A GAP package for drawing sets of integers

Version 0.4.0

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Colophon

This manual describes the GAP package IntPic , Version 0.4.0, for visualizing and creating publication quality pictures of sets of integers.

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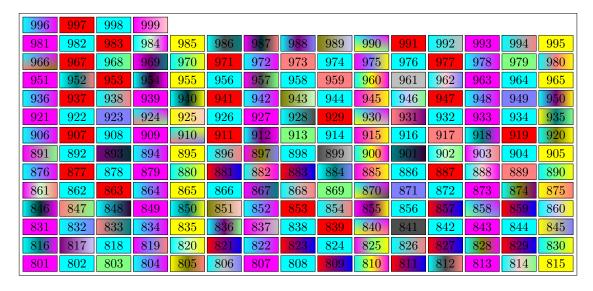
Chapter 1

The IntPic package

1.1 Overview and Introduction

The IntPic package has as its main goal producing Tikz code for arrays of integers to be included in a LATEX file, which can then be processed. Some of the integers are emphasized, by using different colors for the cells.

IntPic grew up from my will to have a pictorial view of some sets of integers. I wanted, in particular, get a pictorial view of the results produced by the NumericalSgps package [DGSM15]. Effort has then been made to serve a slightly more general purpose. For instance, if the user wants to have a pictorial idea of how many primes there are between 800 and 1000, or show it to his students and, perhaps, which among these primes are twin primes, he will probably be happy by producing a picture like the following



It has clearly too much information, given through the different colors. The twin primes in the given range are in red-blue, while the remaining primes in the same range are in red.

This package contains relatively few lines of code. The heavier part is the documentation, where many examples are presented.

The design of this greatly benefits from my long experience on producing visualization tools for GAP objects. The package sgpviz [DM08] is the visible part. More recently, I got involved in a more

general project, the Viz package [DENMP12]. The experience gained there, especially through long and fruitful discussions with J. Mitchell, influenced me a lot. This package will probably be part of that more general project. For the moment it is independent, but its use in conjunction with the Viz package is recommended since in this case an immediate visualization is provided.

The package produces tikz code that the user may then use at his wish. In particular, he can use it in publications. But prior to obtaining results that lead to a publication, the user may benefit of viewing thousands of images. There is a (almost platform independent) function in Viz that is intended to make this task easy. It benefits from the GAP stuff on creating a temporary directory where the computations occur. The cleaning task is also left to GAP, which leaves the user free of the need of collecting the garbage. In order to produce the drawings, LATEX, as well as some LATEX packages, in particular tikz and pgf, must be installed and working. I will assume that this is the case. All the images in [DFGSL14] have been produced by using the IntPic package.

This package consists basically of a function with many options associated. The purpose of the manual is to illustrate the use of the options. Many examples are presented. A file, named examples.g contains the GAP code, including the one to save the tikz code, to produce the examples in the manual.

1.2 **Installing IntPic**

In this section we give a brief description of how to start using IntPic. If you have any problems getting IntPic working, then you could try emailing me at mdelgado@fc.up.pt.

It is assumed that you have a working copy of GAP with version number 4.5 or higher. The most up-to-date version of GAP and instructions on how to install it can be obtained from the main GAP web page https://www.gap-system.org.

If the IntPic package was obtained as a part of the GAP distribution from the "Download" section of the GAP website, you may proceed to Section 1.3. Alternatively, the IntPic package may be installed using a separate archive, for example, for an update or an installation in a non-default location (see (Reference: GAP Root Directories)).

Below we describe the installation procedure for the .tar.gz archive format, which can be obtained from http://cmup.fc.up.pt/cmup/mdelgado/intpic/. Installation using other archive formats or non UNIX-like systems is performed in a similar way.

To install the IntPic package, unpack the archive file, which should have a name of the form intpic-XXX.tar.gz for some version number XXX, by typing

```
gzip -dc intpic-XXX.tar.gz | tar xpv
It may be unpacked in one of the following locations:
```

• in the pkg directory of your GAP installation;

- or in a directory named .gap/pkg in your home directory (to be added to the GAP root directory unless GAP is started with -r option);
- or in a directory named pkg in another directory of your choice (e.g. in the directory mygap in your home directory).

In the latter case one must start GAP with the -1 option, e.g. if your private pkg directory is a subdirectory of mygap in your home directory you might type:

```
gap -1 ";myhomedir/mygap"
```

where *myhomedir* is the path to your home directory, which may be replaced by a tilde (the empty path before the semicolon is filled in by the default path of the GAP home directory).

1.3 Loading IntPic

To use the IntPic Package you have to request it explicitly. This is done by calling LoadPackage (Reference: LoadPackage):

The package banner, followed by true, will be shown, if the load has been successful.

If you want to load the IntPic package by default, you can put the LoadPackage command into your gaprc file (see Section (Reference: The gap.ini and gaprc files)).

Chapter 2

The IntPic package main function

This chapter consists of two sections, the first of which describes the main function of the package. The second one can be thought just as an example to produce a table where the integers appear ordered in a non standard way.

2.1 The main function

The function IP_TikzArrayOfIntegers (2.1.1) is the main function of the IntPic package. It aims to produce tikz code for displaying arrays of integers.

2.1.1 Tikz code for arrays of integers

```
▷ IP_TikzArrayOfIntegers(arg)
```

(function)

The arguments (at most 3) are:

- 1. (optional)
 - a table of integers. In this case, the length of the rows is the maximum of the lengths of the sublists in the table, *or*
 - a list of integers and, optionally, an integer which indicates the length of the rows; when the length of the rows is not indicated, a compromise between the width and the height is tried
- 2. a record of options. One of the fields of this record, named highlights, is an array whose entries are the numbers to be highlighted: one color per sublist. See details and other options in Chapter 5.

When no list nor table is present, the smallest range containing all the integers to be highlighted is taken.

