

a)

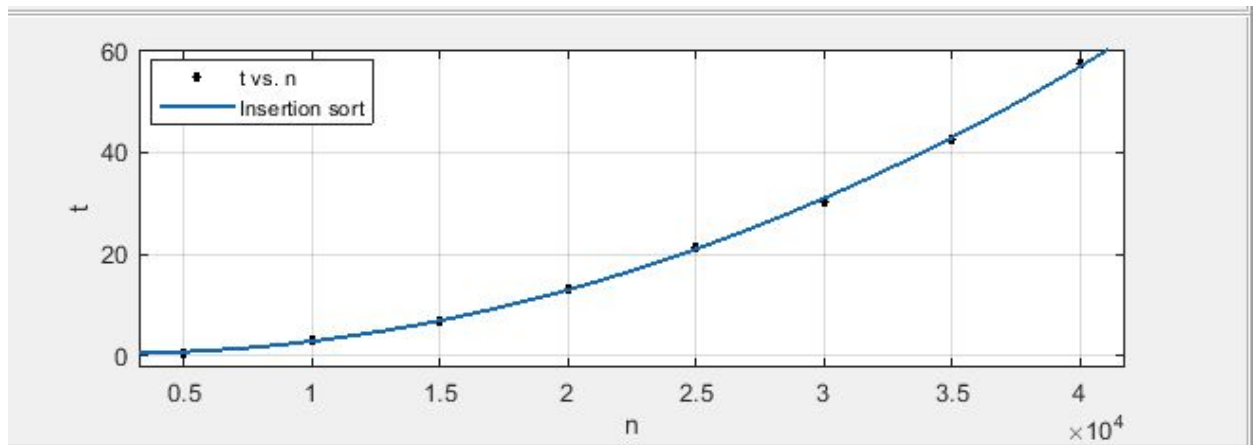
| | A | B |
|----|------------|-----------|
| 1 | Merge Sort | |
| 2 | n | t |
| 3 | 5000 | 0.015625 |
| 4 | 10000 | 0.03125 |
| 5 | 15000 | 0.046875 |
| 6 | 20000 | 0.0625 |
| 7 | 25000 | 0.078125 |
| 8 | 30000 | 0.09375 |
| 9 | 35000 | 0.109375 |
| 10 | 40000 | 0.125 |
| 11 | 45000 | 0.1484375 |
| 12 | 50000 | 0.171875 |

| | A | B |
|----|----------------|-------------|
| 1 | Insertion sort | |
| 2 | n | t (seconds) |
| 3 | 5000 | 0.578125 |
| 4 | 10000 | 3.171875 |
| 5 | 15000 | 6.9375 |
| 6 | 20000 | 13.296875 |
| 7 | 25000 | 21.5 |
| 8 | 30000 | 30.265625 |
| 9 | 35000 | 42.625 |
| 10 | 40000 | 57.40625 |
| 11 | | |

The arrays were generated using python's "random" library. The program would generate n many random numbers within the range [1 - 10,000], and store them in a list. This allowed for numbers to show up more than once.

b)

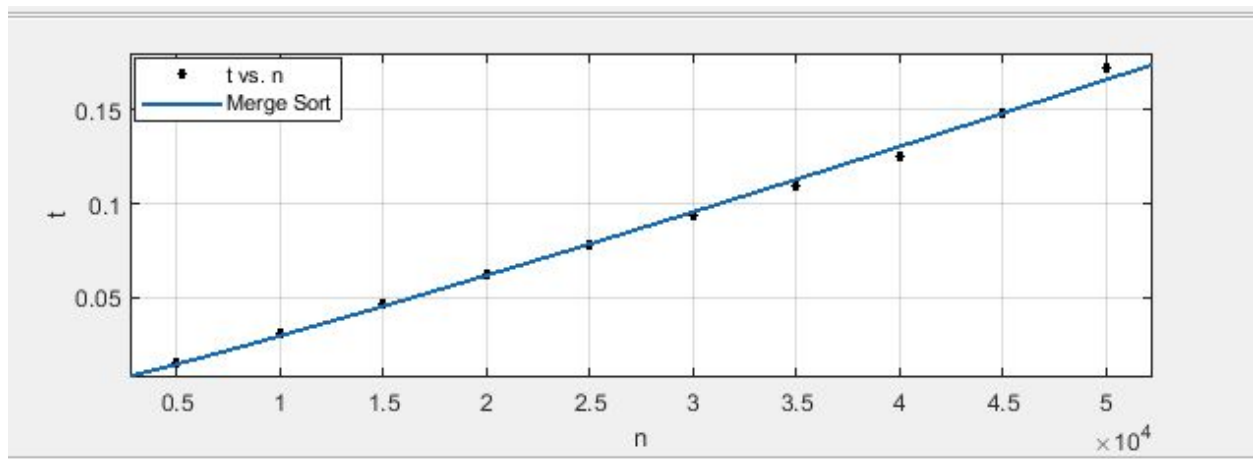
Insertion sort:



$$f(x) = p1 \cdot x^2 + p2 \cdot x + p3$$

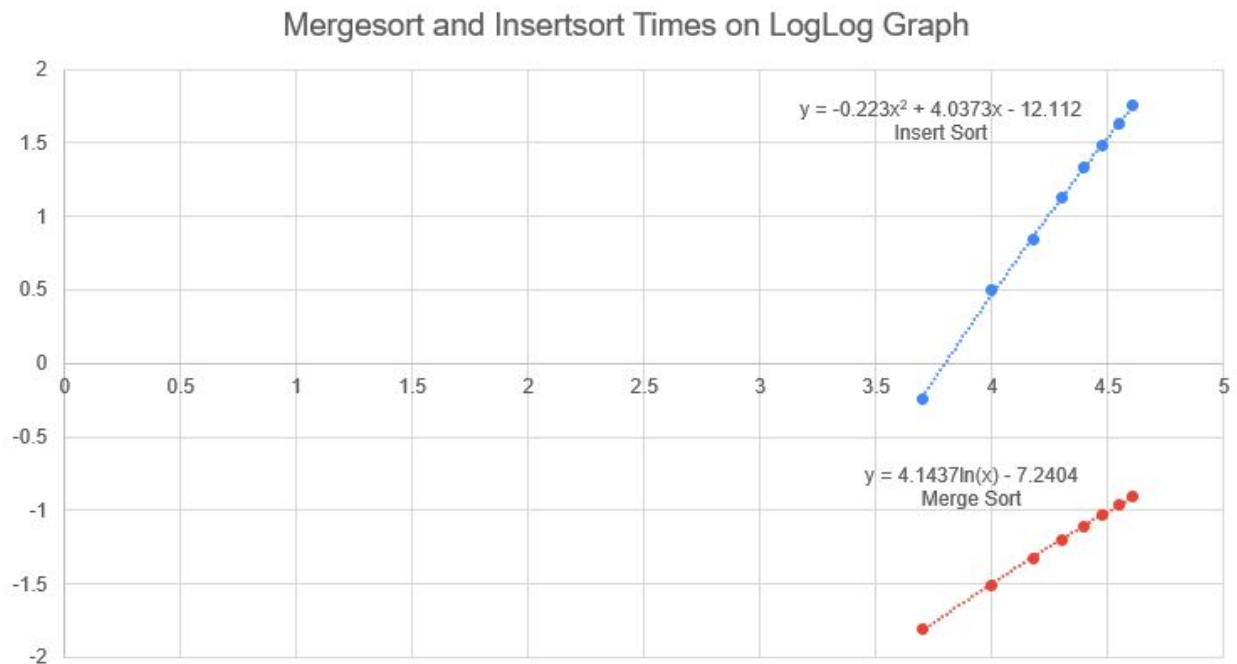
$$\begin{aligned} p1 &= 3.955e-08 \\ p2 &= -0.0001766 \\ p3 &= 0.7355 \end{aligned}$$

Merge sort:



$$\begin{aligned} f(x) &= a \cdot x \cdot \log(x) + b \\ a &= 3.025e-07 \\ b &= 0.001983 \end{aligned}$$

c)



d)

The expected time for insertion sort to sort 200,000 elements is 1547.42 seconds.

The expected time for merge sort to sort 200,000 elements is 0.32 seconds.

e)

Insertion sort: 1935.515625 seconds

This one was pretty in the range of the expected value, though with so many elements it's easy for the array to be in a starting state that isn't completely even in its randomness.

Merge sort: 0.84375 seconds

I think this one was pretty far off because the original data set was fairly linear looking, so for large numbers like 200,000, we wouldn't get close to the expected logarithmic graph.

Something like a much wider spanning data set would probably fix this issue.