W25 HW3

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Problem 1: Age Data Preprocessing

Suppose that we have age data including the following numbers in sorted order. Then answer the questions below.

```
age <- c(13, 15, 16, 16, 19, 20, 20, 21, 22, 22, 25, 25, 25, 25, 30, 33, 33, 35, 35, 35, 35, 36, 40, 45
```

(a) Smoothing by bin means (bin depth = 3)

```
depth <- 3
nbins <- floor(length(age) / depth)</pre>
smoothed <- c() # create empty vector</pre>
for (i in 0:(nbins - 1)) { # loop through bins of data
  start <- i * depth + 1
  end <- start + depth - 1
  bin <- age[start:end] # add age data to bin</pre>
  bin_mean <- mean(bin) # calculate mean</pre>
  smoothed <- c(smoothed, rep(bin_mean, depth)) # populate bin with mean values
}
# add remaining values
if (length(age) > nbins * depth) {
  remaining <- age[(nbins * depth + 1):length(age)]</pre>
  smoothed <- c(smoothed, rep(mean(remaining), length(remaining)))</pre>
}
smoothed_result <- data.frame(Original = age, Smoothed = smoothed)</pre>
smoothed_result
```

```
## 0riginal Smoothed
## 1 13 14.66667
## 2 15 14.66667
## 3 16 14.66667
## 4 16 18.33333
## 5 19 18.33333
## 6 20 18.33333
```

```
## 7
            20 21.00000
## 8
            21 21.00000
## 9
            22 21.00000
            22 24.00000
## 10
## 11
            25 24.00000
## 12
            25 24.00000
## 13
            25 26.66667
## 14
            25 26.66667
## 15
            30 26.66667
## 16
            33 33.66667
## 17
            33 33.66667
## 18
            35 33.66667
            35 35.00000
## 19
## 20
            35 35.00000
## 21
            35 35.00000
## 22
            36 40.33333
## 23
           40 40.33333
## 24
            45 40.33333
## 25
            46 56.00000
## 26
            52 56.00000
## 27
            70 56.00000
```

Comment: Smoothing by bin means reduces variance and helps reveal patterns, but can distort outliers.

(b) Outlier detection using IQR

```
Q1 <- quantile(age, 0.25)
Q3 <- quantile(age, 0.75)
IQR_val <- IQR(age)

lower_bound <- Q1 - (1.5 * IQR_val)
upper_bound <- Q3 + (1.5 * IQR_val)

outliers <- age[age < lower_bound | age > upper_bound]
cat("The outliers for the data set are:", outliers, "\n")
```

The outliers for the data set are: 70

(c) Min-max normalization of age 35 to [0.0, 1.0]

```
minmax <- (35 - min(age)) / (max(age) - min(age))
cat("The min-max normalization of age 35 to [0.0, 1.0] is:", minmax, "\n")
```

The min-max normalization of age 35 to [0.0, 1.0] is: 0.3859649

(d) Z-score normalization of age 35

```
mean_age <- mean(age)
sd_age <- sd(age)
z_score <- (35 - mean_age) / sd_age
cat("The z-score normalization of age 35 is:", z_score, "\n")</pre>
```

The z-score normalization of age 35 is: 0.3891971

(e) Decimal scaling normalization of age 35

```
k <- nchar(as.character(max(abs(age))))
decimal_scaled <- 35 / (10^k)
cat("The decimal scaling normalization of age 35 is:", decimal_scaled, "\n")
## The decimal scaling normalization of age 35 is: 0.35</pre>
```

Problem 2: Min-Max Normalization Function

```
minmax_normalize <- function(a, min_new, max_new) {
    min_old <- min(a)
    max_old <- max(a)
    scaled <- (a - min_old) / (max_old - min_old)
    scaled * (max_new - min_new) + min_new
}

# Test usage

cat("The min max normalization function with values 10, 20 produces:\n", minmax_normalize(age, 10, 20),

## The min max normalization function with values 10, 20 produces:
## 10 10.35088 10.52632 10.52632 11.05263 11.22807 11.22807 11.40351 11.57895 11.57895 12.10526 12.1052

cat("\n")

cat("The min max normalization function with values 0.0 , 1.0 produces:\n", minmax_normalize(age, 0, 1)

## The min max normalization function with values 0.0 , 1.0 produces:</pre>
```