The aspect of the string tkz produced is not very appealing. We show it once, by asking it explicitly in the next example. In the forthcoming examples we keep using two semicolons to avoid showing this kind of strings.

```
gap> tkz;
"%tikz\n\\begin{tikzpicture}[every node/.style={draw,scale=1pt,\nminimum width\
=20pt,inner sep=3pt,\nline width=1pt,draw=black}]\n\\matrix[row sep=2pt,column\
sep=2pt]\n{\\node[fill=-red]{86};&\n\\node[fill=green]{87};&\n\\node[fill=-re\\
d]{88};&\n\\node[fill=red]{89};\\\\n\\node[fill=green]{81};&\n\\node[fill=-re\\\
d]{82};&\n\\node[fill=red]{83};&\n\\node[left color=-red,right color=green]{84\\
};&\n\\node[]{85};\\\\n};\n\\end{tikzpicture}\n"
```

This string can be used at the users wish. In particular, it can be sent to the standard output using the command Print (Reference: Print).

```
_{-} The tikz code _{-}
gap> Print(tkz);
%tikz
\begin{tikzpicture}[every node/.style={draw,scale=1pt,
minimum width=20pt,inner sep=3pt,
line width=1pt,draw=black}]
\matrix[row sep=2pt,column sep=2pt]
{\node[fill=-red]{86};&
\node[fill=green]{87};&
\node[fill=-red]{88};&
\node[fill=red]{89};\
\node[fill=green]{81};&
\node[fill=-red]{82};&
\node[fill=red]{83};&
\node[left color=-red,right color=green]{84};&
\node[]{85};\\
};
\end{tikzpicture}
```

It can now be copied and pasted in a LATEX document (having the appropriate packages in the preamble). See Chapter 4 for details and alternatives.

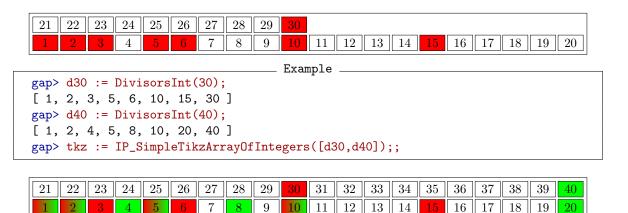
The next function uses the previous one, but is called with a simpler argument. It will hopefully be useful for simple drawings. The length of each row and the umber of columns varies. A compromise based on some experiments has been established in order to obtain not too large nor too high images.

2.1.2 Tikz code for arrays, in a simplified way

```
▷ IP_SimpleTikzArrayOfIntegers(arg) (function)
```

The argument is either a list of integers or a matrix of integers. The integers involved are embedded in a range rg of minimum length and highlighted by using the list of default colors.

```
gap> d := DivisorsInt(30);
[ 1, 2, 3, 5, 6, 10, 15, 30 ]
gap> IP_SimpleTikzArrayOfIntegers(d);;
```



2.2 Producing tables

When the user is interested in tables of a certain kind, it may be a good idea to write some code to produce these tables. The following function (whose code is part of the file *ip_tables.gi* in the *gap* folder of this package) is convenient to deal with numerical semigroups with two generators and has been used to produce the images contained in [DFGSL14].

2.2.1 IP TableWithModularOrder

```
▷ IP_TableWithModularOrder(o, a, b, depth, height, rep, pos) (function)
```

The arguments rep and pos are booleans (true or false). When rep is true there is some repetition: the last column is equal to the first, but pushed down some rows. When pos is true, no rows below 0 are considered, (contradicting depth, if needed).

The first five arguments arguments o, a, b, depth and height are integers. What they represent is described in what follows. There is assigned some kind of a referential on the constructed table and the fist argument, o, stands for the origin. A table with b columns (b+1 columns when rep is true) is constructed as follows. The row containing the origin is

```
• o + [0..b - 1] * a, if rep is false, or
```

• o + [0..b] * a, if rep is true

The remaining rows are obtained by adding b (the upper ones) or subtracting b (the others) to these rows

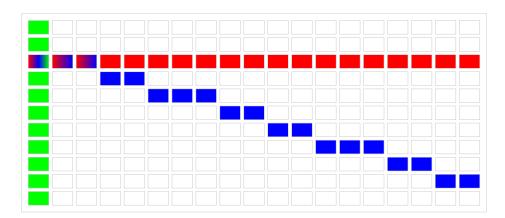
Note: when a < b are co-prime, this construction provides a representation of the integers as an array.

```
gap> a := 8;; b := 19;;
gap> ns := NumericalSemigroup(a,b);;
gap> c := ConductorOfNumericalSemigroup(ns);;
gap> origin := 2*c-1;
251
gap> ground := [origin..origin+b-1];;
gap>
gap> height:=2;;
```

```
gap> depth:=8;;
       xaxis := [origin];;
gap>
       for n in [1..b-1] do
gap>
      Add(xaxis, origin+n*a);
   od;
       yaxis := [];;
gap>
       for n in [-depth..height] do
gap>
      Add(yaxis, origin+n*b);
>
    od;
gap>
gap> table := IP_TableWithModularOrder(origin,a,b,depth,height,false,false);;
gap> arr := [xaxis,yaxis,ground];
[ [ 251, 259, 267, 275, 283, 291, 299, 307, 315, 323, 331, 339, 347, 355,
      363, 371, 379, 387, 395],
  [ 99, 118, 137, 156, 175, 194, 213, 232, 251, 270, 289 ], [ 251 .. 269 ] ]
gap> tkz:=IP_TikzArrayOfIntegers(table,rec(highlights:=arr));;
```

289	297	305	313	321	329	337	345	353	361	369	377	385	393	401	409	417	425	433
270	278	286	294	302	310	318	326	334	342	350	358	366	374	382	390	398	406	414
2 <mark>5</mark> 1	259	267	275	283	291	299	307	315	323	331	339	347	355	363	371	379	387	395
232	240	248	256	264	272	280	288	296	304	312	320	328	336	344	352	360	368	376
213	221	229	237	245	253	261	269	277	285	293	301	309	317	325	333	341	349	357
194	202	210	218	226	234	242	250	258	266	274	282	290	298	306	314	322	330	338
175	183	191	199	207	215	223	231	239	247	255	263	271	279	287	295	303	311	319
156	164	172	180	188	196	204	212	220	228	236	244	252	260	268	276	284	292	300
137	145	153	161	169	177	185	193	201	209	217	225	233	241	249	257	265	273	281
118	126	134	142	150	158	166	174	182	190	198	206	214	222	230	238	246	254	262
99	107	115	123	131	139	147	155	163	171	179	187	195	203	211	219	227	235	243

The next picture is obtained in the same way. The information that only the shape has interest is given by including the option shape_only:="". The variable tkz should be defined in a similar manner to the following one.



Next, a minimum of changes, just to illustrate the effect of rep and pos.

```
gap> table := IP_TableWithModularOrder(origin,a,b,depth,50,true,true);;
gap> tkz:=IP_TikzArrayOfIntegers(table,rec(highlights:=arr));;
```

289	297	305	313	321	329	337	345	353	361	369	377	385	393	401	409	417	425	433	441
270	278	286	294	302	310	318	326	334	342	350	358	366	374	382	390	398	406	414	422
2 <mark>5</mark> 1	259	267	275	283	291	299	307	315	323	331	339	347	355	363	371	379	387	395	403
232	240	248	256	264	272	280	288	296	304	312	320	328	336	344	352	360	368	376	384
213	221	229	237	245	253	261	269	277	285	293	301	309	317	325	333	341	349	357	365
194	202	210	218	226	234	242	250	258	266	274	282	290	298	306	314	322	330	338	346
175	183	191	199	207	215	223	231	239	247	255	263	271	279	287	295	303	311	319	327
156	164	172	180	188	196	204	212	220	228	236	244	252	260	268	276	284	292	300	308
137	145	153	161	169	177	185	193	201	209	217	225	233	241	249	257	265	273	281	289
118	126	134	142	150	158	166	174	182	190	198	206	214	222	230	238	246	254	262	270
99	107	115	123	131	139	147	155	163	171	179	187	195	203	211	219	227	235	243	2 <mark>5</mark> 1
80	88	96	104	112	120	128	136	144	152	160	168	176	184	192	200	208	216	224	232
61	69	77	85	93	101	109	117	125	133	141	149	157	165	173	181	189	197	205	213
42	50	58	66	74	82	90	98	106	114	122	130	138	146	154	162	170	178	186	194
23	31	39	47	55	63	71	79	87	95	103	111	119	127	135	143	151	159	167	175
4	12	20	28	36	44	52	60	68	76	84	92	100	108	116	124	132	140	148	156
-15	-7	1	9	17	25	33	41	49	57	65	73	81	89	97	105	113	121	129	137
-34	-26	-18	-10	-2	6	14	22	30	38	46	54	62	70	78	86	94	102	110	118
-53	-45	-37	-29	-21	-13	-5	3	11	19	27	35	43	51	59	67	75	83	91	99
-72	-64	-56	-48	-40	-32	-24	-16	-8	0	8	16	24	32	40	48	56	64	72	80

Chapter 3

The colors in the IntPic package

The idea in what concerns the colors is the following: the reader is free to choose his colors (taking into account that the latex xcolor package is used), but we try to make users life reasonably easy. He is allowed to choose tones. The default colors used by IntPic are not many, although (from our experience) sufficient for most examples.

3.1 Colors by tones

The colors are divided by tones.

```
gap> IP_ColorsRedTones; #red
[ "red", "red!50", "red!20", "red!80!green!50", "red!80!blue!60" ]

gap> IP_ColorsGreenTones; #green
[ "green", "green!50", "green!20", "green!80!red!50", "green!80!blue!60" ]

1 2 3 4 5

blue

gap> IP_ColorsBlueTones; #blue
[ "blue", "blue!50", "blue!20", "blue!80!red!50", "blue!80!green!60" ]

1 2 3 4 5

cyan

gap> IP_ColorsCompRedTones; # cyan (complement of red)
[ "-red", "-red!50", "-red!20", "-red!80!green!50", "-red!80!blue!60" ]
```

```
gap> IP_ColorsCompGreenTones; # magenta (complement of green)
[ "-green", "-green!50", "-green!20", "-green!80!red!50", "-green!80!blue!60"
]
```

```
    1
    2
    3
    4
    5
```

```
gap> IP_ColorsCompBlueTones; # yellow (complement of blue)
[ "-blue", "-blue!50", "-blue!20", "-blue!80!red!50", "-blue!80!green!60" ]
```



```
gap> IP_ColorsDGrayTones; # dark gray

[ "black!80", "black!70", "black!60", "black!50", "black!40" ]
```



```
gap> IP_ColorsLGrayTones; # light gray
[ "black!30", "black!25", "black!20", "black!15", "black!10" ]
```

1 2 3 4 5

3.2 Lists of colors

```
list of colors by tones

gap> IP_Colors;

[ "red", "red!50", "red!20", "red!80!green!50", "red!80!blue!60", "green",
    "green!50", "green!20", "green!80!red!50", "green!80!blue!60", "blue",
    "blue!50", "blue!20", "blue!80!red!50", "blue!80!green!60", "-red",
    "-red!50", "-red!20", "-red!80!green!50", "-red!80!blue!60", "-green",
    "-green!50", "-green!20", "-green!80!red!50", "-green!80!blue!60", "-blue",
    "-blue!50", "-blue!20", "-blue!80!red!50", "-blue!80!green!60", "black!80",
    "black!70", "black!60", "black!50", "black!40", "black!30", "black!25",
    "black!20", "black!15", "black!10"]
```

