

Causal inference is not just a statistics problem

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Causal Inference is not a
statistics problem

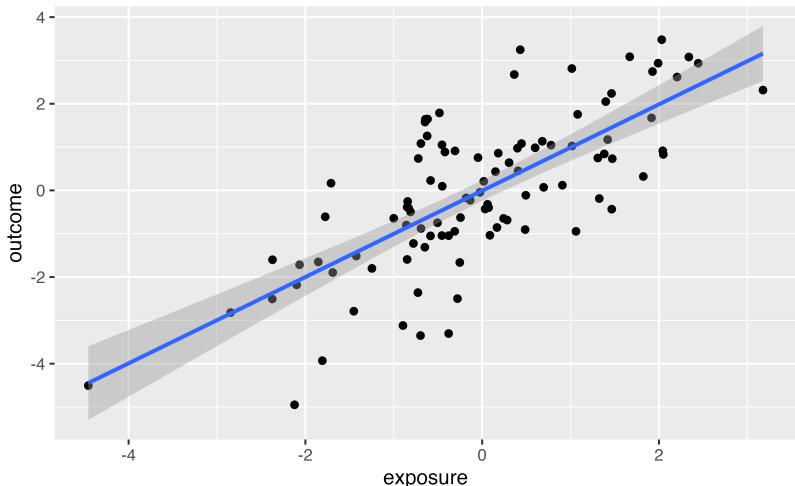
Causal Inference is not
just a statistics problem

The problem

We have measured variables, what should we adjust for?

exposure	outcome	covariate
0.49	1.71	2.24
0.07	0.68	0.92
0.40	-1.60	-0.10
•	•	•
•	•	•
•	•	•
0.55	-1.73	-2.34

A bit more info



```
1 cor(exposure, covariate)
```

```
[1] 0.7
```

The exposure and measured factor are positively correlated

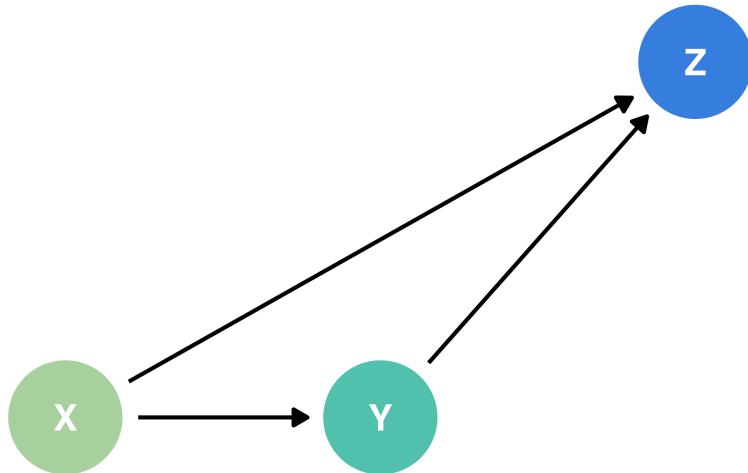
One unit increase in the exposure yields an average increase in the outcome of 1



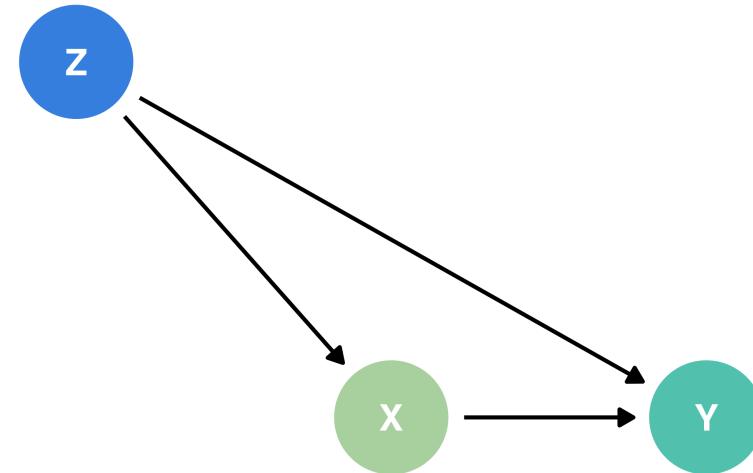
**To adjust or not
adjust? That is the
question.**