0 0.03508772 0.05263158 0.05263158 0.1052632 0.122807 0.122807 0.1403509 0.1578947 0.1578947 0.2105

Problem 3: Information Gain for Decision Tree

The formula for information gain is given by $InfoGain(T, A) = Entropy(T) - \sum_{v \in Values(A)} \frac{|T_v|}{|T|} \cdot Entropy(T_v)$, where T is the full dataset and T_v is a subset corresponding to value v of attribute A.

```
data <- data.frame(</pre>
  department = c("sales", "sales", "systems", "systems", "systems", "systems", "marketing", "m
  age = c("31_35", "26_30", "31_35", "21_25", "31_35", "26_30", "41_45", "36_40", "31_35", "46_50", "26
  salary = c("46K_50K", "26K_30K", "31K_35K", "46K_50K", "66K_70K", "46K_50K", "66K_70K", "46K_50K", "4
 status = c("senior", "junior", "junior", "senior", "junior", "senior", "senior", "senior", "junior",
  count = c(30, 40, 40, 20, 5, 3, 3, 10, 4, 4, 6)
#print(data)
entropy <- function(p) {</pre>
 p \leftarrow p[p > 0]
  -sum(p * log2(p))
# Step 1: calculate overall dataset entropy
status_total <- aggregate(count ~ status, data = data, sum)</pre>
total_count <- sum(status_total$count)</pre>
p_class <- status_total$count / total_count</pre>
entropy_total <- entropy(p_class)</pre>
cat("The entropy of the dataset is:", entropy_total, "\n")
## The entropy of the dataset is: 0.8990308
# Step 2: calculate informtion for attributes
info_gain <- function(df, attr) {</pre>
  vals <- unique(df[[attr]]) # get unique attribute values</pre>
  weighted_entropy <- 0</pre>
  for (val in vals) {
    subset <- df[df[[attr]] == val, ]</pre>
    subset_total <- sum(subset$count) # count number of records in subset</pre>
    junior_count <- sum(subset$count[subset$status == "junior"])</pre>
    senior count <- sum(subset$count[subset$status == "senior"])</pre>
    p_junior <- junior_count / subset_total #probability (junior)</pre>
    p_senior <- senior_count / subset_total #probability (senior)</pre>
    subset_entropy <- entropy(c(p_junior, p_senior))</pre>
    weighted_entropy <- weighted_entropy + (subset_total / total_count) * subset_entropy</pre>
  gain <- entropy_total - weighted_entropy # info qain = total entropy - weighted subset entropy
 return(gain)
# Calculate info gain for each attribute
cat("The info gain for department is:", info_gain(data, "department"), "\n")
```

The info gain for department is: 0.04860679

```
cat("The info gain for age is:", info_gain(data, "age"), "\n")

## The info gain for age is: 0.4247351

cat("The info gain for salary is:", info_gain(data, "salary"), "\n")

## The info gain for salary is: 0.5375181
```

Problem 4: If-Then Rules from Decision Tree

```
cat(" Root of decision tree is Salary (highest info gain)\n",
   "First split is on Department\n",
   "Age split is not needed\n")
## Root of decision tree is Salary (highest info gain)
## First split is on Department
## Age split is not needed
cat(" If salary = 26k_30k then status = junior\n",
   "If salary = 31k_35k then status = junior\n",
    "If salary = 36k_40k then status = senior\n",
    "If salary = 41k_45k then status = junior\n",
   "If salary = 46k_50k and department = sales then status = senior\n",
   "If salary = 46k 50k and department = systems then status = junior\n",
   "If salary = 46k_50k and department = marketing then status = senior\n",
   "If salary = 66k_70k then status = senior")
## If salary = 26k_30k then status = junior
## If salary = 31k_35k then status = junior
## If salary = 36k_40k then status = senior
## If salary = 41k_45k then status = junior
## If salary = 46k 50k and department = sales then status = senior
## If salary = 46k_50k and department = systems then status = junior
## If salary = 46k_50k and department = marketing then status = senior
## If salary = 66k_70k then status = senior
```