3.3 The IntPic default list of colors

The colors are shuffled by concatenating the transposed of the matrix ListsOfIP_Colors. The list obtained is taken as the default list of colors.

```
default list of colors

gap> ShuffledIP_colors;
[ "red", "green", "blue", "-red", "-green", "-blue", "black!80", "black!30",
    "red!50", "green!50", "blue!50", "-red!50", "-green!50", "-blue!50",
    "black!70", "black!25", "red!20", "green!20", "blue!20", "-red!20",
    "-green!20", "-blue!20", "black!60", "black!20", "red!80!green!50",
    "green!80!red!50", "blue!80!red!50", "-red!80!green!50", "-green!80!red!50", "black!15", "red!80!blue!60",
    "green!80!blue!60", "blue!80!green!60", "-red!80!blue!60",
    "-green!80!blue!60", "-blue!80!green!60", "black!40", "black!10"]
```



These are the IntPic default colors. Although the user is free to use other colors, we warn that there is a need of compatibility with the colors used in other packages (the LATEX XCOlor, for instance). To emphasize the integers of some sets by using some of the colors in some list of colors (for instance the default colors) one may use empty lists to force the non usage of the colors whose order in the list of colors is the order of these empty lists in the array of integers to be emphasized.

```
Example

gap> m3 := Filtered([1..40],i->i mod 3=0);
[ 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36, 39 ]

gap> m5 := Filtered([1..40],i->i mod 5=0);
[ 5, 10, 15, 20, 25, 30, 35, 40 ]

gap> m7 := Filtered([1..40],i->i mod 7=0);
[ 7, 14, 21, 28, 35 ]

gap>
gap> arr := [[],[],m3,[],m5,[],m7];;
gap> tkz:=IP_TikzArrayOfIntegers([1..40],10,rec(highlights:=arr));;
```

31	32	33	34	35	36	37	38	39	40
21	22	23	24	25	26	27	28	29	30
11	12	13	14	15	16	17	18	19	20
1	2	3	4	5	6	7	8	9	10

3.4 Functions to deal with colors

For the moment we only provide one function, which shuffles colors from lists of colors.

3.4.1 Shuffle colors from lists of colors

```
    ▷ ShuffleIP_Colors(mat) (function)
```

The argument mat is a list of lists of colors of the same length. The output is obtained by concatenating the transposed of mat.

```
Example

gap> ShuffleIP_Colors([IP_ColorsRedTones,IP_ColorsCompBlueTones]);

[ "red", "-blue", "red!50", "-blue!50", "red!20", "-blue!20",

"red!80!green!50", "-blue!80!red!50", "red!80!blue!60", "-blue!80!green!60"

]
```



Chapter 4

Visualization of the pictures created

This chapter describes two easy ways to visualize the images created by using the IntPic package. Both require LATEX and some LATEX packages, such as Tikz and pgf, to be installed and working. One of the ways we will describe is almost completely automatic. It makes use of the function Splash, borrowed from the Viz package. The other is not so automatic but has the advantage of not requiring other packages, besides the LATEX ones, and should work in any operation system.

4.1 Viewing using Viz

Producing and displaying a picture from a tikz string tkz may me achieved in a simple way. (Warning: extensive tests have only been done with Linux.) One just have to type the following:

```
IP_Splash (tkz);
```

A picture is popped up after this use of the function IP_Splash.. To see the name of the temporary directory created to perform the computations, and thus being able to copy the files involved to any other place, one should set the info level InfoViz to 1 or more. The following example illustrates this and the use of some options of the function IP_Splash. For instance, the pdf viewer can be changed.

```
infoviz: temporary directory

gap> SetInfoLevel(InfoViz,1);
gap> IP_Splash(tkz,rec(viewer:="okular"));
#I The temporary directory used is: /tmp/tmJcpphI/
```

The temporary directory /tmp/tmJcpphI/ contains the file and vizpicture.tex. The file vizpicture.tex is the LATEX document to be processed. Other files, namely the vizpicture.pdf are created by the pdflatex command that is called by the IP_Splash function.

Warning: In the case of large pictures, it may happen the LATEX memory being exceeded. In this case, no image is produced and the user is not warned.

4.2 Viewing without using Viz

This section describes a way to visualize images without sing Viz. Besides being useful in the case of not having a working copy of Viz, it is rather convenient when the decision of where to save the pictures is made. In this case, you may start your gap session in the desired place, the working

directory. Furthermore, if your intention is, for instance, to include the images in a document, you may just decide the name for the file containing the tikz code and let your document input it. The glogal variables IP_Preamble and Closing can be used to pruduce a complete LATEX document rather than only the tizk code for the picture. The document may then be processed by using pdflatex and the picture viewed by using some pdf viewer. The pdf produced can be included in a LATEX document instead of the tizk code. In the later case, the code is processed each time the document is processed, which should perhaps be avoided in the case of large images.

Note the use of the preview package, which is used to produce the complete picture without having to pay attention to the paper size nor to crop the image. It is useful for viewing purposes and also to include the pdf file produced in a LATEX document to be processed with pdflatex.

```
gap> Print(IP_Closing);
\end{preview}
\end{document}
```

4.2.1 A complete example

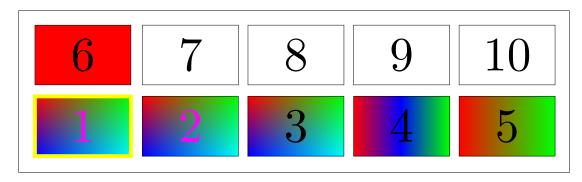
Admit you want to produce a document which contains the picture corresponding to the tikz code obtained through the instructions

```
instructions to obtain some tikz code

arr := [[1,2,3,4,5,6],[1,2,3,4,5],[1,2,3,4],[1,2,3],[1,2],[1]];;

tkz := IP_TikzArrayOfIntegers([1..10],5,rec(highlights:=arr));;
```

The picture is:



The elements of the set [1,2,3,4,5,6] are highlighted using the first color (red); those of the set [1,2,3,4,5] are highlighted using the second color (green); those of the set [1,2,3,4] are highlighted using the third color (blue); those of the set [1,2,3] are highlighted using the fourth color (cyan); those of the set [1,2] are highlighted using the fifth color (magenta); those of the set [1] is highlighted using the sixth color (yellow).

