

**PRELIMINARY INDIRECT MEASUREMENT OF
COSMIC-RAY PROTON SPECTRUM USING EARTH'S
 γ -RAY DATA FROM *FERMI* LARGE AREA TELESCOPE**

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**A THESIS SUBMITTED IN PARTIAL FULFILLMENT
OF THE REQUIREMENTS FOR
THE DEGREE OF MASTER OF SCIENCE (PHYSICS)
FACULTY OF GRADUATE STUDIES
MAHIDOL UNIVERSITY
2021**

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ACKNOWLEDGEMENTS

First of all, I would like to express my special gratefulness to my advisor Asst. Dr. Warit Mitthunsiri for the wisely advise, providing guidance, and constant support through the program. Thanks for instructing me how to manage with a towering stack of data, challenged coding and for all Python tips. This work would not finish without many suggestions from Prof. David Ruffolo, the head of the space physics and energetic particles laboratory for helping me successfully achieve the goal for each phase of this project and for a great opportunity to work on this field of Physics. Particular thanks to the other co-advisor, Dr. Alejandro Sáiz, the first teacher who has inspired me on computer simulation including helpful suggestions and discussions relating to this work. Many thanks to Dr. Waraporn Nunthiyakul for the cutoff-rigidity program and various tricks of FLUKA simulation, valuable comments about this work and for sharing excellent experiences. I deeply appreciate my Ph.D. Committee for their time and scientific expertise to review my work.

Thanks to the members of space physics laboratory for academic discussions and sharing experiences which was an essential ingredient in the completion of this thesis. Thanks the Department of Physics, Mahidol University for an exceptional experience. Last not least, sincere appreciation goes to my colleagues and friends for their support and encouragement throughout. I acknowledge the financial support I received over these years to the Science Achievement Scholarship of Thailand (SAST) and the Thailand Research Fund (TRF). Ultimately, I would like to thank my parents, my sister, and brothers for their constant support and patient.

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ABSTRACT

Cosmic rays (CRs) are high-energy particles, mostly protons, propagating in space. The rigidity (momentum per charge) spectrum of CRs is well described by a power law for which the spectral index is approximately 2.8 around 30 - 1000 GV. Recent measurements by PAMELA and AMS-02 indicate an abrupt change of the CR proton spectral index at about 340 GV. When CRs interact with the Earth's upper atmosphere, γ rays can be produced and detected by space-based detectors. Here we use the Earth's γ -ray data collected by the *Fermi* Large Area Telescope along with a proton-air interaction model to indirectly determine the CR proton spectral index and compare against observations by other instruments.

KEY WORDS: EARTH'S GAMMA RAYS / COSMIC RAYS/ GEOMAGNETIC FIELD

64 pages

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CHAPTER I

INTRODUCTION

1.1 Overview

The space is full of questionable amazing phenomenon starting from why we have day and night, why the star bright to the advance question about existence of the dark matter. This influence to the mankind to start asking how it happen. Human curiosity bring us so far that now we could observe the sky with high resolution technique. However, the research to gather new knowledge by studying the space is endless and the answering one thing usually bring another mystery. Study of physical science also drag the technology for further step because the limitation of the instrument or technique to explore the nature is another challenging task.

Astrophysical research boundary is expanding through time pass by because the exploration of one thing does open the new door with the dark room waiting for human to shine a light to explore. There are various branch of astrophysical science from theoretical foundation, simulation and experimental physics where they are compliment each other for pushing the frontier of the human knowledge. To study high energy particle accelerators in the universe, the possibility of probing the source is nearly impossible in terms of current technology and resource that required to reach multiple galactic sources that could produce high energy particle called cosmic-rays (CRs). Nevertheless, the technology of observing the particles that arriving the Earth is more plausible for the scientist.

The way to observe cosmic-ray (CR) particles has divided into two ways. One way is measuring the incoming charge particles on ground with a ground-base detector. Alternative way is gathering CRs on the space or basically orbiting spacecraft. Performing analysis on CRs data allow us to interpret the physical properties of CRs particle for both quantatively and qualitatively by taking

simulation and experimental results to compare.

Typically, the spectrum of the CRs would follow the power law with a specific spectral index depending on the rigidity of the charged particles where it was accelerated by a specific source. It is obvious that there will be multiple sources of the CRs in the space including unknown sources. The characteristic of spectrum would be indicated by the source from theoretical simulation and derivations. Consequencely, changing of the spectral index from one rigidity to another rigidity will find the discontinuity if there are the translation from one source type to another source from the superposition of multiple spectrums.

Fermi-LAT has been launched into the sky and orbiting around the Earth and looking around the space in γ -rays regions. It found that the ring of brightness around the Earth's limb where the major factor that cause this phenomenon is the interaction of incoming CRs with the Earth's upper atmosphere as analyzed in Abdo et al. (2009). Then the spectrum of γ -rays that was induced by the incoming CRs highly related on the spectrum of CRs.

The first indirect measurement was conducted with 5 years of observations and indicate that there is breaking of spectral index around 302 GV with a significant level 1σ . The significant level at this stage is not so strong to conclude the study. The reasons probably came from the nature of the CRs if there is no discontinuity in the incident CRs spectrum, the indirect could measurement distort the information so that the significant could be reducing or the exposure time during the observations is still not enough. In order to confirm that we did our best on the data collection side, performing the analysis with more data could also put us out doubt for the last clue.

1.2 Objectives

The objectives of this study are to

- To indirectly measure the cosmic ray proton spectrum in rigidity range gigaelectronvolt (GV)

- To put the weight on the previous study with more dataset
- To improve the optimizaiton technique by using heuristical methodology
- To reduce the calculation time by inventing a whole new parallel code in low level from scratch

1.3 Outline of Thesis

The dissertation would provide the various information from the overview introductory context to the technical detail that employ in this study as well as the result and interpretation. It is structured as follows.

Chapter I will introduce the reader about the overview of the long track from the historical analogy and zooming into the specific branch of research to get the reader to see where we are and what we are doing to fullfill the frontier of the research.

Chapter II is the background knowledge that will be used in this study. This chapter also have a brief of history in cosmic ray research community which contains an important finding and the impactful experiment that bring us to this far in the research field. Some theoretical detail will be provided on par with the historical discovery but the subchapter of the specific topic will describe more detail in depth of astroparticle physics that involving the high energy physics. Not only the concept of physical process but this chapter also have the apparatus informations where the majority of the content covering the detector part in the spacecraft to demonstrate how the apparatus gather the γ -rays data.

Chapter III is mainly consist of multiple literature reviews involving the study to clarify the theoretical idea as well as for filling the fundamental concept that takes reader to understand the next chapter in detail.

Chapter IV would cover the article reviewing. The content is staring from pioneering article of the field and the evolution that inspire this work.

Chapter V consists of datasets selection, flux calculation , problem optimizaiton and interpretation.

CHAPTER II

BACKGROUND

2.1 Cosmic-ray

This section consists of historical discovery, from the origin on this field of study until the latest impactful experiment. Not only historical content, it also contains the physical explanation with phenomenon that involving the CR research.

2.1.1 History

In 1909, the famous experiment that pioneer the study of CR has been led by Theodor Wolf who take conduct the experiment of altitude variation by taking the apparatus to measure the rate of ionization from the ground to the top of the Eiffle Tower in Paris (Gray (1949)). The result shown that there the ionizaiton rate was slightly increase when the altitude is higher which gives the clues that the origin of cosmic-rays was came from the outer space rather than Earth's inner shell. Hörandel (2013)

However, the experiment of measuring the affect of altitude variation with a tiny altitude scale comparing to the Earth's atmosphere would not enough to consolidate the theory. In the same year, the balloon with a similar instrument has been released up to 1.3 kilometers by Karl Bergwitz to put more weight on the first experiment. They found that the ionization has increased by a quater comparing to ground level (De Angelis (2014)). Three years later, suicidal investigation was conducted by an Australian gentleman who brought the detector and himself to fly with the balloon. His name is Victor Hess, people might have no doubt why this name went so famous because he risk his life with the experiment and he was flying over 5 kilometers above the ground (Hess (1912)). Definitely, the result is strongly significant and impactful to the astrophysical research community. Risking life In 1914, Werner Kolhörster repeated the balloon experiment with higher altitude

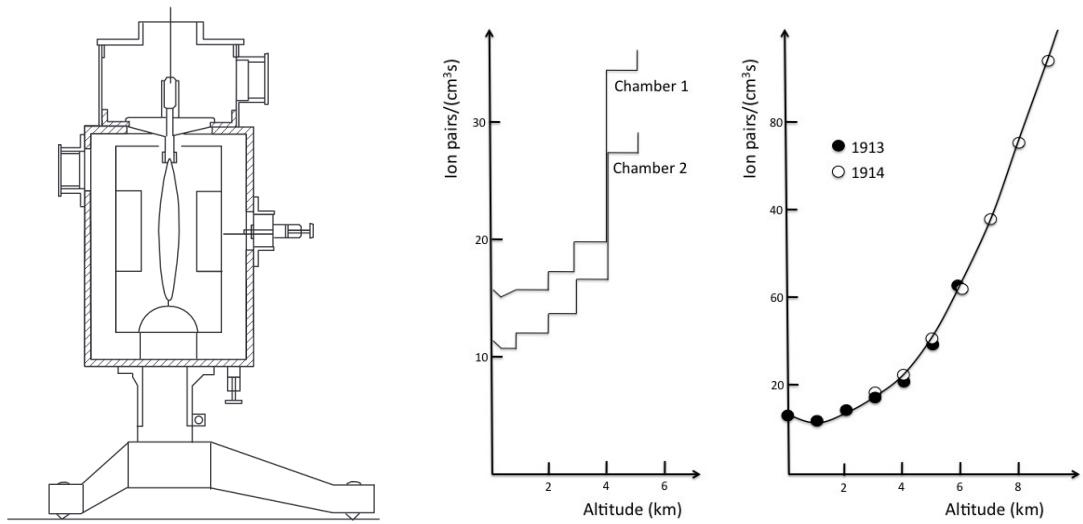


Figure 2.1: Wulf's apparatus and the balloon experimental results

which around 9 kilometers from the sea level and the ionization rate still does increase when the balloon flown higher. This emphasize that the source of those ionizing ray came from Earth's upper atmosphere or the outer space.

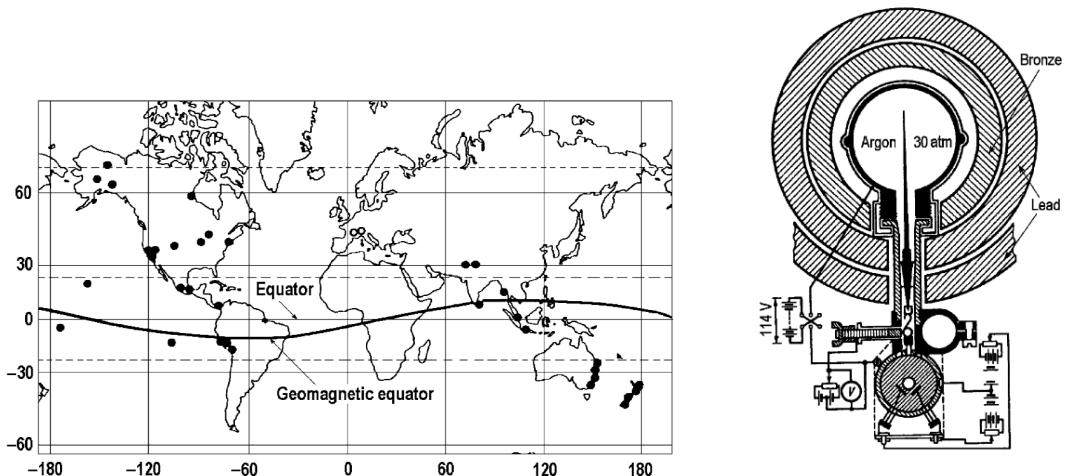


Figure 2.2: Clay Experiment of geographical variation

Not only the altitude variable that related to the intensity of the CRs, but the geographic location of the observation also does affect to the measurement.

The first experiment has been done by John Clay who sailed the ship across the ocean from Holland to Java (Clay (1927, 1928)). The geographical locations that used to measure the CR intensities and the apparatus schematic draft is shown in Figure 2.2. The result shows that the further from equator, the higher CR intensity. Another exploration for the geographic variation was done by John Compton in the following five years. He basically sailed the ship from Sydney (northern hemisphere) to Vancouver (the southern hemisphere) for various seasons during 1936 to 1937 back and forth (Compton & Turner (1937)). The Figure 2.3 demonstrates the latitude variation and the seasonality effects of the multiple trips from the experiment.