Causal Quartet

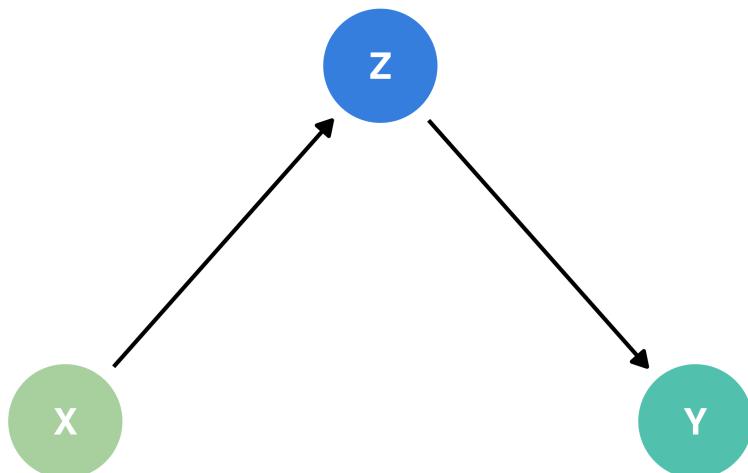
(1) Collider



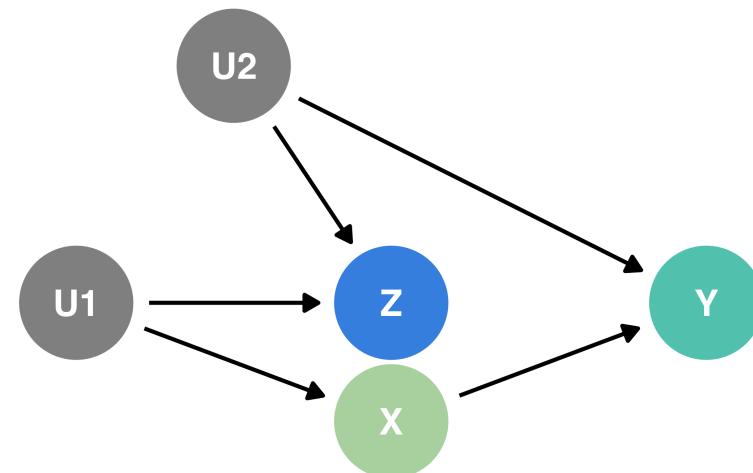
(2) Conounder



(3) Mediator



(4) M-bias





Your turn 1

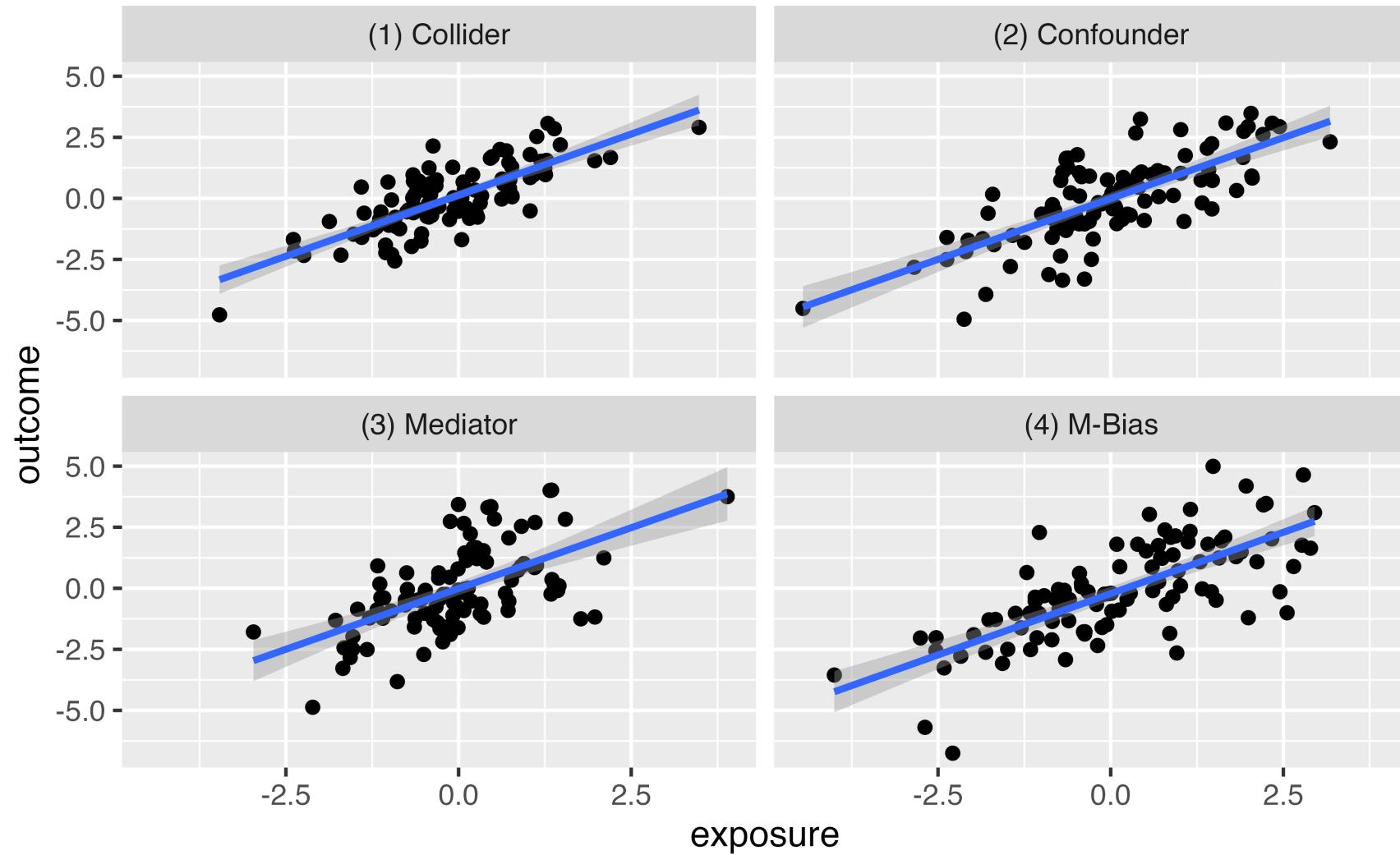
Load the **quartets** package

For each of the following 4 datasets, look at the correlation between **exposure** and **covariate**: **causal.collider**, **causal.confounding**, **causal.mediator**, **causal.m_bias**

For each of the above 4 datasets, create a scatterplot looking at the relationship between **exposure** and **outcome**

For each of the above 4 datasets, fit a linear model to examine the relationship between the **exposure** and the **outcome**

Relationship between exposure and outcome



Relationship between exposure and covariate

```
1 causal_quartet |>
2   group_by(dataset) |>
3   summarise(cor(exposure, covariate))