Let us explain how the six colors used for the cell containing 1 are distributed: upper left corner -- red; upper right corner -- green; lower left corner -- blue; lower right corner -- cyan; the number -- magenta; the border -- yellow.

The colors of the cell containing 2 and 3 are distributed in a similar way.

The colors of the cell containing 4: left -- red; middle -- blue; right -- green.

After the session listed below, the files tikz_pic_for_complete_document.tex and pic_for_complete_document.tex have been created in the current directory (that is, the one where the GAP session has started). For other directories, complete paths may have to be given.

```
the GAP session
gap> tikzfile := "tikz_pic_for_complete_document.tex";;
gap> file := "pic_for_complete_document.tex";;
gap>
gap> arr := [[1,2,3,4,5,6],[1,2,3,4,5],[1,2,3,4],[1,2,3],[1,2],[1]];;
gap> tkz := IP_TikzArrayOfIntegers([1..10],5,rec(highlights:=arr));;
gap>
gap> FileString(tikzfile,tkz);
642
gap> FileString(file,Concatenation(IP_Preamble,tkz,IP_Closing));
961
```

Executing something like

```
the pdf and the jpg of the picture

pdflatex pic_for_complete_document.tex

convert pic_for_complete_document.pdf pic_for_complete_document.jpg
```

the pdf and the jpg formats of the image have been created. The jpg format is useful to be included into an html document, for instance.

Note that the tikz code has been saved into the file tikz_pic_for_complete_document.tex. A complete example of a LATEX document follows.

```
\_ a LaTeX document \_
\documentclass{article}
\usepackage{amsmath}
%\usepackage[active,tightpage]{preview}
%\setlength\PreviewBorder{1pt}
\usepackage{pgf}
\usepackage{tikz}
\usepgfmodule{plot}
\usepgflibrary{plothandlers}
\usetikzlibrary{shapes.geometric}
\usetikzlibrary{shadings}
\usepackage{graphicx}
\author{Author}
\title{How to include images in a \LaTeX\ document}
\date{June, 2013}
\begin{document}
```

```
%\begin{preview}
\maketitle
Using the pdf file:

\begin{center}
  \includegraphics[width=0.80\textwidth]{../images/pic_for_complete_document.pdf}\
\end{center}

Using the PGF/TikZ code:

\begin{center}
  \input{../images/tikz_pic_for_complete_document.tex}\
\end{center}

If you want to scale this image, please chang the "scale" in the file
\textt{tikz_pic_for_complete_document.tex}}

%\end{preview}
\end{document}
```

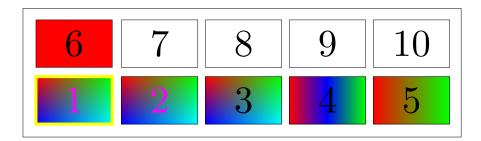
The output, after processing with pdflatex is as follows:

How to include images in a LATEX document

Author

June, 2013

Using the pdf file:



Using the PGF/TikZ code:

6	7	8	9	10
1	2	3	4	5

If you want to scale this image, please chang the "scale" in the file tikz_pic_for_complete_document.tex

4.3 Other examples of use of the IntPic package

4.3.1 Varia

The following example shows how to produce tikz code for a picture containing the odd integers from 801 to 999. Each line (except the highest) contains 15 cells.

```
gap> rg := Filtered([801..889],u->(u mod 2)<>0);;
gap> flen := 15;;
gap> twins := Filtered(Primes, p -> p + 2 in Primes);;
gap> arr := [Primes,Union(twins,twins+2),Filtered(rg,u->(u mod 3)=0)];;
gap> tkz := IP_TikzArrayOfIntegers(rg,flen,rec(highlights:=arr));;
```

The picture obtained highlights the primes, the twin primes and the multiples of 3. As the twins are also primes, a gradient is used to highlight them. In this example the default list of colors is used.

861	863	865	867	869	871	873	875	877	879	881	883	885	887	889
831	833	835	837	839	841	843	845	847	849	851	853	855	857	859
801	803	805	807	809	811	813	815	817	819	821	823	825	827	829

The same computations, but defining other color lists.

```
gap> cls := IP_ColorsCompRedTones;;
gap> rg := Filtered([801..889],u->(u mod 2)<>0);;
gap> flen := 15;;
gap> twins := Filtered(Primes, p -> p + 2 in Primes);;
gap> arr := [Primes,Union(twins,twins+2),Filtered(rg,u->(u mod 3)=0)];;
gap> tkz := IP_TikzArrayOfIntegers(rg,flen,rec(colors := cls,highlights:=arr));;
```

861	863	865	867	869	871	873	875	877	879	881	883	885	887	889
831	833	835	837	839	841	843	845	847	849	851	853	855	857	859
801	803	805	807	809	811	813	815	817	819	821	823	825	827	829

```
gap> cls := IP_ColorsDGrayTones;;
gap> rg := Filtered([801..889],u->(u mod 2)<>0);;
gap> flen := 15;;
gap> twins := Filtered(Primes, p -> p + 2 in Primes);;
gap> arr := [Primes,Union(twins,twins+2),Filtered(rg,u->(u mod 3)=0)];;
gap> tkz := IP_TikzArrayOfIntegers(rg,flen,rec(colors := cls,highlights:=arr));;
```