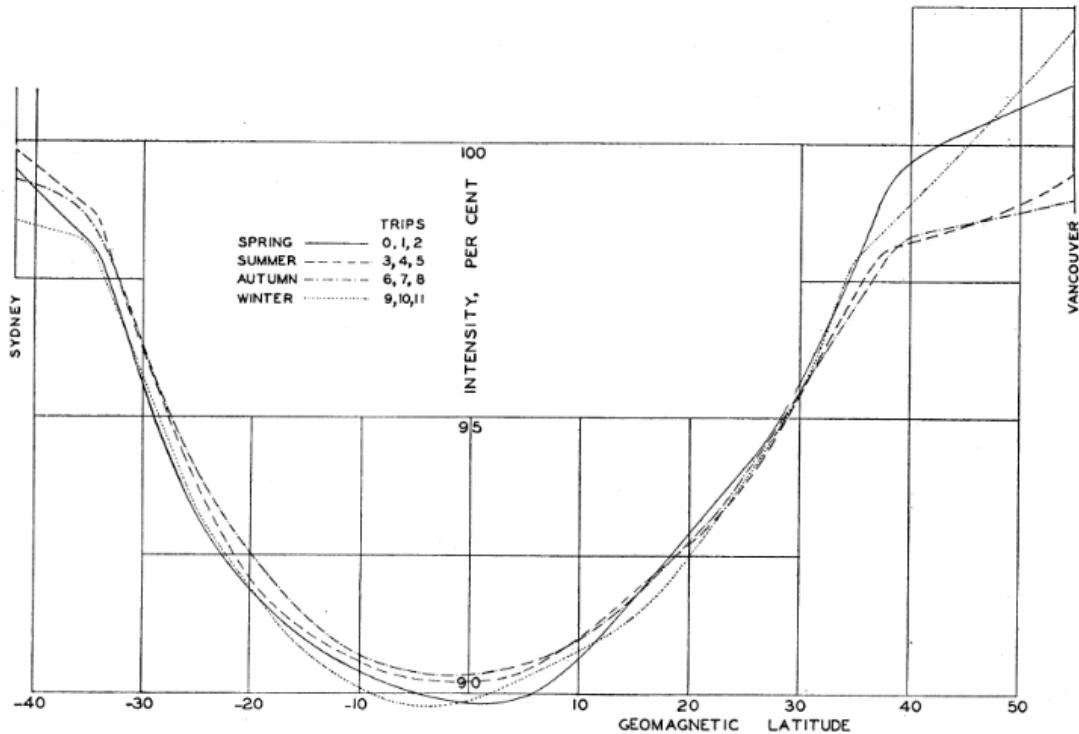


Figure 2.3: Latitude variation for various seasons (Compton & Turner (1937))

The first interpretation study from the discovery has been done by Carl Störmer. The explanation of the CR's altitude variation came from the trajectory of CR particles due to geomagnetic field (Störmer (1934)). In that period, the topic of geomagnetic field and the effects of CRs was quite famous. Another impactful study of the CRs trajectory and the relevant of Earth's magnetic field was conducted

by Bruno Rossi for predicting an asymmetry of the East-West distribution of CR spectrum because the primary CRs does have a positive or negative charge then the cyclic moving direction of the particle was induced by Lorentz force where the direction of the Earth's magnetic field could be identified to determine the direction of the charged particles (Rossi & Greisen (1941)).

The ground based detector is a great option for detecting the CRs where it include primary and secondary CRs. However, investigating the primary CRs is a challenging topic for ground based detector especially for low energy particles. Another interesting option to inspect the asymmetry of East-West could be done by using space based detector that orbiting around the Earth's at some radius in the higher altitude and definitely it would face a lower atmospheric density which consider to be an interesting choice to study the CRs with a lower effects of atmospheric interaction. In 2008, *Fermi* Large Area Telescope (LAT) has been launched to observed γ -ray and lightweight lepton particles which basically are electron and positron. The East-West effects from geomagnetic induction was also emphasized by *Fermi*-LAT.

2.1.2 Physical properties

CRs are high energy particles that propagating through the space. The momentum of the particles came from various acceleration mechanism base on where it from such as supernovae, active galactic nuclei, quasars and gamma-ray bursts. The composition of CRs consists of 90% protons, 8% alphas and other nuclei of heavier elements (Dembinski et al. (2017)). Experimentally, many observations indicate that the spectrum of CRs for all particles and individually does follow the power law in rigidity (momentum per charge) with a specific spectral index depends on their energy range. Theoretically, the observed spectrum with a broad energy range would represented the superposition of arrival CRs with a diverse producers where each producer has their own specific character which is spectral index. By the end of the day, it is barely possible to distinguish the origin of CR particles one by one. Then it is more plausible to provenance the origin of CR particles in the macroscale rather than inspecting in the microscale.

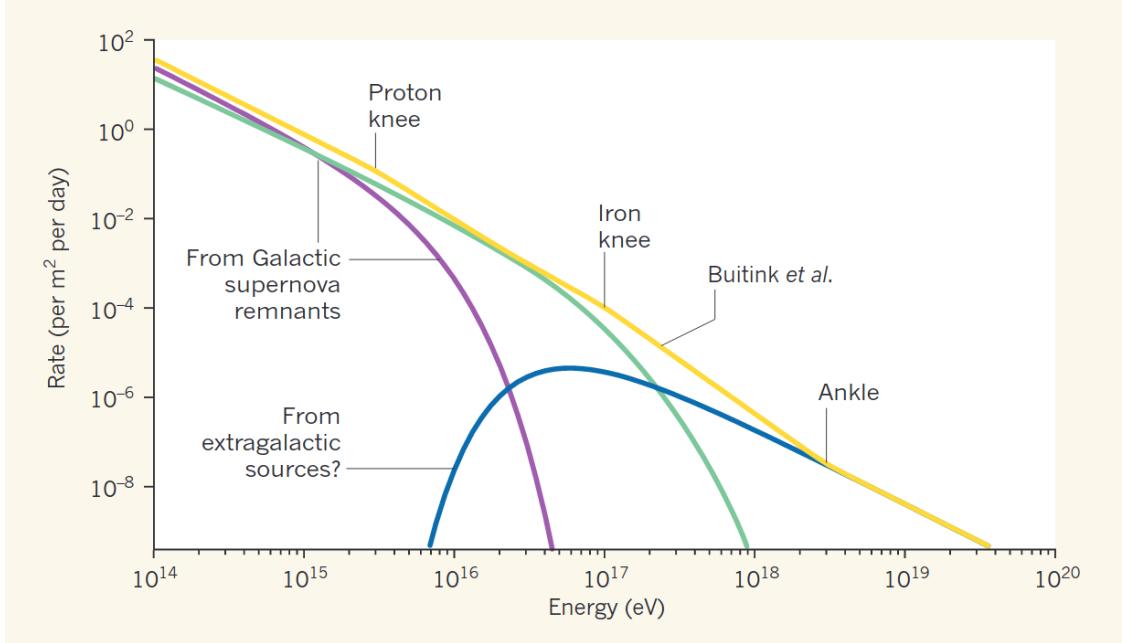


Figure 2.4: Superposition of CR spectrum (Taylor (2016))

As mentioned in an early paragraph, each source of CR does reflect their own specific spectral index in the arrival CR spectrum. In order to validate the theoretical assumption, putting the simulation or calculation of each sources and check with the real data does compliment experimental observations. The superposition of various sources that yield a discontinuity of the spectral indices has been exploited in some energy ranges. Two well known breaking points are knee and ankle where it located in the energy order around 10^{15} eV and 10^{18} eV sequentially. Approximately, the rate to find one particle at knee is around one particle per square meter per year and the possibility that the apparatus could detect the particle in energy at ankle point is roughly one particle per kilometer per year. Figure 2.4 illustrate the concept of superposition from various sources and yield the arrival CR spectrum with a breaking spectral indices.

Not only the below ankle energy that has an interesting properties, but the CR that has energy beyond the ankle energy also has an identical properties. It knowns as "ultra-high energy cosmic rays" (UHECR). One interesting point is that it does not that far from ankle in term of rigidity magnitude which higher around 1 or 2 order of magnitude. The widely known explanation why it could not go so

far is the Greisen–Zatsepin–Kuzmin limit (GZK limit). The theory provides the description why it the UHECR could not propagate though the space but please note that some sources still could produce such a UHECR but the main issue here is the space does not empty. It contains some intermediate matter or dust and the microwave background radiation which it is believed that it came from the residue of the Big Bang or some great explosion or expansion of the space that human never saw it (at least in the human lifetime). The main calculation of the CR kinetic energy limit from GZK was considered only proton particles and the main interaction that makes it stop is basically from the interaction with microwave background radiation that almost perfectly isotropically propagating in the space with an order of traveling proton around hundred light years in the space (Greisen (1966)). The way of this kind of interaction not only does slow down the CR proton by producing neutral pion where it mostly decay into a pair of γ -rays but it could also yield a neutron with a charged pion. Hence, it is also answer why we could see such a high energy neutron that does not only produced in the sky (shower effects) albeit it does not have any charge to be accelerated in the famous acceleration mechanism such as shock acceleration.

The types of CRs could be divided into two kinds based on how they were produced which are

1. **Primary cosmic rays:** they mostly be produced from the Solar system, somewhere in the Milky Way, extragalactic sources and many more. When they interact with the Earth's atmosphere, with the hadronic interaction with the air molecules, they produce the secondary CR particles.
2. **Secondary cosmic rays:** as mentioned in collapsing of the primary CRs, secondary CRs consists of many particles from lightweight leptons to medium weight leptons and from mesons to hadron particles as well. The interaction of the proton with the atmospheric molecule looks simple but the precise calculation from derivation is extremely complicated since there are endless possibility of the (Feynman) path that also produce another products with a certain probability. By the end of the day, we definitely got a few certainties

of particles from their likelihood of the occurrence from the collision which mainly are electrons, positrons, muons, pions and photons as demonstrated in Figure 2.5.

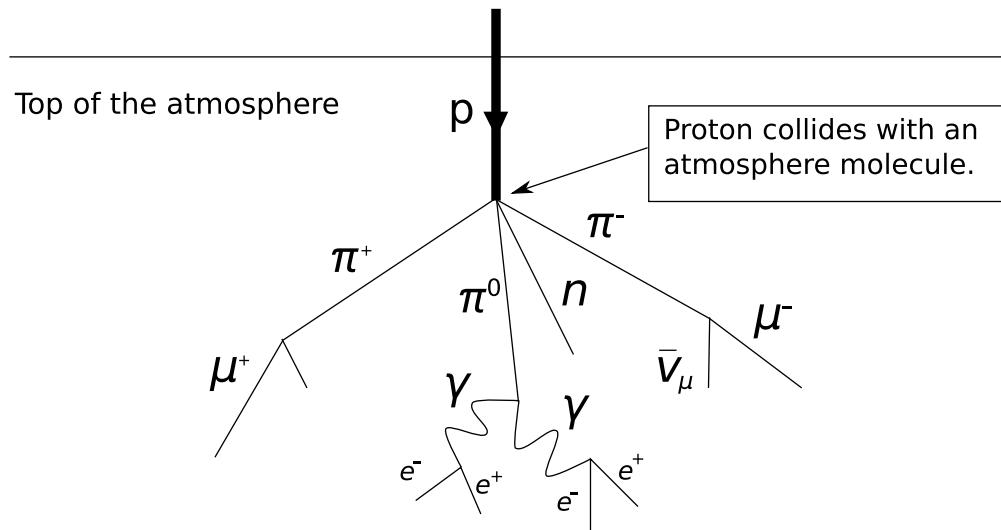


Figure 2.5: Cosmic rays shower from collision of primary CR with the atmospheric molecule

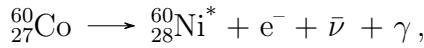
2.1.3 γ -ray production

The production of γ -ray particles happens all the time. It is mandatory to understand how a photon could gain a very high momentum from the nature. The procedure to acquire all those kinetic energy is quite different from how a charged particle obtains their momentum because a charged particle could earn their kinetic energy during their trip of propagating through the space with a Lorentzian force. The γ -rays mostly have only one chance to pick their kinetic energy and it happens when it was produced because it is barely interact with any other particles in the space especially high energy γ -ray. The scenarios that makes photon hold a high energy are listed in the following bullets.

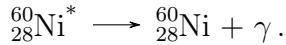
Mechanism of γ -ray producing

- **Decaying of unstable matter:** Radioactive decay is one of the most well known phenomena for the γ -decay mode. One example of the heavy ion decay

is the cobalt-60. It decays into excited state of nickle as



then the excited nickle decay another γ -ray to make it to the stable state



The famous decay of a lower level from a small nuclei that consists of two quarks called "meson". To be more precise, it is known as the pion decay. The path diagram is demonstrated in Figure 2.6 where the neutral pion from the collision process that interact via Yukawa's interaction. The neutral pion itself does not stable then it would have a short amount of lifetime before it dominately decays into two high energy photons. Definitely, neutral

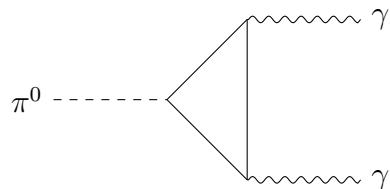


Figure 2.6: Feynman's diagram of neutral pion decays into two γ -rays

pion also could yield one γ -ray and a pair of lightweight leptons, a couple pair of lightweight leptons or even just a pair of lightweight leptons and much more as long as it conserve the momentum, energy and the quantum numbers. The main reason why the majority of their decaying process does yield only photons because the scattering amplitude as the Figure 2.6 does hold a branching ratio around 0.98823 and the rest of them is smaller than 1%. Another interesting property of this decay mode is the momentum vector of their pair γ -ray hold an opposite direction with the same amplitude in the reference frame.

- **electron–positron annihilation:** In the universe, there are some probability of the electron and positron was forced to face each other by some chance from the electromagnetic force or randomly found each other. The interaction when they facing each other dominate by electromagnetic interaction and definitely require a photon as a mediator to allow them talk to each other in

quantum electro dynamics point of view. Definitely, there is a change when those pair of leptons decide to annihilate into high energy photons without running any physical laws. Nevertheless, other kind of a pair of leptons like muon technically could deform into two photons with much higher energy because their rest mass is higher. Surely, a pair of Tau is also allow to produce a pair of photons. However, the lifetime of those medium-weight and heavy-weight leptons could not last that long to survive in practical. The simplest Feynman's path of annihilation of leptons into a pair photons is illustrated in Figure 2.7 from light to heavy leptons sequentially.

