277B: Machine Learning Algorithms Homework assignment #4: Statistical Models for Regression and Classification Assigned Feb. 20 and Due Mar. 1

- **1. Baye's Theorem.** A chemical test is designed to indirectly determine whether the individual has a genetic marker predisposing him/her to having kidney disease. The chemical test has the following characteristics: the probability that a randomly chosen person who has the marker (M) will test positive (i.e. "marker present") is: P[+|M] = 0.95; the probability that a randomly chosen person who does not have the marker will test negative is: P[-|not M] = 0.95; the proportion of people who have the marker is: P[M] = 0.01.
- (a) Define the following quantities: P[-|M]; P[+|not M]; P[not M].
- (b) You have had a chemical test and have tested positive; should you be alarmed? To answer this, find what is the chance that a randomly selected person who tests positive for the marker actually has the marker by using Baye's Theorem. What feature of the given data accounts for the result?
- (c) Suppose that frequency of marker was higher by a factor of 10, i.e. P[M] = 0.10. What is the chance that a randomly selected individual from this group who test positive actually has the marker?
- **2.** Gaussian Naïve Bayes. We wish to classify 178 wines into 3 cultivars by solving it with Naïve Bayes. To do this we will classify the wines by assigning them to the cultivar with the largest P(cultivar $\mid X$), and to find this we must first define a labelled data set of P(wine attribute x \mid cultivar) pairings to learn the relationship where x is one of the attributes, and do this for all attributes.
- (a)(2pt) How should we represent P(wine attribute $x \mid \text{cultivar}$)? Fill in the code for Gaussian() function and give a reason that you choose this functional form. Given a wine that belongs to cultivar 1, what is the chance of it having an Alcohol % of 13 according to the probability distribution function?
- (b)(4pt) Using your normalized chemical descriptor data, divide your data into 3-fold training and testing groups, i.e. using 2/3 training and 1/3 testing for the three divisions and report the results.
- **3. Softmax and Cross Entropy Loss.** Work on the same wine dataset. Now we use another approach to do the classification. Implement a neural network model using PyTorch with no hidden layer (This is equivalent to a linear regression plus nonlinear activation function). Use softmax activation function in the last layer and use cross entropy loss as your loss function.
- (a) (3pt) Pass the data through the network once without backpropagation and print out the output. Observe the difference between with and without the softmax activation layer. What does softmax do?
- (b)(4pt) Divide data into 3-fold training and testing groups, within each fold further divide your training data into 80% training and 20% validation, choose the model for the epoch with lowest validation error. Report error in terms of success rate of classification. How good is the prediction relative to problem 2?