LISTS

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Agenda

- Abstract data types and data structures
- List ADT
- List ADT as an array
- List ADT as a linked list
- Asymptotic efficiency of lists





Abstract data types and data structures

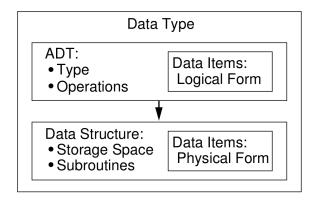
Important concepts

- Type: a collection of values
- Simple vs. composite type
- Data type: a type and operations to manipulate the type
- Abstract data type (ADT): a data type as a software component
- Data structure: implementation for an ADT
- Multiple implementations for the same ADT





Abstract data types and data structures¹







Source: C. Shaffer. Data Structures and Algorithm Analysis. 2013.

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List ADT

Mathematical abstraction

- Sequences of homogenous elements
- A symbol | to denote the current position of the cursor

Example

- Let *I* = ⟨20, 23 | 12, 15⟩
- After inserting 10 in *I*, we have $I' = \langle 20, 23 \mid 10, 12, 15 \rangle$
- After removing an element from I, we have $I'' = \langle 20, 23 \mid 12, 15 \rangle$





List ADT

Operations (let *E* be an arbitrary data type):

- void clear(List I);
- void insert(List I, E item);
- void append(List I, E item);
- E remove(List I);
- void moveToStart(List I);
- void moveToEnd(List I);
- void prev(List I);
- void next(List I);
- int length(List I);
- int currPos(List I);
- void moveToPos(List I, int pos);
- E getValue(List I);





Declaring an ADT in C

Type and operations as prototypes in a .h file

- A function prototype to create an instance of the ADT
- \blacksquare Provide to the functions the values to be manipulated (List* 1)

```
#ifndef _LIST_H
#define _LIST_H
typedef struct list List;
List* create_list(int size); // Creates a new list
void clear(List* 1);
void insert(List* 1, E item);
#endif
```





Declaring an ADT in Java

Typically, an interface, in addition to operations as abstract methods

- No need of a function prototype to create an instance of the ADT
- No need to provide to the methods the values to be manipulated

```
public interface List {

public void clear();

public void insert(E item);

// ...

}
```





Operations implemented in the logical level

We might have operations implemented in the logical level

Same implementation regardless of data structure

Algorithm: boolean find(List I, int k)

```
moveToStart(I);
while currPos(I) < length(I) do
if k = getValue(I) then
return true;
next(I);</pre>
```







return false:

Operations implemented in the logical level

Concrete functions defined in the *.h file

```
#ifndef LIST H
   #define _LIST_H
   // ...
   bool find(List* l, int k) {
       moveToStart(1):
       while(currPos(l) < length(l)) {</pre>
            if (k == getValue(l)) { return true; }
            next(1);
10
        return false;
11
12
   #endif
13
```





Operations implemented in the logical level

Concrete methods defined in an abstract class

```
public abstract class List {
        // ...
        public boolean find(int k) {
            this.moveToStart();
            while (this.currPos() < this.length()) {</pre>
                if (k == this.getValue()) { return true; }
                this.next();
            return false;
10
12
```





Agenda

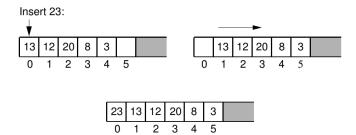
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List ADT implemented as an array²

Insertion



Deletion

Analogous implementation





² Source: C. Shaffer. Data Structures and Algorithm Analysis. 2013.

List ADT implemented as an array

Composite type:

Algorithm: List create_list(int size)

```
1. I.maxSize \leftarrow size;
```

- 2 *I.listSize* \leftarrow *I.curr* \leftarrow 0;
- 3 I.listArray \leftarrow new E[size];
- 4 return /;





List ADT implemented as an array (C)

Data structure: defined in a .c file

```
#include "list.h"
   typedef struct list {
       int maxSize; int listSize; int curr; E* listArray;
   } List;
   List* create list(int size) {
       List* 1 = (List*) malloc(sizeof(List));
       1->maxSize = size;
    1->listSize = 1->curr = 0;
       1->listArray = (E*) malloc(size * sizeof(E));
10
      return 1;
11
12
```