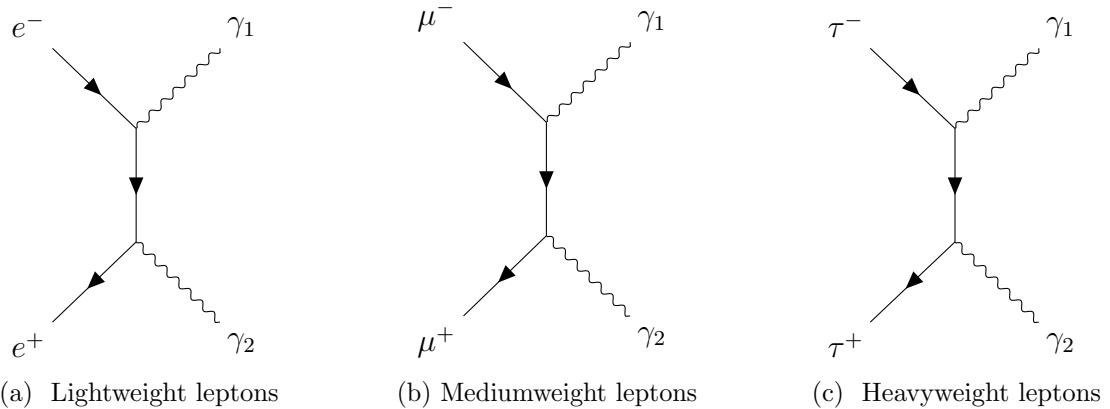


Figure 2.7: Major lepton annihilation path diagram

- **Synchrotron radiation& Bremsstrahlung radiation:** The phenomena of turning momentum direction of charged particle or accelerate into another direction shares a similar description. Conservation of momentum has come into place when considering the bending charged particle that would emit the photon. Regarding the incoming direction of a charged particle and then turning it direction by $\pi/2$ radians. The question that comes into mind is where does those initial momentum in an incoming direction does since the momentum is conserved along the cartesian direction, not only the magnitude. Now the clue is here, they have to emit the photon to converse the momentum of the system.

Let walk through the first example called synchrotron radiation. Keeping some

charged particle circulating around the donut-like apparatus have some cost to pay to make them stay without escaping the tunnel. Unquestionably, dragging some moving particle circulating around some point requires a centripetal force. In this case, applying electromagnetic force without touching it would yield a radiation called synchrotron emission.

The second mechanism is Bremsstrahlung, where a charged particle or typically an electron moving path close to some opposite charged particle or typically a proton. The explanation from Coulomb's law would cover this scheme for the definition that the force is inverse proportional to the distance between two charges. Then moving pass by an opposite charged particle does induce the electron bending and emit the photon because the explained reason from the previous paragraph. This mechanism happens when an CR electrons moving through the matter of Sun's chromosphere and interact with a positive charged and produce some high energy photon but usually it produce in the X-ray energy range.

Mechanism of γ -ray gaining momentum

Even though, γ -ray usually does not prefer to talk to another fundamental particles because scattering amplitude of their interaction is pretty low. Nonetheless, there are some scenarios that γ could gain more kinetic energy and losing their kinetic energy when they traveling in the universe.

- **Inverse Compton scattering** The scattering of a photon (massless particle) with an electron (massive particle) could occur during their trip. Equation 2.1 demonstrate the symbolic relation of the scattering with the electromagnetic interaction and yield the same particles as an incoming particles.

$$e^- \gamma \rightarrow e^- \gamma \quad (2.1)$$

Interaction between an electron and a photon could make them converting the momentum via the scattering process. Since the system momentum has

to be conserved, then there will be one losing momentum and another one gaining momentum or kinetic energy. Suppose one photon is traveling and hit electron or a charged particle, it could transfer the kinetic energy to the particle and their wavelength will be longer. In another word, it is lossing the kinetic energy. On the other hand, this scenario could happen in the opposite way. There is situation when a high energy electron interacting with the photon and turn over its kinetic energy to the photon. After that, a photon could gain more kinetic energy during their trip. The latter scenario is called "Inverse Compton Scattering". The most likelihood choice of interaction of the scheme could be represented in Feynman's path as in Figure 2.8.



Figure 2.8: Trivial Feynman's path of (Inverse) Compton scattering

γ -ray production plants

- **Supernova remnants (SNRs) and molecular cloud:** The supernova explosion is a huge expansion from that approximately expanding as a spherical shell that sweep the inter stellar medium (ISM) and decelerate at some radius after the enlargement. The kinetic energy that transfer from the momentum in the radial axis was modeled and believed to be the kinetic energy of the cosmic ray particles. There are three major processes that involves in this phenomenon which are nuclear pion production, nonthermal electron bremsstrahlung, and Compton scattering (Dermer & Powale (2013)). Last but not least, the shock acceleration could play an important role for this phenomenon.

- **Diffused γ -ray emission from galactic plane:** One of the bright source

that does not locate too far from our territory is the galactic plane. The first reasonable explanation is the distance of the productive objects does not far from Earth comparing to other extragalactic sources. In addition, there are many interesting CR sources in our galaxy. It might be pulsar, some flare of the event of an explosion and so on. The plot that shows the brightness of the galactic plane comparing to the outer space is shown in Figure 2.9.

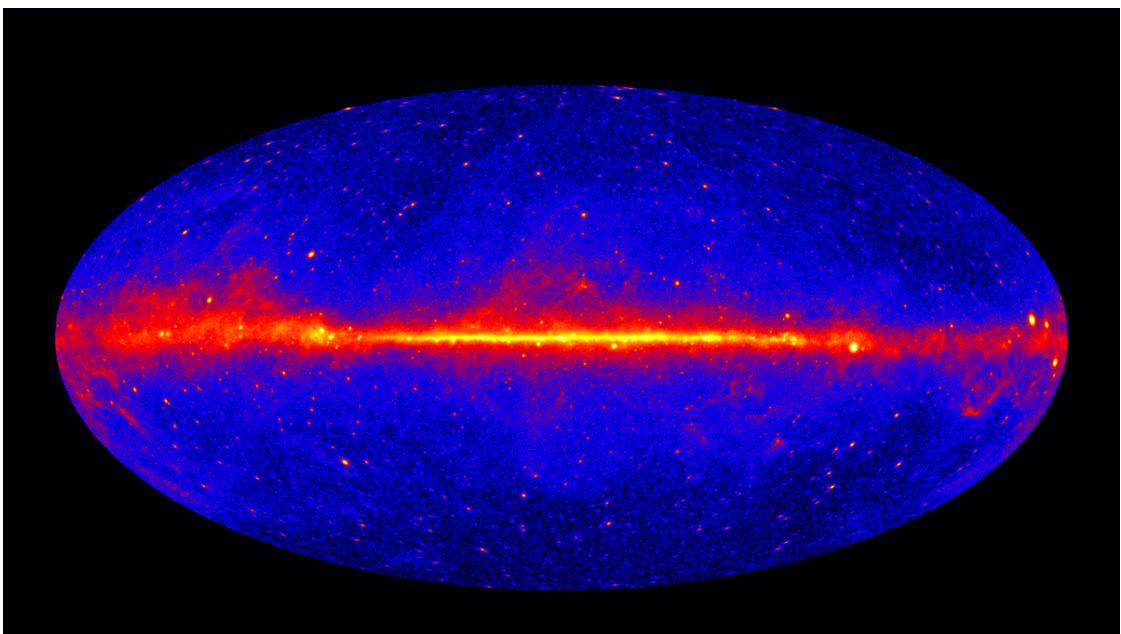


Figure 2.9: Intensity of γ -ray > 1 GeV in galactic coordinate (Image credit: NASA/DOE/*Fermi* LAT Collaboration)

- **Pulsar and Active Galactic Nucleus (AGN):** Another source of the brightness in Figure 2.9 is the bright dots with a different solid angle width in the sky. The majority of those spots consists of γ -ray from pulsar's periodic emission and AGN or extremely luminous AGN namely "Quasar". The cycle of the lighthouse effects from pulsar is very robust as in the scale of atomic clock. Both of them has a very high magnetic field strength. Emissive photons from those sources would be a very high energy due to the acceleration of a charged particle near magnetic poles or the outer.
- **Earth's limb γ -ray production:** The closest γ -ray source is our Earth's atmosphere. To be more precise, the Earth's upper atmosphere is super bright in γ -ray exposure. The main reason that cause the shining of Earth's limb

does come from the collision of the CR's massive particle such as protons and alphas. The interaction of those high energy CR massive particles yield many more particles and main contribution of the γ -ray dazzling came from the neutral pion decay which is the product from the collision process.

2.2 *Fermi* Large Area Telescope (LAT)

One of the famous space telescope that does see the sky in the visible wavelength is *Fermi* Large Area Telescope (LAT). Formerly, it was called Gamma-ray Large Area Space Telescope (GLAST). The mission of the satellite is to collect high energy photon data or γ -ray and it technically could detect the lightweight lepton particles namely electron and positron. The orbiting radius is around 550 kilometers from the sea level. It is designed for observing the full-sky in γ -ray region. It also attach the Gamma-ray Burst Monitor (GBM) to study gamma-ray bursts for seeking an exotic event. The telescope was launched in 11 June 2008 at 16:05 UTC or 21:05 Bangkok time by abroading with Delta II 7920-H rocket.

2.2.1 Overview

According to Figure 2.10, each components of the *Fermi* telescope was designed for a purpose since there is no ideal detector module that could detect kind of particles. There are two main parts where the first part if the major component called Large Area Telescope (LAT) for detecting the γ -ray and the second part is Gamma-ray Burst Monitor (GBM) for seeking an interesting event in the sky. In fact, both of them does detect the γ -ray but in the different energy scale. LAT is the main component where it detect the γ -ray in a few dozen of GeV up to a digit of TeV. For GBM part, the visible photon energy for them is around 8 keV to 40 MeV. The GBM consists of two sub components which are sodium iodide detector for low-energy photons (8 keV to 1 MeV) and bismuth germanate detector for high-energy photons (0.2 MeV to 40 Mev). GBM detectors distribute around the telescope to be a closed circuit camera and looking for a flare of the γ -ray. The

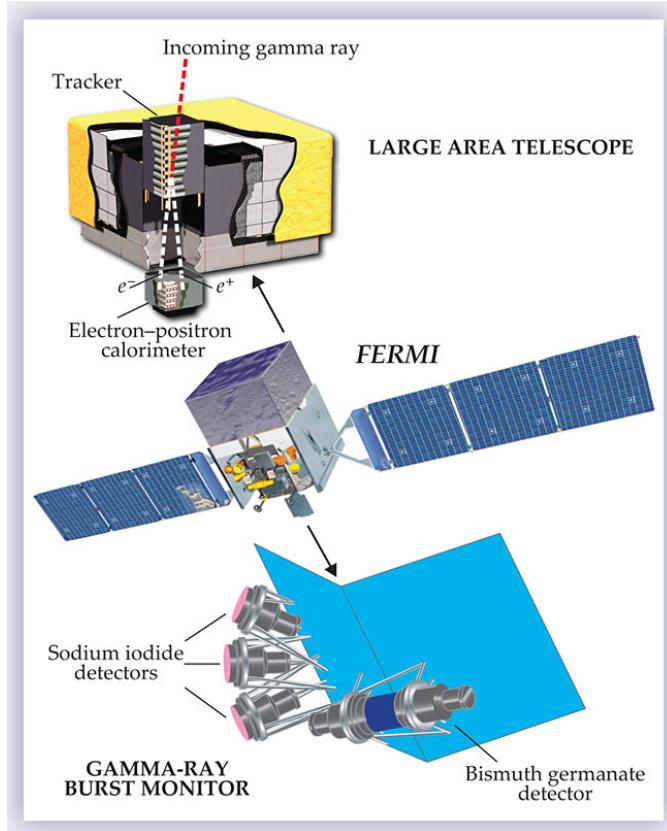


Figure 2.10: Main components of *Fermi*-LAT (Image taken from Michelson et al. (2010))

actual purpose of GBM is not a detector for collecting a high quality data but it is attached in the spacecraft to assist the LAT for mainly looking at an interesting events that could produce a huge amount of γ -rays. The content in this chapter will deep down into more detail of LAT in depth and would not provide more detail of GBM.

2.2.2 Large Area Telescope (LAT)

LAT consists of tracker (TKR) module for tracing the incoming photon, calorimeter (CAL) for measuring the kinetic energy after the particle has been passed through the tracker because a charged particle interact with the CAL and dissipate since it enter the module and anti-coincidence Detector (ACD) for rejecting the background signal. The last part is the on-boarding data acquisition (DAQ) module for investigating the particle's footprint and digitize the signal.

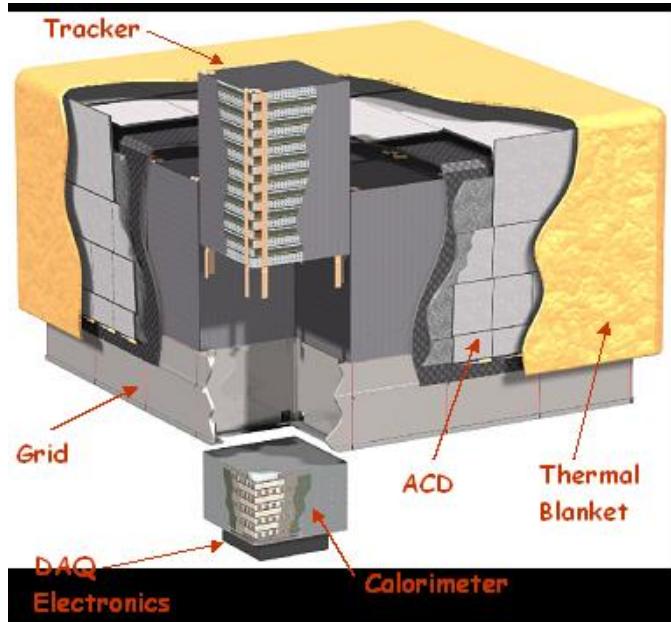


Figure 2.11: Instrument structure (Image taken from <https://fermi.gsfc.nasa.gov>)

Tracker

Higher energy photon or γ -ray talk to the LAT by converting the kinetic energy into a pair of lightweight leptons or e^+e^- pair. The converter-tracker has 16 planes of a large atomic numbers for making the incident γ -ray convert into a pair of e^+e^- as demonstrated in Figure 2.12. After that, a pair of leptons would leave a footprint as an electromagnetic induction in particle tracker where it sensitive for the moving charge particle.

