CS 446: Machine Learning Homework 11

Due on Tuesday, April 17, 2018, 11:59 a.m. Central Time

| 1. [8 points] Generative Adversarial Netw | vork (GAN) |
|---|---|
| (a) What is the cost function for classic as the generator. | cal GANs? Use $D_w(x)$ as the discriminator and $G_{\theta}(x)$ |
| Your answer: | |
| the discriminator using $D(x)$, and | discriminator and generator. In this case we refer to denote the distribution on the data domain induced an equivalent problem to the one asked for in part |
| | |

| (c) | Assuming arbitrary capacity, derive the optimal discriminator $D^*(x)$ in terms of $p_{data}(x)$ and $p_G(x)$. You may need the Euler-Lagrange equation: |
|-----|--|
| | $2I(-D,\dot{D}) = I 2I(-D,\dot{D})$ |

$$\frac{\partial L(x, D, \dot{D})}{\partial D} - \frac{d}{dx} \frac{\partial L(x, D, \dot{D})}{\partial \dot{D}} = 0$$

where $\dot{D} = \partial D/\partial x$.

| Your answer: | | |
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(d) Assume arbitrary capacity and an optimal discriminator $D^*(x)$, show that the optimal generator, $G^*(x)$, generates the distribution $p_G^* = p_{data}$, where $p_{data}(x)$ is the data distribution

You may need the Jensen-Shannon divergence:

$$JSD(p_{\text{data}}, p_G) = \frac{1}{2}D_{KL}(p_{\text{data}}, M) + \frac{1}{2}D_{KL}(p_G, M) \quad \text{with} \quad M = \frac{1}{2}(p_{\text{data}} + p_G)$$

Your answer:

(e) More recently, researchers have proposed to use the Wasserstein distance instead of divergences to train the models since the KL divergence often fails to give meaningful information for training. Consider three distributions, $\mathbb{P}_1 \sim U[0,1]$, $\mathbb{P}_2 \sim U[0.5,1.5]$, and $\mathbb{P}_3 \sim U[1,2]$. Calculate $D_{KL}(\mathbb{P}_1,\mathbb{P}_2)$, $D_{KL}(\mathbb{P}_1,\mathbb{P}_3)$, $\mathbb{W}_1(\mathbb{P}_1,\mathbb{P}_2)$, and $\mathbb{W}_1(\mathbb{P}_1,\mathbb{P}_3)$, where \mathbb{W}_1 is the Wasserstein-1 distance between distributions.

Your answer: