

STACKS | QUEUES

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Agenda

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Stack ADT

Policy: **LIFO** = last-in, first-out

Operations:

- `void clear(Stack s);`
- `void push(Stack s, E it);`
- `E pop(Stack s);`
- `E topValue(Stack s);`
- `int length(Stack s);`

Implementations based on: arrays and **linked lists**



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Stack ADT implemented as a linked list

Composite type (Stack):

```
1  Link top;           // reference to the first element
2  int size;           // number of elements
```

Differently from the List implementation as a linked list: **no header node**

Algorithm: Stack `create_stack()`

```
1  s.top  $\leftarrow$  NULL;
2  s.size  $\leftarrow$  0;
3  return s;
```



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Stack ADT implemented as a linked list

Algorithm: void push(Stack s, E it)

```
1 s.top  $\leftarrow$  create_link(it, s.top);  
2 s.size++;
```

push(s, 7), just after *create_stack()*

top \longrightarrow null



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- 1 $s.top \leftarrow create_link(it, s.top);$
 - 2 $s.size++;$
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$push(s, 7)$, just after $create_stack()$



Stack ADT implemented as a linked list

Algorithm: void push(Stack s, E it)

```
1  $s.top \leftarrow create\_link(it, s.top);$   
2  $s.size++;$ 
```

Better presented as follows



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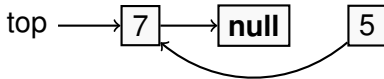
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Stack ADT implemented as a linked list

Algorithm: void push(Stack s, E it)

```
1 s.top ← create_link(it, s.top);  
2 s.size++;
```

push(s, 5)

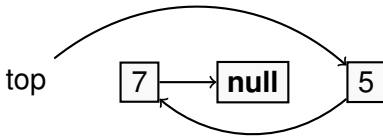


Stack ADT implemented as a linked list

Algorithm: void push(Stack s, E it)

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1 s.top ← create_link(it, s.top);  
2 s.size++;
```

push(*s*, 5)

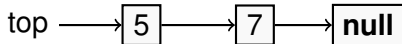


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Stack ADT implemented as a linked list

Algorithm: E pop(Stack s)

```

1 if s.top = NULL then error;
2 it ← s.top.element;
3 s.top ← s.top.next;
4 s.size--;
5 return it;

```

pop(s), just after push(s, 2)



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Stack ADT implemented as a linked list

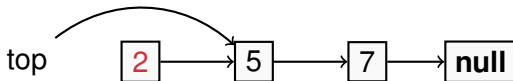
Algorithm: E pop(Stack s)

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5 return  $it$ ;

```

$pop(s)$, just after $push(s, 2)$



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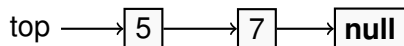
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Stack ADT implemented as a linked list

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4  $s.size--$ ;  
5 return  $it$ ;
```

After memory deallocation (by the user or by the GC)



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Queue ADT

Policy: **FIFO** = first-in, first-out

Operations:

- `void clear(Queue q);`
- `void enqueue(Queue q, E it);`
- `E dequeue(Queue q);`
- `E frontValue(Queue q);`
- `int length(Queue q);`

Implementations based on: arrays and **linked lists**



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Queue ADT implemented as a linked list

Composite Type (Queue):

```
1  Link front; Link rear; int size ;                                // queue size
```

This implementation does consider a **header node**

Algorithm: Queue create_queue()

```
1  q.front  $\leftarrow$  q.rear  $\leftarrow$  create_link(NULL);                // header node
2  q.size  $\leftarrow$  0;
3  return q;
```



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Queue ADT implemented as a linked list

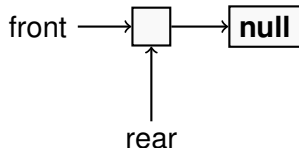
Algorithm: void enqueue(Queue q, E it)

```

1 q.rear.next  $\leftarrow$  create_link(it, NULL);
2 q.rear  $\leftarrow$  q.rear.next;
3 q.size++;

```

enqueue(*q*, 7), just after create_queue() (empty node: header)



Queue ADT implemented as a linked list

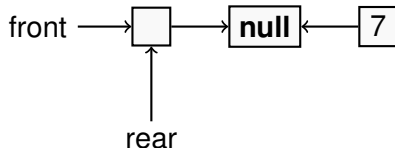
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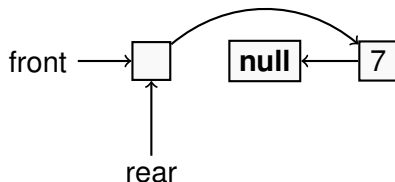
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Queue ADT implemented as a linked list

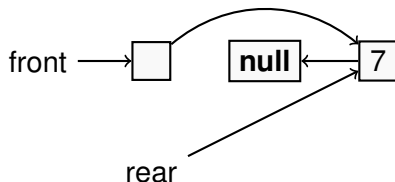
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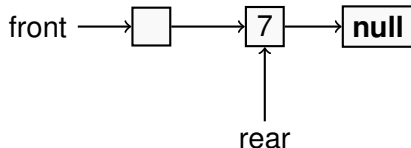


Queue ADT implemented as a linked list

Algorithm: void enqueue(Queue q, E it)