The particle tracking is made from silicon-strip. Tracking information would leave the track in 2-D plane of a particle tracking. In order to trace back and gaining data as the 3-D moving direction, 16 particle tracker has to be taken in account for constructing the electron or positron path. Despite one layer of particle tracking could obtain the information about incoming leptons for x-y plane only, but technical design of LAT does put a 2 layers of silicon-based tracker with a very narrow gap between them. This kind of design could make the LAT performing measurement precision in the angular resolution better than a single layer of a wide gap which affects in the point-spread function (PSF) of the probability distribution from reconstruction direction. According to Figure 2.13, top and the bottom of

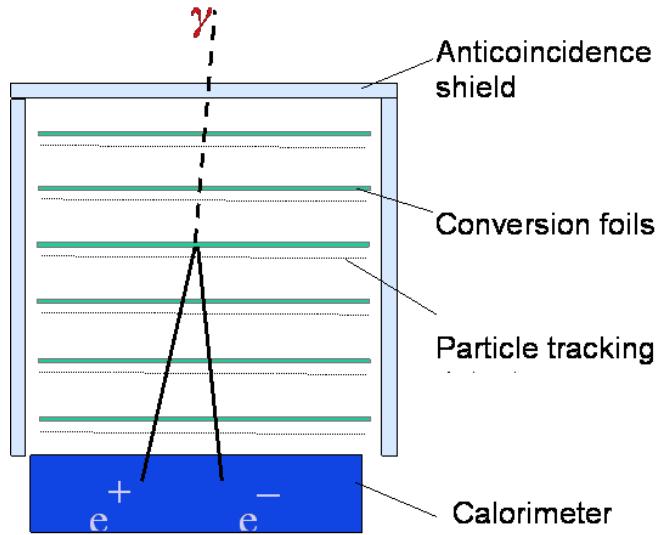


Figure 2.12: Schematic structure of the LAT (Image taken from <https://fermi.gsfc.nasa.gov>)

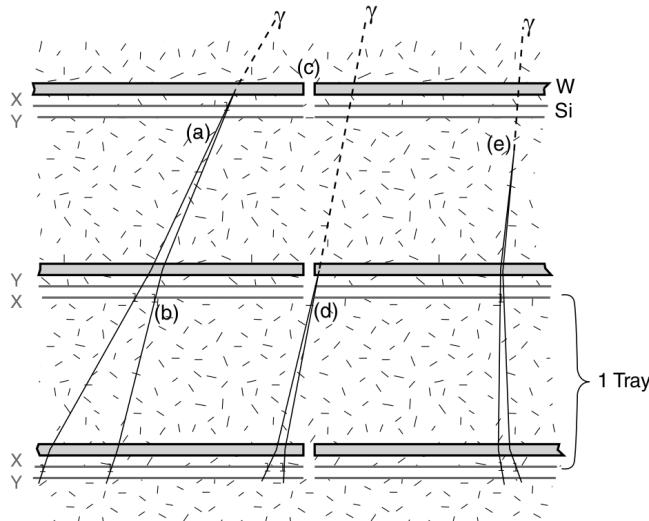


Figure 2.13: LAT's particle tracker (Image taken from Atwood et al. (2009))

silicon trackers and the heavy-nuclei conversion layer called "Tray". Case (a) and (b) in the figure is the ideal case where the γ -ray hit the conversion layer and multiple footprints are recorded. Nevertheless, there is an edge case as in (d) and (e) where the γ -ray has a probability to skip an early layer and choose to convert in the secondary conversion layer and will be detected in the upcoming tracking layer. The major benefit of deploying multiple conversion layers is quite obvious for the better event gathering.

Calorimeter

Unlike particle tracker that talk to a charged particle by utilizing the EM induction without (or barely) disturbing the particle state, calorimeter is a starving component. It consume a lepton and produce electronic readout of the energy from radiation of the lepton in the crystal scintillator. Definitely, size of this part is mainly considered from the radiation lengths of the electron and position particles because it has to record the shower that happen during the decaying process. However, the radiation length highly depends on the kinetic energy of the particle. The LAT itself has been designed for detecting photon energy range between MeV to a few hundred GeV. Hence, the exposure of photon energy beyond TeV is probably not promising in this case.

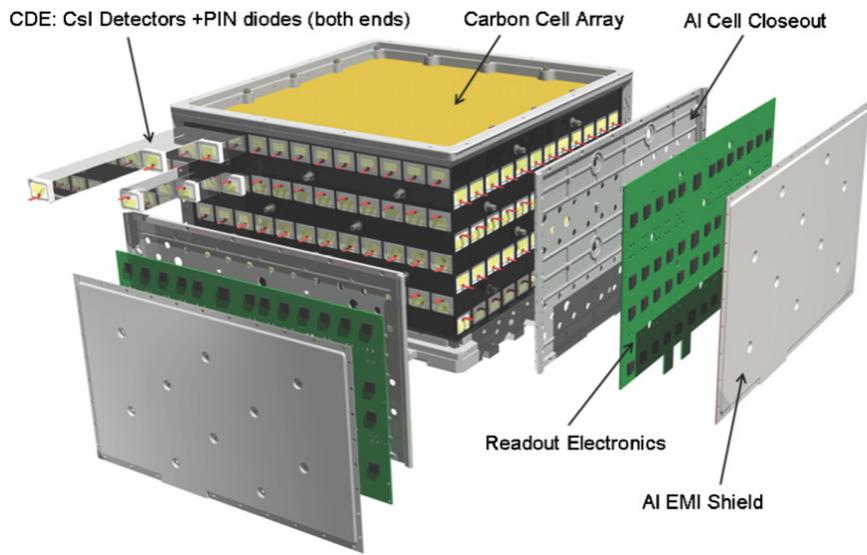


Figure 2.14: LAT's calorimeter (Image taken from Atwood et al. (2009))

The overview apparatus structure is illustrated in Figure 2.14. Each calorimeter module consists of 96 CsI(Tl) scintillator crystal size 2.7 cm x 2.0 cm x 32.6 cm and PIN photodiodes at both ends which connect to the readout electronic components for translating an amount of light that has been sparked in the crystal to digitized signal. Each horizontal layer is combined from 12 crystal components and stacked them 8 times by rotating them 90° each for boosting the angular resolution from the sparking lights. The carbon cell was built for supporting the structure of low

mass particle tracker due to the properties of high stiffness, thermal conductivity and thermal stability. An electron, position or γ -ray will deposit the energy in the calorimeter as the scintillated lights via electromagnetic interaction. The segmented crystal also allow LAT to trace the shower as the spatial imaging.

Anti-coincidence Detector (ACD)

The main objective of ACD is to support the charged-particle background rejection of the CRs. It is cover the tracker over the LAT field of view (FoV) for 4 side and the top part of the LAT. It consists of 89 plastic scintillator tiles with 5×5 array on top and 4 sides of 16 tiles. Each tile component contains two photomultiplier and wavelength shifting fibers embedded in the scintillator. The tile is overlapping another one in one-dimension to reduce the effect of the gaps between them. To be more precise, there are two sets of four called scintillator ribbon for covering the top-down side and a pair around their center. The ACD is required to has 0.9997 efficiency for detecting an incoming charged particle of FoV of the LAT. However, the γ -ray induce the shower that calorimeter will absorb but there is a scenario called "backsplash effect" where the secondary particles in keV range from the electromagnetic shower could interact with the incoming photon and Compton scattering in ACD. Then it could create a veto signal from the recoil electron. In order to solve this issue, the ACD with their neighborhood would take the incident candidate photon into account and could dramatically reduce the effect of the backsplashing.

Data Acquisition System (DAQ)

To acquire an interesting event, event selection could not be done on software on the ground level from the whole raw signal of subsystems because the limitation of the hardware in the current edge. In order to collect an event, raw data will be selected from filtering algorithm on board. The hierarchical structure of data acquisition system (DAQ) was invented for seeking an transient event as shown in Figure 2.15.

The lowest level is tower electronic modules (TEMs) to serve as an

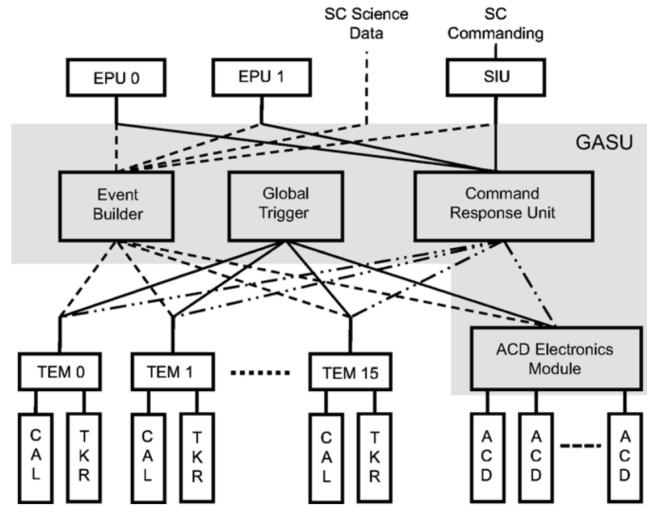


Figure 2.15: Flow chart of LAT's data acquisition system (DAQ) (Image taken from Atwood et al. (2009))

interface for the tracker and calorimeter. All TEMs create event buffering and communicates with Event Builder Module (EBM) which is a component of Global-trigger/ACD-module/Signal distribution Unit (GASU). Command Response Unit (CRU) was built to communicate the software execution in DAQ system. Lastly, Event Processing Unit (EPU) will process a selecting event from TEM and ACD Electronics Module (AEM). Filtering an event could reduce the information flowing rate from a few kHz to around 400 Hz which will be sent back to the ground level.

2.2.3 Event reconstruction

In an early day, the reconstruction algorithm for tracing a photon is Monte Carlo (MC) simulation. Modeling the incident γ -rays and the background has been simulated in the orbiting-like environment before it launch. Meaning that background rejection property already embedded in the LAT since the developing process. The simulation could be used for the detector calibration since the simulation software provide an interaction physical process.

The main logic of the reconstruction is started by tracking the footprint in the tracker and expect the output in calorimeter cube as physical process would yield. After that the event classification mainly consider from the ACD part to classify an event types.

The result from processed data on the fly is level 0 and it will pass down to Earth and reconstructing the photon data called level 1. The more LAT orbiting around the Earth's, the more understanding of the LAT environment and it brings the software improvement for the reconstruction algorithm to exploit the technique of pattern recognitions. First official released is LAT data is Pass 6 and Pass 7 after has been released with the same level 0 data but the reconstructed event is more efficient than the older one by software level. The newest version and likely to be the final version is Pass 8. Not only the reconstruction algorithm that has been developed but the event class is also an crucial concept. As mentioned earlier, the photon is classified into a specific class. There is no free lunch to think that the detector see the particle as a binary classification. It will mix with a likelihood or probability to distinguish the specific kind of interesting event. That is the main reason why *Fermi*-LAT team split the event into multiple classes which mainly are TRANSIENT, SOURCE, ULTRACLEAN and ULTRACLEANVETO.

Definitely, lesser photon candidates has been selected in the ULTRACLEANVETO. Then there is no certain right or wrong for picking the class from researcher point of view. The main criteria would be the objectives of the analysis. If the analyzer want a huge events and could accept some noisy event, then SOURCE or TRANSIENT class is suitable for the analysis and vice versa.

2.2.4 Detector performance and their characteristics

Fermi-LAT has been designed for detecting γ -ray in the space which means that the range of energy that it could see precisely will starting at MeV up to TeV. The effective area in square-meters is defined from the front and the back of the LAT's tracking layer by consider the upper part as a front and the bottom part belowing a certain layer as the back part. Since both front and back part components is made by the same materials and exactly same design. Then total effective area could be sum into a single value. The Figure 2.16 visualize the effectiveness of LAT along a given energy range. According to the plot, LAT performs a measurement well from GeV up to TeV scale.

Another crucial part when dealing with LAT effectiveness is the incidence

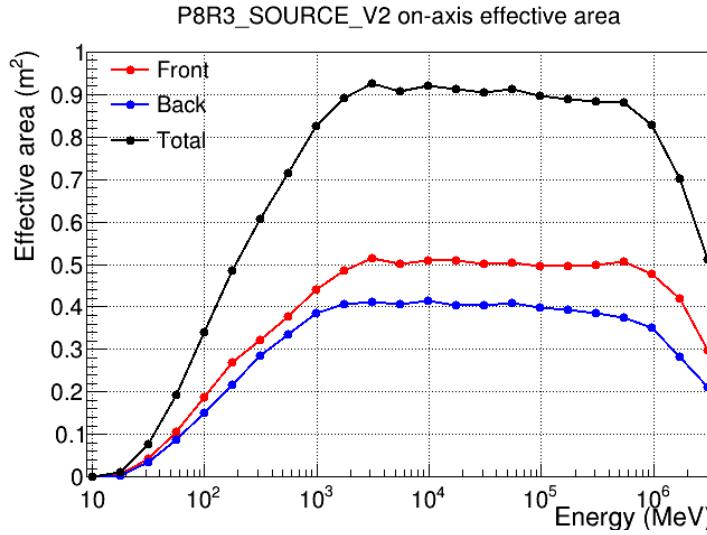


Figure 2.16: Effective area along the photon energy range from MeV to TeV (Maldera (2019))

angle (θ_{LAT}). It highly affects to the number of tracking layers. The higher probability of passing more tracking layers would yield a better LAT's performance. Figure 2.17 shows relation of effective area versus incidence angle.

