \rhd$ AddJointPairwiseDifferencesOfMorphismsFromCoproduct(C, F, weight) & (operation) \\ \end{tabular}$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation JointPairwiseDifferencesOfMorphismsFromCoproduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,D) \mapsto \text{JointPairwiseDifferencesOfMorphismsFromCoproduct}(A,D)$.

7.6.148 AddJointPairwiseDifferencesOfMorphismsIntoDirectProduct (for IsCapCategory, IsFunction)

▷ AddJointPairwiseDifferencesOfMorphismsIntoDirectProduct(C, F) (operation)
▷ AddJointPairwiseDifferencesOfMorphismsIntoDirectProduct(C, F, weight) (operation)
Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation JointPairwiseDifferencesOfMorphismsIntoDirectProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,D)\mapsto \text{JointPairwiseDifferencesOfMorphismsIntoDirectProduct}(A,D)$.

7.6.149 AddKernelEmbedding (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation KernelEmbedding. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \text{KernelEmbedding}(alpha)$.

7.6.150 AddKernelEmbeddingWithGivenKernelObject (for IsCapCategory, IsFunction)

▷ AddKernelEmbeddingWithGivenKernelObject(C, F) (operation)

▷ AddKernelEmbeddingWithGivenKernelObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation KernelEmbeddingWithGivenKernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,P)\mapsto KernelEmbeddingWithGivenKernelObject(alpha,P)$.

7.6.151 AddKernelLift (for IsCapCategory, IsFunction)

ightharpoonup AddKernelLift(C, F) (operation) ightharpoonup AddKernelLift(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation KernelLift. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, T, tau) \mapsto \text{KernelLift}(alpha, T, tau)$.

7.6.152 AddKernelLiftWithGivenKernelObject (for IsCapCategory, IsFunction)

▷ AddKernelLiftWithGivenKernelObject(C, F) (operation)
▷ AddKernelLiftWithGivenKernelObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation KernelLiftWithGivenKernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,T,tau,P) \mapsto \text{KernelLiftWithGivenKernelObject}(alpha,T,tau,P)$.

7.6.153 AddKernelObject (for IsCapCategory, IsFunction)

▷ AddKernelObject(C, F) (operation)

▷ AddKernelObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation KernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \text{KernelObject}(alpha)$.

7.6.154 AddKernelObjectFunctorial (for IsCapCategory, IsFunction)

AddKernelObjectFunctorial(C, F) (operation)

 AddKernelObjectFunctorial(C, F, weight) (operation)

 Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation KernelObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,mu,alphap) \mapsto \text{KernelObjectFunctorial}(alpha,mu,alphap)$.

7.6.155 AddKernelObjectFunctorialWithGivenKernelObjects (for IsCapCategory, IsFunction)

▷ AddKernelObjectFunctorialWithGivenKernelObjects(C, F) (operation)
▷ AddKernelObjectFunctorialWithGivenKernelObjects(C, F, weight) (operation)

Returns: nothing

The function This arguments are a category Cand F. operation adds the given function to the category for the basic operation KernelObjectFunctorialWithGivenKernelObjects. Optionally, a weight (default: can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(P,alpha,mu,alphap,Pp) \mapsto$ KernelObjectFunctorialWithGivenKernelObjects(P, alpha, mu, alphap, Pp).

7.6.156 AddLift (for IsCapCategory, IsFunction)

```
ightharpoonup AddLift(C, F) (operation)

ightharpoonup AddLift(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation Lift. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, beta) \mapsto \text{Lift}(alpha, beta)$.

7.6.157 AddLiftAlongMonomorphism (for IsCapCategory, IsFunction)

```
▷ AddLiftAlongMonomorphism(C, F) (operation)
▷ AddLiftAlongMonomorphism(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation LiftAlongMonomorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(iota,tau) \mapsto \text{LiftAlongMonomorphism}(iota,tau)$.

7.6.158 AddLinearCombinationOfMorphisms (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation LinearCombinationOfMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (source, list_of_ring_elements, list_of_morphisms, range) \mapsto LinearCombinationOfMorphisms(source, list_of_ring_elements, list_of_morphisms, range).$

7.6.159 AddMereExistenceOfSolutionOfLinearSystemInAbCategory (for IsCapCategory, IsFunction)

```
▷ AddMereExistenceOfSolutionOfLinearSystemInAbCategory(C, F) (operation)
▷ AddMereExistenceOfSolutionOfLinearSystemInAbCategory(C, F, weight) (operation)
Returns: nothing
```

F. The arguments are category Cand function This operaadds given function Fthe the operation tion to category for basic

MereExistenceOfSolutionOfLinearSystemInAbCategory. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3, arg4) \mapsto MereExistenceOfSolutionOfLinearSystemInAbCategory(arg2, arg3, arg4)$.

7.6.160 AddMonomorphismIntoInjectiveEnvelopeObject (for IsCapCategory, Is-Function)

 ${\hspace{-0.2cm}\triangleright\hspace{-0.2cm}} \verb| AddMonomorphismIntoInjectiveEnvelopeObject({\it C, F}) \\ \\ (operation)$

▷ AddMonomorphismIntoInjectiveEnvelopeObject(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MonomorphismIntoInjectiveEnvelopeObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A) \mapsto \text{MonomorphismIntoInjectiveEnvelopeObject}(A)$.

7.6.161 AddMonomorphismIntoInjectiveEnvelopeObjectWithGivenInjectiveEnvelopeObject (for IsCapCategory, IsFunction)

▷ AddMonomorphismIntoInjectiveEnvelopeObjectWithGivenInjectiveEnvelopeObject(C, F)
(operation)

Returns: nothing

The arguments are a category Cand function F. This operafunction Fthe category for the operation tion the given to basic ${\tt MonomorphismIntoInjectiveEnvelope0bjectWithGivenInjectiveEnvelope0bject}.$ tionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,I)\mapsto$ MonomorphismIntoInjectiveEnvelopeObjectWithGivenInjectiveEnvelopeObject(A, I).

7.6.162 AddMonomorphismIntoSomeInjectiveObject (for IsCapCategory, IsFunction)

 ${\hspace{0.2cm}} \hspace{0.2cm} \hspace{0.2cm}$

▷ AddMonomorphismIntoSomeInjectiveObject(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MonomorphismIntoSomeInjectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A)\mapsto$ MonomorphismIntoSomeInjectiveObject(A).

7.6.163 AddMonomorphismIntoSomeInjectiveObjectWithGivenSomeInjectiveObject (for IsCapCategory, IsFunction)

 \triangleright AddMonomorphismIntoSomeInjectiveObjectWithGivenSomeInjectiveObject(C, F) (operation)

Returns: nothing

This The arguments function F. are category Cand operagiven function Fthe category the operation tion adds the to for basic MonomorphismIntoSomeInjectiveObjectWithGivenSomeInjectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,I)\mapsto MonomorphismIntoSomeInjectiveObjectWithGivenSomeInjectiveObject(A,I).$

7.6.164 AddMorphismBetweenDirectSums (for IsCapCategory, IsFunction)

ightharpoonup AddMorphismBetweenDirectSums (C, F) (operation) ightharpoonup (operation) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismBetweenDirectSums. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (source_diagram, mat, range_diagram) \mapsto MorphismBetweenDirectSums(source_diagram, mat, range_diagram)$.

7.6.165 AddMorphismBetweenDirectSumsWithGivenDirectSums (for IsCapCategory, IsFunction)

▷ AddMorphismBetweenDirectSumsWithGivenDirectSums(C, F) (operation)
▷ AddMorphismBetweenDirectSumsWithGivenDirectSums(C, F, weight) (operation)
Returns: nothing

The arguments are a category C and a function F. This operation adds the given function Fto the category for the basic operation MorphismBetweenDirectSumsWithGivenDirectSums. Optionally, a weight (default: 100) can be specified which should roughly correspond computational complexity of the function (lower weight = less the complex faster execution). $F: (S, source_d iagram, mat, range_d iagram, T) \rightarrow$ MorphismBetweenDirectSumsWithGivenDirectSums $(S, source_diagram, mat, range_diagram, T)$.

7.6.166 AddMorphismConstructor (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismConstructor. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complex-

ity of the function (lower weight = less complex = faster execution). $F:(arg2, arg3, arg4) \mapsto$ MorphismConstructor(arg2, arg3, arg4).

7.6.167 AddMorphismDatum (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismDatum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{MorphismDatum}(arg2)$.

7.6.168 AddMorphismFromCoimageToImage (for IsCapCategory, IsFunction)

▷ AddMorphismFromCoimageToImage(C, F) (operation)
▷ AddMorphismFromCoimageToImage(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromCoimageToImage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha)\mapsto MorphismFromCoimageToImage(alpha)$.

7.6.169 AddMorphismFromCoimageToImageWithGivenObjects (for IsCapCategory, IsFunction)

```
▷ AddMorphismFromCoimageToImageWithGivenObjects(C, F) (operation)
▷ AddMorphismFromCoimageToImageWithGivenObjects(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromCoimageToImageWithGivenObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(C,alpha,I) \mapsto MorphismFromCoimageToImageWithGivenObjects(C,alpha,I)$.

7.6.170 AddMorphismFromEqualizerToSink (for IsCapCategory, IsFunction)

```
▷ AddMorphismFromEqualizerToSink(C, F) (operation)

▷ AddMorphismFromEqualizerToSink(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromEqualizerToSink. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y,morphisms) \mapsto MorphismFromEqualizerToSink(Y,morphisms)$.

7.6.171 AddMorphismFromEqualizerToSinkWithGivenEqualizer (for IsCapCategory, IsFunction)

 \triangleright AddMorphismFromEqualizerToSinkWithGivenEqualizer(C, F) (operation)

 ${\tt \hspace*{0.5cm} \hspace*{0.5cm} \hspace*{0.5cm}} \hspace*{0.5cm} \hspace*{0.5cm}$

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromEqualizerToSinkWithGivenEqualizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms, P) \mapsto MorphismFromEqualizerToSinkWithGivenEqualizer(Y, morphisms, P)$.

7.6.172 AddMorphismFromFiberProductToSink (for IsCapCategory, IsFunction)

(operation)

▷ AddMorphismFromFiberProductToSink(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromFiberProductToSink. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms) \mapsto MorphismFromFiberProductToSink(morphisms)$.

7.6.173 AddMorphismFromFiberProductToSinkWithGivenFiberProduct (for IsCap-Category, IsFunction)

▷ AddMorphismFromFiberProductToSinkWithGivenFiberProduct(C, F) (operation)

▷ AddMorphismFromFiberProductToSinkWithGivenFiberProduct(C, F, weight) (operation)
Returns: nothing

The arguments function F. This are category Cand operation adds the given function the category for the basic operation ${\tt MorphismFromFiberProductToSinkWithGivenFiberProduct}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(morphisms, P) \mapsto$ MorphismFromFiberProductToSinkWithGivenFiberProduct(morphisms, P).

7.6.174 AddMorphismFromKernelObjectToSink (for IsCapCategory, IsFunction)

AddMorphismFromKernelObjectToSink(C, F)

(operation)

ightharpoonup AddMorphismFromKernelObjectToSink(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromKernelObjectToSink. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha)\mapsto MorphismFromKernelObjectToSink(alpha)$.

7.6.175 AddMorphismFromKernelObjectToSinkWithGivenKernelObject (for IsCap-Category, IsFunction)

- ▷ AddMorphismFromKernelObjectToSinkWithGivenKernelObject(C, F, weight) (operation)
 Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromKernelObjectToSinkWithGivenKernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,P)\mapsto MorphismFromKernelObjectToSinkWithGivenKernelObject(alpha,P)$.

7.6.176 AddMorphismFromSourceToCoequalizer (for IsCapCategory, IsFunction)

 ${\hspace{0.2cm}\triangleright\hspace{0.2cm}} {\hspace{0.2cm}} {\hspace{0.2cm}}$

▷ AddMorphismFromSourceToCoequalizer(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromSourceToCoequalizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y,morphisms)\mapsto MorphismFromSourceToCoequalizer(Y,morphisms)$.

7.6.177 AddMorphismFromSourceToCoequalizerWithGivenCoequalizer (for IsCap-Category, IsFunction)

- ${\tt \hspace*{0.5cm}} \hspace*{0.5cm} \hspace*{0.5cm}$

The arguments Cfunction F. This are category and operation adds the given function to the category for the basic operation ${\tt MorphismFromSourceToCoequalizerWithGivenCoequalizer}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms, P) \mapsto$ MorphismFromSourceToCoequalizerWithGivenCoequalizer(Y, morphisms, P).

7.6.178 AddMorphismFromSourceToCokernelObject (for IsCapCategory, IsFunction)

- \triangleright AddMorphismFromSourceToCokernelObject(C, F) (operation)
- ${\tt \triangleright} \ {\tt AddMorphismFromSourceToCokernelObject(\it{C}, \it{F}, \it{weight})}$

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromSourceToCokernelObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto MorphismFromSourceToCokernelObject(alpha)$.

7.6.179 AddMorphismFromSourceToCokernelObjectWithGivenCokernelObject (for IsCapCategory, IsFunction)

(operation)

Returns: nothing

The arguments are category Cand function This operation adds the given function the category for the basic operation Fto ${\tt MorphismFromSourceToCokernelObjectWithGivenCokernelObject}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,P) \mapsto$ MorphismFromSourceToCokernelObjectWithGivenCokernelObject(alpha, P).

7.6.180 AddMorphismFromSourceToPushout (for IsCapCategory, IsFunction)

AddMorphismFromSourceToPushout(C, F)

(operation)

▷ AddMorphismFromSourceToPushout(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromSourceToPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(morphisms) \mapsto MorphismFromSourceToPushout(morphisms)$.

7.6.181 AddMorphismFromSourceToPushoutWithGivenPushout (for IsCapCategory, IsFunction)

- ▷ AddMorphismFromSourceToPushoutWithGivenPushout(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismFromSourceToPushoutWithGivenPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, P) \mapsto MorphismFromSourceToPushoutWithGivenPushout(morphisms, P)$.

7.6.182 AddMorphismsOfExternalHom (for IsCapCategory, IsFunction)

 \triangleright AddMorphismsOfExternalHom(C, F)

(operation)

 ${\tt \vartriangleright} \ \, {\tt AddMorphismsOfExternalHom}(\mathit{C}, \ \mathit{F}, \ \mathit{weight})$

operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MorphismsOfExternalHom. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{MorphismsOfExternalHom}(arg2, arg3)$.

7.6.183 AddMultiplyWithElementOfCommutativeRingForMorphisms (for IsCap-Category, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation MultiplyWithElementOfCommutativeRingForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(r,alpha) \mapsto \text{MultiplyWithElementOfCommutativeRingForMorphisms}(r,alpha).$

7.6.184 AddObjectConstructor (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ObjectConstructor. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto ObjectConstructor(arg2)$.

7.6.185 AddObjectDatum (for IsCapCategory, IsFunction)

▷ AddObjectDatum(C, F) (operation)

▷ AddObjectDatum(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ObjectDatum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \texttt{ObjectDatum}(arg2)$.

7.6.186 AddPostCompose (for IsCapCategory, IsFunction)

▷ AddPostCompose(C, F) (operation)

▷ AddPostCompose(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PostCompose. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(beta, alpha) \mapsto \texttt{PostCompose}(beta, alpha)$.

7.6.187 AddPostComposeList (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PostComposeList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (source, list_of_morphisms, range) \mapsto PostComposeList(source, list_of_morphisms, range)$.

7.6.188 AddPostInverseForMorphisms (for IsCapCategory, IsFunction)

```
▷ AddPostInverseForMorphisms(C, F) (operation)
▷ AddPostInverseForMorphisms(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PostInverseForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \text{PostInverseForMorphisms}(alpha)$.

7.6.189 AddPreCompose (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PreCompose. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, beta) \mapsto \texttt{PreCompose}(alpha, beta)$.

7.6.190 AddPreComposeList (for IsCapCategory, IsFunction)

```
▷ AddPreComposeList(C, F) (operation)

▷ AddPreComposeList(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PreComposeList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(source, list_of_morphisms, range) \mapsto PreComposeList(source, list_of_morphisms, range)$.

7.6.191 AddPreInverseForMorphisms (for IsCapCategory, IsFunction)

```
▷ AddPreInverseForMorphisms(C, F) (operation)
▷ AddPreInverseForMorphisms(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PreInverseForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha) \mapsto \text{PreInverseForMorphisms}(alpha)$.

7.6.192 AddProjectionInFactorOfDirectProduct (for IsCapCategory, IsFunction)

▷ AddProjectionInFactorOfDirectProduct(C, F) (operation)
▷ AddProjectionInFactorOfDirectProduct(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectionInFactorOfDirectProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,k) \mapsto ProjectionInFactorOfDirectProduct(objects,k)$.

7.6.193 AddProjectionInFactorOfDirectProductWithGivenDirectProduct (for IsCap-Category, IsFunction)

 $> AddProjectionInFactorOfDirectProductWithGivenDirectProduct(\textit{C}, F) \qquad \text{(operation)}$ > AddProjectionInFactorOfDirectProductWithGivenDirectProduct(C, F, weight) (operation)

Returns: nothing

The arguments function F. This are category Cand operafunction basic operation tion adds the given to the category for the ${\tt ProjectionInFactorOfDirectProductWithGivenDirectProduct}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,k,P) \mapsto$ ProjectionInFactorOfDirectProductWithGivenDirectProduct(objects, k, P).

7.6.194 AddProjectionInFactorOfDirectSum (for IsCapCategory, IsFunction)

▷ AddProjectionInFactorOfDirectSum(C, F) (operation)
▷ AddProjectionInFactorOfDirectSum(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectionInFactorOfDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,k) \mapsto ProjectionInFactorOfDirectSum(objects,k)$.

7.6.195 AddProjectionInFactorOfDirectSumWithGivenDirectSum (for IsCapCategory, IsFunction)

▷ AddProjectionInFactorOfDirectSumWithGivenDirectSum(C, F) (operation)
▷ AddProjectionInFactorOfDirectSumWithGivenDirectSum(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectionInFactorOfDirectSumWithGivenDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). F: $(objects, k, P) \mapsto ProjectionInFactorOfDirectSumWithGivenDirectSum(objects, k, P)$.

7.6.196 AddProjectionInFactorOfFiberProduct (for IsCapCategory, IsFunction)

```
▷ AddProjectionInFactorOfFiberProduct(C, F) (operation)
▷ AddProjectionInFactorOfFiberProduct(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectionInFactorOfFiberProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, k) \mapsto ProjectionInFactorOfFiberProduct(morphisms, k)$.

7.6.197 AddProjectionInFactorOfFiberProductWithGivenFiberProduct (for IsCap-Category, IsFunction)

```
 \begin{tabular}{ll} $ > $ AddProjectionInFactorOfFiberProductWithGivenFiberProduct($C$, $F$) & (operation) \\ $ > $ AddProjectionInFactorOfFiberProductWithGivenFiberProduct($C$, $F$, $weight) & (operation) \\ \end{tabular}
```

Returns: nothing

The arguments function F. This are category Cand operaoperation function the tion adds the given to the category basic ${\tt ProjectionInFactorOfFiberProductWithGivenFiberProduct}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, k, P) \mapsto$ ProjectionInFactorOfFiberProductWithGivenFiberProduct(morphisms, k, P).

7.6.198 AddProjectionOntoCoequalizer (for IsCapCategory, IsFunction)

```
▷ AddProjectionOntoCoequalizer(C, F) (operation)
▷ AddProjectionOntoCoequalizer(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectionOntoCoequalizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms) \mapsto ProjectionOntoCoequalizer(Y, morphisms)$.

7.6.199 AddProjectionOntoCoequalizerWithGivenCoequalizer (for IsCapCategory, IsFunction)

```
▷ AddProjectionOntoCoequalizerWithGivenCoequalizer(C, F) (operation)

▷ AddProjectionOntoCoequalizerWithGivenCoequalizer(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectionOntoCoequalizerWithGivenCoequalizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms, P) \mapsto ProjectionOntoCoequalizerWithGivenCoequalizer(Y, morphisms, P)$.

7.6.200 AddProjectiveCoverObject (for IsCapCategory, IsFunction)

```
▷ AddProjectiveCoverObject(C, F) (operation)
▷ AddProjectiveCoverObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectiveCoverObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{ProjectiveCoverObject}(arg2)$.

7.6.201 AddProjectiveDimension (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectiveDimension. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \texttt{ProjectiveDimension}(arg2)$.

7.6.202 AddProjectiveLift (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ProjectiveLift. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, beta) \mapsto \texttt{ProjectiveLift}(alpha, beta)$.

7.6.203 AddPushout (for IsCapCategory, IsFunction)

```
▷ AddPushout(C, F) (operation)

▷ AddPushout(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation Pushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms) \mapsto Pushout(morphisms)$.

7.6.204 AddPushoutFunctorial (for IsCapCategory, IsFunction)

```
▷ AddPushoutFunctorial(C, F) (operation)

▷ AddPushoutFunctorial(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PushoutFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the

function (lower weight = less complex = faster execution). $F:(morphisms, L, morphismsp) \mapsto PushoutFunctorial(morphisms, L, morphismsp)$.

7.6.205 AddPushoutFunctorialWithGivenPushouts (for IsCapCategory, IsFunction)

- ${\hspace{0.2cm}\triangleright\hspace{0.1cm}} {\hspace{0.1cm}} {\hspace{0.1cm}}$
- ▷ AddPushoutFunctorialWithGivenPushouts(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation PushoutFunctorialWithGivenPushouts. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (P, morphisms, L, morphismsp, Pp) \mapsto PushoutFunctorialWithGivenPushouts(<math>P, morphisms, L, morphismsp, Pp)$.

7.6.206 AddRandomMorphismByInteger (for IsCapCategory, IsFunction)

- \triangleright AddRandomMorphismByInteger(C, F) (operation)
- ▷ AddRandomMorphismByInteger(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismByInteger. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(n) \mapsto \text{RandomMorphismByInteger}(n)$.

7.6.207 AddRandomMorphismByList (for IsCapCategory, IsFunction)

- \triangleright AddRandomMorphismByList(C, F) (operation)
- ▷ AddRandomMorphismByList(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismByList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(L) \mapsto \mathtt{RandomMorphismByList}(L)$.

7.6.208 AddRandomMorphismWithFixedRangeByInteger (for IsCapCategory, IsFunction)

- ▷ AddRandomMorphismWithFixedRangeByInteger(C, F) (operation)
- ▷ AddRandomMorphismWithFixedRangeByInteger(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismWithFixedRangeByInteger. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(B,n) \mapsto \text{RandomMorphismWithFixedRangeByInteger}(B,n)$.

7.6.209 AddRandomMorphismWithFixedRangeByList (for IsCapCategory, IsFunction)

 $\qquad \qquad \triangleright \ \, \mathsf{AddRandomMorphismWithFixedRangeByList}(\mathit{C}, \ \mathit{F}) \qquad \qquad \mathsf{(operation)}$

▷ AddRandomMorphismWithFixedRangeByList(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismWithFixedRangeByList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(B,L)\mapsto RandomMorphismWithFixedRangeByList(B,L)$.

7.6.210 AddRandomMorphismWithFixedSourceAndRangeByInteger (for IsCapCategory, IsFunction)

 ${\tt \hspace*{0.5cm}} {\tt \hspace*{0.5cm}}$

 ${\color{blue} \triangleright} \ \, \mathsf{AddRandomMorphismWithFixedSourceAndRangeByInteger(\mathit{C},\ \mathit{F,\ weight})} \qquad \qquad (\mathsf{operation})$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismWithFixedSourceAndRangeByInteger. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,B,n)\mapsto RandomMorphismWithFixedSourceAndRangeByInteger(A,B,n)$.

7.6.211 AddRandomMorphismWithFixedSourceAndRangeByList (for IsCapCategory, IsFunction)

▷ AddRandomMorphismWithFixedSourceAndRangeByList(C, F) (operation)

▷ AddRandomMorphismWithFixedSourceAndRangeByList(C, F, weight)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismWithFixedSourceAndRangeByList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,B,L)\mapsto RandomMorphismWithFixedSourceAndRangeByList(A,B,L)$.

7.6.212 AddRandomMorphismWithFixedSourceByInteger (for IsCapCategory, IsFunction)

 $\qquad \qquad \triangleright \ \, \mathsf{AddRandomMorphismWithFixedSourceByInteger}(\mathit{C}, \ \mathit{F}) \qquad \qquad (\mathsf{operation})$

▷ AddRandomMorphismWithFixedSourceByInteger(C, F, weight)

(operation)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismWithFixedSourceByInteger. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,n)\mapsto RandomMorphismWithFixedSourceByInteger(A,n)$.

7.6.213 AddRandomMorphismWithFixedSourceByList (for IsCapCategory, IsFunction)

▷ AddRandomMorphismWithFixedSourceByList(C, F) (operation)
▷ AddRandomMorphismWithFixedSourceByList(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomMorphismWithFixedSourceByList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,L) \mapsto \text{RandomMorphismWithFixedSourceByList}(A,L)$.

7.6.214 AddRandomObjectByInteger (for IsCapCategory, IsFunction)

▷ AddRandomObjectByInteger(C, F) (operation)
▷ AddRandomObjectByInteger(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomObjectByInteger. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(n) \mapsto \text{RandomObjectByInteger}(n)$.

7.6.215 AddRandomObjectByList (for IsCapCategory, IsFunction)

▷ AddRandomObjectByList(C, F) (operation)

▷ AddRandomObjectByList(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation RandomObjectByList. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(L) \mapsto \mathtt{RandomObjectByList}(L)$.

7.6.216 AddSimplifyEndo (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyEndo. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (mor, n) \mapsto \text{SimplifyEndo}(mor, n)$.

7.6.217 AddSimplifyEndo_IsoFromInputObject (for IsCapCategory, IsFunction)

AddSimplifyEndo_IsoFromInputObject(C, F) (operation)

 AddSimplifyEndo_IsoFromInputObject(C, F, weight) (operation)

 Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyEndo_IsoFromInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifyEndo_IsoFromInputObject(mor,n)$.

7.6.218 AddSimplifyEndo_IsoToInputObject (for IsCapCategory, IsFunction)

```
    AddSimplifyEndo_IsoToInputObject(C, F) (operation)

    AddSimplifyEndo_IsoToInputObject(C, F, weight) (operation)

    Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyEndo_IsoToInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifyEndo_IsoToInputObject(mor,n)$.

7.6.219 AddSimplifyMorphism (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyMorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (mor, n) \mapsto \text{SimplifyMorphism}(mor, n)$.

7.6.220 AddSimplifyObject (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,n)\mapsto \text{SimplifyObject}(A,n)$.

7.6.221 AddSimplifyObject_IsoFromInputObject (for IsCapCategory, IsFunction)

```
▷ AddSimplifyObject_IsoFromInputObject(C, F) (operation)
▷ AddSimplifyObject_IsoFromInputObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyObject_IsoFromInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,n)\mapsto SimplifyObject_IsoFromInputObject(A,n)$.

7.6.222 AddSimplifyObject_IsoToInputObject (for IsCapCategory, IsFunction)

```
▷ AddSimplifyObject_IsoToInputObject(C, F) (operation)
▷ AddSimplifyObject_IsoToInputObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyObject_IsoToInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(A,n) \mapsto \text{SimplifyObject_IsoToInputObject}(A,n)$.

7.6.223 AddSimplifyRange (for IsCapCategory, IsFunction)

```
    AddSimplifyRange(C, F) (operation)

    AddSimplifyRange(C, F, weight) (operation)

    Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyRange. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (mor, n) \mapsto \text{SimplifyRange}(mor, n)$.

7.6.224 AddSimplifyRange_IsoFromInputObject (for IsCapCategory, IsFunction)

```
▷ AddSimplifyRange_IsoFromInputObject(C, F) (operation)

▷ AddSimplifyRange_IsoFromInputObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyRange_IsoFromInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifyRange_IsoFromInputObject(mor,n)$.

