On-the-Fly Free-Energy Parameterization (OTFP)

Basis-function expansion

$$ilde{F}(oldsymbol{z}) = \sum_k \lambda_k \phi_k(oldsymbol{z})$$

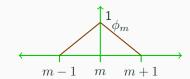
$$\frac{\partial E}{\partial \lambda} = 0 \to A\lambda = b \to \lambda = bA^{-1} \to \tilde{F}(z)$$

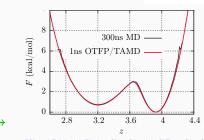
Minimize

Error estimate

$$E(\lambda) = \left\langle \sum_{j} \left[\kappa[z_{j} - \theta_{j}(\boldsymbol{x})] - \frac{\partial \tilde{F}(\boldsymbol{z})}{\partial z_{j}} \right]^{2} \right\rangle_{\text{TAMD}}$$

$$\begin{split} A_{nm} &= \frac{1}{2} \left\langle \sum_{i} \frac{\partial \phi_{m}(\mathbf{z})}{\partial z_{i}} \frac{\partial \phi_{n}(\mathbf{z})}{\partial z_{i}} \right\rangle_{\mathrm{TAMD}} \\ b_{m} &= \left\langle \sum_{i} \frac{\partial \phi_{m}(\mathbf{z})}{\partial z_{i}} \kappa[z_{i} - \theta_{i}(\mathbf{z})] \right\rangle_{\mathrm{TAMD}} \end{split}$$





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