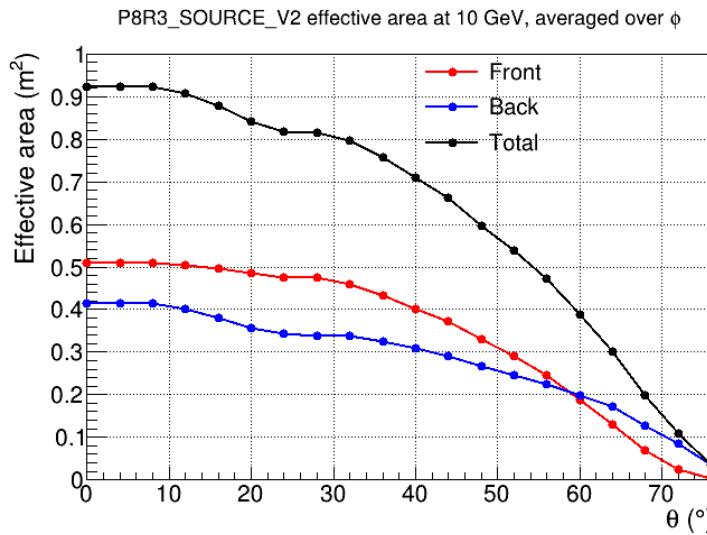


Figure 2.17: Effective area versus incidence angle (Maldera (2019))

Imagine the LAT structure as a cube-like detector. Surely, the LAT boresight is a square where an azimuthal angle (ϕ_{LAT}) of the incoming photon would affect a larger area that the photon could interact as demonstrates in Figure 2.17. The reason why there is a peak for any cycle of $\pi/2$ radian or 90° is the edge

of the LAT would have more area to interact than the lateral. Another evidence for the explanation is the front effective area has less effects since the propagation length is narrow than the back.

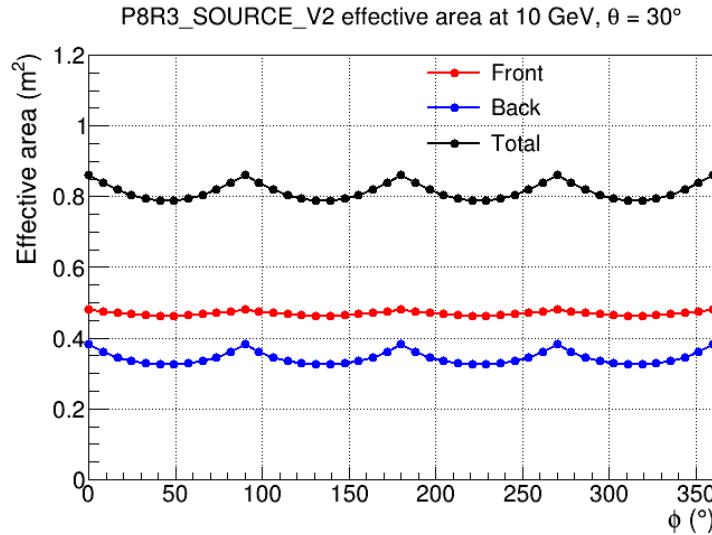


Figure 2.18: Effective area versus azimuthal angle (Maldera (2019))

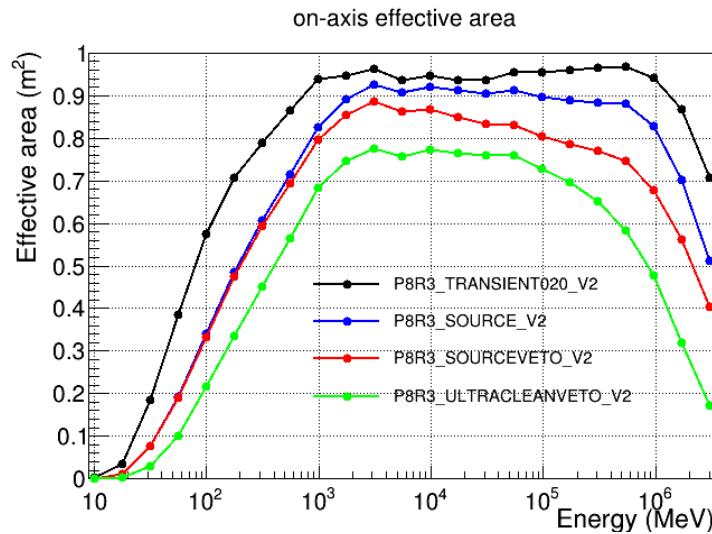


Figure 2.19: Effective area along the energy of each event class (Maldera (2019)))

From the previous subsection, the event class is also play crucial role when considering the effectiveness of the reconstructed event. Undoubtly, the cleanest class namely "ULTRACLEANVETO" would have the worst effective area. In opposite, TRANSIENT class would yield the best effective area as visualized in Figure 2.19.

To sum up, the effective area act for the LAT performance for seeking an event in the unit of square lengths. It is also behave like a function in the practical analysis which pragmatically allow the client to throw incidence angle, azimuthal angle and the energy. Then it will return the effective area in unit of square centi-meters in the raw format.

CHAPTER III

LITERATURE REVIEW

Cosmic-ray could come from different origin from galactic sources to extra-galactic sources. The kinetic energy of cosmic ray also highly depends on where does it from. Low energy CRs usually came from the Sun called “solar energetic particle”. The production process of solar particle event mostly came from the coronal mass ejection (CME) when HZE ions was dragged by a magnetic field in the plasma. The extra-galactic CRs typically has high momentum from the extreme condition of the acceleration mechanism in pulsar, quasars and supernova remnant (SNR). The theoretical description of acceleration in SNR and solar flares is the shock wave acceleration in following paragraph.

One of the most impactful study of CR’s acceleration mechanism was conducted by Fermi (1949). The study describes how high energy CR particle gain such a huge momentum from shock wave that was generated by supernovae or a great explosion from the heavy dense star. How it gains the kinetic energy could be described as a first order shock acceleration and the overall spectrum of charged particles could be represented as the power law in Equation 3.1.

$$\frac{dN(E)}{dE} \propto E^{-\gamma} \quad (3.1)$$

where $\gamma \geq 2$ in the non-relativistic regime. However, moving magnetized plasma cloud can accelerate the charged particle in the space called ”second-order Fermi acceleration”. Both regimes were computed the lorentzian forces regardless of thermal collision in the process.

The CR protons is a major components in the arrival CR particles under multiple observations. However, α -particle is also a second important CR particle when considering a precise calculation of CR interactions. The other majority of heavy weight nucleis that could propagating through the space are C, O, Ne and

so on. The differential flux in kinetic energy of multiple observations is visualized in the Figure 3.1 under the work of Beringer et al. (2012) to take various atomic numbers from various experiments.

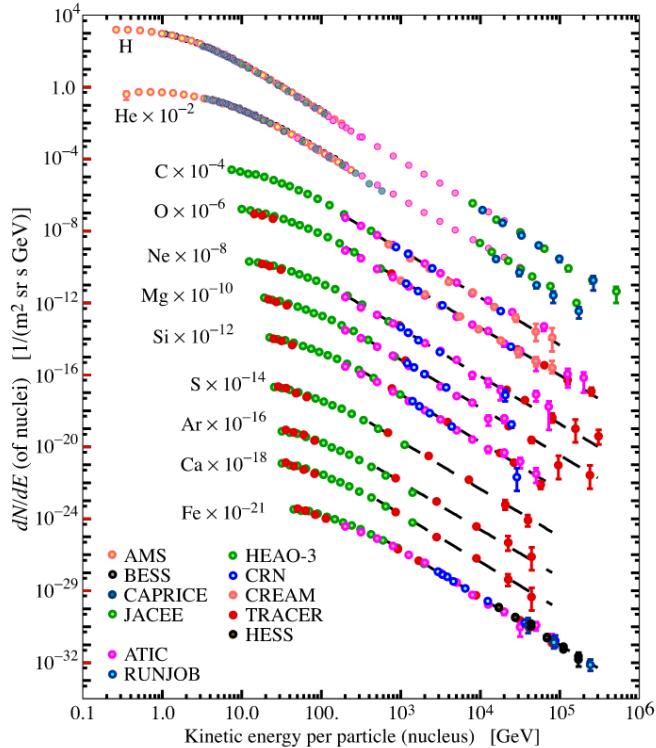


Figure 3.1: Cosmic-ray elemental spectra from various experiments (Beringer et al. (2012))

Since there is a moving plasma inside the Earth, the magnetic field has been generated from the dynamics of the moving charged ions in the plasma. The magnetic field of the Earth's has a north pole at the geometric south pole of the Earth and vice versa. The Earth's magnetic field play an important roles in the arrival CR particles because the lorenzian forces will bend the direction of a moving charged particle depends on the rigidity of the particle. This means the magetic field line mantiles the Earth with a certain direction towards the geometric north pole.

Firstly, it creates the CR cutoff rigidity on the terrestrial where each location of the Earth's require a minimum rigidity of an incident charged particles as a condition for arrival. The Figure 3.2 shows a cutoff rigidity on the Earth's surface.

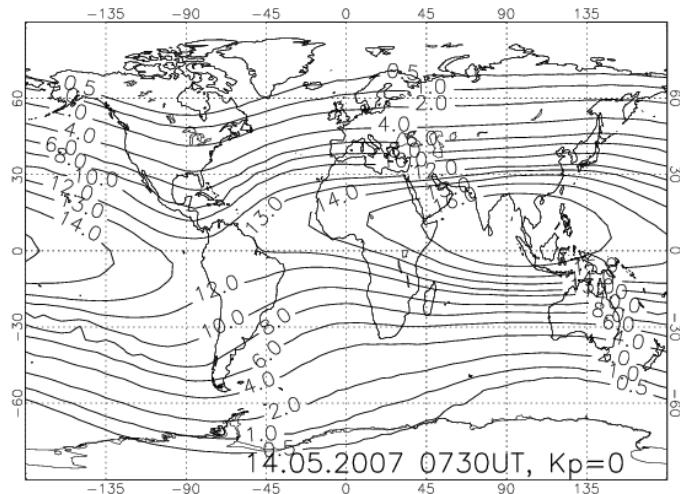


Figure 3.2: World map with computed geomagnetic vertical cutoff rigidity contour lines on a given date (B. et al. (2007))

Secondly, incoming charged CRs with a charged has been dragged by the Earth's magnetic. Then a charged particle would moving as a curve or a spiral depends on the rigidity of an incoming particle which leads to the East-West effects when an orbiting detector could find more particle on the West side more than the East side for a significant level of intensity. A pioneer Earth's γ -ray experiment is conducted by Kraushaar et al. (1965) where the detector was deployed on the Explorer XI satellite and orbiting in the sky.

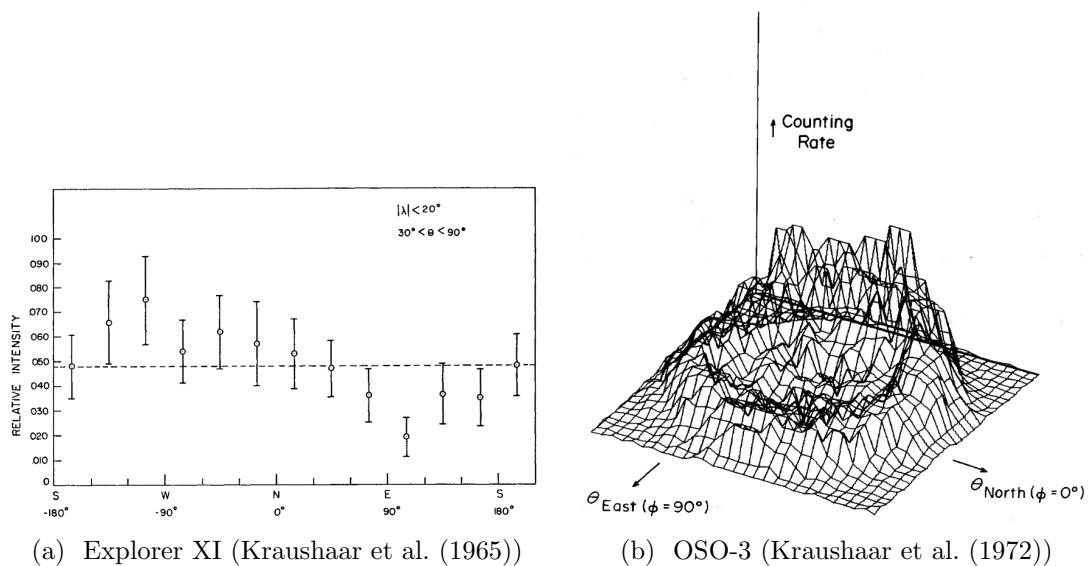


Figure 3.3: The asymmetry of γ -rays East-West intensity

The incoming photon from East and West direction is the crucial evidence of the bending of CRs trajectory by Earth's magnetosphere. The first analysis show a distinguishable intensity from East to West as visualized in Figure 3.3a. The second experiment where the γ -ray detector is attached on Third Orbiting Solar Observatory (OSO-3) and collecting the γ -ray in MeV range. The 2-D plot of the intensity is shown in Figure 3.3b.

Moreover, An early analysis found that the observing γ -rays intensity along the zenith angle from different geomagnetic latitude (λ) is differentiable as shown in Figure 3.4. The reason behind this outcome came from the Earth's rigidity where the incoming particles near the equatorial has less chance to arrive than the north pole and likely to interact with the atmospheric molecules and emits the γ -rays. This is the secondary evidence of how geomagnetic fields play an important role on the trajectory of the CR particles.

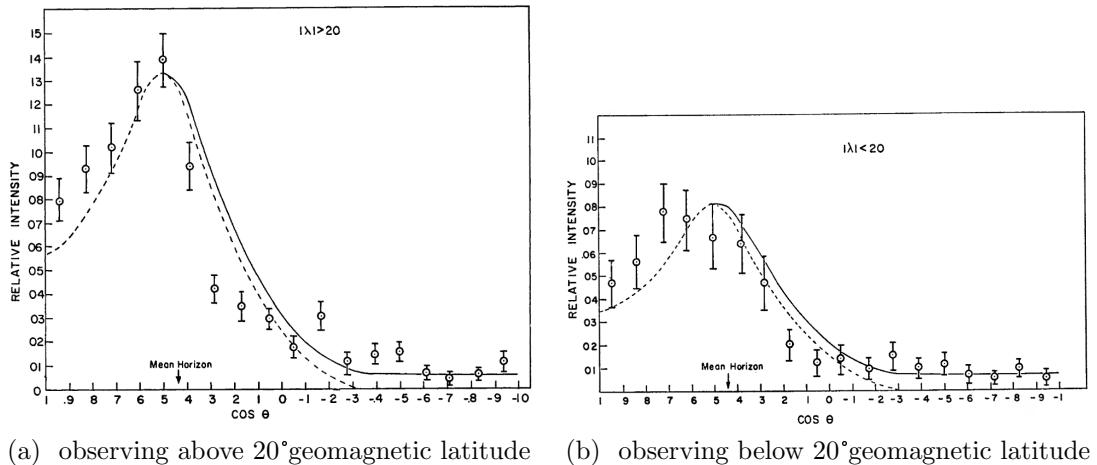


Figure 3.4: γ -ray intensity along the zenith angle (Kraushaar et al. (1965))

The following experiment of Earth's albedo observations is conducted by sending a second small astronomy satellite (SAS-2) with higher resolution in angle and observing above 35 MeV up to GeV range (Thompson et al. (1981)). The projected 3-D representation of intensity is shown in Figure 3.5a. A few decades later, another precise $\gamma - ray$ detector has been attached in the CGRO satellite (Petry (2005)). An outcome from the analysis illustrated the bright region around the Earth's limb region as in Figure 3.5b.