# A tibble: 4 × 2
  dataset      `cor(exposure, covariate)`
  <chr>          <dbl>
1 (1) Collider    0.700
2 (2) Confounder  0.696
3 (3) Mediator    0.696
4 (4) M-Bias       0.696
```

Correct effects

Data generating mechanism	Correct causal model	Correct causal effect
(1) Collider	$Y \sim X$	1.0
(2) Confounder	$Y \sim X ; Z$	0.5
(3) Mediator	Direct effect: $Y \sim X ; Z$ Total Effect: $Y \sim X$	Direct effect: 0.0 Total effect: 1.0
(4) M-Bias	$Y \sim X$	1.0

D'Agostino McGowan L, Gerke T, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

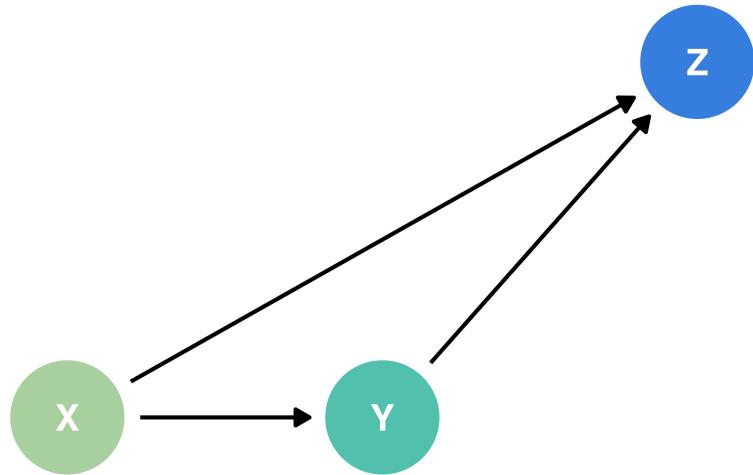
Observed effects

Data generating mechanism	ATE not adjusting for Z	ATE		Correlation of X and Z
		adjusting for Z	Z	
(1) Collider	1.00	0.55		0.70
(2) Confounder	1.00	0.50		0.70
(3) Mediator	1.00	0.00		0.70
(4) M-Bias	1.00	0.88		0.70