861 863	865	867	869	871	873	875	877	879	881	883	885	887	889
831 833	835	837	839	841	843	845	847	849	851	853	855	857	859
801 803	805	807	809	811	813	815	817	819	821	823	825	827	829

```
gap> cls := ["blue","-blue","black"];;
gap> rg := Filtered([801..889],u->(u mod 2)<>0);;
gap> flen := 15;;
gap> twins := Filtered(Primes, p -> p + 2 in Primes);;
gap> arr := [Primes,Union(twins,twins+2),Filtered(rg,u->(u mod 3)=0)];;
gap> tkz := IP_TikzArrayOfIntegers(rg,flen,rec( colors := cls,highlights:=arr));;
```

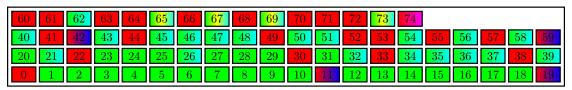
863	865	869	871	875	877	881	883	887	889
833	835	839	841	845	847	851	853	857	859
803	805	809	811	815	817	821	823	827	829

The following example uses the NumericalSgps package.

```
MinimalGeneratingSystemOfNumericalSemigroup(ns),
FundamentalGapsOfNumericalSemigroup(ns),
[ConductorOfNumericalSemigroup(ns)],
PseudoFrobeniusOfNumericalSemigroup(ns)];;
gap>
gap> tkz := IP_TikzArrayOfIntegers(flen,rec(colors := cls,highlights:=arr));;
```



Using the default colors



4.3.2 The banner

The code in the following example has been used to produce one possible banner for the homepage of the IntPic package. It is a nice picture that gives an idea about the primes less than 5000. Of course, other ranges could have been chosen. I warn the user that pictures involving a large amount of data may face the problem of exceeding TEX capacity...

```
Example
gap> row_length := 100;; # the maximum length of a row
gap> nrows := 50;; # the number of rows
gap> n := row_length*nrows;
5000
gap> ##compute the primes less than n
gap> # Primes is a GAP variable representing the list of primes less than n
gap> mp := Maximum(Primes);
997
gap> newprimes := [];;
gap> while mp < n do</pre>
   mp := NextPrimeInt(mp);
    Add(newprimes, mp);
> od;
gap> small_primes := Union(Primes, newprimes);;
gap> ##compute the first element of each pair of twin primes less than n
gap> twins := Filtered(small_primes, p -> IsPrime(p+2));;
gap> rg := [1..n];;
gap> arr := [Intersection(small_primes,rg),[],[],
          Intersection(Union(twins, twins+2), rg), [], [], [], [], [], [],
          [],[],[],[],[],Difference(rg,small_primes)];;
gap> tkz:=IP_TikzArrayOfIntegers([1..n],row_length,rec(highlights:=arr,
>
               cell_width := "6",colsep:="0",rowsep:="0",inner_sep:="2",
>
               shape_only:="",line_width:="0",line_color:="black!20" ));;
```

in kanturati kanturati kanturati da 1 seri seri termunik bilanggal sini sini ngga termunik dalam seri dalam bi Sanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggalanggala	
ri dion vile fine ciòn et e lles de la 2010 dell'esco ple villa dell'esti delle lige vell less cell dell'esc La residenti della comi dell'esco dell'esco dell'esco dell'esco dell'esco dell'esti dell'esco dell'esco dell'e La residenti delle si en esci dell'esco sello sello esco celle con la control elle solo dell'esco dell'esco dell'esco	
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ka bilak dena ya mishe nasa dalah ilah dalah biri belar belar bera dian dian dalah dalah dalah siya kabi biri Karayan anga mishi baga dalah dalah mesa dalah dalah biri dalah dalah dalah siya salah dalah belar dalah dalah	
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이 병에 위한 하는 없는 분인 원이 하면 일본 여는 여행 살면 살린 전에 하는 옷에 이를 잃어 하는 일은 일은	
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ka maka anga miah dago gogi gray inga abab kaug mhaa gara gaba nuga a na agak ayin abka kata dabba abba ka m	
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Chapter 5

The IntPic package options.

5.1 Available options

The list of allowed options, some of which already familiar from the examples, can be obtained as follows:

```
Example

gap> RecNames(IP_TikzDefaultOptionsForArraysOfIntegers);

[ "other", "colors", "highlights", "shape_only", "colsep", "rowsep",

"cell_width", "allow_adjust_cell_width", "scale", "inner_sep",

"line_width", "line_color" ]
```

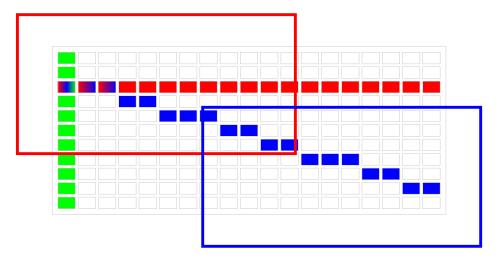
Its meaning is as follows:

- colors: any list of colors (to be used with the LATEX package xcolor)
- highlights: a list of lists of integers the elements of the first are colored by using the first color, etc. In cases of elements that appear in more than one list a kind of gradient (made with 4 colors at most) is used to fill the cell; the number may be printed with a fifth color and a sixt color may be used for the border.
- shape_only: an option to be used when only the shape is important. When true or "" is used, all the nodes are empty; using a symbol, for instance a *, this symbol is printed in all the nodes.
- colsep: the tikz matrix option column sep
- rowsep: the tikz matrix option row sep
- cell_width: the tikz matrix option minimum width
- scale: the tikz matrix option scale
- inner_sep: the tikz matrix option inner sep
- line_width: the tikz matrix option line width
- line_color: the tikz matrix option line color: the color of the cell borders