The previous details is full of so many experimental evidences. However,

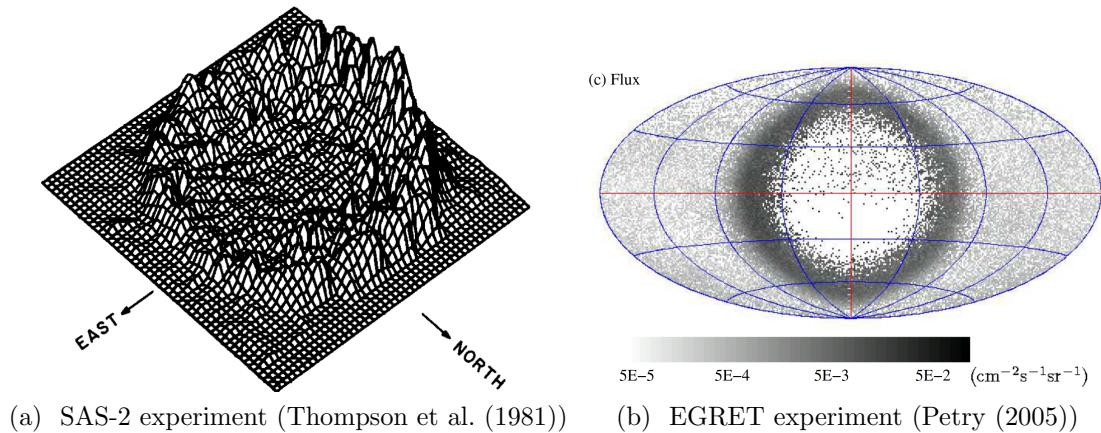


Figure 3.5: The Earth's centered intensity plot from the satellite based observations

Morris (1984) put the weights on assumption of bright region as seen as albedo in γ -ray came from the interaction of proton and the atmospheric nucleis. The study shows the γ -rays intensity and the variation of air depth by differing the zenith angle along limb region as plotted in Figure 3.6 and Thompson et al. (1981) data has been exploit in the analysis.

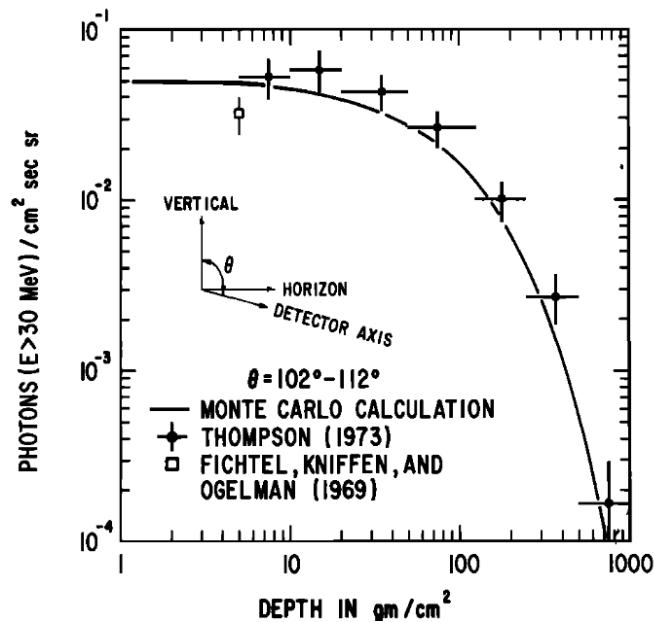


Figure 3.6: Calculated γ -ray intensity with the variation of zenithal angle (Morris (1984))

Furthermore, this study compute the γ -ray spectrum from the bright region as seen as albedo from the Earth's limb and lunar albedo. The Figure 3.7

shows the spectrum from theoretical calculation. Figure 3.7a identify the 2 bounds of the limb's region with an appromated air depth. Appealingly, another evidence of the solar activity could cause a lower arrival CR particles since the propagating magnetic field drag a charged particle towards outer space. The distinguishable spectrum from this phenomanon is demonstrated in Figure 3.7b.

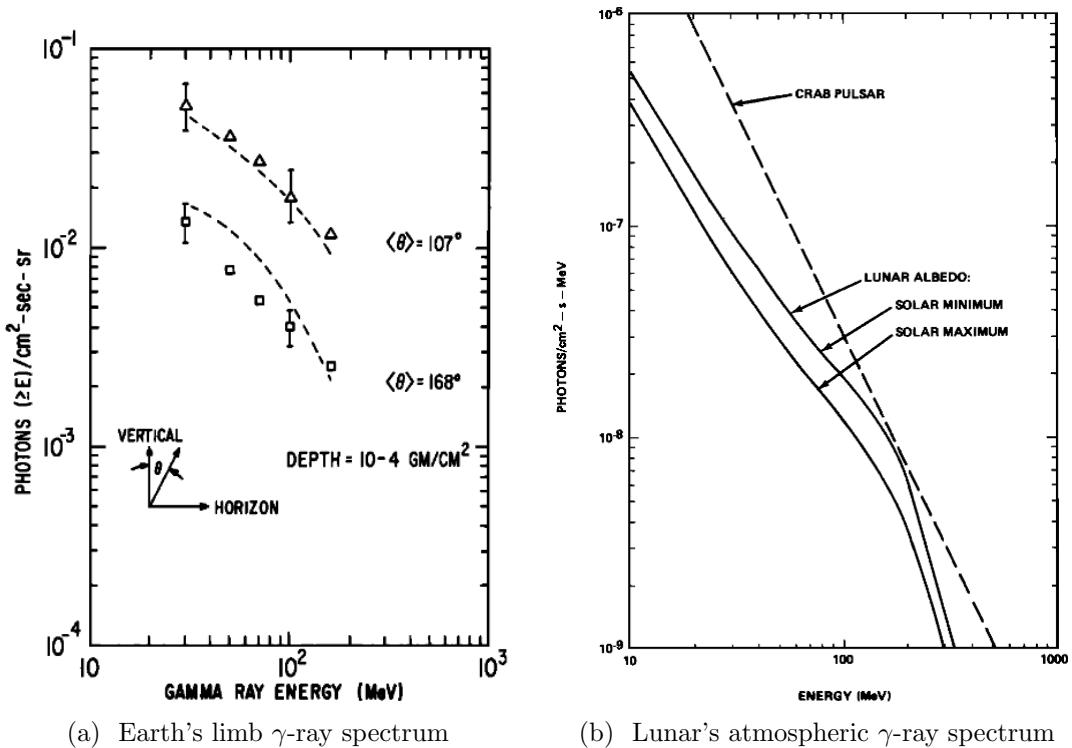


Figure 3.7: γ -ray spectrum from proton-nuclei interactions (Morris (1984))

Not so long after *Fermi*-LAT was launched in the sky. In 2009, an early examination of the induced γ -ray emission was observed by the most precise γ -ray detector Abdo et al. (2009). Since there is a huge improvement in the technological side which makes LAT capable of detecting high energy γ -ray from MeV up to TeV. Another discovery from this study was a East-West effects is highly depends on the energy where it was converted from the incident energy of CR particles. The higher energy means the higher rigidity and it would reflect how hard magnetic field could bend the trajectory. The intensity was divided into 4 energy ranges from a few GeV to a higher GeV that could be considerd as the relativistic scheme where the kinetic energy is much higher than the mass as shown in Figure 3.8.

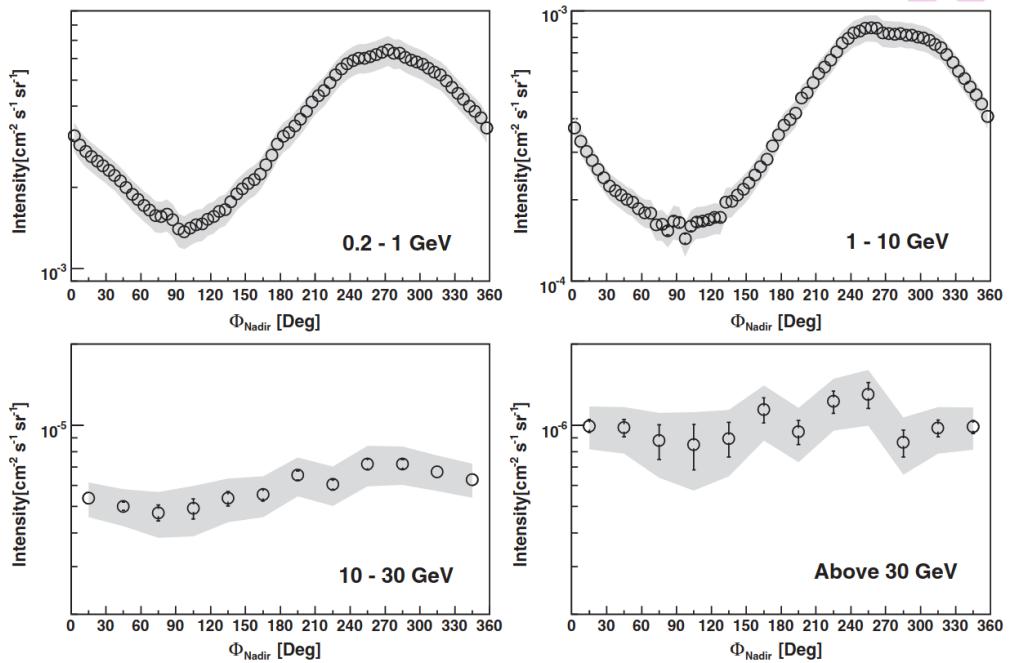


Figure 3.8: γ -rays intensity from limb emission in 4 energy ranges (Abdo et al. (2009))

Since this work is to indirectly measure the proton spectrum in GeV range. The direct measurement in an early study of high energy CR particles such as proton and helium was observed by Haino et al. (2004). Another following experiment is Adriani et al. (2011). Both of them still lack of capability to detect such a high energy in scale of hundred GeV. Nevertheless, there is a clue about the breaking energy in the proton spectrum with a very low statistics and leave a room for the further study.

Since there is just a clue from the previous direct observations. The indirect measurement of CR proton spectrum has been performed in energy between 90 GeV to 6 TeV by taking advantage of the brightness of Earth's limb from collision of incident CR protons (Ackermann et al. (2014)). The 5 years of γ -ray data has been exploit by investigating the incident proton spectrum via proton-proton collision model for finding whether an CR protons has a breaking point of slope in the power law spectrum. The study found that there is a breaking spectral index in proton spectrum above 200 GeV Nonetheless, Statistical analysis turns out that there is 1σ significant level.

Back in 2011, one of the most efficient space-based CR detector was launched by the arriage of Endeavor space shuttle. The detecor has been attached into the international space station (ISS). The main mission of AMS-02 is to search an antimatter, dark matter from measuring CRs. It has capability to detect an antimatter such as positron and antiproton. This detector is also able to detect other heavy weight nuclei like B, CNO, Ne and etc. In 2015, a proton spectrum has been directly reported and found the breaking at 340 GV (Aguilar et al. (2015)) with a very high statistics. Not only the proton but the helium spectrum is also measured and reported in Aguilar et al. (2015).

According to the previous study (Ackermann et al. (2014)), low statistical significant potentially came from lack of the dataset or the methodology from the consequence of indirect measurement. In this work, the similar study will be performed with a larger data size from ~ 9 years of observation. Hopefully, the study could answer the first mentioned clue and to put the weights on previous work. Moreover, an improvement of the optimization process by employing the heuristic optimization as well as the high performance calculation of the exposure map for a leses computational time in γ -ray spectrum calculation.

CHAPTER IV

METHODOLOGY

Procedure of getting data to perform an analysis from the collected data is very important. In order to get a precise Earth's limb γ -ray spectrum to trace back the incident proton spectrum, it is crucial to carefully determine the selection criteria from raw data in many angle base on the objectives. This chapter will begin by giving information of γ -ray flux extraction by providing information of data filtering and the extracting process from scratch. Secondly, hadronic collision model that forwardly yield the γ -ray spectrum will be discuss and tracing the incident CR's proton spectrum algorithm from heuristic optimization. Lastly, the last sub-chapter contains details of statistical analysis.

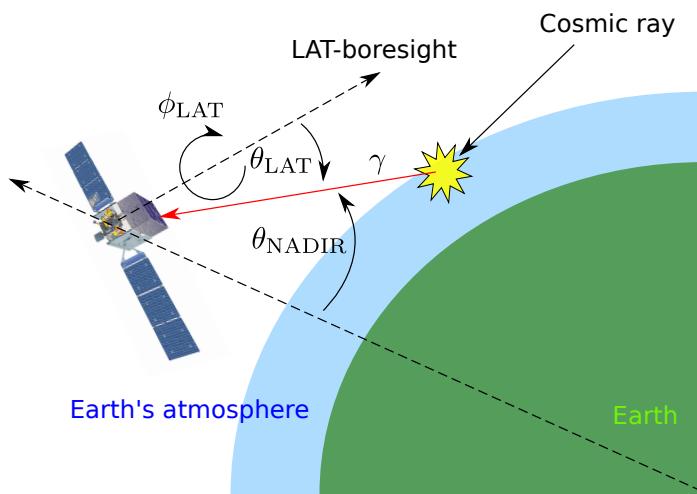


Figure 4.1: Schematics of γ -ray production

The required fundamental concept of spacecraft orientation and the observations of Earth's limb γ emission is another crucial concept. The Figure 4.1 demonstrates the important axis which are θ_{NADIR} represent the angle of how

further from Earth's center in the spacecraft point of view as well as θ_{LAT} to the angle from incident γ -ray to the detector normal in domain between 0 to 90° and ϕ_{LAT} as the clockwise angle from 0 to 2π .