7.6.225 AddSimplifyRange_IsoToInputObject (for IsCapCategory, IsFunction)

```
▷ AddSimplifyRange_IsoToInputObject(C, F) (operation)
▷ AddSimplifyRange_IsoToInputObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifyRange_IsoToInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifyRange_IsoToInputObject(mor,n)$.

7.6.226 AddSimplifySource (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySource. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (mor, n) \mapsto \text{SimplifySource}(mor, n)$.

7.6.227 AddSimplifySourceAndRange (for IsCapCategory, IsFunction)

```
▷ AddSimplifySourceAndRange(C, F) (operation)
▷ AddSimplifySourceAndRange(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySourceAndRange. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (mor, n) \mapsto \text{SimplifySourceAndRange}(mor, n)$.

7.6.228 AddSimplifySourceAndRange_IsoFromInputRange (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySourceAndRange_IsoFromInputRange. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifySourceAndRange_IsoFromInputRange(mor,n)$.

7.6.229 AddSimplifySourceAndRange_IsoFromInputSource (for IsCapCategory, IsFunction)

```
▷ AddSimplifySourceAndRange_IsoFromInputSource(C, F) (operation)
▷ AddSimplifySourceAndRange_IsoFromInputSource(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySourceAndRange_IsoFromInputSource. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifySourceAndRange_IsoFromInputSource(mor,n)$.

7.6.230 AddSimplifySourceAndRange_IsoToInputRange (for IsCapCategory, Is-Function)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySourceAndRange_IsoToInputRange. Option-

ally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto \texttt{SimplifySourceAndRange}_{\texttt{IsoToInputRange}}(mor,n)$.

7.6.231 AddSimplifySourceAndRange_IsoToInputSource (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySourceAndRange_IsoToInputSource. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifySourceAndRange_IsoToInputSource(mor,n)$.

7.6.232 AddSimplifySource_IsoFromInputObject (for IsCapCategory, IsFunction)

```
▷ AddSimplifySource_IsoFromInputObject(C, F) (operation)
▷ AddSimplifySource_IsoFromInputObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySource_IsoFromInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto \text{SimplifySource}_{\text{I}} \text{soFromInputObject}(mor,n)$.

7.6.233 AddSimplifySource_IsoToInputObject (for IsCapCategory, IsFunction)

```
▷ AddSimplifySource_IsoToInputObject(C, F) (operation)
▷ AddSimplifySource_IsoToInputObject(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SimplifySource_IsoToInputObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(mor,n) \mapsto SimplifySource_IsoToInputObject(mor,n)$.

7.6.234 AddSolveLinearSystemInAbCategory (for IsCapCategory, IsFunction)

```
    AddSolveLinearSystemInAbCategory(C, F) (operation)

    AddSolveLinearSystemInAbCategory(C, F, weight) (operation)

    Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SolveLinearSystemInAbCategory. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3, arg4) \mapsto$ SolveLinearSystemInAbCategory(arg2, arg3, arg4).

7.6.235 AddSomeInjectiveObject (for IsCapCategory, IsFunction)

```
▷ AddSomeInjectiveObject(C, F) (operation)

▷ AddSomeInjectiveObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SomeInjectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \text{SomeInjectiveObject}(arg2)$.

7.6.236 AddSomeIsomorphismBetweenObjects (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SomeIsomorphismBetweenObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(object_1, object_2) \mapsto SomeIsomorphismBetweenObjects(object_1, object_2)$.

7.6.237 AddSomeProjectiveObject (for IsCapCategory, IsFunction)

```
▷ AddSomeProjectiveObject(C, F) (operation)

▷ AddSomeProjectiveObject(C, F, weight) (operation)
```

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SomeProjectiveObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2) \mapsto \texttt{SomeProjectiveObject}(arg2)$.

7.6.238 AddSomeReductionBySplitEpiSummand (for IsCapCategory, IsFunction)

```
▷ AddSomeReductionBySplitEpiSummand(C, F) (operation)
▷ AddSomeReductionBySplitEpiSummand(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SomeReductionBySplitEpiSummand. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto SomeReductionBySplitEpiSummand(alpha)$.

7.6.239 AddSomeReductionBySplitEpiSummand_MorphismFromInputRange (for IsCapCategory, IsFunction)

tion)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SomeReductionBySplitEpiSummand_MorphismFromInputRange. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto SomeReductionBySplitEpiSummand_MorphismFromInputRange(<math>alpha$).

7.6.240 AddSomeReductionBySplitEpiSummand_MorphismToInputRange (for Is-CapCategory, IsFunction)

- $\qquad \qquad \triangleright \ \, \mathsf{AddSomeReductionBySplitEpiSummand_MorphismToInputRange}(\mathcal{C}, \ F) \qquad \qquad (\mathsf{operation})$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SomeReductionBySplitEpiSummand_MorphismToInputRange. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha) \mapsto SomeReductionBySplitEpiSummand_MorphismToInputRange(<math>alpha$).

7.6.241 AddSubtractionForMorphisms (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SubtractionForMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,beta) \mapsto SubtractionForMorphisms(alpha,beta)$.

7.6.242 AddSumOfMorphisms (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation SumOfMorphisms. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (source, list_of_morphisms, range) \mapsto SumOfMorphisms(source, list_of_morphisms, range)$.

7.6.243 AddTerminalObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation TerminalObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: () \mapsto \texttt{TerminalObject}()$.

7.6.244 AddTerminalObjectFunctorial (for IsCapCategory, IsFunction)

```
▷ AddTerminalObjectFunctorial(C, F) (operation)
▷ AddTerminalObjectFunctorial(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation TerminalObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:() \mapsto \texttt{TerminalObjectFunctorial}()$.

7.6.245 AddTerminalObjectFunctorialWithGivenTerminalObjects (for IsCapCategory, IsFunction)

```
▷ AddTerminalObjectFunctorialWithGivenTerminalObjects(C, F) (operation)
▷ AddTerminalObjectFunctorialWithGivenTerminalObjects(C, F, weight) (operation)
Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation TerminalObjectFunctorialWithGivenTerminalObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(P,Pp) \mapsto \text{TerminalObjectFunctorialWithGivenTerminalObjects}(P,Pp)$.

7.6.246 AddUniversalMorphismFromCoequalizer (for IsCapCategory, IsFunction)

```
▷ AddUniversalMorphismFromCoequalizer(C, F) (operation)

▷ AddUniversalMorphismFromCoequalizer(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromCoequalizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (Y, morphisms, T, tau) \mapsto UniversalMorphismFromCoequalizer(Y, morphisms, T, tau)$.

7.6.247 AddUniversalMorphismFromCoequalizerWithGivenCoequalizer (for IsCap-Category, IsFunction)

```
▷ AddUniversalMorphismFromCoequalizerWithGivenCoequalizer(C, F) (operation)
▷ AddUniversalMorphismFromCoequalizerWithGivenCoequalizer(C, F, weight) (operation)
Returns: nothing
```

The arguments function F. This are category Cand operation adds the given function to the category for the basic operation

UniversalMorphismFromCoequalizerWithGivenCoequalizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y,morphisms,T,tau,P) \mapsto$ UniversalMorphismFromCoequalizerWithGivenCoequalizer(Y,morphisms,T,tau,P).

7.6.248 AddUniversalMorphismFromCoproduct (for IsCapCategory, IsFunction)

(operation)

(operation)

 ${\tt \hspace*{0.5cm}} {\tt \hspace*{0.5cm}} {\tt \hspace*{0.5cm}} {\tt \hspace*{0.5cm}} {\tt \hspace*{0.5cm}} {\tt AddUniversalMorphismFromCoproduct}({\tt C, F, weight}) \\$

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromCoproduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,T,tau)\mapsto UniversalMorphismFromCoproduct(objects,T,tau)$.

7.6.249 AddUniversalMorphismFromCoproductWithGivenCoproduct (for IsCap-Category, IsFunction)

- $\qquad \qquad \triangleright \ \, \mathsf{AddUniversalMorphismFromCoproductWithGivenCoproduct}\left(\mathit{C},\ \mathit{F}\right) \qquad \qquad (\mathsf{operation})$
- ${\tt \hspace*{0.5cm}} \hspace*{0.5cm} \hspace*{0.5cm}$

Returns: nothing

The arguments are a category Cand function This operafunction tion adds the given to the category for the basic operation ${\tt UniversalMorphismFromCoproductWithGivenCoproduct}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects, T, tau, P) \mapsto$ UniversalMorphismFromCoproductWithGivenCoproduct(objects, T, tau, P).

7.6.250 AddUniversalMorphismFromDirectSum (for IsCapCategory, IsFunction)

▷ AddUniversalMorphismFromDirectSum(C, F)

(operation)

▷ AddUniversalMorphismFromDirectSum(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects, T, tau) \mapsto UniversalMorphismFromDirectSum(objects, T, tau)$.

7.6.251 AddUniversalMorphismFromDirectSumWithGivenDirectSum (for IsCap-Category, IsFunction)

- ${\tt \hspace*{0.5cm}} {\tt \hspace*{0.5cm}}$
- ${\tt \hspace*{0.5cm}} \hspace*{0.5cm} \hspace*{0.5cm}$

function This The arguments are a category Cand F. operation adds the given function the category the basic operation Optionally, a weight (default: ${\tt UniversalMorphismFromDirectSumWithGivenDirectSum}.$ 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects, T, tau, P) \mapsto$ ${\tt UniversalMorphismFromDirectSumWithGivenDirectSum} (objects, T, tau, P).$

7.6.252 AddUniversalMorphismFromImage (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromImage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, tau) \mapsto UniversalMorphismFromImage(alpha, tau)$.

7.6.253 AddUniversalMorphismFromImageWithGivenImageObject (for IsCapCategory, IsFunction)

▷ AddUniversalMorphismFromImageWithGivenImageObject(C, F) (operation)

▷ AddUniversalMorphismFromImageWithGivenImageObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromImageWithGivenImageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (alpha, tau, I) \mapsto UniversalMorphismFromImageWithGivenImageObject(alpha, tau, I)$.

7.6.254 AddUniversalMorphismFromInitialObject (for IsCapCategory, IsFunction)

▷ AddUniversalMorphismFromInitialObject(C, F) (operation)

▷ AddUniversalMorphismFromInitialObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromInitialObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T) \mapsto \text{UniversalMorphismFromInitialObject}(T)$.

7.6.255 AddUniversalMorphismFromInitialObjectWithGivenInitialObject (for Is-CapCategory, IsFunction)

 $\begin{tabular}{ll} $ > $ AddUniversalMorphismFromInitialObjectWithGivenInitialObject({\it C}, {\it F}) $ & operation) \\ $ > $ AddUniversalMorphismFromInitialObjectWithGivenInitialObject({\it C}, {\it F}, {\it weight}) $ & operation) \\ \end{tabular}$

function This The arguments are a category Cand F. operation adds the given function to the category the basic operation UniversalMorphismFromInitialObjectWithGivenInitialObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T,P)\mapsto$ ${\tt UniversalMorphismFromInitialObjectWithGivenInitialObject}(T,P).$

7.6.256 AddUniversalMorphismFromPushout (for IsCapCategory, IsFunction)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, T, tau) \mapsto UniversalMorphismFromPushout(morphisms, T, tau)$.

7.6.257 AddUniversalMorphismFromPushoutWithGivenPushout (for IsCapCategory, IsFunction)

- $\qquad \qquad \triangleright \ \, \mathsf{AddUniversalMorphismFromPushoutWithGivenPushout(\mathit{C},\ \mathit{F})} \qquad \qquad (operation)$
- > AddUniversalMorphismFromPushoutWithGivenPushout(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromPushoutWithGivenPushout. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, T, tau, P) \mapsto UniversalMorphismFromPushoutWithGivenPushout(morphisms, T, tau, P)$.

7.6.258 AddUniversalMorphismFromZeroObject (for IsCapCategory, IsFunction)

- ▷ AddUniversalMorphismFromZeroObject(C, F)
- (operation)

▷ AddUniversalMorphismFromZeroObject(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T)\mapsto U$ niversalMorphismFromZeroObject(T).

7.6.259 AddUniversalMorphismFromZeroObjectWithGivenZeroObject (for IsCap-Category, IsFunction)

- > AddUniversalMorphismFromZeroObjectWithGivenZeroObject(C, F) (operation)
- ► AddUniversalMorphismFromZeroObjectWithGivenZeroObject(C, F, weight) (operation)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismFromZeroObjectWithGivenZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (T,P) \mapsto U$ niversalMorphismFromZeroObjectWithGivenZeroObject(T,P).

7.6.260 AddUniversalMorphismIntoCoimage (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoCoimage. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(alpha,tau) \mapsto UniversalMorphismIntoCoimage(alpha,tau)$.

7.6.261 AddUniversalMorphismIntoCoimageWithGivenCoimageObject (for IsCap-Category, IsFunction)

▷ AddUniversalMorphismIntoCoimageWithGivenCoimageObject(C, F) (operation)
▷ AddUniversalMorphismIntoCoimageWithGivenCoimageObject(C, F, weight) (operation)
Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoCoimageWithGivenCoimageObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). F: $(alpha,tau,C) \mapsto$ UniversalMorphismIntoCoimageWithGivenCoimageObject(alpha,tau,C).

7.6.262 AddUniversalMorphismIntoDirectProduct (for IsCapCategory, IsFunction)

```
▷ AddUniversalMorphismIntoDirectProduct(C, F) (operation)

▷ AddUniversalMorphismIntoDirectProduct(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoDirectProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,T,tau) \mapsto UniversalMorphismIntoDirectProduct(objects,T,tau)$.

7.6.263 AddUniversalMorphismIntoDirectProductWithGivenDirectProduct (for Is-CapCategory, IsFunction)

 \triangleright AddUniversalMorphismIntoDirectProductWithGivenDirectProduct(C, F) (operation) \triangleright AddUniversalMorphismIntoDirectProductWithGivenDirectProduct(C, F, weight) (operation)

This The arguments are a category Cand function F. operation adds the given function to the category the basic operation ${\tt Universal Morphism Into Direct Product With Given Direct Product}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,T,tau,P)\mapsto$ ${\tt UniversalMorphismIntoDirectProductWithGivenDirectProduct} (objects, T, tau, P).$

AddUniversalMorphismIntoDirectSum (for IsCapCategory, IsFunction) 7.6.264

▷ AddUniversalMorphismIntoDirectSum(C, F) (operation)

▷ AddUniversalMorphismIntoDirectSum(C, F, weight)

(operation)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function Fto the category for the basic operation UniversalMorphismIntoDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects,T,tau) \mapsto$ UniversalMorphismIntoDirectSum(objects, T, tau).

7.6.265 AddUniversalMorphismIntoDirectSumWithGivenDirectSum (for IsCapCategory, IsFunction)

- ▷ AddUniversalMorphismIntoDirectSumWithGivenDirectSum(C, F) (operation) ▷ AddUniversalMorphismIntoDirectSumWithGivenDirectSum(C, F, weight)
 - **Returns:** nothing

The F. arguments are category Cand function This operaadds the given function Fto the category for the basic operation UniversalMorphismIntoDirectSumWithGivenDirectSum. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(objects, T, tau, P) \mapsto$ ${\tt UniversalMorphismIntoDirectSumWithGivenDirectSum} (objects, T, tau, P).$

AddUniversalMorphismIntoEqualizer (for IsCapCategory, IsFunction) 7.6.266

- ▷ AddUniversalMorphismIntoEqualizer(C, F) (operation)
- ▷ AddUniversalMorphismIntoEqualizer(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function Fto the category for the basic operation UniversalMorphismIntoEqualizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y,morphisms,T,tau) \mapsto$ UniversalMorphismIntoEqualizer(Y, morphisms, T, tau).

7.6.267 AddUniversalMorphismIntoEqualizerWithGivenEqualizer (for IsCapCategory, IsFunction)

- ▷ AddUniversalMorphismIntoEqualizerWithGivenEqualizer(C, F) (operation)
- ▷ AddUniversalMorphismIntoEqualizerWithGivenEqualizer(C, F, weight) (operation) **Returns:** nothing

function This The arguments are a category Cand F. operation adds given function to the category the basic operation UniversalMorphismIntoEqualizerWithGivenEqualizer. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(Y, morphisms, T, tau, P) \mapsto$ ${\tt UniversalMorphismIntoEqualizerWithGivenEqualizer}(Y, morphisms, T, tau, P).$

7.6.268 AddUniversalMorphismIntoFiberProduct (for IsCapCategory, IsFunction)

▷ AddUniversalMorphismIntoFiberProduct(C, F)

(operation)

▷ AddUniversalMorphismIntoFiberProduct(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoFiberProduct. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (morphisms, T, tau) \mapsto UniversalMorphismIntoFiberProduct(morphisms, T, tau)$.

7.6.269 AddUniversalMorphismIntoFiberProductWithGivenFiberProduct (for Is-CapCategory, IsFunction)

 \triangleright AddUniversalMorphismIntoFiberProductWithGivenFiberProduct(C, F) (operation) \triangleright AddUniversalMorphismIntoFiberProductWithGivenFiberProduct(C, F, weight) (operation)

Returns: nothing

The arguments category Cand function F. This are operation adds given function Fto the category for the basic operation ${\tt UniversalMorphismIntoFiberProductWithGivenFiberProduct}.$ Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(morphisms,T,tau,P)\mapsto$ Universal Morphism Into Fiber Product With Given Fiber Product (morphisms, T, tau, P).

7.6.270 AddUniversalMorphismIntoTerminalObject (for IsCapCategory, IsFunction)

▷ AddUniversalMorphismIntoTerminalObject(C, F)

(operation)

▷ AddUniversalMorphismIntoTerminalObject(C, F, weight)

(operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoTerminalObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T) \mapsto \text{UniversalMorphismIntoTerminalObject}(T)$.

7.6.271 AddUniversalMorphismIntoTerminalObjectWithGivenTerminalObject (for IsCapCategory, IsFunction)

- ▷ AddUniversalMorphismIntoTerminalObjectWithGivenTerminalObject(C, F) (operation)
- ▷ AddUniversalMorphismIntoTerminalObjectWithGivenTerminalObject(C, F, weight)

(operation)

Returns: nothing

The arguments category CF. are a and function This operaadds the given function Fto the category for the basic operation $Universal {\tt MorphismIntoTerminalObjectWithGivenTerminalObject}.$ Optionally, weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T,P)\mapsto \mathtt{UniversalMorphismIntoTerminalObjectWithGivenTerminalObject}(T,P).$

7.6.272 AddUniversalMorphismIntoZeroObject (for IsCapCategory, IsFunction)

ightharpoonup AddUniversalMorphismIntoZeroObject(C, F) (operation) ightharpoonup AddUniversalMorphismIntoZeroObject(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T) \mapsto \text{UniversalMorphismIntoZeroObject}(T)$.

7.6.273 AddUniversalMorphismIntoZeroObjectWithGivenZeroObject (for IsCap-Category, IsFunction)

▷ AddUniversalMorphismIntoZeroObjectWithGivenZeroObject(C, F) (operation)
▷ AddUniversalMorphismIntoZeroObjectWithGivenZeroObject(C, F, weight) (operation)
Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation UniversalMorphismIntoZeroObjectWithGivenZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(T,P)\mapsto U$ niversalMorphismIntoZeroObjectWithGivenZeroObject(T,P).

7.6.274 AddVerticalPostCompose (for IsCapCategory, IsFunction)

▷ AddVerticalPostCompose(C, F) (operation)

▷ AddVerticalPostCompose(C, F, weight) (operation)

Returns: nothing

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation VerticalPostCompose. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{VerticalPostCompose}(arg2, arg3)$.

7.6.275 AddVerticalPreCompose (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation VerticalPreCompose. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: (arg2, arg3) \mapsto \text{VerticalPreCompose}(arg2, arg3)$.

7.6.276 AddZeroMorphism (for IsCapCategory, IsFunction)

```
▷ AddZeroMorphism(C, F) (operation)

▷ AddZeroMorphism(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ZeroMorphism. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(a,b) \mapsto \text{ZeroMorphism}(a,b)$.

7.6.277 AddZeroObject (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ZeroObject. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: () \mapsto \mathsf{ZeroObject}()$.

7.6.278 AddZeroObjectFunctorial (for IsCapCategory, IsFunction)

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ZeroObjectFunctorial. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F: () \mapsto \texttt{ZeroObjectFunctorial}()$.

7.6.279 AddZeroObjectFunctorialWithGivenZeroObjects (for IsCapCategory, IsFunction)

```
▷ AddZeroObjectFunctorialWithGivenZeroObjects(C, F) (operation)
▷ AddZeroObjectFunctorialWithGivenZeroObjects(C, F, weight) (operation)

Returns: nothing
```

The arguments are a category C and a function F. This operation adds the given function F to the category for the basic operation ZeroObjectFunctorialWithGivenZeroObjects. Optionally, a weight (default: 100) can be specified which should roughly correspond to the computational complexity of the function (lower weight = less complex = faster execution). $F:(P,Pp) \mapsto \text{ZeroObjectFunctorialWithGivenZeroObjects}(P,Pp)$.

Chapter 8

Managing Derived Methods

8.1 Info Class

8.1.1 DerivationInfo

▷ DerivationInfo (info class)

Info class for derivations.

8.1.2 ActivateDerivationInfo

▷ ActivateDerivationInfo(arg) (function)

8.1.3 DeactivateDerivationInfo

▷ DeactivateDerivationInfo(arg) (function)

8.2 Derivation Objects

8.2.1 IsDerivedMethod (for IsAttributeStoringRep)

▷ IsDerivedMethod(arg)

(filter)

Returns: true or false

A derivation object describes a derived method. It contains information about which operation the derived method implements, and which other operations it relies on.

8.2.2 CreateDerivation

 $\verb|> CreateDerivation(target_op_name, description, used_ops_with_multiples, func, weight, category_filter, loop_multiplier, category_getters) \\ (function)$

Creates a new derivation object. The argument target_op_name is the name of the operation which the derived method implements. The argument description should describe the derivation. The argument used_ops_with_multiples contains

- the name of each operation used by the derived method,
- together with a positive integer specifying how many times that operation is used and
- either a category getter or fail.

This is given as a list of lists, where each sublist has as first entry the name of an operation, as second entry an integer and as third entry either a function or fail. This function should accept the category for which this derivation will be installed, and return a category for which the operation in the first entry must be installed for the derivation to be considered applicable. The argument func contains the actual implementation of the derived method. The argument weight is an additional number to add when calculating the resulting weight of the target operation using this derivation. Unless there is any particular reason to regard the derivation as exceedingly expensive, this number should be 1. The argument category_filter is a filter (or function) describing which categories the derivation is valid for. If it is valid for all categories, then this argument should have the value IsCapCategory. The output of category_filter must not change during the installation of operations. In particular, it must not rely on CanCompute to check conditions.

8.2.3 Description (for IsDerivedMethod)

 \triangleright Description(d) (attribute)

A description of the derivation.

8.2.4 AdditionalWeight (for IsDerivedMethod)

▷ AdditionalWeight(d)

(attribute)

Additional weight for the derivation.

8.2.5 DerivationFunction (for IsDerivedMethod)

▷ DerivationFunction(d)

(attribute)

The implementation of the derivation.

8.2.6 CategoryFilter (for IsDerivedMethod)

▷ CategoryFilter(d)

(attribute)

Filter describing which categories the derivation is valid for.

8.2.7 IsApplicableToCategory (for IsDerivedMethod, IsCapCategory)

▷ IsApplicableToCategory(d, C)

(operation)

Returns: true if the category C is known to satisfy the category filter of the derivation d. Checks if the derivation is known to be valid for a given category.

8.2.8 TargetOperation (for IsDerivedMethod)

▷ TargetOperation(d)

(attribute)

Returns: The name (as a string) of the operation implemented by the derivation d

8.2.9 UsedOperationsWithMultiplesAndCategoryGetters (for IsDerivedMethod)

□ UsedOperationsWithMultiplesAndCategoryGetters(d)

(attribute)

Returns: The names of the operations used by the derivation d, together with their multiplicities and category getters. The result is a list consisting of lists of the form [op_name, mult, getter], where op_name is a string, mult a positive integer and getter is a function or fail.

8.2.10 InstallDerivationForCategory (for IsDerivedMethod, IsPosInt, IsCapCategory)

▷ InstallDerivationForCategory(d, weight, C)

(operation)

Install the derived method d for the category C. The integer weight is the computed weight of the operation implemented by this derivation.

8.2.11 FunctionCalledBeforeInstallation (for IsDerivedMethod)

(attribute)

Input is a derived method. Output is a unary function that takes as an input a category and does not output anything. This function is always called before the installation of the derived method for a concrete instance of a category.

8.3 Derivation Graphs

8.3.1 IsDerivedMethodGraph (for IsAttributeStoringRep)

▷ IsDerivedMethodGraph(arg)

(filter)

Returns: true or false

A derivation graph consists of a set of operations and a set of derivations specifying how some operations can be implemented in terms of other operations.

8.3.2 MakeDerivationGraph (for IsDenseList)

▷ MakeDerivationGraph(operations)

(operation)

Make a derivation graph containing the given set of operations and no derivations. The argument *operations* should be a list of strings, the names of the operations. The set of operations is fixed once the graph is created. Derivations can be added to the graph by calling AddDerivation.

8.3.3 AddOperationsToDerivationGraph (for IsDerivedMethodGraph, IsDenseList)

▷ AddOperationsToDerivationGraph(graph, operations)

(operation)

Adds a list of operation names *operations* to a given derivation graph *graph*. This is used in extensions of CAP which want to have their own basic operations, but do not want to pollute the CAP kernel any more. Please use it with caution. If a weight list/category was created before it will not be aware of the operations.

8.3.4 AddDerivation

