$$\mathcal{L}_{1} \xrightarrow{R} Sh(\mathcal{L}_{0}, J)$$

$$\mathcal{L}_{0} \xrightarrow{PSh} PSh(\mathcal{L}_{0})$$