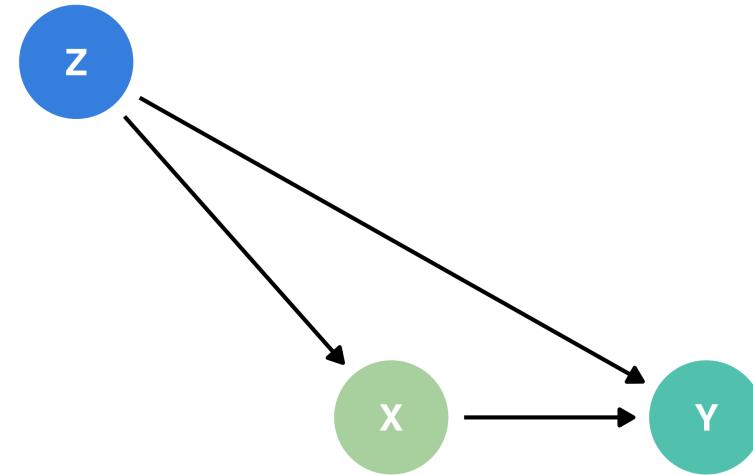
D'Agostino McGowan L, Gerke T, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

The solution

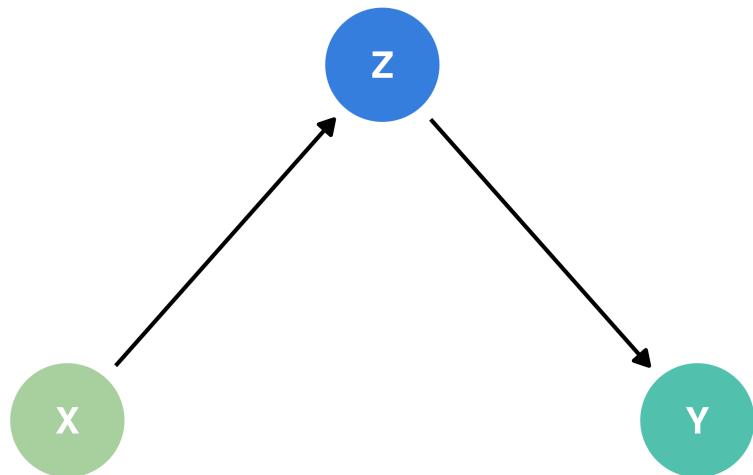
(1) Collider



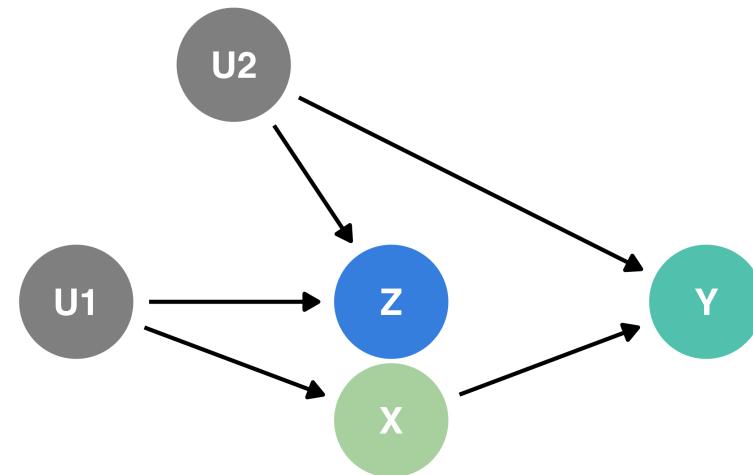
(2) Confounder



(3) Mediator



(4) M-bias



The *partial* solution

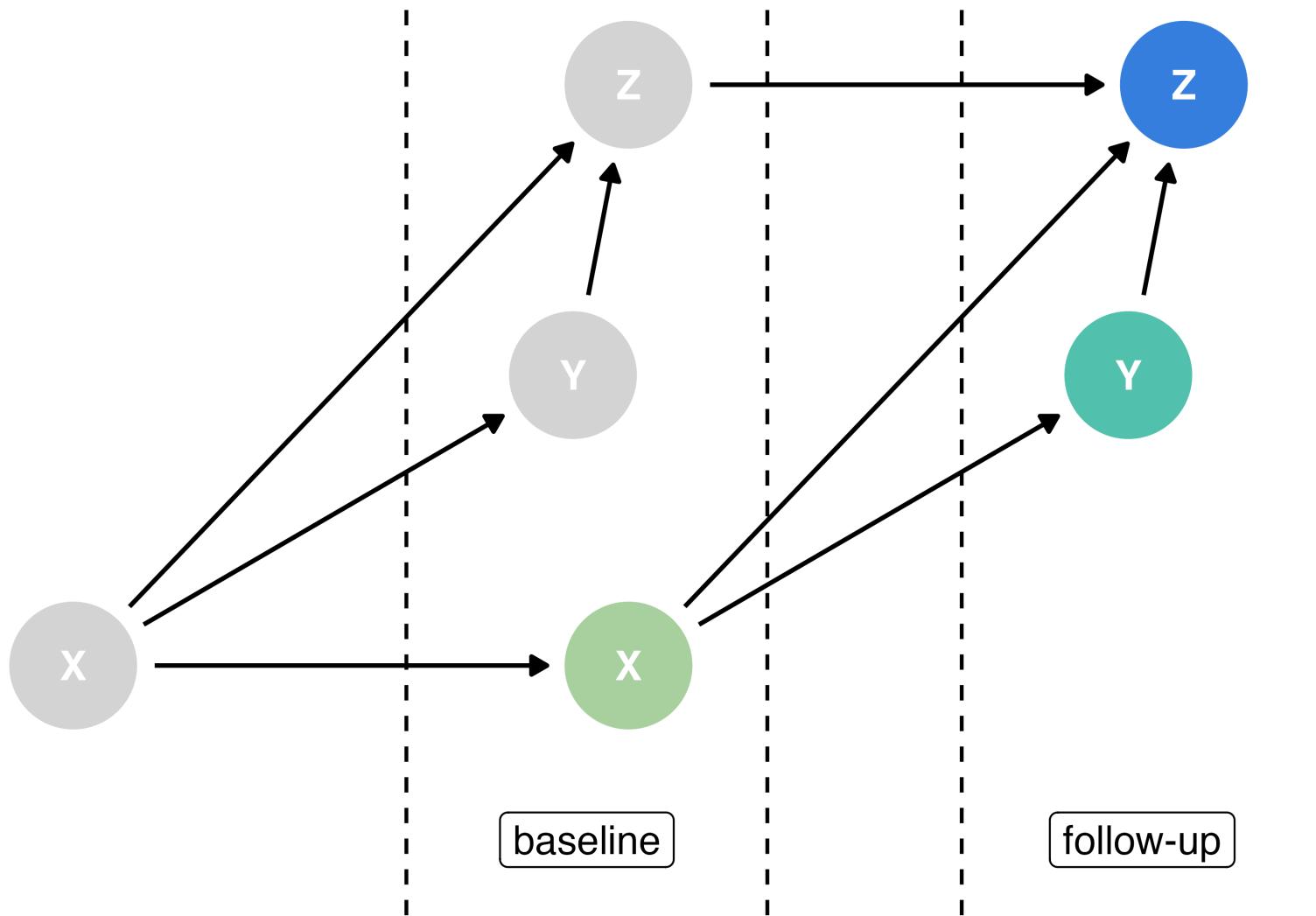
```
1 causal.collider_time

# A tibble: 100 × 6
  exposure_baseline outcome_baseline covariate_baseline
    <dbl>            <dbl>            <dbl>
1     -1.43           0.287          -0.0963
2      0.0593         -0.978          -1.11 
3      0.370           0.348           0.647 
4     0.00471          0.851           0.755 
5      0.340           1.94            1.19  
6     -3.61           -0.235          -0.588 
7      1.44            -0.827          -1.13  
8      1.02            -0.0410          0.689 
9     -2.43            -2.10            -1.49  
10     -1.26           -2.41            -2.78 

# i 90 more rows
# i 3 more variables: exposure_followup <dbl>,
#   outcome_followup <dbl>, covariate_followup <dbl>
```