```
> AddDerivation(graph, target_op, description, used_ops_with_multiples_and_category_getters, func, weight, category_filter, loop_multiplier, category_getters, function_called_before_installation) (function)
```

Add a derivation to a derivation graph.

8.3.5 AddDerivationToCAP

▷ AddDerivationToCAP(arg)

(function)

8.3.6 Operations (for IsDerivedMethodGraph)

 \triangleright Operations (G) (attribute)

Gives the operations in the graph G, as a list of strings.

8.3.7 DerivationsUsingOperation (for IsDerivedMethodGraph, IsString)

▷ DerivationsUsingOperation(G, op_name)

(operation)

Finds all the derivations in the graph G that use the operation named op_name , and returns them as a list.

8.3.8 DerivationsOfOperation (for IsDerivedMethodGraph, IsString)

▷ DerivationsOfOperation(G, op_name)

(operation)

Finds all the derivations in the graph G targeting the operation named op_name (that is, the derivations that provide implementations of this operation), and returns them as a list.

8.4 Managing Derivations in a Category

8.4.1 IsOperationWeightList (for IsAttributeStoringRep)

 \triangleright IsOperationWeightList(arg)

(filter)

Returns: true or false

An operation weight list manages the use of derivations in a single category C. For every operation, it keeps a weight value which indicates how costly it is to perform that operation in the category C. Whenever a new operation is implemented in C, the operation weight list should be notified about this and given a weight to assign to this operation. It will then automatically install all possible derived

methods for C in such a way that every operation has the smallest possible weight (the weight of a derived method is computed by using the weights of the operations it uses).

8.4.2 MakeOperationWeightList (for IsCapCategory, IsDerivedMethodGraph)

▷ MakeOperationWeightList(C, G)

(operation)

Create the operation weight list for a category. This should only be done once for every category, and the category should afterwards remember the returned object. The argument C is the CAP category this operation weight list is associated to, and the argument C is a derivation graph containing operation names and derivations.

8.4.3 DerivationGraph (for IsOperationWeightList)

▷ DerivationGraph(owl)

(attribute)

Returns the derivation graph used by the operation weight list ow1.

8.4.4 CategoryOfOperationWeightList (for IsOperationWeightList)

▷ CategoryOfOperationWeightList(ow1)

(attribute)

Returns the CAP category associated to the operation weight list owl.

8.4.5 CurrentOperationWeight (for IsOperationWeightList, IsString)

▷ CurrentOperationWeight(owl, op_name)

(operation)

Returns the current weight of the operation named op_name.

8.4.6 OperationWeightUsingDerivation (for IsOperationWeightList, IsDerived-Method)

▷ OperationWeightUsingDerivation(owl, d)

(operation)

Finds out what the weight of the operation implemented by the derivation *d* would be if we had used that derivation.

8.4.7 DerivationOfOperation (for IsOperationWeightList, IsString)

▷ DerivationOfOperation(owl, op_name)

(operation)

Returns the derivation which is currently used to implement the operation named op_name. If the operation is not implemented by a derivation (that is, either implemented directly or not implemented at all), then fail is returned.

8.4.8 TriggerDerivationsUsingOperation (for IsOperationWeightList, IsString)

▷ TriggerDerivationsUsingOperation(owl, op_name)

(operation)

Performs a search from the operation op_name , and triggers all derivations that give improvements over the current state. This is used internally by InstallDerivations and Reevaluate. It should normally not be necessary to call this function directly.

8.4.9 Reevaluate (for IsOperationWeightList)

▷ Reevaluate(owl) (operation)

Reevaluate the installed derivations, installing better derivations if possible. This should be called if new derivations become available for the category, either because the category has acquired more knowledge about itself (e.g. it is told that it is abelian) or because new derivations have been added to the graph.

8.4.10 Saturate (for IsOperationWeightList)

▷ Saturate(owl) (operation)

Saturates the derivation graph, i.e., calls reevaluate until no more changes in the derivation graph occur.

8.4.11 AddPrimitiveOperation (for IsOperationWeightList, IsString, IsInt)

▷ AddPrimitiveOperation(owl, op_name, weight)

(operation)

Add the operation named op_name to the operation weight list owl with weight weight.

8.4.12 PrintDerivationTree (for IsOperationWeightList, IsString)

▷ PrintDerivationTree(owl, op_name)

(operation)

Print a tree representation of the way the operation named op_name is implemented in the category of the operation weight list ow1.

8.4.13 PrintTree (for IsObject, IsFunction, IsFunction)

▷ PrintTree(arg1, arg2, arg3)

(operation)

Prints a tree structure.

8.4.14 PrintTreeRec (for IsObject, IsFunction, IsFunction, IsInt)

▷ PrintTreeRec(arg1, arg2, arg3, arg4)

(operation)

Chapter 9

Technical Details

9.1 The Category Cat

9.1.1 ObjectCache (for IsCapFunctor)

▷ ObjectCache(functor)

(attribute)

Returns: IsCachingObject

Returns the caching object which stores the results of the functor functor applied to objects.

9.1.2 MorphismCache (for IsCapFunctor)

▷ MorphismCache(functor)

(attribute)

Returns: IsCachingObject

Returns the caching object which stores the results of the functor functor applied to morphisms.

9.2 Tools

9.2.1 FunctionWithNamedArguments

▷ FunctionWithNamedArguments(specification, func)

(function)

Returns: a function

Simulates named arguments in GAP as follows:

- specification is a list of pairs with first entry the name of the argument and second entry a default value (which must be immutable).
- func must be a function with first argument CAP_NAMED_ARGUMENTS.
- The return value is a function with one argument fewer than func.

When calling the returned function, the arguments are passed on to func. To simulate named arguments, any GAP options appearing in specification are consumed and put into the record CAP_NAMED_ARGUMENTS.

9.2.2 CAP_INTERNAL_GET_DATA_TYPE_FROM_STRING

▷ CAP_INTERNAL_GET_DATA_TYPE_FROM_STRING(filter_string[, category]) (function)

Returns: a record

The function takes one of the strings listed under filter_list in 7.3 as input and returns the corresponding data type (see CapJitInferredDataTypes (CompilerForCAP: CapJitInferredDataTypes) for details). If no category is given, data types with generic filters (IsCapCategoryObject, IsCapCategoryMorphism etc.) are returned. However, those cannot be used in the context of CompilerForCAP because the component category cannot be set in this case.

9.2.3 CAP_INTERNAL_GET_DATA_TYPES_FROM_STRINGS

▷ CAP_INTERNAL_GET_DATA_TYPES_FROM_STRINGS(list_of_strings[, category]) (function)
Returns: a list

Applies CAP_INTERNAL_GET_DATA_TYPE_FROM_STRING (9.2.2) to all elements of *list* and returns the result.

9.2.4 CAP_INTERNAL_REPLACED_STRING_WITH_FILTER

▷ CAP_INTERNAL_REPLACED_STRING_WITH_FILTER(filter_string[, category]) (function)

Returns: a filter

The function takes one of the strings listed under filter_list in 7.3 as input. The corresponding filter of the category category is returned. If no category is given, generic filters (IsCapCategoryObject, IsCapCategoryMorphism etc.) are used.

9.2.5 CAP_INTERNAL_REPLACED_STRINGS_WITH_FILTERS

▶ CAP_INTERNAL_REPLACED_STRINGS_WITH_FILTERS(list[, category]) (function)
Returns: Replaced list

Applies CAP_INTERNAL_REPLACED_STRING_WITH_FILTER (9.2.4) to all elements of list and returns the result.

9.2.6 CAP_INTERNAL_RETURN_OPTION_OR_DEFAULT

CAP_INTERNAL_RETURN_OPTION_OR_DEFAULT(string, value) (function)
Returns: option value

Returns the value of the option with name string, or, if this value is fail, the object value.

9.2.7 CAP_INTERNAL_FIND_APPEARANCE_OF_SYMBOL_IN_FUNCTION

▷ CAP_INTERNAL_FIND_APPEARANCE_OF_SYMBOL_IN_FUNCTION(function, symbol_list,
loop_multiple, replacement_record) (function)

Returns: a list of symbols with multiples

The function searches for the appearance of the strings in symbol list on the function function and returns a list of pairs, containing the name of the symbol and the number of appearance. If the symbol appears in a loop, the number of appearance is counted times the loop multiple. Moreover, if appearances of found strings should be replaced by collections of other strings, then these can be specified in the replacement record.

9.2.8 CAP_INTERNAL_MERGE_PRECONDITIONS_LIST

▷ CAP_INTERNAL_MERGE_PRECONDITIONS_LIST(list1, list2)

(function)

Returns: merge list

The function takes two lists containing pairs of symbols (strings) and multiples. The lists are merged that pairs where the string only appears in one list is then added to the return list, if a pair with a string appears in both lists, the resulting lists only contains this pair once, with the higher multiple from both lists.

9.2.9 CAP_INTERNAL_ASSERT_VALUE_IS_OF_TYPE_GETTER

▷ CAP_INTERNAL_ASSERT_VALUE_IS_OF_TYPE_GETTER(data_type,
human_readable_identifier_getter)

(function)

Returns: a function

Returns a function f which throws an error if its first argument is not of type data_type. human_readable_identifier_getter is a function returning a string which is used to refer to the first argument of f in the error message. The arguments of f except the first argument are passed on to human_readable_identifier_getter.

9.2.10 CAP_INTERNAL_ASSERT_IS_CELL_OF_CATEGORY

▷ CAP_INTERNAL_ASSERT_IS_CELL_OF_CATEGORY(cell, category, human_readable_identifier_getter)

(function)

The function throws an error if cell is not a cell of category. If category is the boolean false, only general checks not specific to a concrete category are performed. human_readable_identifier_getter is a 0-ary function returning a string which is used to refer to cell in the error message.

9.2.11 CAP_INTERNAL_ASSERT_IS_OBJECT_OF_CATEGORY

▷ CAP_INTERNAL_ASSERT_IS_OBJECT_OF_CATEGORY(object, category, human_readable_identifier_getter)

(function)

The function throws an error if object is not an object of category. If category is the boolean false, only general checks not specific to a concrete category are performed. human_readable_identifier_getter is a 0-ary function returning a string which is used to refer to cell in the error message.

9.2.12 CAP_INTERNAL_ASSERT_IS_MORPHISM_OF_CATEGORY

▷ CAP_INTERNAL_ASSERT_IS_MORPHISM_OF_CATEGORY(morphism, category, human_readable_identifier_getter)

(function)

The function throws an error if morphism is not a morphism of category. If category is the boolean false, only general checks not specific to a concrete category are performed. human_readable_identifier_getter is a 0-ary function returning a string which is used to refer to cell in the error message.

9.2.13 CAP_INTERNAL_ASSERT_IS_TWO_CELL_OF_CATEGORY

▷ CAP_INTERNAL_ASSERT_IS_TWO_CELL_OF_CATEGORY(two_cell, category,
human_readable_identifier_getter) (function)

The function throws an error if two_cell is not a 2-cell of category. If category is the boolean false, only general checks not specific to a concrete category are performed. human_readable_identifier_getter is a 0-ary function returning a string which is used to refer to cell in the error message.

9.2.14 CachingStatistic

▷ CachingStatistic(category[, operation]) (function)

Prints statistics for all caches in category. If operation is given (as a string), only statistics for the given operation cache is stored.

9.2.15 BrowseCachingStatistic

▷ BrowseCachingStatistic(category)

(function)

Displays statistics for all caches in *category*. in a Browse window. Here "status" indicates if the cache is weak, strong, or inactive, "hits" is the number of successful cache accesses, "misses" the number of unsuccessful cache accesses, and "stored" the number of objects currently stored in the cache.

9.2.16 InstallDeprecatedAlias

▷ InstallDeprecatedAlias(alias_name, function_name, deprecation_date) (function)

Makes the function given by function_name available under the alias alias_name with a deprecation warning including the date deprecation_date.

9.2.17 IsSpecializationOfFilter

▷ IsSpecializationOfFilter(filter1, filter2)

(function)

Checks if filter2 is more special than filter1, i.e. if filter2 implies filter1. filter1 and/or filter2 can also be one of the strings listed under filter_list in 7.3 and in this case are replaced by the corresponding filters (e.g. IsCapCategory, IsCapCategoryObject, IsCapCategoryMorphism, ...).

9.2.18 IsSpecializationOfFilterList

 \triangleright IsSpecializationOfFilterList(filter_list1, filter_list2) (function)

Checks if filter_list2 is more special than filter_list1, i.e. if both lists have the same length and any element of filter_list2 is more special than the corresponding element

of filter_list1 in the sense of IsSpecializationOfFilter (9.2.17). filter_list1 and filter_list2 can also be the string "any", respresenting a most general filter list of any length.

9.2.19 InstallMethodForCompilerForCAP

```
▷ InstallMethodForCompilerForCAP(same, as, for, InstallMethod) (function)
```

Installs a method via InstallMethod and adds it to the list of methods known to the compiler. See CapJitAddKnownMethod (9.2.21) for requirements.

9.2.20 InstallOtherMethodForCompilerForCAP

```
\triangleright InstallOtherMethodForCompilerForCAP(same, as, for, InstallOtherMethod) (function)
```

Installs a method via InstallOtherMethod and adds it to the list of methods known to the compiler. See CapJitAddKnownMethod (9.2.21) for requirements.

9.2.21 CapJitAddKnownMethod

```
▷ CapJitAddKnownMethod(operation, filters, method) (function)
```

Adds a method to the list of methods known to the compiler. If the first filter implies IsCapCategory, method selection only takes the number of arguments and the first filter into account. This allows to resolve operations even in the case that the syntax tree cannot fully be typed. If the first filter does not imply IsCapCategory, method selection takes all filters into account. To strictly distinguish between the two cases, IsCapCategory must not imply the first filter (except if the first filter is equal to IsCapCategory). Method selection is strict in the sense that two different methods for the same operation must not be comparable. That is, they must have a different number of filters or the filters at at least one position must not be related via implication. In particular, adding two methods with a CAP category as first argument (or a convenience method for a CAP operation) with the same number of arguments and one category filter implying the other is not supported.

9.2.22 CapJitAddTypeSignature

```
▷ CapJitAddTypeSignature(name, input_filters, output_data_type) (function)
```

(experimental) Adds a type signature for the global function or operation given by name to the compiler. <code>input_filters</code> must be a list of filters, or the string '"any"' representing a most general filter list of any length. <code>output_data_type</code> must be a filter, a data type, or a function. If it is a function with one argument, it must accept a list of input types and return the corresponding data type of the output. If it is a function with two arguments, it must accept the arguments of a function call of <code>name</code> (as syntax trees) and the function stack and return a record with components <code>args</code> (the possibly modified arguments) and <code>output_type</code> (the data type of the output). See <code>CapJitInferredDataTypes</code> (CompilerForCAP: CapJitInferredDataTypes) for more details on data types.

9.2.23 CapJitDataTypeOfListOf

```
▷ CapJitDataTypeOfListOf(element_type)
```

(function)

(function)

(experimental) Returns the data type of a list whose elements are of type element_type. element_type must be a filter or a data type.

9.2.24 CapJitDataTypeOfNTupleOf

```
▷ CapJitDataTypeOfNTupleOf(n, element_types...)
```

(experimental) Returns the data type of an n-tuple whose entries are of types corresponding to element_types. element_types... must be filters or data types.

9.2.25 CapJitDataTypeOfRing

(experimental) Returns the data type of the ring (or elements of the ring) ring.

9.2.26 CapJitDataTypeOfCategory

```
▷ CapJitDataTypeOfCategory(category)

▷ CapJitDataTypeOfObjectOfCategory(category)

▷ CapJitDataTypeOfMorphismOfCategory(category)

▷ CapJitDataTypeOfTwoCellOfCategory(category)

○ CapJitDataTypeOfTwoCellOfCategory(category)

(function)
```

(experimental) Returns the data type of the category (or objects, morphisms, or two cells in the category) category.

9.2.27 CapJitTypedExpression

```
▷ CapJitTypedExpression(value, data_type_getter) (function)
```

(experimental) Simply returns value, but allows to specify the data type of value for CompilerForCAP. data_type_getter must be a literal function or a global variable pointing to a function. The function must accept no arguments or a single argument, and return a valid data type. If the function accepts a single argument, it must be inside a CAP operation or method known to CompilerForCAP (for example, see InstallMethodForCompilerForCAP (9.2.19)), and the current category (i.e. the first argument of the CAP operation or method known to CompilerForCAP) will be passed to the function. IMPORTANT: If data_type_getter is a literal function, it must not contain references to variables in its context. Otherwise the code might access random memory locations. See CapJitInferredDataTypes (CompilerForCAP: CapJitInferredDataTypes) for more details on data types.

9.2.28 CapFixpoint

```
▷ CapFixpoint(predicate, func, initial_value)
```

(function)

Computes a fixpoint of func with regard to equality given by predicate, starting with initial_value. If no such fixpoint exists, the execution does not terminate.

9.2.29 Iterated (for IsList, IsFunction, IsObject)

```
▷ Iterated(list, func, initial_value)
```

(operation)

Shorthand for Iterated (Concatenation ([initial_value], list), func).

9.2.30 Iterated (for IsList, IsFunction, IsObject, IsObject)

```
▷ Iterated(list, func, initial_value, terminal_value)
```

(operation)

Shorthand for Iterated(Concatenation([initial_value], list, [terminal_value]), func).

9.2.31 TransitivelyNeededOtherPackages

```
    □ TransitivelyNeededOtherPackages(package_name)
```

(function)

Returns a list of package names which are transitively needed other packages of the package package_name.

9.2.32 PackageOfCAPOperation

```
▷ PackageOfCAPOperation(operation_name)
```

(function)

Returns the name of the package to which the CAP operation given by operation_name belongs or fail if the package is not known.

9.2.33 SafePosition (for IsList, IsObject)

```
▷ SafePosition(list, obj)
```

(operation)

Returns: an integer

Returns Position (list, obj) while asserting that this value is not fail.

9.2.34 SafeUniquePosition (for IsList, IsObject)

```
ightharpoonup SafeUniquePosition(list, obj)
```

(operation)

Returns: an integer

Returns Position (list, obj) while asserting that this value is not fail and the position is unique.

9.2.35 SafePositionProperty (for IsList, IsFunction)

▷ SafePositionProperty(list, func)

(operation)

Returns: an integer

Returns PositionProperty (list, func) while asserting that this value is not fail.

9.2.36 SafeUniquePositionProperty (for IsList, IsFunction)

▷ SafeUniquePositionProperty(list, func)

(operation)

Returns: an integer

Returns a position in *list* for which *func* returns true when applied to the corresponding entry while asserting that there exists exactly one such position.

9.2.37 SafeFirst (for IsList, IsFunction)

▷ SafeFirst(list, func)

(operation)

Returns: an element of the list

Returns First (list, func) while asserting that this value is not fail.

9.2.38 SafeUniqueEntry (for IsList, IsFunction)

▷ SafeUniqueEntry(list, func)

(operation)

Returns: an element of the list

Returns a value in list for which func returns true while asserting that there exists exactly one such entry.

9.2.39 NTuple

▷ NTuple(n, args...)

(function)

Returns: a list

Returns args while asserting that its length is n.

9.2.40 Pair

▷ Pair(first, second)

(function)

Returns: a list

Alias for NTuple (2, first, second).

9.2.41 Triple

▷ Triple(first, second, third)

(function)

Returns: a list

Alias for NTuple (3, first, second, third).

9.2.42 TransposedMatWithGivenDimensions

The arguments are two integers nr_rows , nr_cols and a list of lists listlist such that $nr_rows = Length(listlist)$ and $nr_cols = Length(listlist[i])$ for i = 1 to nr_rows . The output is the transpose of listlist as a list consisting of nr_cols rows and nr_rows columns.

9.2.43 HandlePrecompiledTowers

▶ HandlePrecompiledTowers(category, underlying_category, constructor_name) (function)

Handles the information stored in underlying_category!.compiler_hints.precompiled_towers (if bound) which is a list of records with components:

- remaining_constructors_in_tower: a non-empty list of strings (names of category constructors)
- precompiled_functions_adder: a function accepting a CAP category as input

If constructor_name is the only entry of remaining_constructors_in_tower, precompiled_functions_adder is applied to category (except if the option no_precompiled_code is set to true) and should add precompiled code. Else, if constructor_name is the first entry of remaining_constructors_in_tower, the information is attached to category!.compiler_hints.precompiled_towers after removing constructor_name from remaining_constructors_in_tower. Note: Currently, there is no logic for finding the "optimal" code to install if constructor_name is the only entry of remaining_constructors_in_tower of multiple entries.

9.2.44 CAP_JIT_INCOMPLETE_LOGIC

▷ CAP_JIT_INCOMPLETE_LOGIC(value)

(function)

Simply returns value. Used to signify that the argument is not fully run through all logic functions/templates by CompilerForCAP.

9.2.45 CAP_JIT_EXPR_CASE_WRAPPER

▷ CAP_JIT_EXPR_CASE_WRAPPER(func)

(function)

Simply returns func, which must be a literal function without arguments only containing an if-elif-else statement with each branch consisting of a single return statement. Used to write expressions of the form function() if-elif-else end() as CAP_JIT_EXPR_CASE_WRAPPER(function() if-elif-else end)() because the former is not valid in Julia.

9.2.46 ListWithKeys

▷ ListWithKeys(list, func)

(function)

Returns: a list

Same as List (list, func) but func gets both the key i and list [i] as arguments.

9.2.47 SumWithKeys

▷ SumWithKeys(list, func)

(function)

Returns: a list

Same as Sum(list, func) but func gets both the key i and list [i] as arguments.

9.2.48 ProductWithKeys

▷ ProductWithKeys(list, func)

(function)

Returns: a list

Same as Product (list, func) but func gets both the key i and list [i] as arguments.

9.2.49 ForAllWithKeys

▷ ForAllWithKeys(list, func)

(function)

Returns: a list

Same as ForAll(list, func) but func gets both the key i and list[i] as arguments.

9.2.50 For Any With Keys

▷ ForAnyWithKeys(list, func)

(function)

Returns: a list

Same as ForAny(list, func) but func gets both the key i and list[i] as arguments.

9.2.51 NumberWithKeys

▷ NumberWithKeys(list, func)

(function)

Returns: a list

Same as Number (list, func) but func gets both the key i and list [i] as arguments.

9.2.52 FilteredWithKeys

▷ FilteredWithKeys(list, func)

(function)

Returns: a list

Same as Filtered(list, func) but func gets both the key i and list[i] as arguments.

9.2.53 FirstWithKeys

▷ FirstWithKeys(list, func)

(function)

Returns: a list

Same as First (list, func) but func gets both the key i and list [i] as arguments.

9.2.54 LastWithKeys

9.2.55 CreateGapObjectWithAttributes

```
▷ CreateGapObjectWithAttributes(type[, attribute1, value1, ...]) (function)
Shorthand for ObjectifyWithAttributes( rec( ), type, [attribute1, value1, ...]).
```

Chapter 10

Limits and Colimits

This section describes the support for limits and colimits in CAP. All notions defined in the following are considered with regard to limits, not colimits, except if explicitly stated otherwise. In particular, the diagram specification specifies a diagram over which the limit is taken. The colimit in turn is taken over the opposite diagram.

10.1 Specification of Limits and Colimits

A record specifying a limit in CAP has the following entries:

- object_specification: see below
- morphism_specifiation: see below
- limit_object_name: the name of the method returning the limit object, e.g. DirectProduct or KernelObject
- limit_projection_name (optional): the name of the method returning the projection(s) from the limit object, e.g. ProjectionInFactorOfDirectProduct or KernelEmbedding. Defaults to Concatenation("ProjectionInFactorOf", limit_object_name).
- limit_universal_morphism_name (optional): the name of the method returning the universal morphism into the limit object, e.g. UniversalMorphismIntoDirectProduct or KernelLift. Defaults to Concatenation("UniversalMorphismInto", limit_object_name).
- colimit_object_name: the name of the method returning the colimit object, e.g. Coproduct or CokernelObject
- colimit_injection_name (optional): the name of the method returning the injection(s) into the colimit object, e.g. InjectionOfCofactorOfCoproduct or CokernelProjection. Defaults to Concatenation("InjectionOfCofactorOf", colimit_object_name).
- colimit_universal_morphism_name (optional): the name of the method returning the universal morphism from the colimit object, e.g. UniversalMorphismFromCoproduct or CokernelColift. Defaults to Concatenation("UniversalMorphismFrom", colimit_object_name).

limit_object_name and colimit_object_name can be the same, e.g. for DirectSum or ZeroObject. The object_specification and morphism_specification together specify the shape of the diagram defining the limit or colimit. The syntax is the following:

- object_specification is a list of strings. Only the strings "fixedobject" and "varobject" are allowed as entries of the list. These are called "types" in the following.
- morphism_specification is a list of triples. The first and third entry of a triple are integers greater or equal to 1 and less or equal to Length(object_specification). The second entry is one of the following strings: "fixedmorphism", "varmorphism", "zeromorphism". This entry is called "type" in the following.

Semantics is given as follows:

- The type "fixedobject" specifies a single object. The type "varobject" specifies arbitrarily many objects.
- The first and the third entry of a triple specify the source and range of a morphism (or multiple morphisms) encoded by the position in object_specification respectively. The type "fixedmorphism" specifies a single morphism. In this case, source and range can only be of type "fixedobject", not of type "varobject". The type "varmorphism" specifies arbitrarily many morphisms. In this case, if the source (resp. range) is of type "fixedobject" all the morphisms must have the same source (resp. range). On the contrary, if the source (resp. range) is of the type "varobject", the objects correspond one-to-one to the sources (resp. ranges) of the morphisms. The type "zeromorphism" is currently ignored but will be endowed with semantics in the future.

For example, a FiberProduct diagram consists of arbitrarily many morphisms which have arbitrary sources but the same common range. This can be expressed as follows:

```
rec(
   object_specification := [ "fixedobject", "varobject" ],
   morphism_specification := [ [ 2, "varmorphism", 1 ] ],
   limit_object_name := "FiberProduct",
   colimit_object_name := "Pushout",
)
```

Note that not all diagrams which can be expressed with the above are actually supported. For now, at most one unbound object (see below for the definition of "unbound") may be of type "varobject", and if there is such an unbound object it must be the last one among the unbound objects. Similarly, at most one unbound morphism may be of type "varmorphism", and if there is such an unbound morphism it must be the last one among the unbound morphisms.

10.2 Enhancing Limit Specifications

The function CAP_INTERNAL_ENHANCE_NAME_RECORD_LIMITS takes a list of limits (given by records as explained above), and computes some additional properties. For example, the number of so-called unbound objects, unbound morphisms and (non-)targets is computed. The term "unbound" signifies that for creating a concrete diagram, these objects or morphisms have to be specified by the user because they cannot be derived by CAP:

- Unbound morphisms are the triples which are of type "fixedmorphism" or "varmorphism".
- Unbound objects are the objects which are not source or range of an unbound morphism.

Finally, targets are the objects which are not the range of a morphism. These are of interest for the following reason: for limits, only projections into targets are relevant because the projections into other objects can simply be computed by composition. Similarly, one only has to give morphisms into these targets to compute a universal morphism.

The number of unbound objects, unbound morphisms and (non-)targets is expressed by the integers 0, 1 and 2:

- 0: no such object/morphism/target exists
- 1: there exists exactly one such object/target of type "fixedobject" respectively exactly one such morphism of type "fixedmorphism"
- 2: else

10.3 Functions

10.3.1 CAP_INTERNAL_GENERATE_CONVENIENCE_METHODS_FOR_LIMITS