List ADT implemented as an array (Java)

Data structure: defined in a concrete class

```
public class ArrayList implements List { // List: an interface
       private int maxSize; private int listSize;
       private int curr; private E[] listArray;
       // The constructor has the role of ``create list''
       public ArrayList(int size) {
           this.maxSize = size;
           this.listSize = this.curr = 0;
           this.listArray = new E[size];
10
11
       //...
12
13
```





Algorithm: void insert(List I, E it)

```
if I.listSize ≥ I.maxSize then error;
i ← I.listSize;
while i > I.curr do
I.listArray[i] ← I.listArray[i − 1]; // shift right
i--;
I.listArray[I.curr] ← it;
```

- 6 $I.listArray[I.curr] \leftarrow it;$

insert(1,7), just after create_list(5) (c denotes curr)

index:	0	1	2	3	4
value:	-	-	-	-	-
	С				





Algorithm: void insert(List I, E it)

```
if I.listSize > I.maxSize then error;
i \leftarrow I.listSize:
while i > l.curr do
    I.listArray[i] \leftarrow I.listArray[i-1];
                                                             // shift right
    i--:
I.listArray[I.curr] \leftarrow it;
I.listSize++:
```

insert (1,7), just after create_list (5) (c denotes curr)

index:	0	1	2	3	4
value:	-	-	-	-	-
	С				
	i				





Algorithm: void insert(List I, E it)

```
if I.listSize ≥ I.maxSize then error;
i ← I.listSize;
while i > I.curr do
I.listArray[i] ← I.listArray[i - 1]; // shift right
i--;
I.listArray[I.curr] ← it;
```

insert(1,7), just after create_list(5) (c denotes curr)

index:	0	1	2	3	4
value:	7	-	-	-	-
	С				
	i				





I.listSize++;

Algorithm: void insert(List I, E it)

```
if I.listSize > I.maxSize then error;
    i \leftarrow I.listSize:
    while i > l.curr do
        I.listArray[i] \leftarrow I.listArray[i-1];
4
                                                                  // shift right
        i--:
5
    I.listArray[I.curr] \leftarrow it;
```

insert(1,5)

I.listSize++:

index:	0	1	2	3	4
value:	7	-	-	-	-
	С				
		i			





Algorithm: void insert(List I, E it)

```
i if I.listSize ≥ I.maxSize then error;
i ← I.listSize;
while i > I.curr do
I.listArray[i] ← I.listArray[i - 1];
// shift right
I.listArray[I.curr] ← it;
```

insert(1,5)

I.listSize++:

index:	0	1	2	3	4
value:	7	7	-	-	-
	С				
		i			





Algorithm: void insert(List I, E it)

```
if I.listSize ≥ I.maxSize then error;
i ← I.listSize;
while i > I.curr do
I.listArray[i] ← I.listArray[i - 1]; // shift right
i--;
I.listArray[I.curr] ← it;
```

insert(1,5)

I.listSize++:

index:	0	1	2	3	4
value:	7	7	-	-	-
	С				
	i				





Algorithm: void insert(List I, E it)

```
i if I.listSize ≥ I.maxSize then error;
i ← I.listSize;
while i > I.curr do
I.listArray[i] ← I.listArray[i - 1];
// shift right
I.listArray[I.curr] ← it;
```

insert(1,5)

I.listSize++;

index:	0	1	2	3	4
value:	5	7	-	-	-
	С				
	i				





List ADT implemented as an array

Algorithm: void moveToStart(List I)

1 $l.curr \leftarrow 0$;

Algorithm: void moveToEnd(List I)

1 $l.curr \leftarrow l.listSize$;

Algorithm: void prev(List I)

if $l.curr \neq 0$ then l.curr--;

Algorithm: void next(List I)

if I.curr < I.listSize then curr++;</pre>





Algorithm: E remove(List I)

```
if I.curr < 0 ∨ curr ≥ listSize then return NULL;
E it ← I.listArray[I.curr]; i ← I.curr;
while i < I.listSize − 1 do
I.listArray[i] ← I.listArray[i + 1]; // shift left
i++;
I.listSize--;</pre>
```

remove(1), just after insert(1,2); next(1)

index:	0	1	2	3	4
value:	2	5	7	-	-
		С			





return it:

Algorithm: E remove(List I)

index:	0	1	2	3	4
value:	2	5	7	-	-
		С			
		i			





Algorithm: E remove(List I)

```
if I.curr < 0 ∨ curr ≥ listSize then return NULL;
E it ← I.listArray[I.curr]; i ← I.curr;
while i < I.listSize − 1 do
I.listArray[i] ← I.listArray[i + 1]; // shift left
i++;
I.listSize--;
return it;</pre>
```

index:	0	1	2	3	4
value:	2	7	7	-	-
		С			
		i			





Algorithm: E remove(List I)

```
if I.curr < 0 ∨ curr ≥ listSize then return NULL;
E it ← I.listArray[I.curr]; i ← I.curr;
while i < I.listSize − 1 do
I.listArray[i] ← I.listArray[i + 1]; // shift left
i++;
I.listSize--;
return it;</pre>
```

index:	0	1	2	3	4
value:	2	7	7	-	-
		С			
			i		





Algorithm: E remove(List I)

```
if I.curr < 0 ∨ curr ≥ listSize then return NULL;
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while i < I.listSize − 1 do
I.listArray[i] ← I.listArray[i + 1]; // shift left
i++;
I.listSize--;
return it;</pre>
```

index:	0	1	2	3	4
value:	2	7	7	-	-
		С			
			i		





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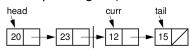


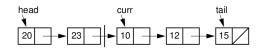
List ADT implemented as a linked list³

Empty list: header node vs. space cases (insert and remove)



Attention to where curr is pointing to (not as follows)



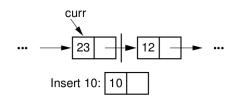


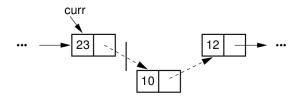




 $^{^3\}mbox{Source}$ C. Shaffer. Data Structures and Algorithm Analysis. 2013.

List ADT implemented as a linked list: insertion⁴



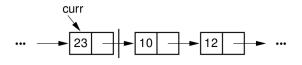


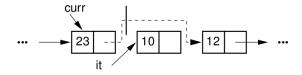




⁴Source: C. Shaffer. Data Structures and Algorithm Analysis. 2013.

List ADT implemented as a linked list: deletion⁵





Important: memory deallocation

- With no garbage collection: user's duty
- With garbage collection: GC's duty





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⁵ Source: C. Shaffer. Data Structures and Algorithm Analysis. 2013.

List ADT implemented as a linked list

Composite type (Link):

Algorithm: Link create_link(E it, Link nextval)

n.element \leftarrow *it*; *n.next* \leftarrow *nextval*; **return** *n*;

Algorithm: Link create_link(Link nextval)

1 $n.next \leftarrow nextval$; return n;





List ADT implemented as a linked list

Composite type (List):

- 1 Link head;
- 2 Link tail;
- 3 Link curr;
- 4 int *cnt*;

// list size

Algorithm: List create_list()

```
1 l.curr \leftarrow l.tail \leftarrow l.head \leftarrow create\_link(NULL); // header node
```

- 2 *l.cnt* \leftarrow 0;
- з return /;

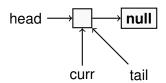




List ADT implemented as a linked list: <|> ↔ <|7>

Algorithm: void insert(List I, E it)

- $l.curr.next \leftarrow create_link(it, l.curr.next);$
- **if** l.tail = l.curr **then** $l.tail \leftarrow l.curr.next$:
- 1.cnt++;



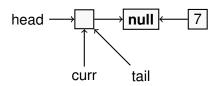




List ADT implemented as a linked list: <|> ↔ <|7>

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- **if** l.tail = l.curr **then** $l.tail \leftarrow l.curr.next$:
- 1.cnt++;



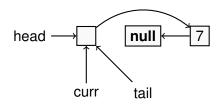




List ADT implemented as a linked list: <|> ↔ <|7>

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- $l.curr.next \leftarrow create_link(it, l.curr.next);$
- **if** l.tail = l.curr **then** $l.tail \leftarrow l.curr.next$:
- 1.cnt++;



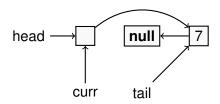




List ADT implemented as a linked list: <|> → <|7>

Algorithm: void insert(List I, E it)

- 1 I.curr.next ← create_link(it, I.curr.next);
- if l.tail = l.curr then $l.tail \leftarrow l.curr.next$;
- 3 *l.cnt*++;





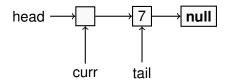


List ADT implemented as a linked list: <|> → <|7>

Algorithm: void insert(List I, E it)

- 1 $l.curr.next \leftarrow create_link(it, l.curr.next);$
- if I.tail = I.curr then I.tail \leftarrow I.curr.next;
- 3 *l.cnt*++;

Better presented as follows





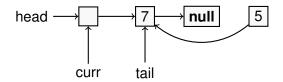


List ADT implemented as a linked list: <|7> → <|5,7>

Algorithm: void insert(List I, E it)

- 1 I.curr.next ← create_link(it, I.curr.next);
- if I.tail = I.curr then I.tail \leftarrow I.curr.next;
- 3 *l.cnt*++;

insert(1,5)





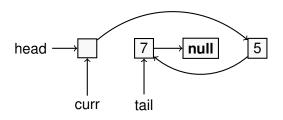


List ADT implemented as a linked list: <|7> → <|5,7>

Algorithm: void insert(List I, E it)

- $l.curr.next \leftarrow create_link(it, l.curr.next);$
- **if** l.tail = l.curr **then** $l.tail \leftarrow l.curr.next$:
- 1.cnt++;

insert(1,5)





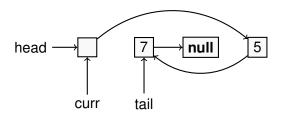


List ADT implemented as a linked list: <|7> → <|5,7>

Algorithm: void insert(List I, E it)

- $l.curr.next \leftarrow create_link(it, l.curr.next);$
- **if** l.tail = l.curr **then** $l.tail \leftarrow l.curr.next$:
- 1.cnt++;

insert(1,5)







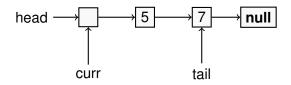
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List ADT implemented as a linked list: $< |7> \leftrightarrow < |5,7>$

Algorithm: void insert(List I, E it)

- $l.curr.next \leftarrow create_link(it, l.curr.next);$
- **if** l.tail = l.curr **then** $l.tail \leftarrow l.curr.next$:
- 1.cnt++;

Better presented as follows







List ADT implemented as a linked list

Algorithm: void moveToStart(List I)

I.curr ← I.head:

Algorithm: void prev(List I)

- if *l.curr* = *l.head* then return:
- 2 Link temp \leftarrow 1.head;
- **while** $temp.next \neq l.curr$ **do** $temp \leftarrow temp.next$;
- $l.curr \leftarrow temp;$

Algorithm: void next(List I)

if $l.curr \neq l.tail$ then $l.curr \leftarrow l.curr.next$;



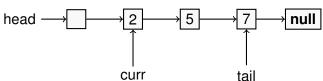


List ADT impl. as a linked list: <2|5,7> → <2|7>

Algorithm: E remove(List I)

- if I.curr.next = NULL then return NULL;
- 2 E it ← I.curr.next.element;
- if l.tail = l.curr.next then $l.tail \leftarrow l.curr$;
- 4 *l.curr.next* ← *l.curr.next.next*; *l.cnt--*;
- 5 **return** *it*;

remove(1), just after insert(1,2); next(1)





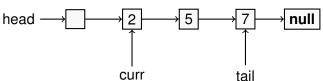


List ADT impl. as a linked list: $\langle 2|5,7 \rangle \leftrightarrow \langle 2|7 \rangle$

Algorithm: E remove(List I)

- **if** *l.curr.next* = *NULL* **then return** *NULL*:
- $E it \leftarrow I.curr.next.element$:
- **if** l.tail = l.curr.next **then** $l.tail \leftarrow l.curr$:
- $l.curr.next \leftarrow l.curr.next.next$; l.cnt--;
- return it:

```
remove(1), just after insert(1,2); next(1)
```