4.1 Data selection

In this work, 9 years of LAT's flight data has been used to analyze reconstructed photon and their metadata of spacecraft log recorded in a similar format periodically every half minutes. The reconstructed algorithm version is the latest version which is Pass 8 with the cleanest photon events that exists from *Fermi*-LAT data catalogues called ULTRACLEANVETO. To be more precise, the photon data is collected from publically available raw FITs file from the

Only high energy limb's photon will be selected from 10 GeV up to 1 TeV. It makes the traceback analysis for gaining the information of CR proton spectrum in rigidity between 60 GV to 2 TV. The definition of γ -ray's limb region is obtained from Abdo et al. (2009) in a given nadir angle from 68.4° to 70.0° . The maximum of incident angle (θ_{LAT}) that was measured from the z-axis of the LAT's foresight is 70° .

4.2 Flux extraction

There are multiple step from trivial to complex calculation to obtain the differential flux. The definition when saying flux is actually a differential flux that be calculated one chunk of energy range at a time as Equation 4.1

$$\text{Flux} \equiv \frac{dN_\gamma}{dE} = \frac{\int_{\text{Limb region}} (\text{Count map}/\text{Exposure map})}{\Delta\Omega\Delta E}. \quad (4.1)$$

Since the CR spectrum follows a power law as the exponential form $dN/dR \propto R^\gamma$ as mentioned in the background section. Then the log-log relation of the flux versus rigidity would behave like a trivial linear trend in the plot. Not only the rigidity, but in the high energy CR like 10 GeV also makes the energy of the particle almost

the same as the rigidity does. Consequently, the γ -ray spectrum is equally divided in the energy space in the log scale for 50 bins.

To get the spectrum, it is obvious to construct the histogram with 50 bins in a given energy scale as explained in the previous paragraph. The flux of each bin could be computed separately by initializing the empty count map and the exposure map where it represents the exposure time and the effectiveness of the spacecraft when looking at each angle in the sky. Let's consider the following example for a deeper understanding. The ideal scenario is when incident γ -ray pass through the LAT in a normal line of the detector. Definitely, the performance would be the highest as it could do. On the other hand, if the incident γ -ray arrive with high tile angle from the LAT's plane (High θ_{LAT}). An angle resolution is selected to be 2° in ϕ_{NADIR} and 0.1° in θ_{NADIR} . The reason behind these numbers is simply from the toy experiment of plotting the result in the 2D histogram and it is selected to be the one as the bin value is not too noisy and it is not so big due to the limb region could not be seen clearly which leads to the matched photon mixed up with the Earth's γ -rays and collecting too many primary CR photon.

Basically, the procedure is summarized in these following steps.

1. Make 2D histograms with 25 bins per decade of energy
2. Select photon data and fill in the 2D histograms
3. Calculate exposure maps which include the effective area and livetime of the LAT as it observed the Earth
4. Compute the flux by applying Equation 4.1 in for bin
5. Taking consider background subtraction from a average uniform background photon distribution by treating bin by bin

4.2.1 Exposure map gathering

In fact, step 3 is the most complicate stage in this work. Practically, *Fermi*-LAT was designed for observing the space which makes the spacecraft

logging in equatorial coordinates not for the Earth's polar coordinates. The LAT position is recorded in equatorial coordinates as well as the LAT's boresight of the detector plane to log their orientation during the orbit. In the end of the day, the coordinates transformation would be perform from multiple frame of references to LAT boresight for acquiring the exposure of LAT's FoV and reference the effectiveness from LAT's boresight angle dependency. The following content is the full detail of how things going on under the hood.

Coordinate Transformations

Firstly, the spacecraft orbit is recorded in the equatorial coordinate which in spherical point of view. Defining the cartesian coordinate that share the origin between celestial point of view and the spacecraft by letting one axis point to the spacecraft could assist the calculation more convenient as the Figure 4.2. Please note that the x-axis in equatorial coordinate is called "Equinox".

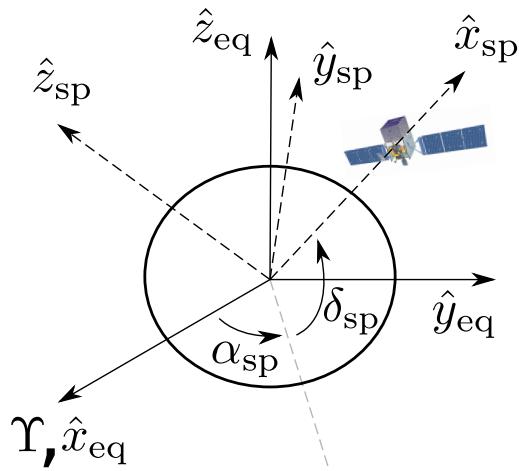


Figure 4.2: Coordinate transform between celestial and spacecraft

However, mapping into the cartesian coordinate by adopting a unit vector in 3 dimensions has been written as Equation 4.2 and the symbolic transformation is represented in Equation 4.3.

$$\begin{aligned}\hat{x}_{\text{sp}} &= \cos \delta_{\text{sp}} \cos \alpha_{\text{sp}} \hat{x}_{\text{eq}} + \cos \delta_{\text{sp}} \sin \alpha_{\text{sp}} \hat{y}_{\text{eq}} + \sin \delta_{\text{sp}} \hat{z}_{\text{eq}} \\ \hat{z}_{\text{sp}} &= -\sin \delta_{\text{sp}} \cos \alpha_{\text{sp}} \hat{x}_{\text{eq}} + \sin \delta_{\text{sp}} \sin \alpha_{\text{sp}} \hat{y}_{\text{eq}} + \cos \delta_{\text{sp}} \hat{z}_{\text{eq}} \\ \hat{y}_{\text{sp}} &= \hat{z}_{\text{sp}} \times \hat{x}_{\text{sp}}\end{aligned}\quad (4.2)$$

$$\hat{r}_{\text{sp}} \equiv T_{\text{eq} \rightarrow \text{sp}}(\delta_{\text{sp}}, \alpha_{\text{sp}}) \hat{r}_{\text{eq}} \quad (4.3)$$

The transformation matrix $T_{\text{eq} \rightarrow \text{sp}}$ has been implemented as a matrix in practical analysis due to the convenient for calculation and the compaction in the programming point of view.

Secondly, LAT's boresight coordinates is also referenced in equatorial coordinates. Figure 4.3 demonstrates the relation between an incident plane of detector on equatorial coordinate and the nadir angle for regarding the exposure from LAT to Earth.

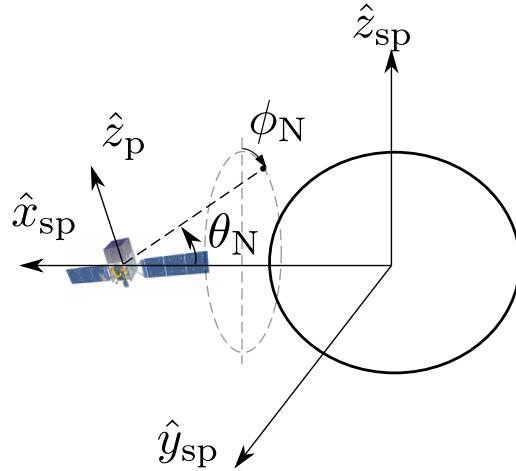


Figure 4.3: Coordinate transform between spacecraft and nadir angle

Unquestionably, it have to be converted into a cartesian point of view to do a mathematical operation for simplicity. A full representation of the coordinates could be written as Equation 4.4 and the compact form is in the Equation 4.5.

$$\begin{aligned}\hat{x}_p &= \cos \delta_p^x \cos \alpha_p^x \hat{x}_{eq} + \cos \delta_p^x \sin \alpha_p^x \hat{y}_{eq} + \sin \delta_p^x \hat{z}_{eq} \\ \hat{z}_p &= \cos \delta_p^z \cos \alpha_p^z \hat{x}_{eq} + \cos \delta_p^z \sin \alpha_p^z \hat{y}_{eq} + \sin \delta_p^z \hat{z}_{eq} \\ \hat{y}_p &= \hat{z}_p \times \hat{x}_p\end{aligned}\quad (4.4)$$

$$\hat{r}_p \equiv T_{eq \rightarrow p}(\delta_p^x, \alpha_p^x, \delta_p^z, \alpha_p^z) \hat{r}_{eq} \quad (4.5)$$

Similarly, $T_{eq \rightarrow p}$ is also considered as a transformation matrix in the computation for monotizing the source code as well as keeping consistency in the logic.

Again, all those representation just for mapping the LAT's boresight coordinate to link with the nadir coordinate to accumulate the exposure from the spacecraft's FoV. The spacecraft coordinate can be written as an dependency of Earth's polar coordinate as Equation 4.6 in the cartesian system.

$$\hat{r}_{sp}^o(\theta_N, \phi_N) \equiv -\cos \theta_N \hat{x}_{sp} + \sin \theta_N \cos \phi_N \hat{z}_{sp} + \sin \theta_N \sin \phi_N \hat{y}_{sp} \quad (4.6)$$

By the end of the day, extracting the relations to simplify the LAT's boresight coordinate could be contained by one inversion of transformation matrix from equatorial to spacecraft and transform it to plane of detector as written in the compact form in the Equation 4.7.

$$\hat{r}_p^o(\theta_N, \phi_N) = T_{eq \rightarrow p}(\delta_p^x, \alpha_p^x, \delta_p^z, \alpha_p^z) [T_{eq \rightarrow sp}(\delta_{sp}, \alpha_{sp})]^{-1} \hat{r}_{sp}^o(\theta_N, \phi_N) \quad (4.7)$$

Geometrically, angular coordinate of LAT plane could be obtained from normalized component of the cartesian unit vector as in Figure 4.4. The exposure accumulation has been calculated in every single grid from the previous relation.

Parallel Computations

From the previous section, it is obvious that the complexity of the code becoming large due to the transformation operation. For example, a plain matrix inversion cost $\mathcal{O}(n^3)$ where n is 3 because it is 3 by 3 matrix in this case. Not only

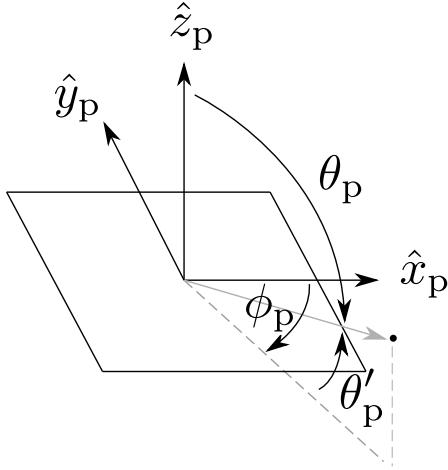


Figure 4.4: Detector’s boresight in cartesian and polar coordinate

the inversion, but the matrix multiplication also cost the same amount of complexity which cause a long run in the execution time because the original program has been designed in sequential execution.

Nevertheless, the spacecraft log file namely “FT2” has been records row by row which equivalently to a CSV format as a plain table with the specific columns. Since the objectives is to determine the exposure map by counting the exposure time as well as the effectiveness of the spacecraft from each angle for a given small range of energy which means that the energy could be approximate as one energy for getting the effective area in each angle of the LAT during calculation. Moreover, the exposure could be calculate parallelly for each step or in each row of the FT2 due to the property of exposure map. Consequently, splitting exposure map and calculate parallelly is possible to get rid of the performance issue.

The code is implemented in Message Passing Interface (MPI). The framework provides a simple protocol without knowing any type of protocol or zero required network knowledge. It assists the user to freely control multiple process with a full control of each process. According to Flynn’s taxonomy of computation, this work exploits the Multiple Instruction Multiple Data (MIMD) architecture to utilizing the resources in a distributed systems.

To begin with the calculation, initializing the exposure map with a

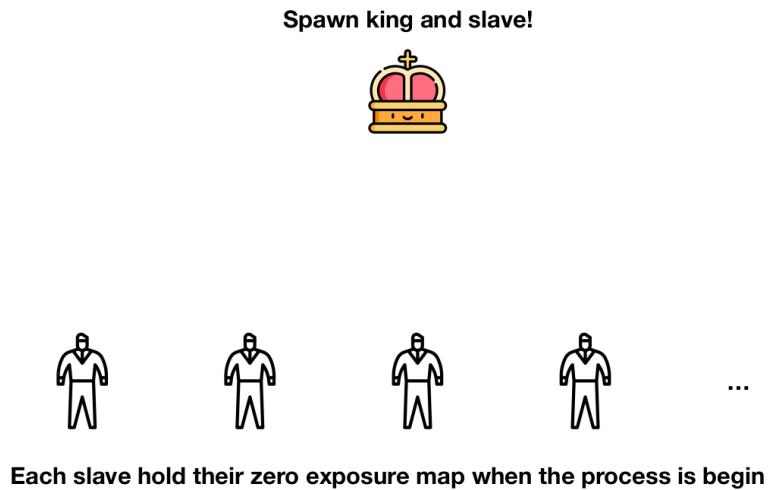


Figure 4.5: Spawning the king and slave processes

separate workers and send multiple rows to the workers in the same amount is trivial and waste a lot of resources since there will be a fast worker who do a calculation really fast and the slow worker due to the cluster is composed of non-monolithic nodes with a different performance. The trivial calculation will lock the resource in the cluster and blocks the other researcher who wants to run because the resource allocation issue. To maximize the usage of the CPU based cluster computing, there is a mechanism called “Master-Slave technique”. The algorithm has been designed for utilizing the resource by spawning a king as the process manager and multiple slaves to be a process worker. The starting process could be demonstrated in the Figure 4.5.