```
▷ CAP_INTERNAL_GENERATE_CONVENIENCE_METHODS_FOR_LIMITS(package_name,
method_name_record, limits) (function)
```

This function takes a package name, a method name record and a list of enhanced limits, and generates convenience methods for the limits as a string of GAP code. The result is compared to the content of the file package_name/gap/LimitConvenienceOutput.gi. If a difference is found, a warning is raised and the generated string is written to a temporary file for manual inspection.

10.3.2 CAP INTERNAL VALIDATE LIMITS IN NAME RECORD

▷ CAP_INTERNAL_VALIDATE_LIMITS_IN_NAME_RECORD(method_name_record, limits) (function)

This function takes a method name record and a list of enhanced limits, and validates the entries of the method name record. Prefunctions, full prefunctions and postfunctions are excluded from the validation.

Chapter 11

The Category Constructor

11.1 Info class

11.1.1 InfoCategoryConstructor

▷ InfoCategoryConstructor

(info class)

Info class controlling the debugging output of CategoryConstructor (11.2.1).

11.2 Constructors

11.2.1 CategoryConstructor (for IsRecord)

▷ CategoryConstructor(options)

(operation)

Returns: a CAP category

Creates a CAP category subject to the options given via options, which is a record with the following keys:

- name (optional): name of the category
- category_filter, category_object_filter, category_morphism_filter (mandatory): passed to CreateCapCategoryWithDataTypes (1.3.4)
- object_datum_type, morphism_datum_type (optional): passed to CreateCapCategoryWithDataTypes (1.3.4)
- commutative_ring_of_linear_category (optional): ring attached as CommutativeRingOfLinearCategory (1.4.9) to the category
- range_category_of_homomorphism_structure (optional): category attached as RangeCategoryOfHomomorphismStructure (1.4.10) to the category (or the string "self" to attach the category to itself)
- properties (optional): list of categorical properties the category will have, see CAP_INTERNAL_CATEGORICAL_PROPERTIES_LIST
- object_constructor (optional): function added as an installation of ObjectConstructor (2.7.1) to the category

- object_datum (optional): function added as an installation of ObjectDatum (2.7.3) to the category
- morphism_constructor (optional): function added as an installation of MorphismConstructor (3.3.1) to the category
- morphism_datum (optional): function added as an installation of MorphismDatum (3.3.2) to the category
- list_of_operations_to_install (mandatory): a list of names of CAP operations which should be installed for the category
- is_computable (optional): whether the category can decide IsCongruentForMorphisms
- supports_empty_limits (optional): whether the category supports empty lists in inputs to operations of limits and colimits
- underlying_category_getter_string (optional): see below
- underlying_category (optional): see below
- underlying_object_getter_string (optional): see below
- underlying_morphism_getter_string (optional): see below
- top_object_getter_string (optional): see below
- top_morphism_getter_string (optional): see below
- generic_output_source_getter_string (optional): see below
- generic_output_range_getter_string (optional): see below
- create_func_bool: see below
- create_func_object: see below
- create_func_morphism: see below
- create_func_list_of_objects: see below

The values of the keys create_func_* should be either the string "default" or functions which accept the category and the name of a CAP operation of the corresponding return_type. Values for return types occuring for operations in list_of_operations_to_install are mandatory. The functions must return either strings or pairs of a string and an integer: The strings (after some replacements described below) will be evaluated and added as installations of the corresponding operations to the category with weights given by the integer (if provided). The value "default" chooses a suitable default string (see the implementation for details) and gets the weights from underlying_category. The following placeholders may be used in the strings and are replaced automatically:

- operation_name will be replaced by the name of the operation
- input_arguments... will be replaced by the input_arguments_names specified in the method name record (see 7.3)

- underlying_arguments...: If the constructed category is created from another category, underlying_category_getter_string, underlying_object_getter_string, and underlying_morphism_getter_string may be strings of functions computing the underlying category (when applied to the constructed category) and the underlying object resp. morphism (when applied to the constructed category and an object resp. morphism in the constructed category). These functions are applied to input_arguments and underlying_arguments is replaced by the result.
- number_of_arguments will be replaced by the number of input/underlying arguments
- top_source and top_range: If the return type is morphism, source and range are computed if possible and top_source and top_range are replaced by the results. For computing source and range, the output_source_getter_string and output_range_getter_string from the method name record are used if available (see 7.3). In some categories, source and range can always be obtained in a generic way (e.g. from the morphism datum). In this case, generic_output_source_getter_string and generic_output_range_getter_string can be set and are used if the required information is not available in the method name record.
- top_object_getter and top_morphism_getter are used in the "default" strings and are replaced by top_object_getter_string and top_morphism_getter_string, respectively.

Chapter 12

Reinterpretations of categories

12.1 Introduction

The support for building towers of category constructors is one of the main design features of CAP. Many categories that appear in the various applications can be modeled by towers of multiple category constructors. The category constructor ReinterpretationOfCategory (12.6.1) allows adding one last layer on top which allows expressing the desired (re)interpretation of such a modeling tower. In particular, this category constructor allows specifying the name of the category together with customized methods for the operations

- ObjectConstructor
- MorphismConstructor
- · ObjectDatum
- MorphismDatum

in order to reflect the desired (re)interpretation with a user-interface that is independent of the modeling tower (see below for details). Note that the same tower might have multiple interpretations.

Table: A tower of categories modeling the category R

The reinterpretation R is isomorphic to the top category cat_n in the tower. In practice, the word "tower" stands more generally for a finite poset with a greatest element.

12.2 Tutorial

We will show how one can reinterpret a category with the following guiding example: We reinterpret Opposite(CategoryOfRows(R)) as CategoryOfColumns(R) using ReinterpretationOfCategory (12.6.1) with the options described in the following (see CategoryOfColumns_as_Opposite_CategoryOfRows.gi in FreydCategoriesForCAP for a full implementation).

- Set the options category_filter, category_object_filter, and category_morphism_filter to the filters corresponding to the data structure of the desired reinterpretation, e.g. IsCategoryOfColumns, IsCategoryOfColumsObject, and IsCategoryOfColumsMorphism.
- 2. Set object_constructor, object_datum, morphism_constructor, and morphism_datum to the functions one would write for ObjectConstructor and so on for a primitive implementation of the desired reinterpretation. In our example, object_constructor takes the reinterpretation R (which lies in IsCategoryOfColumns due to the filter set in the first step) and an integer, and returns a CAP object in the category with attribute RankOfObject set to the integer, just like a primitive implementation of CategoryOfColumns would do.
- 3. Set modeling_tower_object_constructor, modeling_tower_object_datum, modeling_tower_morphism_constructor, modeling_tower_morphism_datum: and modeling_tower_object_constructor gets the same input as object_constructor but must return the corresponding object in the tower cat_n. modeling_tower_object_datum has the same output as object_datum but gets the reinterpretation R and an object in the tower cat_n as an input. In our example, modeling_tower_object_constructor gets the reinterpretation R and an integer as in step 2 and wraps the integer as a CategoryOfRowsObject and the result as an object in the opposite category. modeling_tower_object_datum gets the reinterpretation R and an object in Opposite (CategoryOfRows (R)) (that is, an integer boxed as a category of rows object boxed as an object in the opposite category) and returns the underlying integer. modeling tower morphism constructor and modeling_tower_morphism_datum are given analogously.

By composing modeling_tower_object_datum with object_constructor and modeling_tower_morphism_datum with morphism_constructor (with suitable source and range), ReinterpretationOfCategory defines a functor "Reinterpretation" from cat_n to R. Similarly, it defines a functor "Model" from R to cat_n by composing object_datum with modeling_tower_object_constructor and morphism_datum with modeling_tower_morphism_constructor (with suitable source and range). "Reinterpretation" should be an isomorphism of categories with inverse "Model". More precisely, one has to take care of the following things:

- Since R should just be a reinterpretation of cat_n with a nicer data structure, we certainly want "Reinterpretation" to be an equivalence of categories with pseudo-inverse "Model".
- ReinterpretationOfCategory copies all properties from cat_n to R, including properties like IsSkeletalCategory which are not necessarily preserved by mere equivalences.
- To fulfill the specification of WithGiven operations, reinterpreting a WithGiven object A in cat_n as an object in R and taking its model again must give an object equal to A. So we require applying "Reinterpretation" and then "Model" to give the identity. Conversely, let B_1 be an object in R. We take its model and reinterpret this again to form an object B_2. By construction of R, B_1 and B_2 are equal if and only if their models are equal. But since applying "Reinterpretation" and then "Model" gives the identity, taking the model of B_2 simply gives an object equal to the model of B_1. Thus, also B_1 and B_2 are equal. Hence, "Reinterpretation" has to be an equivalence which is a bijection on objects, and hence an isomorphism (although "Model" is not necessarily its inverse). Note: Alternatively, one can make sure that

WithGiven operations in cat_n are only called via the corresponding non-WithGiven operation in cat_n. This can be achieved by reinterpreting all operations of cat_n (i.e. creating R with only_primitive_operations := false), disabling redirect functions (i.e. creating R with the option overhead := false) and not calling WithGiven operations of R manually.

12.3 Implementation details

Operations in ReinterpretationOfCategory are implemented as follows:

- 1. Apply object_datum and morphism_datum to the input to get the underlying data.
- 2. Apply modeling_tower_object_constructor and modeling_tower_morphism_constructor to the underlying data to get objects and morphisms in the tower cat_n.
- 3. Apply the operation of the tower cat_n.
- 4. Apply modeling_tower_object_datum or modeling_tower_morphism_datum to the result to get the underlying data.
- 5. Apply object_constructor or morphism_constructor to the underlying data to get an object or a morphism in the reinterpretation R.

The first two steps define the functor "Model" and the last two steps define the functor "Reinterpretation". "Reinterpretation" on objects and morphisms is called ReinterpretationOfObject and ReinterpretationOfMorphism in the code. "Model" on objects and morphisms is called ModelingObject and ModelingMorphism in the code.

12.4 Relation to CompilerForCAP

The operation of the tower cat_n (step 3 above) usually unboxes objects and morphisms, operates on the underlying data, and boxes the result. The unboxing usually cancels with step 2 above, and boxing the result usually cancels with step 4 above. If one now compiles the operations of the reinterpretation R, only the following steps remain:

- 1. Apply object_datum and morphism_datum to the input to get the underlying data.
- 2. Operate on the underlying data. (previously part of step 3)
- 3. Apply object_constructor or morphism_constructor to the underlying data to get an object or a morphism in the reinterpretation R. (previously step 5)

This is exactly what a primitive implementation would look like. Thus, in many cases compiling a reinterpretation immediately gives a primitive implementation with no remaining references to the tower cat_n.

12.5 Attributes

12.5.1 ModelingCategory (for IsCapCategory)

▷ ModelingCategory(R)

(attribute)

Returns: a category

The tower cat_n modeling the reinterpretation R.

12.6 Constructors

12.6.1 ReinterpretationOfCategory (for IsCapCategory, IsRecord)

▷ ReinterpretationOfCategory(category, options)

(operation)

Returns: a category

Reinterprets a category category (the "modeling category") to form a new category R (the "reinterpretation") subject to the options given via options, which is a record with the following keys:

- name: the name of the reinterpretation R,
- category_filter, category_object_filter, category_morphism_filter, object_datum_type, morphism_datum_type, object_constructor, object_datum, morphism_constructor, morphism_datum: same meaning as for CategoryConstructor (11.2.1), which is used to create the reinterpretation R,
- modeling_tower_object_constructor: a function which gets the reinterpretation R and an object datum (in the sense of object_datum) and returns the corresponding modeling object in the modeling category,
- modeling_tower_object_datum: a function which gets the reinterpretation R and an object in the modeling category and returns the corresponding object datum (in the sense of object_datum),
- modeling_tower_morphism_constructor: a function which gets the reinterpretation R, a source in the modeling category, a morphism datum (in the sense of morphism_datum), and a range in the modeling category and returns the corresponding modeling morphism in the modeling category,
- modeling_tower_morphism_datum: a function which gets the reinterpretation R and a morphism in the modeling category and returns the corresponding morphism datum (in the sense of morphism_datum),
- only_primitive_operations (optional, default false): whether to only reinterpret primitive operations or all operations.

12.6.2 ReinterpretationFunctor (for IsCapCategory)

▷ ReinterpretationFunctor(R)

(attribute)

Returns: a functor

Returns the functor from the modeling category ModelingCategory(R) to the reinterpretation R which maps each object/morphism to its reinterpretation.

12.6.3 ModelingObject (for IsCapCategory, IsCapCategoryObject)

▷ ModelingObject(R, obj)

(operation)

Returns: a CAP category object

Returns the object in ModelingCategory(R) modeling the object ob i in the reinterpretation R.

12.6.4 ReinterpretationOfObject (for IsCapCategory, IsCapCategoryObject)

▷ ReinterpretationOfObject(R, obj)

(operation)

Returns: a CAP category object

Returns the reinterpretation in R of an object obj in ModelingCategory(R).

12.6.5 ModelingMorphism (for IsCapCategory, IsCapCategoryMorphism)

▷ ModelingMorphism(R, mor)

(operation)

Returns: a CAP category morphism

Returns the morphism in ModelingCategory(R) modeling the morphism mor in the reinterpretation R.

12.6.6 ReinterpretationOfMorphism (for IsCapCategory, IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject)

▷ ReinterpretationOfMorphism(R, source, obj, range)

(operation)

Returns: a CAP category morphism

Returns the reinterpretation in R with given source and range of a morphism mor in ModelingCategory(R).

Chapter 13

Create wrapper hulls of a category

13.1 GAP categories

13.1.1 IsWrapperCapCategory (for IsCapCategory)

▷ IsWrapperCapCategory(arg)

(filter)

Returns: true or false

The GAP category of a wrapper CAP category.

13.1.2 IsWrapperCapCategoryObject (for IsCapCategoryObject)

▷ IsWrapperCapCategoryObject(arg)

(filter)

Returns: true or false

The GAP category of objects in a wrapper CAP category.

13.1.3 IsWrapperCapCategoryMorphism (for IsCapCategoryMorphism)

▷ IsWrapperCapCategoryMorphism(arg)

(filter)

Returns: true or false

The GAP category of morphisms in a wrapper CAP category.

13.2 Attributes

13.2.1 UnderlyingCell (for IsWrapperCapCategoryObject)

▷ UnderlyingCell(object)

(attribute)

Returns: a category object

The cell underlying the wrapper category object object.

13.2.2 UnderlyingCell (for IsWrapperCapCategoryMorphism)

▷ UnderlyingCell(morphism)

(attribute)

Returns: a category morphism

The cell underlying the wrapper category morphism morphism.

13.3 Constructors

13.3.1 AsObjectInWrapperCategory (for IsWrapperCapCategory, IsCapCategory-Object)

▷ AsObjectInWrapperCategory(category, object)

(operation)

Returns: an object

Wrap an object object (in the category underlying the wrapper category category) to form an object in category.

13.3.2 AsMorphismInWrapperCategory (for IsWrapperCapCategoryObject, IsCap-CategoryMorphism, IsWrapperCapCategoryObject)

▷ AsMorphismInWrapperCategory(source, morphism, range)

(operation)

Returns: a morphism

Wrap a morphism morphism (in the category underlying the wrapper category CapCategory(source)) to form a morphism in CapCategory(source) with given source and range.

13.3.3 AsMorphismInWrapperCategory (for IsWrapperCapCategory, IsCapCategoryMorphism)

▷ AsMorphismInWrapperCategory(category, morphism)

(operation)

Returns: a morphism

Wrap a morphism morphism (in the category underlying the wrapper category category) to form a morphism in category.

13.3.4 / (for IsCapCategoryCell, IsWrapperCapCategory)

▷ /(cell, category)

(operation)

Convenience method for AsObjectInWrapperCategory (13.3.1) and AsMorphismInWrapperCategory (13.3.3).

13.3.5 WrapperCategory (for IsCapCategory, IsRecord)

▷ WrapperCategory(category, options)

(operation)

Returns: a category

Wraps a category category to form a new category subject to the options given via options, which is a record with the following keys:

- name (optional): the name of the wrapper category
- only_primitive_operations (optional, default false): whether to only wrap primitive operations or all operations

Additionally, the following options of CategoryConstructor (11.2.1) are supported: category_filter, category_object_filter, category_morphism_filter. The filters must imply IsWrapperCapCategory, IsWrapperCapCategoryObject, and IsWrapperCapCategoryMorphism, respectively.

13.3.6 WrappingFunctor (for IsWrapperCapCategory)

▷ WrappingFunctor(W)

(attribute)

Returns: a functor

Return the functor from the wrapped category ModelingCategory(W) to the wrapper category W which simply wraps objects/morphisms.

Chapter 14

Dummy implementations

A dummy implementation of a concept seems to provide an interface for the concept, but calling any operation in this interface will simply signal an error. Hence, when using a dummy implementation, we can be sure that we only rely on the abstract interface but not on any implementation details, for the simple reason that there is no actual implementation. This is useful for testing or compilation against a generic implementation of a concept.

14.1 Dummy rings

14.1.1 IsDummyRing

□ IsDummyRing
 (filter)

The GAP filter of dummy rings.

14.1.2 IsDummyRingElement

▷ IsDummyRingElement (filter)

The GAP filter of elements of a dummy ring.

14.1.3 IsDummyCommutativeRing

▷ IsDummyCommutativeRing (filter)

The GAP filter of dummy commutative rings.

14.1.4 IsDummyCommutativeRingElement

 ${\tt \triangleright IsDummyCommutativeRingElement} \tag{filter}$

The GAP filter of elements of a dummy commutative ring.

(filter)

(filter)

14.1.5 IsDummyField

▷ IsDummyField
 (filter)

The GAP filter of dummy fields.

14.1.6 IsDummyFieldElement

▷ IsDummyFieldElement (filter)

The GAP filter of elements of a dummy field.

14.1.7 DummyRing

▷ DummyRing()

Returns: a dummy ring

14.1.8 DummyCommutativeRing

▷ DummyCommutativeRing() (function)

Returns: a dummy commutative ring

14.1.9 DummyField

▷ DummyField() (function)

Returns: a dummy field

14.2 Dummy categories

14.2.1 IsDummyCategory (for IsCapCategory)

□ IsDummyCategory(arg)
 (filter)

Returns: true or false

The GAP category of a dummy CAP category.

14.2.2 IsDummyCategoryObject (for IsCapCategoryObject)

▷ IsDummyCategoryObject(arg)

Returns: true or false

The GAP category of objects in a dummy CAP category.

14.2.3 IsDummyCategoryMorphism (for IsCapCategoryMorphism)

Returns: true or false

▷ IsDummyCategoryMorphism(arg)

The GAP category of morphisms in a dummy CAP category.

14.2.4 DummyCategory (for IsRecord)

▷ DummyCategory(options)

(operation)

Returns: a category

Creates a dummy category subject to the options given via *options*, which is a record passed on to CategoryConstructor (11.2.1). Note that the options {category,object,morphism}_filter will be set to IsDummyCategory{,Object,Morphism} and the options {object,morphism}_{constructor,datum} and create_func_* will be set to dummy implementations (throwing errors when actually called). The dummy category will pretend to support empty limits by default.

14.3 Dummy homalg rings

The operations in this section require MatricesForHomalg to be loaded.

14.3.1 IsDummyHomalgRing

▷ IsDummyHomalgRing

(filter)

The GAP filter of dummy homalg rings.

14.3.2 IsDummyHomalgRingElement

▷ IsDummyHomalgRingElement

(filter)

The GAP filter of elements of a dummy homalg ring.

14.3.3 IsDummyCommutativeHomalgRing

▷ IsDummyCommutativeHomalgRing

(filter)

The GAP filter of dummy commutative homalg rings.

14.3.4 IsDummyCommutativeHomalgRingElement

▷ IsDummyCommutativeHomalgRingElement

(filter)

The GAP filter of elements of a dummy commutative homalg ring.

14.3.5 IsDummyHomalgField

▷ IsDummyHomalgField

(filter)

The GAP filter of dummy homalg fields.

14.3.6 IsDummyHomalgFieldElement

▷ IsDummyHomalgFieldElement

(filter)

The GAP filter of elements of a dummy homalg field.

14.3.7 DummyHomalgRing

▷ DummyHomalgRing()

(function)

Returns: a dummy homalg ring

14.3.8 DummyCommutativeHomalgRing

▷ DummyCommutativeHomalgRing()

(function)

Returns: a dummy commutative homalg ring

14.3.9 DummyHomalgField

▷ DummyHomalgField()

(function)

Returns: a dummy homalg field

Chapter 15

Examples and Tests

15.1 Dummy implementations

15.1.1 Dummy categories

```
_{-} Example _{	ext{-}}
gap> LoadPackage( "CAP", false );
true
gap> list_of_operations_to_install := [
     "ObjectConstructor",
     "MorphismConstructor",
    "ObjectDatum",
    "MorphismDatum"
    "IsCongruentForMorphisms",
    "PreCompose",
     "IdentityMorphism",
      "DirectSum",
> ];;
gap> dummy := DummyCategory( rec(
     list_of_operations_to_install := list_of_operations_to_install,
      properties := [ "IsAdditiveCategory" ],
> ) );;
gap> ForAll( list_of_operations_to_install, o -> CanCompute( dummy, o ) );
gap> IsAdditiveCategory( dummy );
true
```

15.1.2 Dummy rings

```
gap> LoadPackage( "CAP", false );
true
gap> DummyRing();
Dummy ring 1
gap> DummyRing();
Dummy ring 2
gap> IsRing( DummyRing());
true
gap> DummyCommutativeRing();
```

```
Dummy commutative ring 1
gap> DummyCommutativeRing();
Dummy commutative ring 2
gap> IsRing( DummyCommutativeRing());
true
gap> IsCommutative( DummyCommutativeRing());
true
gap> DummyField();
Dummy field 1
gap> DummyField();
Dummy field 2
gap> IsRing( DummyField());
true
gap> IsField( DummyField());
true
```

15.2 Functors

We create a binary functor F with one covariant and one contravariant component in two ways. Here is the first way to model a binary functor:

```
gap> ring := HomalgRingOfIntegers();;
gap> vec := LeftPresentations( ring );;
gap> F := CapFunctor( "CohomForVec", [ vec, [ vec, true ] ], vec );;
gap> obj_func := function( A, B ) return TensorProductOnObjects( A, DualOnObjects( B ) ); end;;
gap> mor_func := function( source, alpha, beta, range ) return TensorProductOnMorphismsWithGivenTensorProductOnMorphismsFunction( F, obj_func );;
gap> AddObjectFunction( F, mor_func );;
```

CAP regards F as a binary functor on a technical level, as we can see by looking at its input signature:

```
gap> InputSignature( F );
[ [ Category of left presentations of Z, false ], [ Category of left presentations of Z, true ] ]
```

We can see that ApplyFunctor works both on two arguments and on one argument (in the product category).

```
gap> V1 := TensorUnit( vec );;
gap> V3 := DirectSum( V1, V1, V1 );;
gap> pi1 := ProjectionInFactorOfDirectSum( [ V1, V1 ], 1 );;
gap> pi2 := ProjectionInFactorOfDirectSum( [ V3, V1 ], 1 );;
gap> value1 := ApplyFunctor( F, pi1, pi2 );;
gap> input := Product( pi1, Opposite( pi2 ) );;
gap> value2 := ApplyFunctor( F, input );;
gap> IsCongruentForMorphisms( value1, value2 );
true
```

Here is the second way to model a binary functor:

```
gap> F2 := CapFunctor( "CohomForVec2", Product( vec, Opposite( vec ) ), vec );;
gap> AddObjectFunction( F2, a -> obj_func( a[1], Opposite( a[2] ) ) );;
gap> AddMorphismFunction( F2, function( source, datum, range ) return mor_func( source, datum[1] gap> value3 := ApplyFunctor( F2,input );;
gap> IsCongruentForMorphisms( value1, value3 );
true
```

CAP regards F2 as a unary functor on a technical level, as we can see by looking at its input signature:

```
gap> InputSignature( F2 );

[ [ Product of: Category of left presentations of Z, Opposite( Category of left presentations of
```

Installation of the first functor as a GAP-operation. It will be installed both as a unary and binary version.

```
gap> InstallFunctor( F, "F_installation" );;
gap> F_installation( pi1, pi2 );;
gap> F_installation( input );;
gap> F_installationOnObjects( V1, V1 );;
gap> F_installationOnObjects( Product( V1, Opposite( V1 ) ) );;
gap> F_installationOnMorphisms( pi1, pi2 );;
gap> F_installationOnMorphisms( input );;
```

Installation of the second functor as a GAP-operation. It will be installed only as a unary version.

```
gap> InstallFunctor( F2, "F_installation2" );;
gap> F_installation2( input );;
gap> F_installation20n0bjects( Product( V1, Opposite( V1 ) ) );;
gap> F_installation20nMorphisms( input );;
```

15.3 HandlePrecompiledTowers

```
_{-} Example
gap> LoadPackage( "CAP", false );
gap> dummy1 := CreateCapCategory( );;
gap> dummy2 := CreateCapCategory();;
gap> dummy3 := CreateCapCategory( );;
gap> PrintAndReturn := function ( string )
      Print( string, "\n" ); return string; end;;
gap> dummy1!.compiler_hints := rec();;
gap> dummy1!.compiler_hints.precompiled_towers := [
      remaining_constructors_in_tower := [ "Constructor1" ],
      precompiled_functions_adder := cat ->
        PrintAndReturn( "Adding precompiled operations for Constructor1" ),
>
   ),
>
>
   rec(
>
      remaining_constructors_in_tower := [ "Constructor1", "Constructor2" ],
      precompiled_functions_adder := cat ->
```

```
> PrintAndReturn( "Adding precompiled operations for Constructor2" ),
> ),
> ];;
gap> HandlePrecompiledTowers( dummy2, dummy1, "Constructor1" );
Adding precompiled operations for Constructor1
gap> HandlePrecompiledTowers( dummy3, dummy2, "Constructor2" );
Adding precompiled operations for Constructor2
```

15.4 Terminal category

```
_ Example _
gap> LoadPackage( "CAP", false );
true
gap> T := TerminalCategoryWithMultipleObjects( );
TerminalCategoryWithMultipleObjects( )
gap> i := InitialObject( T );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> t := TerminalObject( T );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> z := ZeroObject( T );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Display( i );
InitialObject
gap> Display( t );
TerminalObject
gap> Display( z );
ZeroObject
gap> IsIdenticalObj( i, z );
false
gap> IsIdenticalObj( t, z );
false
gap> id_z := IdentityMorphism( z );
<A zero, identity morphism in TerminalCategoryWithMultipleObjects()>
gap> fn_z := ZeroObjectFunctorial( T );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> IsEqualForMorphisms( id_z, fn_z );
false
gap> IsCongruentForMorphisms( id_z, fn_z );
gap> a := "a" / T;
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Display( a );
gap> IsWellDefined( a );
gap> aa := ObjectConstructor( T, "a" );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Display( aa );
gap> IsEqualForObjects( a, aa );
true
gap> IsIsomorphicForObjects( a, aa );
```

```
true
gap> IsIsomorphism( SomeIsomorphismBetweenObjects( a, aa ) );
gap> b := "b" / T;
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Display( b );
gap> IsEqualForObjects( a, b );
false
gap> IsIsomorphicForObjects( a, b );
gap> mor_ab := SomeIsomorphismBetweenObjects( a, b );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> IsIsomorphism( mor_ab );
true
gap> Display( mor_ab );
| SomeIsomorphismBetweenObjects
٧
gap> Hom_ab := MorphismsOfExternalHom( a, b );;
gap> Length( Hom_ab );
gap> Hom_ab[1];
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( Hom_ab[1] );
| InterpretMorphismFromDistinguishedObjectToHomomorphismStructureAsMorphism
b
gap> Hom_ab[1] = mor_ab;
gap> HomStructure( mor_ab );
<A zero, identity morphism in TerminalCategoryWithSingleObject( )>
gap> m := MorphismConstructor( a, "m", b );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( m );
а
m
gap> IsWellDefined( m );
gap> n := MorphismConstructor( a, "n", b );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( n );
a
n
```

```
٧
b
gap> IsEqualForMorphisms( m, n );
gap> IsCongruentForMorphisms( m, n );
true
gap> m = n;
true
gap> hom_mn := HomStructure( m, n );
<A zero, identity morphism in TerminalCategoryWithSingleObject( )>
gap> id := IdentityMorphism( a );
<A zero, identity morphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( id );
| IdentityMorphism
gap> m = id;
gap> id = MorphismConstructor( a, "xyz", a );
gap> zero := ZeroMorphism( a, a );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( zero );
a
ZeroMorphism
v
gap> id = zero;
true
gap> IsLiftable( m, n );
gap> lift := Lift( m, n );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( lift );
Lift
v
gap> IsColiftable( m, n );
gap> colift := Colift( m, n );
<A zero, isomorphism in TerminalCategoryWithMultipleObjects( )>
gap> Display( colift );
b
Colift
v
b
```

```
gap> DirectProduct( T, [ ] );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Equalizer( T, z, [ ] );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Coproduct( T, [ ] );
<A zero object in TerminalCategoryWithMultipleObjects( )>
gap> Coequalizer( T, z, [ ] );
<A zero object in TerminalCategoryWithMultipleObjects( )>
```

```
_{-} Example .
gap> LoadPackage( "CAP", false );
gap> T := TerminalCategoryWithSingleObject( );
TerminalCategoryWithSingleObject( )
gap> i := InitialObject( T );
<A zero object in TerminalCategoryWithSingleObject( )>
gap> t := TerminalObject( T );
<A zero object in TerminalCategoryWithSingleObject( )>
gap> z := ZeroObject( T );
<A zero object in TerminalCategoryWithSingleObject( )>
gap> Display( i );
A zero object in TerminalCategoryWithSingleObject().
gap> Display( t );
A zero object in TerminalCategoryWithSingleObject().
gap> Display( z );
A zero object in TerminalCategoryWithSingleObject().
gap> IsIdenticalObj( i, z );
false
gap> IsIdenticalObj( t, z );
false
gap> IsWellDefined( z );
true
gap> id_z := IdentityMorphism( z );
<A zero, identity morphism in TerminalCategoryWithSingleObject( )>
gap> fn_z := ZeroObjectFunctorial( T );
<A zero, identity morphism in TerminalCategoryWithSingleObject( )>
gap> IsWellDefined( fn_z );
true
gap> IsEqualForMorphisms( id_z, fn_z );
gap> IsCongruentForMorphisms( id_z, fn_z );
gap> IsLiftable( id_z, fn_z );
true
gap> Lift( id_z, fn_z );
<A zero, identity morphism in TerminalCategoryWithSingleObject( )>
gap> IsColiftable( id_z, fn_z );
true
gap> Colift( id_z, fn_z );
<A zero, identity morphism in TerminalCategoryWithSingleObject( )>
gap> DirectProduct( T, [ ] );
<A zero object in TerminalCategoryWithSingleObject( )>
gap> Equalizer( T, z, [ ] );
```

