Fixed-point-free permutations

Input: A set S of permutations of $\{1, \ldots, n\}$.

Probem: Does $G = \langle S \rangle$ contain a fixed-point-free element?

This problem is NP-complete in general. However, if we are promised that G is transitive, then it has a constant-time algorithm (Jordan 1873)