```
1 q.rear.next  $\leftarrow$  create_link(it, NULL);  
2 q.rear  $\leftarrow$  q.rear.next;  
3 q.size++;
```

Better presented as follows:



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Queue ADT implemented as a linked list

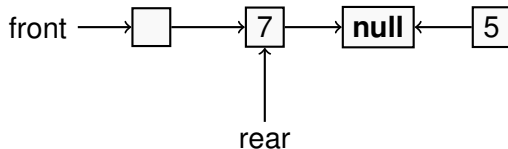
Algorithm: void enqueue(Queue q, E it)

```

1  q.rear.next ← create_link(it, NULL);
2  q.rear ← q.rear.next;
3  q.size++;

```

enqueue(*q*, 5)



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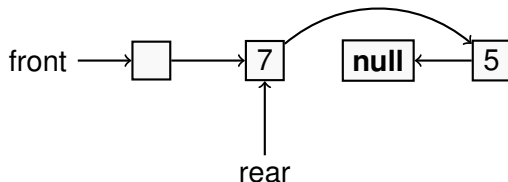
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Queue ADT implemented as a linked list

Algorithm: void enqueue(Queue q, E it)

```
1 q.rear.next ← create_link(it, NULL);  
2 q.rear ← q.rear.next;  
3 q.size++;
```

enqueue (q, 5)



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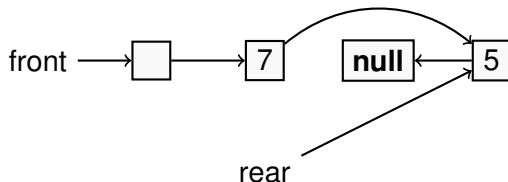
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```

enqueue (q, 5)

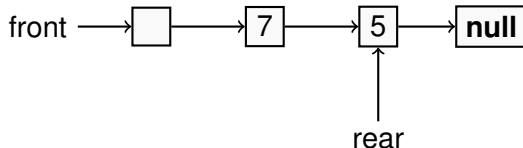


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Better presented as follows



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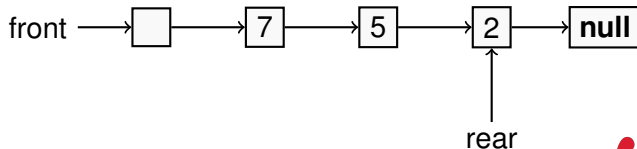
Algorithm: E dequeue(Queue q)

```

1 if q.size = 0 then error;
2 it ← q.front.next.element;
3 q.front.next ← q.front.next.next;
4 if q.front.next = NULL then q.rear ← q.front;
5 q.size--;
6 return it;

```

dequeue (q) , just after enqueue (q, 2)



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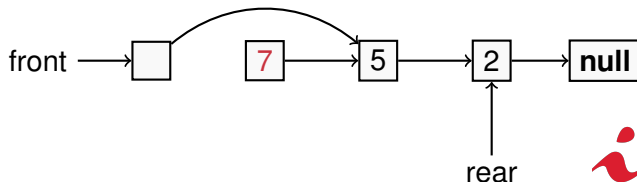
Algorithm: E dequeue(Queue q)

```

1 if  $q.size = 0$  then error;
2  $it \leftarrow q.front.next.element$ ;
3  $q.front.next \leftarrow q.front.next.next$ ;
4 if  $q.front.next = NULL$  then  $q.rear \leftarrow q.front$ ;
5  $q.size--$ ;
6 return  $it$ ;

```

dequeue (q) , just after enqueue (q, 2)



Queue ADT implemented as a linked list

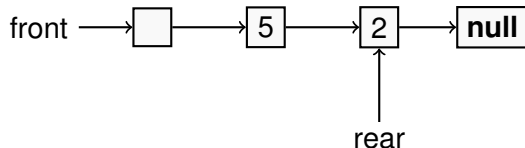
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4 if  $q.front.next = NULL$  then  $q.rear \leftarrow q.front$ ;
5  $q.size--$ ;
6 return  $it$ ;

```

After memory deallocation (by the user or by the GC)



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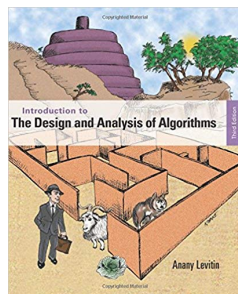


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