```
<A zero object in TerminalCategoryWithSingleObject( )>
gap> Coproduct( T, [ ] );
<A zero object in TerminalCategoryWithSingleObject( )>
gap> Coequalizer( T, z, [ ] );
<A zero object in TerminalCategoryWithSingleObject( )>
```

Chapter 16

Terminal category

16.1 GAP Categories

16.1.1 IsCapTerminalCategoryWithSingleObject (for IsCapCategory)

▷ IsCapTerminalCategoryWithSingleObject(T)

(filter)

Returns: true or false

The GAP type of a terminal category with a single object.

16.1.2 IsObjectInCapTerminalCategoryWithSingleObject (for IsCapCategoryObject)

▷ IsObjectInCapTerminalCategoryWithSingleObject(T)

(filter)

Returns: true or false

The GAP type of an object in a terminal category with a single object.

16.1.3 IsMorphismInCapTerminalCategoryWithSingleObject (for IsCapCategory-Morphism)

 ${\tt \triangleright} \ \, {\tt IsMorphismInCapTerminalCategoryWithSingleObject(\it{T})}\\$

(filter)

Returns: true or false

The GAP type of a morphism in a terminal category with a single object.

16.1.4 IsCapTerminalCategoryWithMultipleObjects (for IsCapCategory)

▷ IsCapTerminalCategoryWithMultipleObjects(T)

(filter)

Returns: true or false

The GAP type of a terminal category with multiple objects.

16.1.5 IsObjectInCapTerminalCategoryWithMultipleObjects (for IsCapCategoryObject)

▷ IsObjectInCapTerminalCategoryWithMultipleObjects(T)

(filter)

Returns: true or false

The GAP type of an object in a terminal category with multiple objects.

16.1.6 IsMorphismInCapTerminalCategoryWithMultipleObjects (for IsCapCategoryMorphism)

▷ IsMorphismInCapTerminalCategoryWithMultipleObjects(T)

(filter)

Returns: true or false

The GAP type of a morphism in a terminal category with multiple objects.

16.1.7 IsTerminalCategory (for IsCapCategory)

 \triangleright IsTerminalCategory(C)

(property)

Returns: true or false

The property of the category C being terminal.

16.2 Constructors

16.2.1 TerminalCategoryWithSingleObject

▷ TerminalCategoryWithSingleObject(arg)

(function)

Construct a terminal category with a single object.

16.2.2 TerminalCategoryWithMultipleObjects

▷ TerminalCategoryWithMultipleObjects(arg)

(function)

Construct a terminal category with multiple objects.

16.2.3 CAP_INTERNAL_CONSTRUCTOR_FOR_TERMINAL_CATEGORY

▷ CAP_INTERNAL_CONSTRUCTOR_FOR_TERMINAL_CATEGORY(options)

(function)

Returns: a CAP category

This function takes a record of options suited for CategoryConstructor. It makes common adjustments for TerminalCategoryWithSingleObject and TerminalCategoryWithMultipleObjects to the list of operations to install and the categorical properties of the given record, before passing it on to CategoryConstructor.

16.3 Attributes

16.3.1 TerminalCategoryWithSingleObjectUniqueObject (for IsCapTerminalCategoryWithSingleObject)

 ${\tt \triangleright} \ \, {\tt TerminalCategoryWithSingleObjectUniqueObject(arg)}$

(attribute)

Returns: a CAP object

The unique object in a terminal category with a single object.

16.3.2 TerminalCategoryWithSingleObjectUniqueMorphism (for IsCapTerminalCategoryWithSingleObject)

□ TerminalCategoryWithSingleObjectUniqueMorphism(arg)

(attribute)

Returns: a CAP morphism

The unique morphism in a terminal category with a single object.

16.3.3 FunctorFromTerminalCategory (for IsCapCategoryObject)

 ${\scriptstyle \rhd} \ \ {\tt FunctorFromTerminalCategory} (\it object)$

(attribute)

Returns: a CAP functor

A functor from AsCapCategory(TerminalObject(CapCat)) mapping the unique object to object.

Index

*	AddCoastrictionToImageWithGivenImage
for IsRingElement, IsCapCategoryMor-	Object
phism, 35	for IsCapCategory, IsFunction, 108
/	for IsCapCategory, IsFunction, IsInt, 108
for IsCapCategoryCell, IsWrapperCapCate-	AddCoefficientsOfMorphism
gory, 203	for IsCapCategory, IsFunction, 108
for IsObject, IsCapCategory, 23	for IsCapCategory, IsFunction, IsInt, 108
	AddCoequalizer
ActivateDerivationInfo, 174	for IsCapCategory, IsFunction, 108
Add	for IsCapCategory, IsFunction, IsInt, 108
for IsCapCategory, IsCapCategoryMor-	AddCoequalizerFunctorial
phism, 28	for IsCapCategory, IsFunction, 109
for IsCapCategory, IsCapCategoryObject, 19	for IsCapCategory, IsFunction, IsInt, 109
for IsCapCategory, IsCapCategoryTwoCell,	AddCoequalizerFunctorialWithGiven-
52	Coequalizers
AddAdditionForMorphisms	for IsCapCategory, IsFunction, 109
for IsCapCategory, IsFunction, 106	for IsCapCategory, IsFunction, IsInt, 109
for IsCapCategory, IsFunction, IsInt, 106	AddCoimageObject
AddAdditiveGenerators	for IsCapCategory, IsFunction, 109
for IsCapCategory, IsFunction, 107	for IsCapCategory, IsFunction, IsInt, 109
for IsCapCategory, IsFunction, IsInt, 107	AddCoimageObjectFunctorial
${\tt AddAdditiveInverseForMorphisms}$	for IsCapCategory, IsFunction, 109
for IsCapCategory, IsFunction, 107	for IsCapCategory, IsFunction, IsInt, 109
for IsCapCategory, IsFunction, IsInt, 107	AddCoimageObjectFunctorialWithGiven-
${\tt AddAstrictionToCoimage}$	CoimageObjects
for IsCapCategory, IsFunction, 107	for IsCapCategory, IsFunction, 110
for IsCapCategory, IsFunction, IsInt, 107	for IsCapCategory, IsFunction, IsInt, 110
AddAstrictionToCoimageWithGiven-	AddCoimageProjection
CoimageObject	for IsCapCategory, IsFunction, 110
for IsCapCategory, IsFunction, 107	for IsCapCategory, IsFunction, IsInt, 110
for IsCapCategory, IsFunction, IsInt, 107	AddCoimageProjectionWithGivenCoimage-
AddBasisOfExternalHom	Object
for IsCapCategory, IsFunction, 108	for IsCapCategory, IsFunction, 110
for IsCapCategory, IsFunction, IsInt, 108	for IsCapCategory, IsFunction, IsInt, 110
${\tt AddCategoricalProperty,7}$	AddCokernelColift
AddCoastrictionToImage	for IsCapCategory, IsFunction, 110
for IsCapCategory, IsFunction, 108	for IsCapCategory, IsFunction, IsInt, 110
for IsCapCategory, IsFunction, IsInt, 108	AddCokernelColiftWithGivenCokernel-

Object	Coproducts
for IsCapCategory, IsFunction, 111	for IsCapCategory, IsFunction, 114
for IsCapCategory, IsFunction, IsInt, 111	for IsCapCategory, IsFunction, IsInt, 114
AddCokernelObject	AddDerivation, 177
for IsCapCategory, IsFunction, 111	AddDerivationToCAP, 177
for IsCapCategory, IsFunction, IsInt, 111	AddDirectProduct
AddCokernelObjectFunctorial	for IsCapCategory, IsFunction, 114
for IsCapCategory, IsFunction, 111	for IsCapCategory, IsFunction, IsInt, 114
for IsCapCategory, IsFunction, IsInt, 111	AddDirectProductFunctorial
AddCokernelObjectFunctorialWithGiven-	for IsCapCategory, IsFunction, 114
CokernelObjects	for IsCapCategory, IsFunction, IsInt, 114
for IsCapCategory, IsFunction, 111	AddDirectProductFunctorialWithGiven-
for IsCapCategory, IsFunction, IsInt, 111	DirectProducts
AddCokernelProjection	for IsCapCategory, IsFunction, 115
for IsCapCategory, IsFunction, 112	for IsCapCategory, IsFunction, IsInt, 115
for IsCapCategory, IsFunction, IsInt, 112	AddDirectSum
AddCokernelProjectionWithGiven-	for IsCapCategory, IsFunction, 115
CokernelObject	for IsCapCategory, IsFunction, IsInt, 115
for IsCapCategory, IsFunction, 112	AddDirectSumFunctorial
for IsCapCategory, IsFunction, IsInt, 112	for IsCapCategory, IsFunction, 115
AddColift	for IsCapCategory, IsFunction, IsInt, 115
for IsCapCategory, IsFunction, 112	AddDirectSumFunctorialWithGivenDirect
for IsCapCategory, IsFunction, IsInt, 112	Sums
AddColiftAlongEpimorphism	for IsCapCategory, IsFunction, 115
for IsCapCategory, IsFunction, 112	for IsCapCategory, IsFunction, IsInt, 115
for IsCapCategory, IsFunction, IsInt, 112	AddDistinguishedObjectOfHomomorphism-
AddComponentOfMorphismFromCoproduct	Structure
for IsCapCategory, IsFunction, 112	for IsCapCategory, IsFunction, 116
for IsCapCategory, IsFunction, IsInt, 112	for IsCapCategory, IsFunction, IsInt, 116
AddComponentOfMorphismFromDirectSum	AddEmbeddingOfEqualizer
for IsCapCategory, IsFunction, 113	for IsCapCategory, IsFunction, 116
for IsCapCategory, IsFunction, IsInt, 113	for IsCapCategory, IsFunction, IsInt, 116
AddComponentOfMorphismIntoDirect-	AddEmbeddingOfEqualizerWithGiven-
Product	Equalizer
for IsCapCategory, IsFunction, 113	for IsCapCategory, IsFunction, 116
for IsCapCategory, IsFunction, IsInt, 113	for IsCapCategory, IsFunction, IsInt, 116
AddComponentOfMorphismIntoDirectSum	AddEpimorphismFromProjectiveCover-
for IsCapCategory, IsFunction, 113	Object
for IsCapCategory, IsFunction, IsInt, 113	for IsCapCategory, IsFunction, 116
AddCoproduct	for IsCapCategory, IsFunction, IsInt, 116
for IsCapCategory, IsFunction, 113	AddEpimorphismFromProjectiveCover-
for IsCapCategory, IsFunction, IsInt, 113	ObjectWithGivenProjectiveCover
AddCoproductFunctorial	Object
for IsCapCategory, IsFunction, 114	for IsCapCategory, IsFunction, 117
for IsCapCategory, IsFunction, IsInt, 114	for IsCapCategory, IsFunction, IsInt, 117
AddCoproductFunctorialWithGiven-	AddEpimorphismFromSomeProjectiveObjec

for IsCapCategory, IsFunction, 117	for IsCapCategory, IsFunction, IsInt, 120
for IsCapCategory, IsFunction, IsInt, 117	AddHorizontalPreCompose
AddEpimorphismFromSomeProjective-	for IsCapCategory, IsFunction, 120
ObjectWithGivenSomeProjective-	for IsCapCategory, IsFunction, IsInt, 120
Object	AddIdentityMorphism
for IsCapCategory, IsFunction, 117	for IsCapCategory, IsFunction, 121
for IsCapCategory, IsFunction, IsInt, 117	for IsCapCategory, IsFunction, IsInt, 121
AddEqualizer	AddIdentityTwoCell
for IsCapCategory, IsFunction, 117	for IsCapCategory, IsFunction, 121
for IsCapCategory, IsFunction, IsInt, 117	for IsCapCategory, IsFunction, IsInt, 121
AddEqualizerFunctorial	AddImageEmbedding
for IsCapCategory, IsFunction, 118	for IsCapCategory, IsFunction, 121
for IsCapCategory, IsFunction, IsInt, 118	for IsCapCategory, IsFunction, IsInt, 121
AddEqualizerFunctorialWithGiven-	AddImageEmbeddingWithGivenImageObject
Equalizers	for IsCapCategory, IsFunction, 121
for IsCapCategory, IsFunction, 118	for IsCapCategory, IsFunction, IsInt, 121
for IsCapCategory, IsFunction, IsInt, 118	AddImageObject
AddFiberProduct	for IsCapCategory, IsFunction, 121
for IsCapCategory, IsFunction, 118	for IsCapCategory, IsFunction, IsInt, 121
for IsCapCategory, IsFunction, IsInt, 118	AddImageObjectFunctorial
AddFiberProductFunctorial	for IsCapCategory, IsFunction, 122
for IsCapCategory, IsFunction, 118	for IsCapCategory, IsFunction, IsInt, 122
for IsCapCategory, IsFunction, IsInt, 118	AddImageObjectFunctorialWithGiven-
AddFiberProductFunctorialWithGiven-	ImageObjects
AddFiberProductFunctorialWithGiven- FiberProducts	<pre>ImageObjects for IsCapCategory, IsFunction, 122</pre>
	<u> </u>
FiberProducts	for IsCapCategory, IsFunction, 122
FiberProducts for IsCapCategory, IsFunction, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven-	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, 122 AddInitialObject
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddInitialObject for IsCapCategory, IsFunction, 123
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, 119	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, 119 AddHomomorphismStructureOnMorphisms-	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms- WithGivenObjects	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 AddInitialObjectFunctorial MdInitialObjectFunctorialWithGiven-
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms- WithGivenObjects for IsCapCategory, IsFunction, 120	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 AddInitialObjectFunctorialWithGiven- InitialObjects
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, 119 AddHomomorphismStructureOnMorphisms WithGivenObjects for IsCapCategory, IsFunction, 120 for IsCapCategory, IsFunction, 15Int, 120	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 AddInitialObjectFunctorialWithGiven- InitialObjects for IsCapCategory, IsFunction, 130 AddInitialObjectFunctorialWithGiven- InitialObjects for IsCapCategory, IsFunction, 123
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms- WithGivenObjects for IsCapCategory, IsFunction, 120 for IsCapCategory, IsFunction, IsInt, 120 AddHomomorphismStructureOnObjects	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 AddInitialObjectFunctorialWithGiven- InitialObjects for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123
FiberProducts for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObject for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomologyObjectFunctorialWithGiven- HomologyObjects for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, IsInt, 119 AddHomomorphismStructureOnMorphisms for IsCapCategory, IsFunction, 119 for IsCapCategory, IsFunction, 119 AddHomomorphismStructureOnMorphisms- WithGivenObjects for IsCapCategory, IsFunction, 120 for IsCapCategory, IsFunction, IsInt, 120 AddHomomorphismStructureOnObjects for IsCapCategory, IsFunction, 1210 For IsCapCategory, IsFunction, 120 For IsCapCategory, IsFunction, 120 For IsCapCategory, IsFunction, 120	for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableInjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, IsInt, 122 AddIndecomposableProjectiveObjects for IsCapCategory, IsFunction, 122 for IsCapCategory, IsFunction, 122 AddInitialObject for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorial for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, IsInt, 123 AddInitialObjectFunctorialWithGiven- InitialObjects for IsCapCategory, IsFunction, 123 for IsCapCategory, IsFunction, 123 AddInjectionOfCofactorOfCoproduct

${\tt GivenCoproduct}$	for IsCapCategory, IsFunction, 127
for IsCapCategory, IsFunction, 124	for IsCapCategory, IsFunction, IsInt, 127
for IsCapCategory, IsFunction, IsInt, 124	AddInverseOfMorphismFromCoimageTo-
AddInjectionOfCofactorOfDirectSum	${\tt ImageWithGivenObjects}$
for IsCapCategory, IsFunction, 124	for IsCapCategory, IsFunction, 127
for IsCapCategory, IsFunction, IsInt, 124	for IsCapCategory, IsFunction, IsInt, 127
AddInjectionOfCofactorOfDirectSumWith-	AddIsAutomorphism
GivenDirectSum	for IsCapCategory, IsFunction, 127
for IsCapCategory, IsFunction, 124	for IsCapCategory, IsFunction, IsInt, 127
for IsCapCategory, IsFunction, IsInt, 124	AddIsBijectiveObject
AddInjectionOfCofactorOfPushout	for IsCapCategory, IsFunction, 127
for IsCapCategory, IsFunction, 124	for IsCapCategory, IsFunction, IsInt, 127
for IsCapCategory, IsFunction, IsInt, 124	AddIsCodominating
AddInjectionOfCofactorOfPushoutWith-	for IsCapCategory, IsFunction, 128
GivenPushout	for IsCapCategory, IsFunction, IsInt, 128
for IsCapCategory, IsFunction, 125	AddIsColiftable
for IsCapCategory, IsFunction, IsInt, 125	for IsCapCategory, IsFunction, 128
AddInjectiveColift	for IsCapCategory, IsFunction, IsInt, 128
for IsCapCategory, IsFunction, 125	AddIsColiftableAlongEpimorphism
for IsCapCategory, IsFunction, IsInt, 125	for IsCapCategory, IsFunction, 128
AddInjectiveDimension	for IsCapCategory, IsFunction, IsInt, 128
for IsCapCategory, IsFunction, 125	AddIsCongruentForMorphisms
for IsCapCategory, IsFunction, IsInt, 125	for IsCapCategory, IsFunction, 128
AddInjectiveEnvelopeObject	for IsCapCategory, IsFunction, IsInt, 128
for IsCapCategory, IsFunction, 125	AddIsDominating
for IsCapCategory, IsFunction, IsInt, 125	for IsCapCategory, IsFunction, 128
AddInterpretMorphismAsMorphism-	for IsCapCategory, IsFunction, IsInt, 128
FromDistinguishedObjectTo-	AddIsEndomorphism
HomomorphismStructure	for IsCapCategory, IsFunction, 129
for IsCapCategory, IsFunction, 125	for IsCapCategory, IsFunction, IsInt, 129
for IsCapCategory, IsFunction, IsInt, 126	AddIsEpimorphism
AddInterpretMorphismAsMorphism-	for IsCapCategory, IsFunction, 129
FromDistinguishedObjectTo-	for IsCapCategory, IsFunction, IsInt, 129
HomomorphismStructureWithGiven-	AddIsEqualAsFactorobjects
Objects	for IsCapCategory, IsFunction, 129
for IsCapCategory, IsFunction, 126	for IsCapCategory, IsFunction, IsInt, 129
for IsCapCategory, IsFunction, IsInt, 126	AddIsEqualAsSubobjects
AddInterpretMorphismFromDistinguished-	for IsCapCategory, IsFunction, 129
ObjectToHomomorphismStructure-	for IsCapCategory, IsFunction, IsInt, 129
AsMorphism	${\tt AddIsEqualForCacheForMorphisms}$
for IsCapCategory, IsFunction, 126	for IsCapCategory, IsFunction, 130
for IsCapCategory, IsFunction, IsInt, 126	for IsCapCategory, IsFunction, IsInt, 130
AddInverseForMorphisms	AddIsEqualForCacheForObjects
for IsCapCategory, IsFunction, 126	for IsCapCategory, IsFunction, 130
for IsCapCategory, IsFunction, IsInt, 126	for IsCapCategory, IsFunction, IsInt, 130
AddInverseOfMorphismFromCoimageToImage	AddIsEqualForMorphisms

for IsCapCategory, IsFunction, 130	CokernelOfJointPairwise-
for IsCapCategory, IsFunction, IsInt, 130	DifferencesOfMorphismsFrom-
AddIsEqualForMorphismsOnMor	Coproduct
for IsCapCategory, IsFunction, 130	for IsCapCategory, IsFunction, 136
for IsCapCategory, IsFunction, IsInt, 130	for IsCapCategory, IsFunction, IsInt, 136
AddIsEqualForObjects	AddIsomorphismFromCoimageToCokernelOf-
for IsCapCategory, IsFunction, 130	Kernel
for IsCapCategory, IsFunction, IsInt, 130	for IsCapCategory, IsFunction, 136
AddIsEqualToIdentityMorphism	for IsCapCategory, IsFunction, IsInt, 136
for IsCapCategory, IsFunction, 131	AddIsomorphismFromCokernelOfJoint-
for IsCapCategory, IsFunction, IsInt, 131	PairwiseDifferencesOfMorphisms-
AddIsEqualToZeroMorphism	FromCoproductToCoequalizer
for IsCapCategory, IsFunction, 131	for IsCapCategory, IsFunction, 136
for IsCapCategory, IsFunction, IsInt, 131	for IsCapCategory, IsFunction, IsInt, 136
AddIsHomSetInhabited	AddIsomorphismFromCokernelOfKernelTo-
for IsCapCategory, IsFunction, 131	Coimage
for IsCapCategory, IsFunction, IsInt, 131	for IsCapCategory, IsFunction, 137
AddIsIdempotent	for IsCapCategory, IsFunction, IsInt, 137
for IsCapCategory, IsFunction, 131	AddIsomorphismFromCoproductToDirectSum
for IsCapCategory, IsFunction, IsInt, 131	for IsCapCategory, IsFunction, 137
AddIsInitial	for IsCapCategory, IsFunction, IsInt, 137
for IsCapCategory, IsFunction, 132	AddIsomorphismFromDirectProductTo-
for IsCapCategory, IsFunction, IsInt, 132	DirectSum
AddIsInjective	for IsCapCategory, IsFunction, 137
for IsCapCategory, IsFunction, 132	for IsCapCategory, IsFunction, IsInt, 137
for IsCapCategory, IsFunction, IsInt, 132	AddIsomorphismFromDirectSumToCoproduct
AddIsIsomorphicForObjects	for IsCapCategory, IsFunction, 137
for IsCapCategory, IsFunction, 132	for IsCapCategory, IsFunction, IsInt, 137
for IsCapCategory, IsFunction, IsInt, 132	AddIsomorphismFromDirectSumToDirect-
AddIsIsomorphism	Product
for IsCapCategory, IsFunction, 132	for IsCapCategory, IsFunction, 138
for IsCapCategory, IsFunction, IsInt, 132	for IsCapCategory, IsFunction, IsInt, 138
AddIsLiftable	AddIsomorphismFromEqualizerOfDirect-
for IsCapCategory, IsFunction, 132	ProductDiagramToFiberProduct
for IsCapCategory, IsFunction, IsInt, 132	for IsCapCategory, IsFunction, 138
AddIsLiftableAlongMonomorphism	for IsCapCategory, IsFunction, IsInt, 138
for IsCapCategory, IsFunction, 133	AddIsomorphismFromEqualizerToKernel-
for IsCapCategory, IsFunction, IsInt, 133	OfJointPairwiseDifferencesOf-
AddIsMonomorphism	${ t MorphismsIntoDirectProduct}$
for IsCapCategory, IsFunction, 133	for IsCapCategory, IsFunction, 138
for IsCapCategory, IsFunction, IsInt, 133	for IsCapCategory, IsFunction, IsInt, 138
AddIsomorphismFromCoequalizerOf-	AddIsomorphismFromFiberProductTo-
CoproductDiagramToPushout	EqualizerOfDirectProductDiagram
for IsCapCategory, IsFunction, 135	for IsCapCategory, IsFunction, 139
for IsCapCategory, IsFunction, IsInt, 135	for IsCapCategory, IsFunction, IsInt, 139
AddIsomorphismFromCoequalizerTo-	AddIsomorphismFromHomologyObjectToIts-
1	<u>.</u>

${\tt ConstructionAsAnImageObject}$	AddIsSplitEpimorphism
for IsCapCategory, IsFunction, 139	for IsCapCategory, IsFunction, 133
for IsCapCategory, IsFunction, IsInt, 139	for IsCapCategory, IsFunction, IsInt, 133
AddIsomorphismFromImageObjectToKernel-	AddIsSplitMonomorphism
OfCokernel	for IsCapCategory, IsFunction, 134
for IsCapCategory, IsFunction, 139	for IsCapCategory, IsFunction, IsInt, 134
for IsCapCategory, IsFunction, IsInt, 139	AddIsTerminal
AddIsomorphismFromInitialObjectToZero-	for IsCapCategory, IsFunction, 134
Object	for IsCapCategory, IsFunction, IsInt, 134
for IsCapCategory, IsFunction, 139	AddIsWellDefinedForMorphisms
for IsCapCategory, IsFunction, IsInt, 139	for IsCapCategory, IsFunction, 134
AddIsomorphismFromItsConstructionAsAn-	for IsCapCategory, IsFunction, IsInt, 134
ImageObjectToHomologyObject	AddIsWellDefinedForMorphismsWithGiven-
for IsCapCategory, IsFunction, 140	SourceAndRange
for IsCapCategory, IsFunction, IsInt, 140	for IsCapCategory, IsFunction, 134
AddIsomorphismFromKernelOfCokernelTo-	for IsCapCategory, IsFunction, IsInt, 134
ImageObject	AddIsWellDefinedForObjects
for IsCapCategory, IsFunction, 140	for IsCapCategory, IsFunction, 135
for IsCapCategory, IsFunction, IsInt, 140	for IsCapCategory, IsFunction, IsInt, 135
AddIsomorphismFromKernelOfJoint-	AddIsWellDefinedForTwoCells
PairwiseDifferencesOfMorphisms-	for IsCapCategory, IsFunction, 135
IntoDirectProductToEqualizer	for IsCapCategory, IsFunction, IsInt, 135
for IsCapCategory, IsFunction, 140	AddIsZeroForMorphisms
for IsCapCategory, IsFunction, IsInt, 140	for IsCapCategory, IsFunction, 135
AddIsomorphismFromPushoutTo-	for IsCapCategory, IsFunction, IsInt, 135
CoequalizerOfCoproductDiagram	AddIsZeroForObjects
for IsCapCategory, IsFunction, 141	for IsCapCategory, IsFunction, 135
for IsCapCategory, IsFunction, IsInt, 141	for IsCapCategory, IsFunction, IsInt, 135
AddIsomorphismFromTerminalObjectTo-	AdditionalWeight
ZeroObject	for IsDerivedMethod, 175
for IsCapCategory, IsFunction, 141	AdditionForMorphisms
for IsCapCategory, IsFunction, IsInt, 141	for IsCapCategoryMorphism, IsCapCatego
AddIsomorphismFromZeroObjectToInitial-	ryMorphism, 34
Object	AdditiveGenerators
for IsCapCategory, IsFunction, 141	for IsCapCategory, 12
for IsCapCategory, IsFunction, IsInt, 141	AdditiveInverseForMorphisms
AddIsomorphismFromZeroObjectTo-	for IsCapCategoryMorphism, 35
TerminalObject	AddJointPairwiseDifferencesOf-
for IsCapCategory, IsFunction, 141	MorphismsFromCoproduct
for IsCapCategory, IsFunction, IsInt, 141	for IsCapCategory, IsFunction, 142
AddIsOne	for IsCapCategory, IsFunction, IsInt, 142
for IsCapCategory, IsFunction, 133	AddJointPairwiseDifferencesOf-
for IsCapCategory, IsFunction, IsInt, 133	MorphismsIntoDirectProduct
AddIsProjective	for IsCapCategory, IsFunction, 142
for IsCapCategory, IsFunction, 133	for IsCapCategory, IsFunction, IsInt, 142
for IsCapCategory, IsFunction, IsInt, 133	AddKernelEmbedding
- · ·	<u> </u>

for IsCapCategory, IsFunction, 142	for IsCapCategory, IsFunction, IsInt, 145
for IsCapCategory, IsFunction, IsInt, 142	AddMonomorphismIntoSomeInjective-
AddKernelEmbeddingWithGivenKernel-	ObjectWithGivenSomeInjective-
Object	Object
for IsCapCategory, IsFunction, 142	for IsCapCategory, IsFunction, 146
for IsCapCategory, IsFunction, IsInt, 142	for IsCapCategory, IsFunction, IsInt, 146
AddKernelLift	AddMorphism
for IsCapCategory, IsFunction, 143	for IsCapCategory, IsAttributeStoringRep,
for IsCapCategory, IsFunction, IsInt, 143	28
AddKernelLiftWithGivenKernelObject	AddMorphismBetweenDirectSums
for IsCapCategory, IsFunction, 143	for IsCapCategory, IsFunction, 146
for IsCapCategory, IsFunction, IsInt, 143	for IsCapCategory, IsFunction, IsInt, 146
AddKernelObject	AddMorphismBetweenDirectSumsWithGiven-
for IsCapCategory, IsFunction, 143	DirectSums
for IsCapCategory, IsFunction, IsInt, 143	for IsCapCategory, IsFunction, 146
AddKernelObjectFunctorial	for IsCapCategory, IsFunction, IsInt, 146
for IsCapCategory, IsFunction, 143	AddMorphismConstructor
for IsCapCategory, IsFunction, IsInt, 143	for IsCapCategory, IsFunction, 146
AddKernelObjectFunctorialWithGiven-	for IsCapCategory, IsFunction, IsInt, 146
KernelObjects	AddMorphismDatum
for IsCapCategory, IsFunction, 143	for IsCapCategory, IsFunction, 147
for IsCapCategory, IsFunction, IsInt, 143	for IsCapCategory, IsFunction, IsInt, 147
AddLift	AddMorphismFromCoimageToImage
for IsCapCategory, IsFunction, 144	for IsCapCategory, IsFunction, 147
for IsCapCategory, IsFunction, IsInt, 144	for IsCapCategory, IsFunction, IsInt, 147
AddLiftAlongMonomorphism	AddMorphismFromCoimageToImageWith-
for IsCapCategory, IsFunction, 144	GivenObjects
	g .
for IsCapCategory, IsFunction, IsInt, 144	for IsCapCategory, IsFunction, 147
AddLinearCombinationOfMorphisms	for IsCapCategory, IsFunction, IsInt, 147 AddMorphismFromEqualizerToSink
for IsCapCategory, IsFunction, 144	for IsCapCategory, IsFunction, 147
for IsCapCategory, IsFunction, IsInt, 144	
AddMereExistenceOfSolutionOfLinear-	for IsCapCategory, IsFunction, IsInt, 147
SystemInAbCategory	AddMorphismFromEqualizerToSinkWith-
for IsCapCategory, IsFunction, 144	GivenEqualizer
for IsCapCategory, IsFunction, IsInt, 144	for IsCapCategory, IsFunction, 148
AddMonomorphismIntoInjectiveEnvelope-	for IsCapCategory, IsFunction, IsInt, 148
Object	AddMorphismFromFiberProductToSink
for IsCapCategory, IsFunction, 145	for IsCapCategory, IsFunction, 148
for IsCapCategory, IsFunction, IsInt, 145	for IsCapCategory, IsFunction, IsInt, 148
AddMonomorphismIntoInjectiveEnvelope-	AddMorphismFromFiberProductToSinkWith-
ObjectWithGivenInjective-	GivenFiberProduct
EnvelopeObject	for IsCapCategory, IsFunction, 148
for IsCapCategory, IsFunction, 145	for IsCapCategory, IsFunction, IsInt, 148