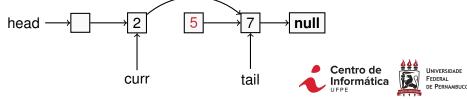


List ADT impl. as a linked list: <2|5,7> → <2|7>

Algorithm: E remove(List I)

- if I.curr.next = NULL then return NULL;
- ≥ E it ← I.curr.next.element;
- if l.tail = l.curr.next then $l.tail \leftarrow l.curr$;
- 4 I.curr.next ← I.curr.next.next; I.cnt--;
- 5 **return** it:

remove(1), just after insert(1,2); next(1)

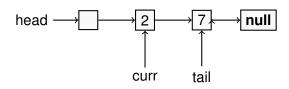


List ADT impl. as a linked list: <2|5,7> → <2|7>

Algorithm: E remove(List I)

- if I.curr.next = NULL then return NULL;
- 2 $E it \leftarrow I.curr.next.element$;
- if l.tail = l.curr.next then $l.tail \leftarrow l.curr$;
- 4 *l.curr.next* ← *l.curr.next.next*; *l.cnt--*;
- 5 **return** *it*;

After memory deallocation (by the user or by the GC)







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Asymptotic efficiency of lists⁶

Data Structure	Time Complexity								Space Complexity
	Average				Worst				Worst
	Access	Search	Insertion	Deletion	Access	Search	Insertion	Deletion	
<u>Array</u>	0(1)	O(n)	0(n)	O(n)	0(1)	0(n)	0(n)	0(n)	0(n)
Stack	O(n)	O(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
<u>Queue</u>	O(n)	0(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Singly-Linked List	O(n)	0(n)	0(1)	Θ(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Doubly-Linked List	O(n)	0(n)	0(1)	0(1)	0(n)	0(n)	0(1)	0(1)	0(n)
Skip List	O(log(n))	O(log(n))	0(log(n))	0(log(n))	0(n)	0(n)	0(n)	0(n)	O(n log(n))
Hash Table	N/A	0(1)	0(1)	0(1)	N/A	O(n)	0(n)	0(n)	0(n)
Binary Search Tree	0(log(n))	Θ(log(n))	0(log(n))	Θ(log(n))	0(n)	0(n)	0(n)	0(n)	0(n)
Cartesian Tree	N/A	Θ(log(n))	0(log(n))	Θ(log(n))	N/A	0(n)	0(n)	0(n)	0(n)
B-Tree	O(log(n))	Θ(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)
Red-Black Tree	0(log(n))	O(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)
Splay Tree	N/A	O(log(n))	0(log(n))	O(log(n))	N/A	0(log(n))	0(log(n))	0(log(n))	0(n)
AVL Tree	O(log(n))	Θ(log(n))	O(log(n))	Θ(log(n))	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)
KD Tree	O(log(n))	Θ(log(n))	0(log(n))	Θ(log(n))	0(n)	0(n)	0(n)	0(n)	0(n)

IF672 - Algorithms and Data Structures





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 $^{^6}$ Source: http://bigocheatsheet.com/

Other considerations

List ADT as an array

- ± Predefined maximum size (alternative: dynamic arrays)
 - Dynamic allocation of arrays does not imply dynamic arrays
 - Amortised analysis (append): cost of copy becomes not relevant
- + No extra space with pointers (links)
- Space consumed by unused positions

List ADT as a linked list

- + With no predefined maximum size
- + No extra space for no longer accessible elements
- Space consumed by pointers (links)





Other considerations

List ADT as an array

- ± Predefined maximum size (alternative: dynamic arrays)
 - Dynamic allocation of arrays does not imply dynamic arrays
 - Amortised analysis (append): cost of copy becomes not relevant
- + No extra space with pointers (links)
- Space consumed by unused positions

List ADT as a linked list

- + With no predefined maximum size
- + No extra space for no longer accessible elements
- Space consumed by pointers (links)

Variations

- Pool of free nodes (freelist)
- Doubly-linked lists
- Circular-linked lists





Agenda

- 1 Abstract data types and data structures
- 2 List ADT
- 3 List ADT as an array
- 4 List ADT as a linked list
- 5 Asymptotic efficiency of lists
- 6 Bibliography

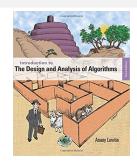




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LISTS

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