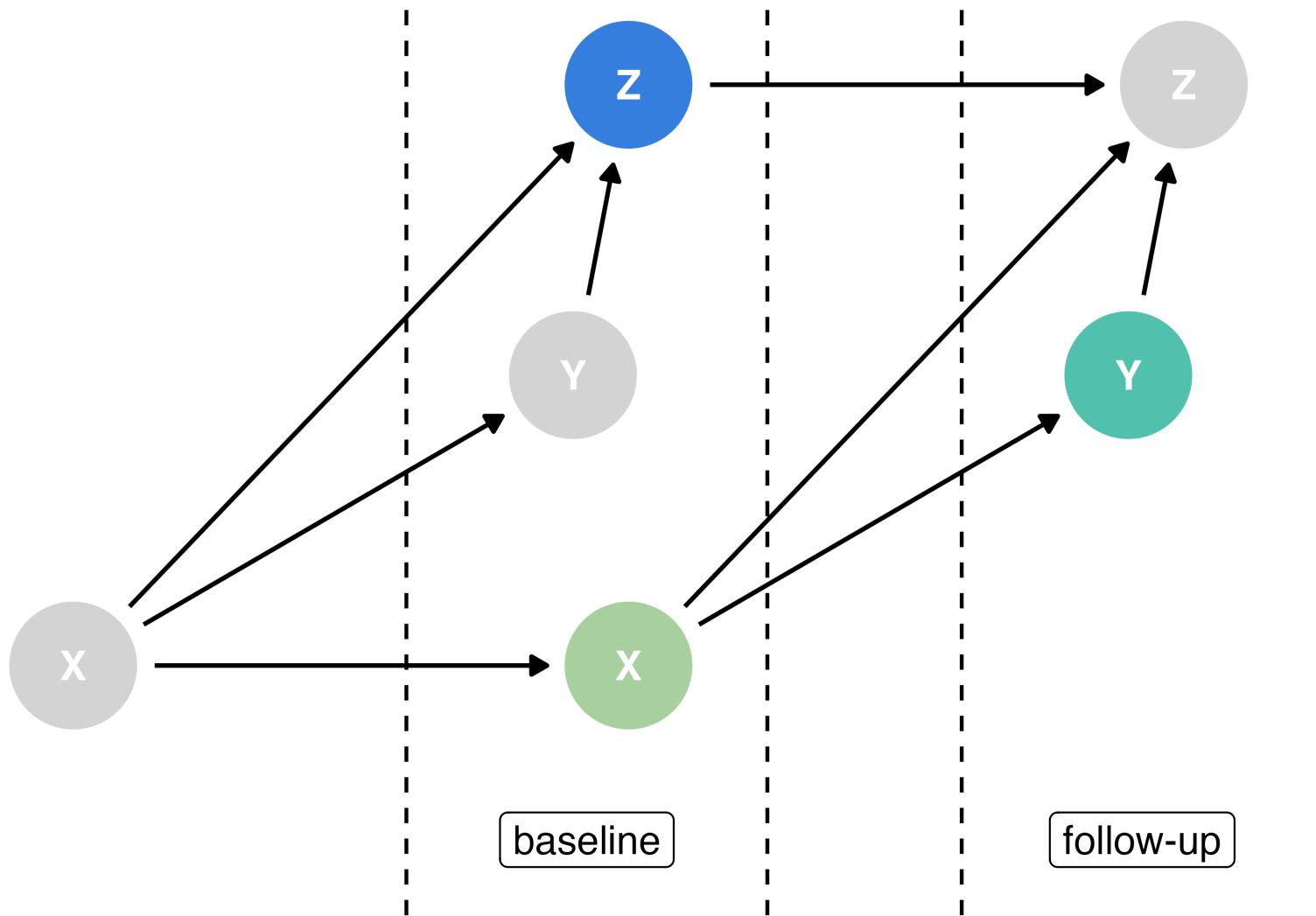
Time-varying data

Time-varying DAG



True causal effect: 1 Estimated causal effect: 0.55

Time-varying DAG



True causal effect: 1 Estimated causal effect: 1

```
outcome_followup ~ exposure_baseline +  
covariate_baseline
```

The *partial* solution

Data generating mechanism	ATE not adjusting for pre-exposure Z	ATE adjusting for pre-exposure Z	Correct causal effect
(1) Collider	1.00	1.00	1.00
(2) Confounder	1.00	0.50	0.50
(3) Mediator	1.00	1.00	1.00
(4) M-Bias	1.00	0.88	1.00

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On M-Bias

- The relationship between Z and the unmeasured confounders needs to be really large (Liu et al 2012)
- “To obsess about the possibility of [M-bias] generates bad practical advice in all but the most unusual circumstances” (Rubin 2009)
- There are (almost) no true zeros (Gelman 2011)
- Asymptotic theory shows that induction of M-bias is quite sensitive to various deviations from the exact M-Structure (Ding and Miratrix 2014)

Your turn 2

For each of the following 4 datasets, fit a linear linear model examining the relationship between **outcome_followup** and **exposure_baseline** adjusting for **covariate_baseline**:
causal_collider_time,
causal_confounding_time,
causal_mediator_time,
causal_m_bias_time