for IsCapCategory, IsFunction, IsInt, 145	AddMorphismFromKernelObjectToSink
AddMonomorphismIntoSomeInjectiveObject	for IsCapCategory, IsFunction, 148
for IsCapCategory, IsFunction, 145	for IsCapCategory, IsFunction, IsInt, 148

AddMorphismFromKernelObjectToSinkWith-	AddObjectFunction
GivenKernelObject	for IsCapFunctor, IsFunction, 57
for IsCapCategory, IsFunction, 149	AddOperationsToDerivationGraph
for IsCapCategory, IsFunction, IsInt, 149	for IsDerivedMethodGraph, IsDenseList,
AddMorphismFromSourceToCoequalizer	176
for IsCapCategory, IsFunction, 149	AddPostCompose
for IsCapCategory, IsFunction, IsInt, 149	for IsCapCategory, IsFunction, 151
AddMorphismFromSourceToCoequalizer-	for IsCapCategory, IsFunction, IsInt, 151
WithGivenCoequalizer	AddPostComposeList
for IsCapCategory, IsFunction, 149	for IsCapCategory, IsFunction, 151
for IsCapCategory, IsFunction, IsInt, 149	for IsCapCategory, IsFunction, IsInt, 151
AddMorphismFromSourceToCokernelObject	AddPostInverseForMorphisms
for IsCapCategory, IsFunction, 149	for IsCapCategory, IsFunction, 152
for IsCapCategory, IsFunction, IsInt, 149	for IsCapCategory, IsFunction, IsInt, 152
AddMorphismFromSourceToCokernelObject-	AddPreCompose
WithGivenCokernelObject	for IsCapCategory, IsFunction, 152
for IsCapCategory, IsFunction, 150	for IsCapCategory, IsFunction, IsInt, 152
for IsCapCategory, IsFunction, IsInt, 150	AddPreComposeList
AddMorphismFromSourceToPushout	for IsCapCategory, IsFunction, 152
for IsCapCategory, IsFunction, 150	for IsCapCategory, IsFunction, IsInt, 152
for IsCapCategory, IsFunction, IsInt, 150	AddPreInverseForMorphisms
AddMorphismFromSourceToPushoutWith-	for IsCapCategory, IsFunction, 152
GivenPushout	for IsCapCategory, IsFunction, IsInt, 152
for IsCapCategory, IsFunction, 150	AddPrimitiveOperation
for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150	AddPrimitiveOperation for IsOperationWeightList, IsString, IsInt,
for IsCapCategory, IsFunction, IsInt, 150	AddPrimitiveOperation for IsOperationWeightList, IsString, IsInt, 179
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction	for IsOperationWeightList, IsString, IsInt, 179
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative-	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct- WithGivenDirectProduct
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative-	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct- WithGivenDirectProduct
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction,	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60 AddObject	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60 AddObject for IsCapCategory, IsAttributeStoringRep, 19	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60 AddObject for IsCapCategory, IsAttributeStoringRep,	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum for IsCapCategory, IsFunction, 153
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60 AddObject for IsCapCategory, IsAttributeStoringRep, 19 AddObjectConstructor	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 AddProjectionInFactorOfFiberProduct
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60 AddObject for IsCapCategory, IsAttributeStoringRep, 19 AddObjectConstructor for IsCapCategory, IsFunction, 151	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 AddProjectionInFactorOfFiberProduct for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfFiberProduct for IsCapCategory, IsFunction, 154
for IsCapCategory, IsFunction, IsInt, 150 AddMorphismFunction for IsCapFunctor, IsFunction, 57 AddMorphismsOfExternalHom for IsCapCategory, IsFunction, 150 for IsCapCategory, IsFunction, IsInt, 150 AddMultiplyWithElementOfCommutative- RingForMorphisms for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151 AddNaturalTransformationFunction for IsCapNaturalTransformation, IsFunction, 60 AddObject for IsCapCategory, IsAttributeStoringRep, 19 AddObjectConstructor for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, 151 for IsCapCategory, IsFunction, IsInt, 151	for IsOperationWeightList, IsString, IsInt, 179 AddProjectionInFactorOfDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectProduct WithGivenDirectProduct for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfDirectSumWith- GivenDirectSum for IsCapCategory, IsFunction, 153 for IsCapCategory, IsFunction, 153 AddProjectionInFactorOfFiberProduct for IsCapCategory, IsFunction, IsInt, 153 AddProjectionInFactorOfFiberProduct for IsCapCategory, IsFunction, 154 for IsCapCategory, IsFunction, IsInt, 154

for IsCapCategory, IsFunction, IsInt, 154	for IsCapCategory, IsFunction, IsInt, 157
AddProjectionOntoCoequalizer	AddRandomMorphismWithFixedSourceBy-
for IsCapCategory, IsFunction, 154	Integer
for IsCapCategory, IsFunction, IsInt, 154	for IsCapCategory, IsFunction, 157
AddProjectionOntoCoequalizerWithGiven-	for IsCapCategory, IsFunction, IsInt, 157
Coequalizer	AddRandomMorphismWithFixedSourceByList
for IsCapCategory, IsFunction, 154	for IsCapCategory, IsFunction, 158
for IsCapCategory, IsFunction, IsInt, 154	for IsCapCategory, IsFunction, IsInt, 158
AddProjectiveCoverObject	AddRandomObjectByInteger
for IsCapCategory, IsFunction, 155	for IsCapCategory, IsFunction, 158
for IsCapCategory, IsFunction, IsInt, 155	for IsCapCategory, IsFunction, IsInt, 158
AddProjectiveDimension	AddRandomObjectByList
for IsCapCategory, IsFunction, 155	for IsCapCategory, IsFunction, 158
for IsCapCategory, IsFunction, IsInt, 155	for IsCapCategory, IsFunction, IsInt, 158
AddProjectiveLift	AddSimplifyEndo
for IsCapCategory, IsFunction, 155	for IsCapCategory, IsFunction, 158
for IsCapCategory, IsFunction, IsInt, 155	for IsCapCategory, IsFunction, IsInt, 158
AddPushout	AddSimplifyEndo_IsoFromInputObject
for IsCapCategory, IsFunction, 155	for IsCapCategory, IsFunction, 158
for IsCapCategory, IsFunction, IsInt, 155	for IsCapCategory, IsFunction, IsInt, 158
AddPushoutFunctorial	AddSimplifyEndo_IsoToInputObject
for IsCapCategory, IsFunction, 155	for IsCapCategory, IsFunction, 159
for IsCapCategory, IsFunction, IsInt, 155	for IsCapCategory, IsFunction, IsInt, 159
AddPushoutFunctorialWithGivenPushouts	AddSimplifyMorphism
	for IsCapCategory, IsFunction, 159
for IsCapCategory, IsFunction, 156 for IsCapCategory, IsFunction, IsInt, 156	for IsCapCategory, IsFunction, IsInt, 159
	AddSimplifyObject
AddRandomMorphismByInteger	
for IsCapCategory, IsFunction, 156	for IsCapCategory, IsFunction, 159
for IsCapCategory, IsFunction, IsInt, 156	for IsCapCategory, IsFunction, IsInt, 159
AddRandomMorphismByList	AddSimplifyObject_IsoFromInputObject
for IsCapCategory, IsFunction, 156	for IsCapCategory, IsFunction, 159
for IsCapCategory, IsFunction, IsInt, 156	for IsCapCategory, IsFunction, IsInt, 159
AddRandomMorphismWithFixedRangeBy-	AddSimplifyObject_IsoToInputObject
Integer	for IsCapCategory, IsFunction, 160
for IsCapCategory, IsFunction, 156	for IsCapCategory, IsFunction, IsInt, 160
for IsCapCategory, IsFunction, IsInt, 156	AddSimplifyRange
AddRandomMorphismWithFixedRangeByList	for IsCapCategory, IsFunction, 160
for IsCapCategory, IsFunction, 157	for IsCapCategory, IsFunction, IsInt, 160
for IsCapCategory, IsFunction, IsInt, 157	AddSimplifyRange_IsoFromInputObject
AddRandomMorphismWithFixedSourceAnd-	for IsCapCategory, IsFunction, 160
RangeByInteger	for IsCapCategory, IsFunction, IsInt, 160
for IsCapCategory, IsFunction, 157	${\tt AddSimplifyRange_IsoToInputObject}$
for IsCapCategory, IsFunction, IsInt, 157	for IsCapCategory, IsFunction, 160
${\tt AddRandomMorphismWithFixedSourceAnd-}$	for IsCapCategory, IsFunction, IsInt, 160
${ t RangeByList}$	
for IsCapCategory, IsFunction, 157	AddSimplifySource for IsCapCategory, IsFunction, 160

for IsCapCategory, IsFunction, IsInt, 160	${\tt MorphismToInputRange}$
AddSimplifySourceAndRange	for IsCapCategory, IsFunction, 164
for IsCapCategory, IsFunction, 161	for IsCapCategory, IsFunction, IsInt, 164
for IsCapCategory, IsFunction, IsInt, 161	AddSubtractionForMorphisms
AddSimplifySourceAndRange_IsoFrom-	for IsCapCategory, IsFunction, 164
InputRange	for IsCapCategory, IsFunction, IsInt, 164
for IsCapCategory, IsFunction, 161	AddSumOfMorphisms
for IsCapCategory, IsFunction, IsInt, 161	for IsCapCategory, IsFunction, 164
AddSimplifySourceAndRange_IsoFrom-	for IsCapCategory, IsFunction, IsInt, 164
InputSource	AddTerminalObject
for IsCapCategory, IsFunction, 161	for IsCapCategory, IsFunction, 164
for IsCapCategory, IsFunction, IsInt, 161	for IsCapCategory, IsFunction, IsInt, 164
AddSimplifySourceAndRange_IsoToInput-	AddTerminalObjectFunctorial
Range	for IsCapCategory, IsFunction, 165
for IsCapCategory, IsFunction, 161	for IsCapCategory, IsFunction, IsInt, 165
for IsCapCategory, IsFunction, IsInt, 161	AddTerminalObjectFunctorialWithGiven-
AddSimplifySourceAndRange_IsoToInput-	TerminalObjects
Source	for IsCapCategory, IsFunction, 165
for IsCapCategory, IsFunction, 162	for IsCapCategory, IsFunction, IsInt, 165
for IsCapCategory, IsFunction, IsInt, 162	AddTwoCell
AddSimplifySource_IsoFromInputObject	for IsCapCategory, IsAttributeStoringRep,
for IsCapCategory, IsFunction, 162	52
for IsCapCategory, IsFunction, IsInt, 162	AddUniversalMorphismFromCoequalizer
AddSimplifySource_IsoToInputObject	for IsCapCategory, IsFunction, 165
	for IsCapCategory, IsFunction, IsInt, 165
for IsCapCategory, IsFunction, 162	- · ·
for IsCapCategory, IsFunction, IsInt, 162 AddSolveLinearSystemInAbCategory	AddUniversalMorphismFromCoequalizer-
	WithGivenCoequalizer
for IsCapCategory, IsFunction, 162	for IsCapCategory, IsFunction, 165
for IsCapCategory, IsFunction, IsInt, 162	for IsCapCategory, IsFunction, IsInt, 165
AddSomeInjectiveObject	AddUniversalMorphismFromCoproduct
for IsCapCategory, IsFunction, 163	for IsCapCategory, IsFunction, 166
for IsCapCategory, IsFunction, IsInt, 163	for IsCapCategory, IsFunction, IsInt, 166
AddSomeIsomorphismBetweenObjects	AddUniversalMorphismFromCoproductWith-
for IsCapCategory, IsFunction, 163	GivenCoproduct
for IsCapCategory, IsFunction, IsInt, 163	for IsCapCategory, IsFunction, 166
AddSomeProjectiveObject	for IsCapCategory, IsFunction, IsInt, 166
for IsCapCategory, IsFunction, 163	AddUniversalMorphismFromDirectSum
for IsCapCategory, IsFunction, IsInt, 163	for IsCapCategory, IsFunction, 166
AddSomeReductionBySplitEpiSummand	for IsCapCategory, IsFunction, IsInt, 166
for IsCapCategory, IsFunction, 163	AddUniversalMorphismFromDirectSumWith-
for IsCapCategory, IsFunction, IsInt, 163	${\tt GivenDirectSum}$
AddSomeReductionBySplitEpiSummand	for IsCapCategory, IsFunction, 166
${\tt MorphismFromInputRange}$	for IsCapCategory, IsFunction, IsInt, 166
for IsCapCategory, IsFunction, 163	${\tt AddUniversalMorphismFromImage}$
for IsCapCategory, IsFunction, IsInt, 163	for IsCapCategory, IsFunction, 167
AddSomeReductionBySplitEpiSummand	for IsCapCategory, IsFunction, IsInt, 167

AddUniversalMorphismFromImageWith-	${\tt AddUniversalMorphismIntoEqualizer}$
${ t Given Image Object}$	for IsCapCategory, IsFunction, 170
for IsCapCategory, IsFunction, 167	for IsCapCategory, IsFunction, IsInt, 170
for IsCapCategory, IsFunction, IsInt, 167	AddUniversalMorphismIntoEqualizerWith-
AddUniversalMorphismFromInitialObject	GivenEqualizer
for IsCapCategory, IsFunction, 167	for IsCapCategory, IsFunction, 170
for IsCapCategory, IsFunction, IsInt, 167	for IsCapCategory, IsFunction, IsInt, 170
AddUniversalMorphismFromInitialObject-	AddUniversalMorphismIntoFiberProduct
WithGivenInitialObject	for IsCapCategory, IsFunction, 171
for IsCapCategory, IsFunction, 167	for IsCapCategory, IsFunction, IsInt, 171
for IsCapCategory, IsFunction, IsInt, 167	AddUniversalMorphismIntoFiberProduct-
AddUniversalMorphismFromPushout	WithGivenFiberProduct
for IsCapCategory, IsFunction, 168	for IsCapCategory, IsFunction, 171
for IsCapCategory, IsFunction, IsInt, 168	for IsCapCategory, IsFunction, IsInt, 171
AddUniversalMorphismFromPushoutWith-	AddUniversalMorphismIntoTerminalObject
GivenPushout	for IsCapCategory, IsFunction, 171
for IsCapCategory, IsFunction, 168	for IsCapCategory, IsFunction, IsInt, 171
for IsCapCategory, IsFunction, IsInt, 168	AddUniversalMorphismIntoTerminal-
AddUniversalMorphismFromZeroObject	ObjectWithGivenTerminalObject
for IsCapCategory, IsFunction, 168	for IsCapCategory, IsFunction, 171
for IsCapCategory, IsFunction, IsInt, 168	for IsCapCategory, IsFunction, IsInt, 171
AddUniversalMorphismFromZeroObject-	AddUniversalMorphismIntoZeroObject
WithGivenZeroObject	for IsCapCategory, IsFunction, 172
for IsCapCategory, IsFunction, 168	for IsCapCategory, IsFunction, IsInt, 172
for IsCapCategory, IsFunction, IsInt, 168	AddUniversalMorphismIntoZeroObject-
AddUniversalMorphismIntoCoimage	WithGivenZeroObject
for IsCapCategory, IsFunction, 169	for IsCapCategory, IsFunction, 172
for IsCapCategory, IsFunction, IsInt, 169	for IsCapCategory, IsFunction, IsInt, 172
AddUniversalMorphismIntoCoimageWith-	AddVerticalPostCompose
GivenCoimageObject	for IsCapCategory, IsFunction, 172
for IsCapCategory, IsFunction, 169	for IsCapCategory, IsFunction, IsInt, 172
for IsCapCategory, IsFunction, IsInt, 169	AddVerticalPreCompose
AddUniversalMorphismIntoDirectProduct	for IsCapCategory, IsFunction, 172
for IsCapCategory, IsFunction, 169	for IsCapCategory, IsFunction, IsInt, 172
for IsCapCategory, IsFunction, IsInt, 169	AddZeroMorphism
AddUniversalMorphismIntoDirectProduct-	for IsCapCategory, IsFunction, 173
WithGivenDirectProduct	for IsCapCategory, IsFunction, IsInt, 173
for IsCapCategory, IsFunction, 169	AddZeroObject
for IsCapCategory, IsFunction, IsInt, 169	for IsCapCategory, IsFunction, 173
AddUniversalMorphismIntoDirectSum	for IsCapCategory, IsFunction, IsInt, 173
for IsCapCategory, IsFunction, 170	AddZeroObjectFunctorial
for IsCapCategory, IsFunction, IsInt, 170	for IsCapCategory, IsFunction, 173
AddUniversalMorphismIntoDirectSumWith-	for IsCapCategory, IsFunction, IsInt, 173
GivenDirectSum	AddZeroObjectFunctorialWithGivenZero-
for IsCapCategory, IsFunction, 170	Objects
for IsCapCategory, IsFunction, 170	for IsCapCategory, IsFunction, 173
101 15Capcategory, 1st unction, 1still, 1/0	101 15Capcategory, 15Function, 1/3

for IsCapCategory, IsFunction, IsInt, 173	for IsCapCategoryMorphism, 27
ApplyFunctor, 58	for IsCapCategoryObject, 19
ApplyNaturalTransformation, 60	CapCategorySwitchLogicOff, 14
AsCapCategory	CapCategorySwitchLogicOn, 14
for IsCapCategoryAsCatObject, 56	CapCategorySwitchLogicPropagationFor-
AsCapCategoryMorphism, 28	MorphismsOff, 13
AsCapCategoryObject, 20	CapCategorySwitchLogicPropagationFor-
AsCatObject	MorphismsOn, 13
for IsCapCategory, 56	CapCategorySwitchLogicPropagationFor-
AsHomalgMatrix	ObjectsOff, 13
for IsCapCategoryMorphism, 28	CapCategorySwitchLogicPropagationFor-
for IsCapCategoryObject, 20	ObjectsOn, 13
AsInteger	CapCategorySwitchLogicPropagationOff,
for IsCapCategoryMorphism, 28	14
for IsCapCategoryObject, 20	CapCategorySwitchLogicPropagationOn, 13
AsMorphismInWrapperCategory	CapFixpoint, 186
for IsWrapperCapCategory, IsCapCategory-	CapFunctor
Morphism, 203	for IsString, IsCapCategory, IsCapCategory
for IsWrapperCapCategoryObject, IsCap-	56
CategoryMorphism, IsWrapperCapCat-	for IsString, IsCapCategory, IsCapCategory
egoryObject, 203	ryAsCatObject, 56
AsObjectInWrapperCategory	for IsString, IsCapCategoryAsCatObject, Is
for IsWrapperCapCategory, IsCapCategory-	CapCategory, 56
Object, 203	for IsString, IsCapCategoryAsCatObject, Is-
AsPrimitiveValue	CapCategoryAsCatObject, 56
for IsCapCategoryMorphism, 28	for IsString, IsList, IsCapCategory, 56
for IsCapCategoryObject, 20	for IsString, IsList, IsCapCategoryAsCatOb
AstrictionToCoimage	ject, 56
for IsCapCategoryMorphism, 97	CapJitAddKnownMethod, 184
AstrictionToCoimageWithGivenCoimage-	CapJitAddTypeSignature, 184
Object	CapJitDataTypeOfCategory, 185
for IsCapCategoryMorphism, IsCapCatego-	CapJitDataTypeOfElementOfRing, 185
ryObject, 97	CapJitDataTypeOfListOf, 185
	CapJitDataTypeOfMorphismOfCategory, 185
BasisOfExternalHom	CapJitDataTypeOfNTupleOf, 185
for IsCapCategoryObject, IsCapCategory-	CapJitDataTypeOfObjectOfCategory, 185
Object, 46	CapJitDataTypeOfRing, 185
BrowseCachingStatistic, 183	CapJitDataTypeOfTwoCellOfCategory, 185
BrowseTimingStatistics, 16	CapJitTypedExpression, 185
CachingStatistic, 183	CAPOperationPrepareFunction, 106
CanCompute	CAP_INTERNAL_ASSERT_IS_CELL_OF_CATE-
-	GORY, 182
for IsCapCategory, IsFunction, 14 for IsCapCategory, IsString, 14	CAP_INTERNAL_ASSERT_IS_MORPHISM_OF_CA-
CAPAddPrepareFunction, 106	TEGORY, 182
-	CAP_INTERNAL_ASSERT_IS_OBJECT_OF_CATE-
CapCategory	GORY, 182
VIIIVIII GRUI V	

CAP_INTERNAL_ASSERT_IS_TWO_CELL_OF_CA-	Coequalizers
TEGORY, 183	for IsCapCategoryObject, IsList, IsCapCat-
CAP_INTERNAL_ASSERT_VALUE_IS_OF_TYPE	egoryMorphism, IsList, IsCapCategory-
GETTER, 182	Object, 85
CAP_INTERNAL_CONSTRUCTOR_FOR_TERMINA-	CoequalizerOp
L_CATEGORY, 218	for IsCapCategoryObject, IsList, 84
CAP_INTERNAL_FIND_APPEARANCE_OF_SYMBO-	CoimageObject
L_IN_FUNCTION, 181	for IsCapCategoryMorphism, 96
CAP_INTERNAL_GENERATE_CONVENIENCE_MET-	CoimageObjectFunctorial
HODS_FOR_LIMITS, 193	for IsCapCategoryMorphism, IsCapCatego-
CAP_INTERNAL_GET_DATA_TYPES_FROM_STR-INGS, 181	ryMorphism, IsCapCategoryMorphism, 97
CAP_INTERNAL_GET_DATA_TYPE_FROM_ST-	CoimageObjectFunctorialWithGiven-
RING, 181	CoimageObjects
CAP_INTERNAL_MERGE_PRECONDITIONS_LIST,	for IsCapCategoryObject, IsCapCategory-
182	Morphism, IsCapCategoryMorphism,
CAP_INTERNAL_REPLACED_STRINGS_WITH_FI-	IsCapCategoryMorphism, IsCapCatego-
LTERS, 181	ryObject, 98
CAP_INTERNAL_REPLACED_STRING_WITH_FI-	CoimageProjection
LTER, 181	for IsCapCategoryMorphism, 96
CAP_INTERNAL_RETURN_OPTION_OR_DEFAULT,	CoimageProjectionWithGivenCoimage-
181	Object
CAP_INTERNAL_VALIDATE_LIMITS_IN_NAME	for IsCapCategoryMorphism, IsCapCatego-
RECORD, 193	ryObject, 96
CAP_JIT_EXPR_CASE_WRAPPER, 188	CokernelColift
CAP_JIT_INCOMPLETE_LOGIC, 188	for IsCapCategoryMorphism, IsCapCatego-
CategoryConstructor	ryObject, IsCapCategoryMorphism, 65
for IsRecord, 194	${\tt CokernelColiftWithGivenCokernelObject}$
CategoryFilter	for IsCapCategoryMorphism, IsCapCatego-
for IsCapCategory, 11	ryObject, IsCapCategoryMorphism, Is-
for IsDerivedMethod, 175	CapCategoryObject, 65
CategoryOfOperationWeightList	CokernelObject
for IsOperationWeightList, 178	for IsCapCategoryMorphism, 64
CoastrictionToImage	CokernelObjectFunctorial
for IsCapCategoryMorphism, 94	for IsCapCategoryMorphism, IsCapCatego-
${\tt CoastrictionToImageWithGivenImage-}$	ryMorphism, IsCapCategoryMorphism,
Object	65
for IsCapCategoryMorphism, IsCapCatego-	for IsList, 65
ryObject, 94	CokernelObjectFunctorialWithGiven-
CoefficientsOfMorphism	CokernelObjects
for IsCapCategoryMorphism, 46	for IsCapCategoryObject, IsCapCatego-
Coequalizer, 84	ryMorphism, IsCapCategoryMor-
CoequalizerFunctorial	phism,IsCapCategoryMorphism,
for IsList, IsCapCategoryMorphism, IsList,	IsCapCategoryMorphism, IsCap-
85	CategoryObject, 66
CoequalizerFunctorialWithGiven-	for IsCapCategoryObject, IsCapCatego-

ryMorphism, IsCapCategoryMor-	19
phism,IsCapCategoryMorphism, IsCap-	CreateCapCategoryTwoCellWith-
CategoryObject, 66	Attributes, 53
CokernelProjection	CreateCapCategoryWithDataTypes, 11
for IsCapCategoryMorphism, 64	CreateDerivation, 174
CokernelProjectionWithGivenCokernel-	CreateGapObjectWithAttributes, 190
Object	CurrentOperationWeight
for IsCapCategoryMorphism, IsCapCategoryObject, 64	for IsOperationWeightList, IsString, 178
Colift	DeactivateCachingOfCategory, 16
for IsCapCategoryMorphism, IsCapCatego-	DeactivateDefaultCaching, 16
ryMorphism, 40	DeactivateDerivationInfo, 174
ColiftAlongEpimorphism	DerivationFunction
for IsCapCategoryMorphism, IsCapCatego-	for IsDerivedMethod, 175
ryMorphism, 39	DerivationGraph
ColiftOrFail	for IsOperationWeightList, 178
for IsCapCategoryMorphism, IsCapCatego-	DerivationInfo, 174
ryMorphism, 40	${\tt DerivationOfOperation}$
CommutativeRingOfLinearCategory	for IsOperationWeightList, IsString, 178
for IsCapCategory, 12	${ t Derivations Of Operation}$
ComponentOfMorphismFromCoproduct	for IsDerivedMethodGraph, IsString, 177
for IsCapCategoryMorphism, IsList, IsInt, 77	${ t Derivations Using Operation}$
ComponentOfMorphismFromDirectSum	for IsDerivedMethodGraph, IsString, 177
for IsCapCategoryMorphism, IsList, IsInt, 75	Description
ComponentOfMorphismIntoDirectProduct	for IsDerivedMethod, 175
for IsCapCategoryMorphism, IsList, IsInt, 80	DirectProduct, 78
ComponentOfMorphismIntoDirectSum	DirectProductFunctorial
for IsCapCategoryMorphism, IsList, IsInt, 75	for IsList, IsList, 79
Coproduct	DirectProductFunctorialWithGiven-
for IsCapCategoryObject, IsCapCategory-	DirectProducts
Object, 76	for IsCapCategoryObject, IsList, IsList, Is
for IsCapCategoryObject, IsCapCategory-	List, IsCapCategoryObject, 79
Object, IsCapCategoryObject, 76	DirectProductOp
for IsList, 76	for IsList, 78
CoproductFunctorial	DirectSum, 71
for IsList, IsList, IsList, 77	DirectSumFunctorial
CoproductFunctorialWithGivenCoproducts	for IsList, IsList, IsList, 75
for IsCapCategoryObject, IsList, IsList, Is-	DirectSumFunctorialWithGivenDirectSums
List, IsCapCategoryObject, 77	for IsCapCategoryObject, IsList, IsList, Is
CreateCapCategory, 10	List, IsCapCategoryObject, 75
for IsString, 10	DirectSumOp
for IsString, IsFunction, IsFunction, IsFunc-	for IsList, 72
tion, IsFunction, 10	DisableAddForCategoricalOperations, 17
CreateCapCategoryMorphismWith-	DisableInputSanityChecks, 16
Attributes, 28	DisableOutputSanityChecks, 16
CreateCapCategoryObjectWithAttributes,	DisableSanityChecks, 16
- · ·	DisableTimingStatistics, 16

DisplayTimingStatistics, 16	for IsCapCategoryObject, IsCapCategory-
DistinguishedObjectOfHomomorphism-	Object, 24
Structure	Equalizer, 80
for IsCapCategory, 43	EqualizerFunctorial
DistinguishedObjectOfHomomorphism-	for IsList, IsCapCategoryMorphism, IsList,
StructureExtendedByFull-	82
Embedding	EqualizerFunctorialWithGivenEqualizers
for IsCapCategory, IsCapCategory, 45	for IsCapCategoryObject, IsList, IsCapCat-
Down	egoryMorphism, IsList, IsCapCategory-
for IsObject, 15	Object, 82
DownOnlyMorphismData	EqualizerOp
for IsCapCategoryMorphism, 15	for IsCapCategoryObject, IsList, 81
DownToBottom	ExtendRangeOfHomomorphismStructureBy-
for IsObject, 15	FullEmbedding
DummyCategory	for IsCapCategory, IsCapCategory, IsFunc-
for IsRecord, 207	tion, IsFunction, IsFunction, IsFunction,
DummyCommutativeHomalgRing, 208	45
DummyCommutativeRing, 206	ExtendRangeOfHomomorphismStructureBy-
DummyField, 206	IdentityAsFullEmbedding
DummyHomalgField, 208	for IsCapCategory, 46
DummyHomalgRing, 208	1 2 3
DummyRing, 206	FiberProduct, 87
, 0,	${\tt FiberProductEmbeddingInDirectProduct}$
EmbeddingOfEqualizer	for IsList, 87
for IsCapCategoryObject, IsList, 81	${\tt FiberProductEmbeddingInDirectSum}$
EmbeddingOfEqualizerWithGivenEqualizer	for IsList, 87
for IsCapCategoryObject, IsList, IsCapCate-	FiberProductFunctorial
goryObject, 81	for IsList, IsList, 89
EnableAddForCategoricalOperations, 17	FiberProductFunctorialWithGivenFiber-
EnableFullInputSanityChecks, 16	Products
EnableFullOutputSanityChecks, 16	for IsCapCategoryObject, IsList, IsList, Is-
EnableFullSanityChecks, 16	List, IsCapCategoryObject, 89
EnablePartialInputSanityChecks, 16	FiberProductOp
EnablePartialOutputSanityChecks, 16	for IsList, 88
EnablePartialSanityChecks, 16	FilteredWithKeys, 189
EnableTimingStatistics, 16	FirstWithKeys, 189
EpimorphismFromProjectiveCoverObject	ForAllWithKeys, 189
for IsCapCategoryObject, 99	ForAnyWithKeys, 189
EpimorphismFromProjectiveCoverObject-	FunctionCalledBeforeInstallation
WithGivenProjectiveCoverObject	for IsDerivedMethod, 176
for IsCapCategoryObject, IsCapCategory-	FunctionWithNamedArguments, 180
Object, 99	FunctorCanonicalizeZeroMorphisms
EpimorphismFromSomeProjectiveObject	for IsCapCategory, 59
for IsCapCategoryObject, 24	FunctorCanonicalizeZeroObjects
EpimorphismFromSomeProjectiveObject-	for IsCapCategory, 59
WithGivenSomeProjectiveObject	FunctorFromTerminalCategory
	for IsCapCategoryObject, 219

FunctorMorphismUperation	for IsCapCategory, 45
for IsCapFunctor, 58	for IsCapCategoryMorphism, 44
FunctorObjectOperation	for IsCapCategoryMorphism, IsCapCatego-
for IsCapFunctor, 57	ryMorphism, 44
	for IsCapCategoryMorphism, IsCapCatego-
HandlePrecompiledTowers, 188	ryObject, 44
HomologyObject	for IsCapCategoryObject, IsCapCategory-
for IsCapCategoryMorphism, IsCapCatego-	Morphism, 44
ryMorphism, 98	for IsCapCategoryObject, IsCapCategory-
${\tt HomologyObjectFunctorial}$	Object, 44
for IsCapCategoryMorphism, IsCapCatego-	for IsCapCategoryObject, IsCapCategory-
ryMorphism, IsCapCategoryMorphism,	Object, IsCapCategoryMorphism, 45
IsCapCategoryMorphism, IsCapCatego-	HorizontalPostCompose
ryMorphism, 98	for IsCapCategoryTwoCell, IsCapCatego-
${\tt HomologyObjectFunctorialWithGiven-}$	ryTwoCell, 53
HomologyObjects	HorizontalPreCompose
for IsCapCategoryObject, IsList, IsCapCate-	for IsCapCategoryTwoCell, IsCapCatego-
goryObject, 98	ryTwoCell, 53
${\tt HomomorphismStructureOnMorphisms}$	HorizontalPreComposeFunctorWith-
for IsCapCategoryMorphism, IsCapCatego-	NaturalTransformation
ryMorphism, 42	for IsCapFunctor, IsCapNaturalTransforma-
HomomorphismStructureOnMorphisms-	tion, 60
${\tt ExtendedByFullEmbedding}$	HorizontalPreComposeNatural-