- allow_adjust_cell_width: the number of points per digit (to avoid discrepancies between the width of the cells when there are numbers with different number of digits to be printed). When the user sets the option cell_width, then allow_adjust_cell_width is automatically set to false
- other: if non empty, the complete tikz code has to be written (it may be useful when several images are to be produced otherwise, changing the tikz code would be enough)

```
Example ______
other := ["\\draw[postaction={draw,line width=1pt,red}] (-80pt,-8pt)
rectangle (16pt,40pt);","\\draw[postaction={draw,line width=1pt,blue}]
(-16pt,8pt) rectangle (80pt,-40pt);"]
```

Adding this option to one of the preceding examples, one obtains the following:



5.2 Default options

The defaults for the available options are as follows

• colors: ShuffledIP_colors

• highlights: [[]]

• shape_only : "false"

• colsep: "2"

• rowsep: "2"

• cell_width: "30"

• scale: "1"

• inner_sep: "3"

• line_width: "0"

```
line_color: "black"allow_adjust_cell_width: "10"negatives: [true]other: []
```

They may be consulted:

```
Example

gap> IP_TikzDefaultOptionsForArraysOfIntegers;

rec( allow_adjust_cell_width := "10", cell_width := "30",

colors := [ "red", "green", "blue", "-red", "-green", "-blue", "black!80",

    "black!30", "red!50", "green!50", "blue!50", "-red!50", "-green!50",

    "-blue!50", "black!70", "black!25", "red!20", "green!20", "blue!20",

    "-red!20", "-green!20", "-blue!20", "black!60", "black!20",

    "red!80!green!50", "green!80!red!50", "blue!80!red!50",

    "-red!80!green!50", "-green!80!red!50", "-blue!80!red!50", "black!50",

    "black!15", "red!80!blue!60", "green!80!blue!60", "blue!80!green!60",

    "-red!80!blue!60", "-green!80!blue!60", "-blue!80!green!60",

    "black!40", "black!10"], colsep := "2", highlights := [ [ ] ],

inner_sep := "3", line_color := "black", line_width := "0",

negatives := true, other := [ ], rowsep := "2",

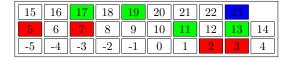
scale := "1", shape_only := "false" )
```

The user may want to change the defaults by editing the file options.gd in the folder gap. The changes are lost whenever any re-installation occurs. It is recommended that in this case a copy is made, although it is not guaranteed that it will work in the next release.

5.3 Ilustrating the use of options

The next example illustrates the use of the option negatives. The images produced are shown below.

```
gap> rg := [-5..23];;
gap> len := 10;;
gap> hg := rec();;
gap> hg.highlights:=[[2,3,5,7],[11,13,17,19],[23]];;
gap> tkz := IP_TikzArrayOfIntegers(rg,len,hg);;
gap> Print(tkz);
gap> #IP_Splash(tkz);
gap> hg.negatives:=false;;
gap> tkz := IP_TikzArrayOfIntegers(rg,len,hg);;
gap> print(tkz);
gap> rint(tkz);
gap> rint(tkz);
gap> Print(tkz);
```





Chapter 6

Usage of IntPic in connection with the numericalsgps package

This chapter describes functions to be used in connection with the numericalsgps package. We found it particularly useful to gain intuition that led to the obtention of the results stated in [DGSRP16].

6.1 Tikz code for drawing numerical semigroups

6.1.1 Tikz code for drawing numerical semigroups

▷ TikzCodeForNumericalSemigroup(arg)

(function)

The arguments (at most 4) are:

- 1. a numerical semigroup
- 2. (optional) a list whose elements are either
 - lists of integers or
 - one of the strings "pseudo_frobenius", "min_generators", "frobenius_number", "conductor", "special_gaps", "fundamental_gaps", "small_elements" (the default: used when no list is present) or
 - the string "ns_table" (the drawing obtained is a table whose top row corresponds to the threshold interval; as a side effect, if it is turned to "true", negative integers are not printed); alternatively, the option can be given in the usual way: rec(ns_table := true)
- 3. a record whose fields are
 - func -- a function name
 - (optional) argument -- an argument (that may be a function name also)
- 4. (optional) a positive integer -- if it is bigger than the conductor or biggest minimal generator, it indicates the number of cells 1 to be drawn and these are drawn in a single line; otherwise, it indicates the maximum number of cells per line.

```
gap> ns := NumericalSemigroup(5,7);;
gap> tkz := TikzCodeForNumericalSemigroup(ns,["ns_table"],rec(negatives:=false));
#I In order to highlight some element, please use a list with one or more of the options given as strings: pseudo_frobenius, min_generators, frobenius_number, conductor, special_gaps, fundamental_gaps, small_elements

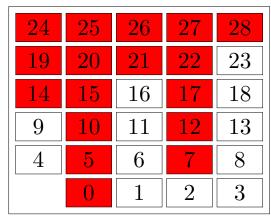
"%tikz\n\begin{tikzpicture}[every node/.style={draw,scale=1pt,\nminimum width\
=20pt,inner sep=3pt,\nline width=0pt,draw=black}]\n\matrix[row sep=2pt,column\
sep=2pt]\n{\node[]{24};&\n\node[]{25};&\n\\node[]{26};&\n\\node[]{27};&\n\\\node[]{28};\\\\n\node[]{19};&\n\\node[]{20};&\n\\node[]{21};&\n\\node[]{22};\
&\n\\node[]{23};\\\\n\\node[]{14};&\n\\node[]{15};&\n\\node[]{11};&\n\\node[]{11};&\n\\node[]{12};&\n\\node[]{12};&\n\\node[]{13};\\\\n\\node[]{4};&\n\\node[]{5};&\n\\node[]{6};&\n\\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2};&\n\\node[]{2}
```

```
gap> tkz := TikzCodeForNumericalSemigroup(ns,["small_elements"],
    rec(ns_table := true,negatives:=false));;
```

The following images are obtained from the tikz code above.

