APPM 4600 - HW #2 - Cambria C 1) (a)  $(1+x)^n = |+ nx + o(x) ds x - 70$   $(1+x)^n - |-nx = o(x)$  1|m  $(1+x)^n - |-nx = ||m| n(1+x)$  x = 70 x = 70 $= n \cdot (1)^{n-1} - n = n - n =$ 11m (0s(x = 0(12) as + 70

(d) 
$$\int_{0}^{\varepsilon} e^{-x^{2}} dx = 0(\varepsilon) \varepsilon = 0$$

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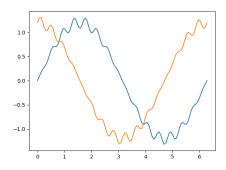
b) relative cond: K= John Action of # Ab2=2×10 Aby & Abo 2 2 relative error:

The relationship between relative error, condition number t perturbation is the following in the order of magnitude of the number relative - condition + perturbation error - number 1010 100-5 7 5=10-5 and order 1010 +10 -5 order of magnitude 5= because each value Hethe perturbations are the same, this behavior wouldn't change because the order of magnitudes of relative error, perturbation; scand that estill the same = pX when x=0, It is

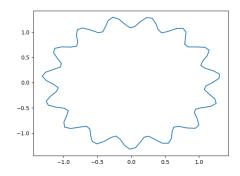
divide by O or subtract to O tor unstable (b) this algorithm isn't stable, because when x=0, you will be subtracting similar values, which gets us interfluence that the floating point arithmetic trouble; making the algorithm unstable (c) actual answer: 10-9 up to 10 decimal places algorithm answer: 1.0000000 82740 371000 1714 gives 7 digits, accurately This is expected because the algorithm Taylor series that is accurate to be digits: Check code - It is ventled - computer ) You don't get any digits of precision because the isimpler! taylor senes Both taylor & np. expm get the same

## Problem 4b ~ Wavy Circles

## **Fixed Parameters**

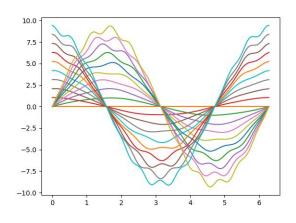


Parametric (x vs theta & y vs theta)

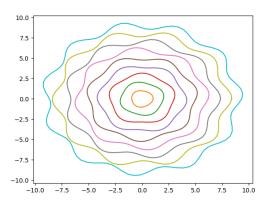


Parametric (x vs y)

## 10 Different Plots (for loops)



Parametric (x vs theta & y vs theta)



Parametric (x vs y)