After that, the FT2 rows will be sent to slaves sequentially until all workers hold a small chunk of data and do their jobs. In practice, there is a metadata attach in the message. One of the option is the status tag. The status tag sends to the worker to declare the state of their process whether it is in the calculation or the finishing. Figure 4.7 illustrates the non-sequential sending of the workload. The idea is simply sending a small task to an available worker and skip a busy worker without disturbing them. This mechanism allows the execution to utilize the resource in the cluster without wasting in the free worker.

By the end of the day, if the task is completely sent. The master process will send the status tag as done to be an announcement of the finishing period.

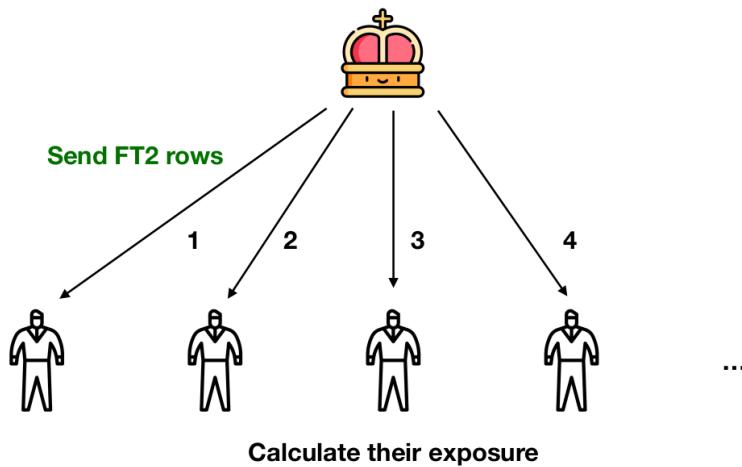


Figure 4.6: Master process send a small task to workers

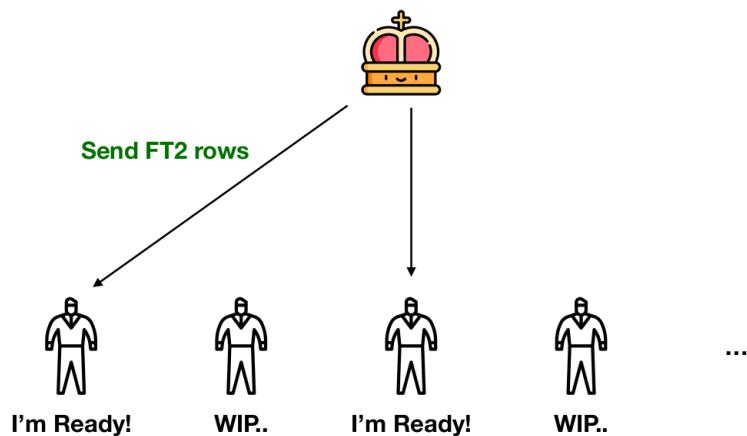


Figure 4.7: Asynchronous sending to an available worker

Then the exposure map of each worker will be gathered in the master process for superposition and dump it to unify an exposure map. In addition, the calculation in an early period of testing is reported in Appendix A.

4.3 Hadronic Collision Model

The proton spectrum power law in rigidity is described in Equation 4.8 as a single power law (SPL) where the γ represent the spectral index of the model. In fact, the spectrum has been observed as the differential flux in energy.

Converting process between ridigity spectrum and the energy spectrum is derived in Appendix B to obtain a precise calculation.

Single power law (SPL)

$$\frac{dN}{dR} = R_0 R^{-\gamma} \quad (4.8)$$

The most crucial part of this work is to determine if there is any breaking in the spectral indices in the power law. To represent a single breaking energy, broken power law (BPL) could be modeled the spectrum in ridigity as Equation 4.9.

Broken power law (BPL)

$$\frac{dN}{dR} = \begin{cases} R_0 R^{-\gamma_1} & : E < E_{\text{Break}} \\ R_0 [R(E_{\text{Break}})]^{\gamma_2 - \gamma_1} R^{-\gamma_2} & : E \geq E_{\text{Break}} \end{cases} \quad (4.9)$$

The scattering process of the hadronic collision from proton hitting the atmospheric molecules. The collision from incoming proton kinetic energy above 10 GeV could be modeled by proton-proton collision with an approximation that depends on the majority of the air components. Model for the collision of proton-proton which yields γ -ray as a secondary product as a distribution in the spectrum has been derived in Equation 4.10 from Kachelrieß & Ostapchenko (2012) work.

$$\frac{dN_\gamma}{dE_\gamma} \propto \int_{E_\gamma}^{E_{\max}} dE' \frac{dN_p}{dE'} \frac{d\sigma^{pp \rightarrow \gamma}(E', E_\gamma)}{dE_\gamma} \quad (4.10)$$

Where $d\sigma^{pp \rightarrow \gamma}(E', E_\gamma)/dE_\gamma$ contains a scattering amplitude of a given kinetic energy proton and the spectrum of the γ -ray. Atmospheric compoents mostly consists of nitrogen as the majority and the oxygen (Wallace & Hobbs (2006)). The cross section from proton-proton collision and proton-nitrogen collision is roughly approximate as the multiplicative relation since there are plateau curve in the energy range in this analysis. The relation of the proton-proton scattering amplitude and the proton-nitrogen is obtained from Atwater & Freier (1986a) where it is highly depends on the atomic numbers of the air molecules.

However, the second highest fraction of the arrival CR particles on Earth is an alpha (α) particle. The helium nuclei can interact with the nitrogen and

produces high energy γ -rays depends on how much kinetic energy α -particles is holding. Another estimation has been explored by applying $\sigma_{\alpha N}/\sigma_{pN}$ to be a constant around 1.6 at the energy range in GeV from the same relationship of proton-air collision model. Hence, derived equation of the scattering process from incoming proton and α -particle with air molecules to produce γ -ray spectrum could be shown as Equation 4.11

$$\frac{dN_\gamma}{dE_\gamma}(E_\gamma) \propto \sum_{E'_i} \left[\frac{E'_i}{E_\gamma} \Delta(\ln E'_i) \right] \left[f_{pp} \frac{dN_p}{dE'_i} \left\{ 1 + \frac{\sigma_{HeN}}{\sigma pN} \left(\frac{dN_p}{dR} \right)^{-1} \frac{dN_{He}}{dR} \frac{dR_{He}}{dR_p} \right\} \right], \quad (4.11)$$

The CR helium spectrum would not be measured in this work since there will be a multiple parameters which leads to an overwhelming local optimum. The spectrum of α -particles is directly measured by Aguilar et al. (2015) and fix the distribution as one function rather modeled spectrum of CR proton spectrum. The full detail of the equation derivation will be demonstrated in C.

4.4 Optimization

Determining the best-fit spectral model requires an objectives function to represent how well model match with an observed data. A proper methodology for fitting or optimization in another word is also a crucial part since there is likely that the local optimum exists in the parameters space. A poor optimization could lead the best-fit stuck in a local minimum and yield a poor result. For better escaping local optima, heuristic optimization is employed for finding the best-fit of the model in parameter space.

Poisson likelihood function

An objective function is defined as Poisson likelihood function in the Equation 4.12. The reason behind the selection of Poisson function came from the observed model and measurement is considered as an amount of photons in each bin of the histogram. Converting the model spectrum to be a count histogram is

simply multiplied by the integral of exposure map in limb region.

$$\mathcal{L} = \prod_{i=1}^N P_{\text{pois}}(n_{i,\text{model}}, n_{i,\text{measurement}}) \quad (4.12)$$

Since the spectrum order is in different order of magnitude, then a proper way to define an objective function is to redefine a likelihood as a log-likelihood function for numerically convenient like Eq 4.13.

$$Sum = \sum_{i=1}^N -\log P_{\text{pois}}(n_{i,\text{model}}, n_{i,\text{measurement}}) \quad (4.13)$$

To sum up, a given proton spectrum yield a distribution of γ -ray spectrum to be converted into a count histogram and comparing with the real measurement. Not only for numerical convenient, but the negative sign also makes an algorithm to minimize the system rather than maximize a likelihood.

Particle Swarm Optimization (PSO)

The Early phase of the optimization, a plain gradient descent optimization has been used for model fitting. The result turns out that with a different initial parameters, the different best-fit model has changed which imply the local minimum in the problem. Even there is no method guarantee the global minimum but the heuristic optimization could be a better option for handling this type of problem. One kind of most widely used algorithm is particle swarm optimization (PSO) and it is invented by Kennedy & Eberhart (1995).

In order to get a best fit spectral indices, employing the Particle Swarm Optimization (PSO) by randomly initiate many particles in a given range of the parameter space and find the local and global best fit in each step of iteration. Then rest of them would slowly moving toward to the local and global position in parameter space with a proper weight. The iteration process will stop when the standard deviation of objective function from every particle less than a decimal. The explicit formula for every iteration k , particle i move with velocity v_k^i is

$$v_{k+1}^i = \omega v_k^i + c^b r_k^b [b_k^i - x_k^i] + c^B r_k^B [B_k^i - x_k^i], \quad (4.14)$$

and updating the particle i with

$$x_{k+1}^i = x_k^i + v_{k+1}^i. \quad (4.15)$$

where

- x_k^i represent variable that particle i hold
- b and B are best local and global parameter sets along the optimization process
- Set $\omega = 0.2$, $c^b = 0.2$ and $c^B = 0.3$

4.5 Statistical significance

Certainly, a larger model parameters or complexity would yield a better performance except it is overfitting the problem. The critical issue is to answer how much significane the alternative model could outperform the trivial model. As the language of statistics would consider as two hypothesis. One for null and one for alternative approach.

For this case, BPL has 2 more degree of freedom (DOF) than SPL. Unquestionably, if there is a good optimization procedure, the objectives function would say BPL is better SPL. As mentioned from the previous paragraph, the significance level has to be taken into account to put the weight on the study. Theoretically, regarding the model likelihood with a given set of parameters could be determined in the general case as Wilk's theorem define the realtion in Equation 4.16.

$$\mathcal{L} \equiv \prod_{\alpha=1}^n f(x_\alpha, \theta_1, \theta_2, \dots, \theta_h) \quad (4.16)$$

where

- x_α is represent a variant from model and data

- θ_i is a degree of freedom (DOF)

The practical usage to compare the null hypothesis and the alternative hypothesis as similar to one-tail hypothesis testing with a given dependency in more DOF has been adopted by Huelsenbeck & Crandall (1997). This method called “Likelihood ratio test (LRT)”. The compact formula is shown in Equation 4.17.

$$\text{LRT} = -2 \ln \left(\frac{\mathcal{L}_{\text{null}}}{\mathcal{L}_{\text{alternative}}} \right) \quad (4.17)$$

4.6 Error Determination

Monte Carlo Simulation

CHAPTER V

RESULTS AND DISCUSSION

The content of this chapter would be reported as the analysis procedure from step one to the end. The first part is the data correction process, count maps from the raw count as well as exposure map from the parallel computation, the spectrum and inversion model fitting by heuristic optimization.

5.1 Limb's angle correction

Theoretically, the peak profile of the θ_{NADIR} would be the same. From the observations, the of nadir angle change through time evolving since the spacecraft altitude is gradually getting lower in each year which will affect the LAT point of view when it see the Earth.

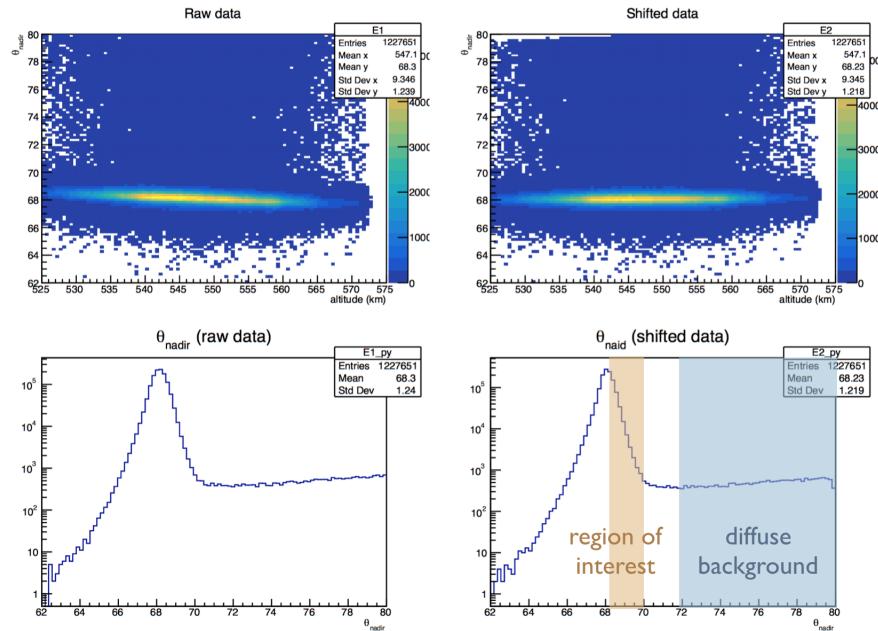


Figure 5.1: Distribution of nadir angle before and after altitude correction

The top-left of Figure 5.1 demonstrates how much spacecraft orbitting

altitude correlate to the θ_{NADIR} by a 2D heatmap plot of photon intensity. The bottom-left histogram came from the projection of the previous raw count 2-D histogram which has a peak around 68° . Both bottom and top right histograms was contructed from exactly same logic but there is one different variable. The shifted nadir angle has been calculated to reduce the effect from the spacecraft and the region of interest has been highlighted as orange for calculating as the limb spectrum and the blue zone is a diffusive background to be used in the background subtraction.

5.2 γ -ray measurement

5.2.1

5.3 Best fit result

5.4 Error determination

CHAPTER VI

CONCLUSION

example cite Curie (1923)

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APPENDICES

APPENDIX A

TESTING THE EXPOSURE MAP

APPENDIX B

POWER LAW IN ENERGY

APPENDIX C
INTERACTION MODEL

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