for IsCapCategory, IsCapCategory, IsCap-	$ ext{TransformationWithFunctor}$
CategoryMorphism, IsCapCategory-	for IsCapNaturalTransformation, IsCap-
Morphism, 45	Functor, 60
HomomorphismStructureOnMorphismsWith-	Tuneton, oo
GivenObjects	IdentityFunctor
for IsCapCategoryObject, IsCapCategory-	for IsCapCategory, 59
Morphism, IsCapCategoryMorphism,	IdentityMorphism
IsCapCategoryObject, 42	for IsCapCategoryObject, 37
HomomorphismStructureOnMorphismsWith-	IdentityTwoCell
GivenObjectsExtendedByFull-	for IsCapCategoryMorphism, 53
Embedding	ImageEmbedding
for IsCapCategory, IsCapCategory, Is-	for IsCapCategoryMorphism, 93
CapCategoryObject, IsCapCategory-	ImageEmbeddingWithGivenImageObject
Morphism, IsCapCategoryMorphism,	for IsCapCategoryMorphism, IsCapCatego-
IsCapCategoryObject, 45	ryObject, 93
HomomorphismStructureOnObjects	ImageObject
for IsCapCategoryObject, IsCapCategory-	for IsCapCategoryMorphism, 93
Object, 42	ImageObjectFunctorial
HomomorphismStructureOnObjects-	for IsCapCategoryMorphism, IsCapCatego-
ExtendedByFullEmbedding	ryMorphism, IsCapCategoryMorphism,
for IsCapCategory, IsCapCategory, IsCap-	94
CategoryObject, IsCapCategoryObject,	ImageObjectFunctorialWithGivenImage-
45	Objects
HomStructure	-

for IsCapCategoryObject, IsCapCategory-	InstallFunctor
Morphism, IsCapCategoryMorphism,	for IsCapFunctor, IsString, 58
IsCapCategoryMorphism, IsCapCatego-	InstallMethodForCompilerForCAP, 184
ryObject, 94	${\tt InstallNaturalTransformation}$
IndecomposableInjectiveObjects	for IsCapNaturalTransformation, IsString, 60
for IsCapCategory, 13	InstallOtherMethodForCompilerForCAP,
IndecomposableProjectiveObjects	184
for IsCapCategory, 12	InterpretMorphismAsMorphismFrom-
InfoCategoryConstructor, 194	DistinguishedObjectTo-
InitialObject	HomomorphismStructure
for IsCapCategory, 70	for IsCapCategoryMorphism, 43
for IsCapCategoryCell, 70	InterpretMorphismAsMorphismFrom-
InitialObjectFunctorial	DistinguishedObjectTo-
for IsCapCategory, 70	HomomorphismStructureExtended-
InitialObjectFunctorialWithGiven-	ByFullEmbedding
InitialObjects	for IsCapCategory, IsCapCategory, IsCap-
for IsCapCategoryObject, IsCapCategory-	CategoryMorphism, 45
Object, 70	InterpretMorphismAsMorphismFrom-
InjectionOfCofactorOfCoproduct	DistinguishedObjectTo-
for IsList, IsInt, 76	HomomorphismStructureWith-
InjectionOfCofactorOfCoproductWith-	GivenObjects
GivenCoproduct	for IsCapCategoryObject, IsCapCategory-
for IsList, IsInt, IsCapCategoryObject, 76	Morphism, IsCapCategoryObject, 43
InjectionOfCofactorOfDirectSum	InterpretMorphismAsMorphismFrom-
III) 00 01 0 II 0 0 I do 0 0 I DI I 0 0 0 D diii	
for IsList, IsInt, 72	DistinguishedObjectTo-
•	
for IsList, IsInt, 72	DistinguishedObjectTo-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor- phism, IsCapCategoryObject, 45
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91 InjectionOfCofactorOfPushoutWithGiven-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91 InjectionOfCofactorOfPushoutWithGiven- Pushout	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor- phism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91 InjectionOfCofactorOfPushoutWithGiven- Pushout for IsList, IsInt, IsCapCategoryObject, 91	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor- phism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91 InjectionOfCofactorOfPushoutWithGiven- Pushout for IsList, IsInt, IsCapCategoryObject, 91 InjectiveColift for IsCapCategoryMorphism, IsCapCatego-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor- phism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91 InjectionOfCofactorOfPushoutWithGiven- Pushout for IsList, IsInt, IsCapCategoryObject, 91 InjectiveColift for IsCapCategoryMorphism, IsCapCategoryMorphism, 25	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor- phism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphismExtendedByFull-
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith- GivenDirectSum for IsList, IsInt, IsCapCategoryObject, 72 InjectionOfCofactorOfPushout for IsList, IsInt, 91 InjectionOfCofactorOfPushoutWithGiven- Pushout for IsList, IsInt, IsCapCategoryObject, 91 InjectiveColift for IsCapCategoryMorphism, IsCapCategoryMorphism, 25 InjectiveDimension for IsCapCategoryObject, 26 InjectiveEnvelopeObject	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphismExtendedByFull- Embedding
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphismExtendedByFull- Embedding for IsCapCategory, IsCapCate
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMor- phism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphismExtendedByFull- Embedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryObject
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphismExtendedByFull- Embedding for IsCapCategory, IsCapCategory, IsCap- CategoryObject, IsCapCategoryObject IsCapCategoryMorphism, 45
for IsList, IsInt, 72 InjectionOfCofactorOfDirectSumWith-	DistinguishedObjectTo- HomomorphismStructureWithGiven- ObjectsExtendedByFullEmbedding for IsCapCategory, IsCapCategory, IsCapCategoryObject, IsCapCategoryMorphism, IsCapCategoryObject, 45 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphism for IsCapCategoryObject, IsCapCategory- Object, IsCapCategoryMorphism, 43 InterpretMorphismFromDistinguished- ObjectToHomomorphismStructure- AsMorphismExtendedByFull- Embedding for IsCapCategory, IsCapCategory, IsCapCategoryObject, IsCapCategoryObject IsCapCategoryMorphism, 45 InverseForMorphisms

InverseOfMorphismFromCoimageToImage-	for IsCapCategory, 8
WithGivenObjects	${\tt IsCategoryWithTerminalObject}$
for IsCapCategoryObject, IsCapCategory-	for IsCapCategory, 8
Morphism, IsCapCategoryObject, 96	IsCategoryWithZeroObject
IsAbCategory	for IsCapCategory, 8
for IsCapCategory, 9	IsCodominating
IsAbelianCategory	for IsCapCategoryMorphism, IsCapCatego-
for IsCapCategory, 9	ryMorphism, 36
IsAbelianCategoryWithEnoughInjectives	IsColiftable
for IsCapCategory, 10	for IsCapCategoryMorphism, IsCapCatego-
IsAbelianCategoryWithEnoughProjectives	ryMorphism, 40
for IsCapCategory, 9	IsColiftableAlongEpimorphism
IsAdditiveCategory	for IsCapCategoryMorphism, IsCapCatego-
for IsCapCategory, 9	ryMorphism, 39
IsApplicableToCategory	IsCongruentForMorphisms
for IsDerivedMethod, IsCapCategory, 175	for IsCapCategoryMorphism, IsCapCatego-
IsAutomorphism	ryMorphism, 34
for IsCapCategoryMorphism, 34	IsDerivedMethod
IsBijectiveObject	for IsAttributeStoringRep, 174
for IsCapCategoryObject, 21	IsDerivedMethodGraph
IsCapCategory	for IsAttributeStoringRep, 176
for IsAttributeStoringRep, 7	IsDominating
IsCapCategoryAsCatObject	for IsCapCategoryMorphism, IsCapCatego-
for IsCapCategoryObject, 55	ryMorphism, 36
IsCapCategoryCell	IsDummyCategory
for IsAttributeStoringRep, 7	for IsCapCategory, 206
IsCapCategoryMorphism	IsDummyCategoryMorphism
for IsCapCategoryCell, 7	for IsCapCategoryMorphism, 206
IsCapCategoryObject	IsDummyCategoryObject
for IsCapCategoryCell, 7	for IsCapCategoryObject, 206
IsCapCategoryTwoCell	IsDummyCommutativeHomalgRing, 207
for IsCapCategoryCell, 7	IsDummyCommutativeHomalgRingElement,
IsCapFunctor	207
for IsCapCategoryMorphism, 55	IsDummyCommutativeRing, 205
IsCapNaturalTransformation	IsDummyCommutativeRingElement, 205
for IsCapCategoryTwoCell, 55	IsDummyField, 206
IsCapTerminalCategoryWithMultiple-	IsDummyFieldElement, 206
Objects	IsDummyHomalgField, 207
for IsCapCategory, 217	IsDummyHomalgFieldElement, 208
IsCapTerminalCategoryWithSingleObject	IsDummyHomalgRing, 207
for IsCapCategory, 217	IsDummyHomalgRingElement, 207
IsCategoryWithDecidableColifts	IsDummyRing, 205
for IsCapCategory, 8	IsDummyRingElement, 205
IsCategoryWithDecidableLifts	IsEndomorphism
for IsCapCategory, 8	for IsCapCategoryMorphism, 33
IsCategoryWithInitialObject	IsEnrichedOverCommutativeRegular-
O ,,	

Semigroup	for IsCapCategoryMorphism, IsCapCategory
for IsCapCategory, 8	ryMorphism, 40
IsEpimorphism	IsLiftableAlongMonomorphism
for IsCapCategoryMorphism, 29	for IsCapCategoryMorphism, IsCapCatego
IsEqualAsFactorobjects	ryMorphism, 39
for IsCapCategoryMorphism, IsCapCatego-	IsLinearCategoryOverCommutativeRing
ryMorphism, 36	for IsCapCategory, 9
IsEqualAsSubobjects	IsLinearCategoryOverCommutativeRing-
for IsCapCategoryMorphism, IsCapCatego-	WithFinitelyGeneratedFree-
ryMorphism, 36	ExternalHoms
IsEqualForCacheForMorphisms	for IsCapCategory, 9
for IsCapCategoryMorphism, IsCapCatego-	IsLocallyOfFiniteInjectiveDimension
ryMorphism, 41	for IsCapCategory, 10
IsEqualForCacheForObjects	IsLocallyOfFiniteProjectiveDimension
for IsCapCategoryObject, IsCapCategory-	for IsCapCategory, 10
Object, 22	IsMonomorphism
IsEqualForMorphisms	for IsCapCategoryMorphism, 29
for IsCapCategoryMorphism, IsCapCatego-	IsMorphismInCapTerminalCategoryWith-
ryMorphism, 34	MultipleObjects
IsEqualForMorphismsOnMor	for IsCapCategoryMorphism, 218
for IsCapCategoryMorphism, IsCapCatego-	${\tt IsMorphismInCapTerminalCategoryWith-}$
ryMorphism, 34	SingleObject
IsEqualForObjects	for IsCapCategoryMorphism, 217
for IsCapCategoryObject, IsCapCategory-	${\tt IsObjectInCapTerminalCategoryWith-}$
Object, 20	MultipleObjects
${\tt IsEqualToIdentityMorphism}$	for IsCapCategoryObject, 217
for IsCapCategoryMorphism, 33	${\tt IsObjectInCapTerminalCategoryWith-}$
IsEqualToZeroMorphism	SingleObject
for IsCapCategoryMorphism, 33	for IsCapCategoryObject, 217
${\tt Is Equipped With Homomorphism Structure}$	Isomorphism From Coequalizer Of Coproduct-
for IsCapCategory, 8	DiagramToPushout
IsHomSetInhabited	for IsList, 90
for IsCapCategoryObject, IsCapCategory-	${\tt IsomorphismFromCoequalizerToCokernel-}$
Object, 42	${\tt Of JointPairwiseDifferencesOf-}$
IsIdempotent	${\tt MorphismsFromCoproduct}$
for IsCapCategoryMorphism, 30	for IsCapCategoryObject, IsList, 86
IsInitial	${\tt IsomorphismFromCoimageToCokernelOf-}$
for IsCapCategoryObject, 21	Kernel
IsInjective	for IsCapCategoryMorphism, 96
for IsCapCategoryObject, 21	IsomorphismFromCokernelOfJoint-
<pre>IsIsomorphicForObjects</pre>	${\tt PairwiseDifferencesOfMorphisms-}$
for IsCapCategoryObject, IsCapCategory-	${\tt FromCoproductToCoequalizer}$
Object, 20	for IsCapCategoryObject, IsList, 86
IsIsomorphism	${\tt IsomorphismFromCokernelOfKernelTo-}$
for IsCapCategoryMorphism, 29	Coimage
IsLiftable	for IsCapCategoryMorphism, 96

${\tt IsomorphismFromCoproductToDirectSum}$	for IsCapCategory, 68
for IsList, 74	<pre>IsomorphismFromZeroObjectToInitial-</pre>
<pre>IsomorphismFromDirectProductTo-</pre>	Object
DirectSum	for IsCapCategory, 67
for IsList, 73	IsomorphismFromZeroObjectToTerminal-
IsomorphismFromDirectSumToCoproduct	Object
for IsList, 73	for IsCapCategory, 68
IsomorphismFromDirectSumToDirect-	IsOne
Product	for IsCapCategoryMorphism, 30
for IsList, 73	IsOperationWeightList
IsomorphismFromEqualizerOfDirect-	for IsAttributeStoringRep, 177
ProductDiagramToFiberProduct	IsPreAbelianCategory
for IsList, 87	for IsCapCategory, 9
IsomorphismFromEqualizerToKernelOf-	IsProjective
JointPairwiseDifferencesOf-	for IsCapCategoryObject, 21
${ t MorphismsIntoDirectProduct}$	IsSkeletalCategory
for IsCapCategoryObject, IsList, 83	for IsCapCategory, 8
IsomorphismFromFiberProductTo-	IsSpecializationOfFilter, 183
EqualizerOfDirectProductDiagram	IsSpecializationOfFilterList, 183
for IsList, 87	IsSplitEpimorphism
IsomorphismFromHomologyObjectToIts-	for IsCapCategoryMorphism, 30
ConstructionAsAnImageObject	IsSplitMonomorphism
for IsCapCategoryMorphism, IsCapCatego-	for IsCapCategoryMorphism, 30
ryMorphism, 99	IsTerminal
IsomorphismFromImageObjectToKernelOf-	for IsCapCategoryObject, 21
Cokernel	IsTerminalCategory
for IsCapCategoryMorphism, 93	for IsCapCategory, 218
IsomorphismFromInitialObjectToZero-	IsWellDefined
Object	for IsCapCategoryCell, 15
for IsCapCategory, 68	${\tt IsWellDefinedForMorphisms}$
IsomorphismFromItsConstructionAsAn-	for IsCapCategoryMorphism, 38
${\tt ImageObjectToHomologyObject}$	IsWellDefinedForMorphismsWithGiven-
for IsCapCategoryMorphism, IsCapCatego-	SourceAndRange
ryMorphism, 99	for IsCapCategoryObject, IsCapCategory-
${\tt IsomorphismFromKernelOfCokernelTo-}$	Morphism, IsCapCategoryObject, 38
ImageObject	${\tt IsWellDefinedForObjects}$
for IsCapCategoryMorphism, 93	for IsCapCategoryObject, 23
IsomorphismFromKernelOfJointPairwise-	${\tt IsWellDefinedForTwoCells}$
DifferencesOfMorphismsInto-	for IsCapCategoryTwoCell, 54
DirectProductToEqualizer	IsWrapperCapCategory
for IsCapCategoryObject, IsList, 83	for IsCapCategory, 202
IsomorphismFromPushoutToCoequalizerOf-	${\tt IsWrapperCapCategoryMorphism}$
${\tt CoproductDiagram}$	for IsCapCategoryMorphism, 202
for IsList, 90	IsWrapperCapCategoryObject
Is omorphism From Terminal Object To Zero-	for IsCapCategoryObject, 202
Object	IsZero

for IsCapCategoryObject, 21	LastWithKeys, 190
IsZeroForMorphisms	LaTeXOutput
for IsCapCategoryMorphism, 34	for IsCapCategory, 18
IsZeroForObjects	for IsCapCategoryCell, 17
for IsCapCategoryObject, 21	Lift
Iterated	for IsCapCategoryMorphism, IsCapCatego-
for IsList, IsFunction, IsObject, 186	ryMorphism, 40
for IsList, IsFunction, IsObject, IsObject,	LiftAlongMonomorphism
186	for IsCapCategoryMorphism, IsCapCategoryMorphism, 39
JointPairwiseDifferencesOfMorphisms-	LiftOrFail
${\tt FromCoproduct}$	for IsCapCategoryMorphism, IsCapCatego-
for IsCapCategoryObject, IsList, 86	ryMorphism, 40
JointPairwiseDifferencesOfMorphisms-	LinearCombinationOfMorphisms
${\tt IntoDirectProduct}$	for IsCapCategoryObject, IsList, IsList, Is-
for IsCapCategoryObject, IsList, 82	CapCategoryObject, 38
	ListCAPPrepareFunctions, 106
KernelEmbedding	ListWithKeys, 189
for IsCapCategoryMorphism, 62	J ,
KernelEmbeddingWithGivenKernelObject	${\tt MakeDerivationGraph}$
for IsCapCategoryMorphism, IsCapCatego-	for IsDenseList, 176
ryObject, 62	${ t MakeOperationWeightList}$
KernelLift LG G L LG G L	for IsCapCategory, IsDerivedMethodGraph,
for IsCapCategoryMorphism, IsCapCatego-	178
ryObject, IsCapCategoryMorphism, 62	${\tt MereExistenceOfSolutionOfLinearSystem-}$
KernelLiftWithGivenKernelObject	${\tt InAbCategory}$
for IsCapCategoryMorphism, IsCapCatego-	for IsList, IsList, 44
ryObject, IsCapCategoryMorphism, Is-	${\tt MissingOperationsForConstructiveness-}$
CapCategoryObject, 62	OfCategory
KernelObject	for IsCapCategory, IsString, 14
for IsCapCategoryMorphism, 61	ModelingCategory
KernelObjectFunctorial	for IsCapCategory, 200
for IsCapCategoryMorphism, IsCapCatego-	${ t Modeling Morphism}$
ryMorphism, IsCapCategoryMorphism,	for IsCapCategory, IsCapCategoryMor-
63	phism, 201
for IsList, 63	ModelingObject
KernelObjectFunctorialWithGivenKernel-Objects	for IsCapCategory, IsCapCategoryObject, 201
for IsCapCategoryObject, IsCapCatego-	MonomorphismIntoInjectiveEnvelope-
ryMorphism, IsCapCategoryMor-	Object
phism,IsCapCategoryMorphism,	for IsCapCategoryObject, 100
IsCapCategoryMorphism, IsCap-	MonomorphismIntoInjectiveEnvelope-
CategoryObject, 63	ObjectWithGivenInjective-
for IsCapCategoryObject, IsCapCatego-	EnvelopeObject
ryMorphism, IsCapCategoryMor-	for IsCapCategoryObject, IsCapCategory-
phism,IsCapCategoryMorphism, IsCap-	Object, 100
CategoryObject, 63	MonomorphismIntoSomeInjectiveObject

for IsCapCategoryObject, 24	MorphismFromSourceToCoequalizer
MonomorphismIntoSomeInjectiveObject-	for IsCapCategoryObject, IsList, 84
WithGivenSomeInjectiveObject	MorphismFromSourceToCoequalizerWith-
for IsCapCategoryObject, IsCapCategory-	GivenCoequalizer
Object, 25	for IsCapCategoryObject, IsList, IsCapCate-
MorphismBetweenDirectSums	goryObject, 85
for IsList, 74	MorphismFromSourceToCokernelObject
for IsList, IsList, IsList, 74	for IsCapCategoryMorphism, 64
MorphismBetweenDirectSumsWithGiven-	MorphismFromSourceToCokernelObject-
DirectSums	WithGivenCokernelObject
for IsCapCategoryObject, IsList, IsList, Is- List, IsCapCategoryObject, 74	for IsCapCategoryMorphism, IsCapCategoryObject, 65
MorphismCache	MorphismFromSourceToPushout
for IsCapFunctor, 180	for IsList, 91
MorphismConstructor	MorphismFromSourceToPushoutWithGiven-
for IsCapCategoryObject, IsObject, IsCap-	Pushout
CategoryObject, 29	for IsList, IsCapCategoryObject, 91
MorphismDatum	MorphismFromZeroObject
for IsCapCategoryMorphism, 29	for IsCapCategoryObject, 67
${\tt MorphismDatumType}$	${\tt MorphismIntoZeroObject}$
for IsCapCategory, 12	for IsCapCategoryObject, 67
MorphismFilter	${\tt MorphismsOfExternalHom}$
for IsCapCategory, 11	for IsCapCategoryObject, IsCapCategory-
${\tt MorphismFromCoimageToImage}$	Object, 46
for IsCapCategoryMorphism, 95	${\tt MultiplyWithElementOfCommutativeRing-}$
${\tt MorphismFromCoimageToImageWithGiven-}$	${\tt For Morphisms}$
Objects	for IsRingElement, IsCapCategoryMor-
for IsCapCategoryObject, IsCapCategory-	phism, 35
Morphism, IsCapCategoryObject, 95	N
MorphismFromEqualizerToSink	Name for LoConCotagony, 11
for IsCapCategoryObject, IsList, 81	for IsCapCategory, 11
${\tt MorphismFromEqualizerToSinkWithGiven-}$	for IsCapNaturalTransformation, 59
Equalizer	NaturalIsomorphismFromIdentityTo- CanonicalizeZeroMorphisms
for IsCapCategoryObject, IsList, IsCapCate-	for IsCapCategory, 59
goryObject, 81	NaturalIsomorphismFromIdentityTo-
MorphismFromFiberProductToSink	CanonicalizeZeroObjects
for IsList, 88	for IsCapCategory, 59
MorphismFromFiberProductToSinkWith-	NaturalTransformation
GivenFiberProduct	for IsCapFunctor, IsCapFunctor, 60
for IsList, IsCapCategoryObject, 88	NTuple, 187
MorphismFromKernelObjectToSink	NumberWithKeys, 189
for IsCapCategoryMorphism, 62	Nambol W1011Noy 5, 109
MorphismFromKernelObjectToSinkWith-	ObjectCache
GivenKernelObject	for IsCapFunctor, 180
for IsCapCategoryMorphism, IsCapCatego-	ObjectConstructor
ryObject, 62	for IsCapCategory, IsObject, 23

ObjectDatum	${\tt ProjectionInFactorOfDirectSum}$
for IsCapCategoryObject, 23	for IsList, IsInt, 72
ObjectDatumType	ProjectionInFactorOfDirectSumWith-
for IsCapCategory, 11	GivenDirectSum
ObjectFilter	for IsList, IsInt, IsCapCategoryObject, 72
for IsCapCategory, 11	ProjectionInFactorOfFiberProduct
Operations	for IsList, IsInt, 88
for IsDerivedMethodGraph, 177	ProjectionInFactorOfFiberProductWith-
OperationWeight	GivenFiberProduct
for IsCapCategory, IsString, 14	for IsList, IsInt, IsCapCategoryObject, 88
OperationWeightUsingDerivation	ProjectionOntoCoequalizer
for IsOperationWeightList, IsDerived-	for IsCapCategoryObject, IsList, 84
Method, 178	ProjectionOntoCoequalizerWithGiven- Coequalizer
PackageOfCAPOperation, 186	for IsCapCategoryObject, IsList, IsCapCate-
Pair, 187	goryObject, 84
PostCompose	ProjectiveCoverObject
for IsCapCategoryMorphism, IsCapCatego-	for IsCapCategoryObject, 99
ryMorphism, 37	ProjectiveDimension
for IsList, 37	for IsCapCategoryObject, 26
PostComposeList	ProjectiveLift
for IsCapCategoryObject, IsList, IsCapCate-	for IsCapCategoryMorphism, IsCapCatego-
goryObject, 38	ryMorphism, 24
PostInverseForMorphisms	Pushout
for IsCapCategoryMorphism, 41	for IsCapCategoryMorphism, IsCapCatego-
PreCompose	ryMorphism, 91
for IsCapCategoryMorphism, IsCapCatego-	for IsList, 91
ryMorphism, 37	PushoutFunctorial
for IsList, 37	for IsList, IsList, IsList, 92
PreComposeList	PushoutFunctorialWithGivenPushouts
for IsCapCategoryObject, IsList, IsCapCategoryObject, 37	for IsCapCategoryObject, IsList, IsList, Is- List, IsCapCategoryObject, 92
PreInverseForMorphisms	PushoutProjectionFromCoproduct
for IsCapCategoryMorphism, 41	for IsList, 90
PrintDerivationTree	PushoutProjectionFromDirectSum
for IsOperationWeightList, IsString, 179	for IsList, 90
PrintTree	101 102100, 70
for IsObject, IsFunction, IsFunction, 179	RandomMorphism
PrintTreeRec	for IsCapCategory, IsInt, 33
for IsObject, IsFunction, IsFunction, IsInt,	for IsCapCategory, IsList, 33
179	for IsCapCategoryObject, IsCapCategory-
ProductWithKeys, 189	Object, IsInt, 33
ProjectionInFactorOfDirectProduct	for IsCapCategoryObject, IsCapCategory-
for IsList, IsInt, 78	Object, IsList, 33
ProjectionInFactorOfDirectProductWith-	RandomMorphismByInteger
GivenDirectProduct	for IsCapCategory, IsInt, 32
for IsList, IsInt, IsCapCategoryObject, 79	${\tt RandomMorphismByList}$

for IsCapCategory, IsList, 32	ReinterpretationOfCategory
RandomMorphismWithFixedRange	for IsCapCategory, IsRecord, 200
for IsCapCategoryObject, IsInt, 33	ReinterpretationOfMorphism
for IsCapCategoryObject, IsList, 33	for IsCapCategory, IsCapCategoryObject,
RandomMorphismWithFixedRangeByInteger	IsCapCategoryMorphism, IsCapCatego-
for IsCapCategoryObject, IsInt, 31	ryObject, 201
RandomMorphismWithFixedRangeByList	ReinterpretationOfObject
for IsCapCategoryObject, IsList, 31	for IsCapCategory, IsCapCategoryObject,
RandomMorphismWithFixedSource	201
for IsCapCategoryObject, IsInt, 33	ResetTimingStatistics, 16
for IsCapCategoryObject, IsList, 33	•
RandomMorphismWithFixedSourceAndRange	SafeFirst
for IsCapCategoryObject, IsCapCategory-	for IsList, IsFunction, 187
Object, IsInt, 33	SafePosition
for IsCapCategoryObject, IsCapCategory-	for IsList, IsObject, 186
Object, IsList, 33	${\tt SafePositionProperty}$
RandomMorphismWithFixedSourceAndRange-	for IsList, IsFunction, 187
ByInteger	${ t SafeUniqueEntry}$
for IsCapCategoryObject, IsCapCategory-	for IsList, IsFunction, 187
Object, IsInt, 31	${ t SafeUniquePosition}$
RandomMorphismWithFixedSourceAndRange-	for IsList, IsObject, 186
ByList	${\tt SafeUniquePositionProperty}$
for IsCapCategoryObject, IsCapCategory-	for IsList, IsFunction, 187
Object, IsList, 32	Saturate
RandomMorphismWithFixedSourceByInteger	for IsOperationWeightList, 179
for IsCapCategoryObject, IsInt, 30	SetCachingOfCategory, 15
RandomMorphismWithFixedSourceByList	SetCachingOfCategoryCrisp, 15
for IsCapCategoryObject, IsList, 31	SetCachingOfCategoryWeak, 15
RandomObject	SetDefaultCaching, 16
for IsCapCategory, IsInt, 22	SetDefaultCachingCrisp, 16
for IsCapCategory, IsList, 22	SetDefaultCachingWeak, 16
RandomObjectByInteger	Simplify
for IsCapCategory, IsInt, 22	for IsCapCategoryMorphism, 50
RandomObjectByList	for IsCapCategoryObject, 25
for IsCapCategory, IsList, 22	SimplifyEndo
Range	for IsCapCategoryMorphism, IsObject, 49
for IsCapCategoryMorphism, 27	${\tt SimplifyEndo_IsoFromInputObject}$
for IsCapCategoryTwoCell, 52	for IsCapCategoryMorphism, IsObject, 49
RangeCategoryOfHomomorphismStructure	${\tt SimplifyEndo_IsoToInputObject}$
for IsCapCategory, 12	for IsCapCategoryMorphism, IsObject, 49
RangeOfFunctor	${\tt SimplifyMorphism}$
for IsCapFunctor, 57	for IsCapCategoryMorphism, IsObject, 47
Reevaluate	SimplifyObject
for IsOperationWeightList, 179	for IsCapCategoryObject, IsObject, 25
ReinterpretationFunctor	${\tt SimplifyObject_IsoFromInputObject}$
for IsCapCategory, 200	for IsCapCategoryObject, IsObject, 25
1 0 0,	SimplifyObject IsoToInputObject

for IsCapCategoryMorphism, IsObject, 48 SimplifyRange_IsoFormInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySource for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFormInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryObject, 24 SomeReductio	for IsCapCategoryMorphism, IsObject, 48 SimplifyRange_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput-Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput-Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceIsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryWorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryWithSingleObjects TerminalCategoryWithSingleObject-UniqueMorphism for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject-UniqueObject for IsCapCategoryWithSingleObject-UniqueObject for IsCapCategoryWithSingleObject-UniqueObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 48 TerminalObjectFunctorial for IsCapCategoryObject, 69 TerminalObjectFunctorial for IsCapCategoryObject, 69 TerminalObjectFunctorial for IsCapCategoryObject, 69 TerminalObjectFunctorial
SimplifyRange_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoForInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoForInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 1sCapCategory Object, 20 SomeProjectiveObject for IsCapCategoryObject, 1sCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 1sCapCategory- Object, 20 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand_ MorphismFromInputRange for IsCapCategoryMorphism, 15 SomeReductionBySplitEpiSummand_ MorphismToInputRange for IsCapCategory, 12 for IsCapCategory, 12	SimplifyRange_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySource for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryWorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryWorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryWorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputObject for IsCapCategoryWorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryWithSingleObject- UniqueObject for IsCapCategoryWithSingleObject- UniqueObject for IsCapCategoryWithSingleObject- UniqueObject for IsCapCategoryWithSingleObject- UniqueObject for IsCapCatego