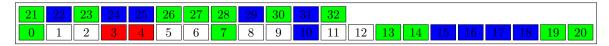
24	25	26	27	28
19	20	21	22	23
14	15	16	17	18
9	10	11	12	13
$\boxed{4}$	5	6	7	8
	0	1	2	3

gap> ns1 := NumericalSemigroup(3,5);;



Example

```
gap> IP_Splash(TikzCodeForNumericalSemigroup(NumericalSemigroup(7,13,19,23),
> [[3,4],"small_elements","fundamental_gaps"],20),rec(viewer := "evince"));
```



```
gap> ns := NumericalSemigroup(7,11,38,41);;
gap> highlights := ["conductor", "min_generators", "small_elements"];;
gap> options := rec(ns_table:=true,colors:=["blue", "red!70", "-red", "black!40"]);;
gap> tkz := TikzCodeForNumericalSemigroup(ns,highlights,options);;
gap> IP_Splash(tkz);
gap> tkz := TikzCodeForNumericalSemigroup(ns,highlights,rec(ns_table:=true));;
gap> IP_Splash(tkz);
```

38	39	40	41	42	43	44
31	32	33	34	35	36	37
24	25	26	27	28	29	30
17	18	19	20	21	22	23
10	11	12	13	14	15	16
3	4	5	6	7	8	9
				0	1	2

38	39	40	41	42	43	44
31	32	33	34	35	36	37
24	25	26	27	28	29	30
17	18	19	20	21	22	23
10	11	12	13	14	15	16
3	4	5	6	7	8	9
				0	1	2

6.1.2 Drawing a numerical semigroup

```
▷ DrawNumericalSemigroup(ns)
```

(function)

This function abbreviates the production of tikz code to display the numerical semigroup ns using some predefined options and elements to highlight (based on the ones of the above example). It also displays the image produced. Note that the production and displaying of the image depends on the function IP_Splash (which can be slow and depends on an appropriate configuration of the system). The output is the tikz code produced.

```
gap> m := 31;;
gap> small_gens := [m,m+1,m+2,m+3];;
gap> other_gens := List([1..Int(m/7)], k -> 7*k+m);;
gap> ns := NumericalSemigroup(Union(small_gens,other_gens));;
gap> DrawNumericalSemigroup(ns);;
```

```
| 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 | 101 | 102 | 103 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 116 | 117 | 118 | 119 | 120 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 130 | 13
```

6.2 Drawing sets of numerical semigroups

6.2.1 Set of numerical semigroups

```
⊳ SetOfNumericalSemigroups(arg)
```

(function)

This function is used to produce lists of numerical semigroups with a fixed genus or Frobenius number. They are filtered and ordered according to some criteria.

The argument is a record of options:

- 1. set -- a record whose possible fields are genus or frobenius
- 2. (optional) filter -- a record whose possible fields are genus, type and/or multiplicity and/or frobenius and/or embedding_dimension
- 3. (optional) order -- ("genus", "type", "multiplicity", "frobenius", "embedding_dimension")

```
gap> ls := SetOfNumericalSemigroups(rec(set:=rec(genus:=6),filter:=rec(type:= 2),
    order:="multiplicity"));;
gap> List(ls,MinimalGenerators);
[[ 3, 8, 13 ], [ 3, 10, 11 ], [ 4, 7, 9 ], [ 5, 6, 7 ], [ 5, 6, 8 ],
        [ 6, 7, 8, 9, 11 ]]
gap> ls := SetOfNumericalSemigroups(rec(set:=rec(genus:=6),filter:=rec(type:= 2),
    order:="frobenius"));;
gap> List(ls,MinimalGenerators);
[[ 3, 10, 11 ], [ 5, 6, 7 ], [ 5, 6, 8 ], [ 3, 8, 13 ], [ 4, 7, 9 ],
        [ 6, 7, 8, 9, 11 ]]
```

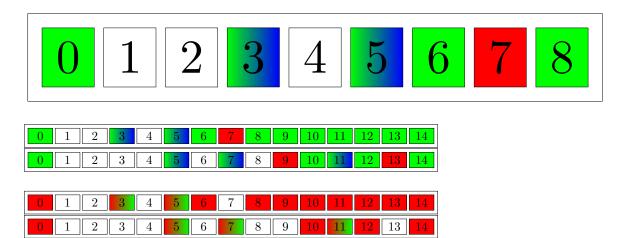
6.2.2 Draw a set of numerical semigroups

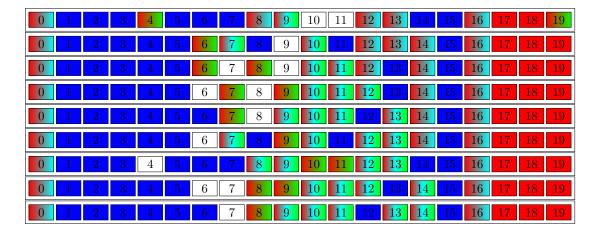
▷ DrawSetOfNumericalSemigroups(arg)

(function)

Produces a single image from the images of a set of numerical semigroups. The arguments (at most 3) are:

- 1. a list of numerical semigroups (given as a list or each given as argument)
- 2. (optional) an integer that (when present) determines the length of each line
- 3. (optional) a record whose fields are
 - (optional) splash -- which (when present) consists of a record of options for the Viz Splash function
 - (optional) highlights: a list to be passed to the function that produces the tikz code for each individual semigroup (whose aim is to say which elements are to be highlighted)





The following example helps in the understanding of the colors present in the first line of previous figure.

```
gap> ns := NumericalSemigroup(4,9,19);;
gap> SmallElements(ns);
[ 0, 4, 8, 9, 12, 13, 16 ]
gap> MinimalGeneratingSystem(ns);
[ 4, 9, 19 ]
gap> ForcedIntegersForPseudoFrobenius(PseudoFrobeniusOfNumericalSemigroup(ns));
[ [ 1, 2, 3, 5, 6, 7, 14, 15 ], [ 0, 8, 9, 12, 13, 16 ] ]
```

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