for IsCapCategoryMorphism, IsObject, 48 SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputBange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInputBange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceIsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory object, 20 SomeIsomorphismBetweenObject for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryWorphism, IsObject, 47 SomeReductionBySplitEpiSummand for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryObject, IsCapCategory- Object, 69 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsCapCategory, 12 subtractionForMorphism, 15CapCategory vMorphism, 35 SumOfMorphism, 35 SumWithKeys, 189 Target Target Target TerminalCategoryWorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWorblism, 218 TerminalCategoryWithSingleObject,	for IsCapCategoryMorphism, IsObject, 48 SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput-Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput-Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInput-Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory-Object, 20 SumUfMorphisms for IsCapCategoryObject, IsList, IsCapCategoryObject, 38 SumUfMcNeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWorphism, 28 SumUfMcneyhisms for IsCapCategoryObject, 18 SumUfMcneyhisms for IsCapCategoryObject, 18 SumUfMcneyhism, 18 CapCategoryObject, 18 SumUfMcneyhism, 18 SumUfMcneyhis
SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 simplifySource	SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput-Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput-Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory-Object, 20 for IsCapCategoryMorphism, IsCapCategory myMorphism, 35 SumOfMorphisms for IsCapCategoryObject, IsList, IsCapCategoryObject, 38 SumUithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWorplism, 21 Target for IsCapCategoryWorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWithSingleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithS
SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 simplifySource	SimplifyRange_IsoToInputObject for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput-Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput-Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput-Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory-Object, 20 for IsCapCategoryMorphism, IsCapCategory myMorphism, 35 SumOfMorphisms for IsCapCategoryObject, IsList, IsCapCategoryObject, 38 SumUithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWorplism, 21 Target for IsCapCategoryWorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWithSingleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithS
for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFomInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputBange for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputDigect for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputDigect for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, I	for IsCapCategoryMorphism, IsObject, 48 SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputDip ect for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputDip ect for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, IsCapCategory- Object, 20 ryMorphism, 35 SumOfMorphisms for IsCapCategoryObject, IsList, IsCapCate goryObject, 38 SumWithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, UniqueObject for IsCapTerminalCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20
SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange	SimplifySource for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SumOfMorphisms for IsCapCategoryObject, IsList, IsList, IsCapCate goryObject, 38 SumWithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorplism, 27 for IsCapCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueMorphism for IsCapTerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueOrphism, 18Object, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueOrphism for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject UniqueOrphism for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject UniqueOrphism for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject UniqueOrphism for IsCapCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueOrphism for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject UniqueOrphism for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingl
for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategory, 12 for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationSUsingOperation for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationSUsingOperation for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationSUsingOperation for IsCapCategory, 12	for IsCapCategoryMorphism, IsObject, 47 SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategoryObject, IsList, IsCapCategory- Object, 20 for IsCapCategoryObject, IsList, IsList, IsCapCategoryObject, 38 SumWithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWithMultipleObjects TerminalCategoryWithMultipleObjects UniqueMorphism for IsCapCategoryWithSingleObject- UniqueObject UniqueObject for IsCapCategoryWithSingleObject- UniqueObject for IsC
SimplifySourceAndRange	SimplifySourceAndRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SumWithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWocell, 52 TargetOperation for IsCapCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, UniqueMorphism for IsCapTerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueObject Uniq
for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInput- Bource for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 1sCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategory, 12 Target for IsCapCategoryMorphism, 27 for IsCapCategoryTwoCell, 52 TargetDperation for IsCapCategoryWithSingleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalObject for IsCapCa	for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 1sCapCategory- Object, 20 SumWithKeys, 189 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWorphism, 27 for IsCapCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, UniqueMorphism for IsCapTerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCa
SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryorFail for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 1sCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand- MorphismFromInputRange MorphismToInputRange Target for IsCapCategoryMorphism, 27 for IsCapCategoryWithOll, 176 TerminalCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject for IsCapCategoryWithSingleObject for	SimplifySourceAndRange_IsoFromInput- Range for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWithMultipleObjects TerminalCategoryWithMultipleObjects UniqueObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueObject UniqueObject for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject InqueObject for IsCapCategoryWithSingleObject for IsCapCategoryOtject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 18CapCategory- Object, 20
Target for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategory, 12 Target for IsCapCategoryMorphism, 27 for IsCapCategoryWocell, 52 TargetDperation for IsCapCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSi	Target for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryorFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 TargetOperation for IsCapCategoryWithMultipleObjects TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject UniqueObject for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject UniqueObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject UniqueObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject UniqueObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject UniqueObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingle
for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand- MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand- MorphismToInputRange for IsCapCategory, 12 for IsCapCategoryMorphism, 27 for IsCapCategoryWithMultipleObjects, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSin	for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 48 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategoryMorphism, 27 for IsCapCategoryWocell, 52 TargetOperation for IsDerivedMethod, 176 TerminalCategoryWithMultipleObjects TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, UniqueObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20
SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand- MorphismFromInputRange for IsCapCategory, 12 for IsCapCategoryUnithMultipleObjects, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObjec	SimplifySourceAndRange_IsoFromInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategoryTwoCell, 52 TargetOperation for IsDerivedMethod, 176 TerminalCategoryWithMultipleObjects TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 Terminal
Source for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrpFail for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategory, 12 TargetOperation for IsDcrivedMethod, 176 TerminalCategoryWithSingleObjects UniqueObject UniqueObject for IsCapTerminalCategoryWithSingleObject IsCapTerminalObject for IsCapCategoryWithSingleObject for IsCapCategoryObject for IsCapCategoryObject for IsCapCategoryObject for IsCapCategoryObject for IsCapCategoryObject for IsCapCategoryObject for IsC	for IsCapCategoryMorphism, IsObject, 49 SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 TargetOperation for IsDerivedMethod, 176 TerminalCategoryWithSingleObjects TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 Term
SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand_ MorphismFromInputRange for IsCapCategory, Morphism, 51 SomeReductionBySplitEpiSummand_ MorphismToInputRange MorphismToInputRange MorphismToInputRange TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryW	SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput-
SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInputSource for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory-Object, 20 SomeProjectiveObject for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand_ MorphismToInputRange for IsCapCategory, 12 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalObject for IsCapCategoryWithSingleObject, 219 TerminalCategoryWithS	SimplifySourceAndRange_IsoToInputRange for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 Termi
SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject for IsCapCategoryObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 24 SomePojectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 UniqueObject UniqueObject for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject for IsCapCategoryWithSingleObject f	for IsCapCategoryMorphism, IsObject, 48 SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 TerminalCategoryWithSingleObject UniqueMorphism for IsCapTerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSin
SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand_ MorphismToInputRange for IsCapCategory, 12 TerminalCategoryWithSingleObject, UniqueObject for IsCapCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 50 IsCapCategoryObject, 50 IsCapCategoryObject, 50 TerminalCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 50 IsCapCategoryObject, 50 TerminalCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 50 IsCapCategoryWithSingleObject, 50 IsCapCategoryObject, 50 IsCapCategoryObject, 50 IsCapCategoryObject, 50 IsCapCategoryObject, 50 IsCapCategoryObj	SimplifySourceAndRange_IsoToInput- Source for IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryorFail for IsCapCategoryObject for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 TerminalCategoryWithSingleObject, UniqueOrphism for IsCapTerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 219 TerminalCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 219
For IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategory, 12 TerminalCategoryWithSingleObject, 21 IniqueOrphism IsCapTerminalCategoryWithSingleObject, 21 IniqueOrphism IsCapTerminalCategoryWithSingleObject, 21 IniqueOrphism IsCapTerminalCategoryWithSingleObject, 21 IniqueOrphism IsCapTerminalCategoryWithSingleObject, 21 IniqueObject UniqueMorphism IsCapTerminalCategoryWithSingleObject, 21 IniqueOrphism IsCapTerminalCategoryWithSingleObject, 21 IniqueOrphism IsCapTerminalCategoryWithSingleObject, 21 IniqueObject IniqueOrphism IniqueOpject IniqueOpject IniqueOrphi	For IsCapCategoryMorphism, IsObject, 49 SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject for IsCapCa
SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, IsCapCategory Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange for IsCapCategory, 12 for IsCapCategoryWithSingleObject, 218 TerminalCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryObject for IsCapCategory, 69 TerminalObject for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObject for IsCapCategoryObject, 69 TerminalObject for IsCapCategoryObject, 69 TerminalObject for IsCapCategory WithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategory, 69 TerminalObject for IsCapCategoryObject, IsCapCategory Object, 218 TerminalObject for IsCapCategory for IsCapCategory for IsCapCategory Object, 20 TerminalObject for IsCapCategory Object, 20 TerminalObject for IsCapCategory	SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory Object, 20 for IsCapCategoryWithSingleOb ject, 219 TerminalCategoryWithSingleObject UniqueObject for IsCapTerminalCategoryWithSingleObject TerminalObject for IsCapTerminalCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObject TerminalObject for IsCapCategoryWithSingleObject IncludeObject I
SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategoryObject, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand- MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand- MorphismToInputRange for IsCapCategory, 12 for IsCapCategoryWithSingleObject, UniqueObject for IsCapCategoryWithSingleObject, UniqueObject for IsCapCategoryWithSingleObject, UniqueObject for IsCapCategoryObject for IsCapCategoryWithSingleObject, UniqueObject for IsCapCategoryWithSingleObject for IsCapCategor	SimplifySource_IsoFromInputObject for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsCapCategoryObject for IsCapCategoryObject, 24 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory Object, 20 for IsCapCategoryWithSingleOb ject, 219 TerminalCategoryWithSingleObject UniqueObject for IsCapTerminalCategoryWithSingleObject for IsCapCategoryWithSingleObject for IsCapCategoryWithSingleObje
for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory-Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand_MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand_MorphismToInputRange for IsCapCategory, 69 for IsCapCategoryObject, IsCapCategory-Object, IsCapCategory-Object, 69 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	for IsCapCategoryMorphism, IsObject, 47 SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory-Object, 20 ject, 219 TerminalCategoryWithSingleObject for IsCapTerminalCategoryWithSingleObject for IsCapCategoryOtject for IsCapCategoryOtject for IsCapCategory, 69 for IsCapCategoryOtject, 24 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven-TerminalObjects TerminalObjects
SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand_ MorphismToInputRange MorphismToInputRange for IsCapCategory, 12 TerminalCategoryWithSingleObject IsCapCategoryWithSingleObject IsCapCategoryWithSingleObject IsCapCategoryWithSingleObject IsCapCategory, 69 for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategoryObject, IsCapCategory Object, 69 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	SimplifySource_IsoToInputObject for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategoryObject, 20 TerminalCategoryWithSingleObject IsCapTerminalCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryObject, 69 for IsCapCategoryCell, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects
for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange for IsCapCategory, 69 TerminalObjectFunctorialWithGiven TerminalObjects for IsCapCategoryObject, IsCapCategory Object, 69 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	for IsCapCategoryMorphism, IsObject, 47 SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategoryObject, 20 UniqueObject for IsCapTerminalCategoryWithSingleOb ject, 218 TerminalObject for IsCapCategory, 69 for IsCapCategoryCell, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects
SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange for IsCapCategoryWithSingleObject, 218 TerminalObject for IsCapCategoryCell, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory Object, 24 TerminalObjectFunctorial for IsCapCategory Object, 29 T	SolveLinearSystemInAbCategory for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategoryWithSingleOb ject, 218 TerminalObject for IsCapCategory, 69 for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects TerminalObjects
for IsList, IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand- MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand- MorphismToInputRange MorphismToInputRange Mo	for IsList, IsList, 43 SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 Ject, 218 TerminalObject for IsCapCategory, 69 for IsCapCategoryCell, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects TerminalObjects
SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand- MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand- MorphismToInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand- MorphismToInputRange for IsCapCategoryMorphism, 51 TerminalObject for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	SolveLinearSystemInAbCategoryOrFail for IsList, IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategoryObject, 20 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects TerminalObjects TerminalObjectFunctorialWithGiven- TerminalObjects
for IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	for IsList, IsList, 44 SomeInjectiveObject for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects TerminalObjects TerminalObjects
for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategoryMorphism, 51 Triple, 187 TwoCellDatumType for IsCapCategory, 69 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjectFunctorialWithGi	for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory Object, 20 for IsCapCategoryObject, IsCapCategory TerminalObjectFunctorialWithGiven TerminalObjects TerminalObjects TerminalObjects
for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategoryMorphism, 51 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjectFunctorialWithGivenDimensions, 188 TriansposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsCapCategoryMorphism, 51 Triple, 187 TwoCellDatumType for IsCapCategory, 12	for IsCapCategoryObject, 24 SomeIsomorphismBetweenObjects for IsCapCategoryObject, IsCapCategory- Object, 20 TerminalObjectFunctorial for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects TerminalObjectFunctorialWithGiven- TerminalObjects
for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategory, 69 TerminalObjectFunctorialWithGiven- TerminalObjects for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	SomeIsomorphismBetweenObjects for IsCapCategory, 69 for IsCapCategoryObject, IsCapCategory- Object, 20 for IsCapCategory- TerminalObjectFunctorialWithGiven- TerminalObjects
for IsCapCategoryObject, IsCapCategory- Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategoryMorphism, 51 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	for IsCapCategoryObject, IsCapCategory- TerminalObjectFunctorialWithGiven- Object, 20 TerminalObjects
Object, 20 SomeProjectiveObject for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange TerminalObjects for IsCapCategoryObject, IsCapCategory- Object, 69 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	Object, 20 TerminalObjects
for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategoryObject, IsCapCategory- Object, 69 TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 TwoCellDatumType for IsCapCategory, 12	
for IsCapCategoryObject, 24 SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange MorphismToInputRange TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	SomeProjectiveObject for iscapcategoryObject, iscapcategory
SomeReductionBySplitEpiSummand for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange TransitivelyNeededOtherPackages, 186 TransposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	01' (0
for IsCapCategoryMorphism, 50 SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange MorphismToInputRange TriansposedMatWithGivenDimensions, 188 TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	T 100 D 1 100
SomeReductionBySplitEpiSummand MorphismFromInputRange for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange TriggerDerivationsUsingOperation for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	T IM (17 1 A ' 100
MorphismFromInputRange for IsOperationWeightList, IsString, 179 for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange for IsOperationWeightList, IsString, 179 Triple, 187 TwoCellDatumType for IsCapCategory, 12	
for IsCapCategoryMorphism, 51 SomeReductionBySplitEpiSummand MorphismToInputRange Triple, 187 TwoCellDatumType for IsCapCategory, 12	\mathbf{f}_{-} \mathbf{u}_{-} \mathbf{f}_{-}
SomeReductionBySplitEpiSummand MorphismToInputRange TwoCellDatumType for IsCapCategory, 12	- 10 7
MorphismToInputRange for IsCapCategory, 12	m
The particular of the content of the	C I C C
for isCapCategoryMorphism. 51	for IsCapCategoryMorphism, 51 TwoCellFilter
for IcConCatagory 11	Source for IsCapCategory, 11

UnderlyingCell	for IsCapCategoryObject, IsCapCategory-
for IsWrapperCapCategoryMorphism, 202	Object, 67
for IsWrapperCapCategoryObject, 202	UniversalMorphismIntoCoimage
UniversalMorphismFromCoequalizer	for IsCapCategoryMorphism, IsList, 97
for IsCapCategoryObject, IsList, IsCapCat-	UniversalMorphismIntoCoimageWithGiven-
egoryObject, IsCapCategoryMorphism,	CoimageObject
85	for IsCapCategoryMorphism, IsList, IsCap-
UniversalMorphismFromCoequalizerWith-	CategoryObject, 97
GivenCoequalizer	${\tt UniversalMorphismIntoDirectProduct}$
for IsCapCategoryObject, IsList, IsCapCat-	for IsList, IsCapCategoryObject, IsList, 79
egoryObject, IsCapCategoryMorphism,	UniversalMorphismIntoDirectProduct-
IsCapCategoryObject, 85	${ t With Given Direct Product}$
UniversalMorphismFromCoproduct	for IsList, IsCapCategoryObject, IsList, Is-
for IsList, IsCapCategoryObject, IsList, 77	CapCategoryObject, 79
UniversalMorphismFromCoproductWith-	${\tt UniversalMorphismIntoDirectSum}$
GivenCoproduct	for IsList, IsCapCategoryObject, IsList, 72
for IsList, IsCapCategoryObject, IsList, Is-	UniversalMorphismIntoDirectSumWith-
CapCategoryObject, 77	GivenDirectSum
UniversalMorphismFromDirectSum	for IsList, IsCapCategoryObject, IsList, Is-
for IsList, IsCapCategoryObject, IsList, 73	CapCategoryObject, 73
UniversalMorphismFromDirectSumWith-	${\tt UniversalMorphismIntoEqualizer}$
GivenDirectSum	for IsCapCategoryObject, IsList, IsCapCat-
for IsList, IsCapCategoryObject, IsList, Is-	egoryObject, IsCapCategoryMorphism,
CapCategoryObject, 73	81
${\tt UniversalMorphismFromImage}$	${\tt UniversalMorphismIntoEqualizerWith-}$
for IsCapCategoryMorphism, IsList, 94	${\tt GivenEqualizer}$
${\tt UniversalMorphismFromImageWithGiven-}$	for IsCapCategoryObject, IsList, IsCapCat-
${\tt ImageObject}$	egoryObject, IsCapCategoryMorphism,
for IsCapCategoryMorphism, IsList, IsCap-	IsCapCategoryObject, 82
CategoryObject, 94	${\tt UniversalMorphismIntoFiberProduct}$
${\tt UniversalMorphismFromInitialObject}$	for IsList, IsCapCategoryObject, IsList, 89
for IsCapCategoryObject, 70	UniversalMorphismIntoFiberProductWith-
${\tt UniversalMorphismFromInitialObject-}$	${\tt GivenFiberProduct}$
${ t With Given Initial Object}$	for IsList, IsCapCategoryObject, IsList, Is-
for IsCapCategoryObject, IsCapCategory-	CapCategoryObject, 89
Object, 70	${\tt UniversalMorphismIntoTerminalObject}$
${\tt UniversalMorphismFromPushout}$	for IsCapCategoryObject, 69
for IsList, IsCapCategoryObject, IsList, 91	${\tt UniversalMorphismIntoTerminalObject-}$
UniversalMorphismFromPushoutWithGiven-	${ t With Given Terminal Object}$
Pushout	for IsCapCategoryObject, IsCapCategory-
for IsList, IsCapCategoryObject, IsList, Is-	Object, 69
CapCategoryObject, 92	${\tt UniversalMorphismIntoZeroObject}$
${\tt UniversalMorphismFromZeroObject}$	for IsCapCategoryObject, 67
for IsCapCategoryObject, 67	${\tt UniversalMorphismIntoZeroObjectWith-}$
${\tt UniversalMorphismFromZeroObjectWith-}$	${\tt GivenZeroObject}$
GivenZeroObject	for IsCapCategoryObject, IsCapCategory-

```
Object, 67
UsedOperationsWithMultiplesAnd-
       CategoryGetters
    for IsDerivedMethod, 176
VerticalPostCompose
    for IsCapCategoryTwoCell, IsCapCatego-
       ryTwoCell, 53
VerticalPreCompose
    for IsCapCategoryTwoCell, IsCapCatego-
       ryTwoCell, 53
WrapperCategory
    for IsCapCategory, IsRecord, 203
WrappingFunctor
   for IsWrapperCapCategory, 204
ZeroMorphism
    for IsCapCategoryObject, IsCapCategory-
       Object, 35
ZeroObject
    for IsCapCategory, 66
    for IsCapCategoryCell, 66
ZeroObjectFunctorial
    for IsCapCategory, 68
{\tt ZeroObjectFunctorialWithGivenZero-}
        Objects
    for IsCapCategoryObject, IsCapCategory-
       Object, 68
```